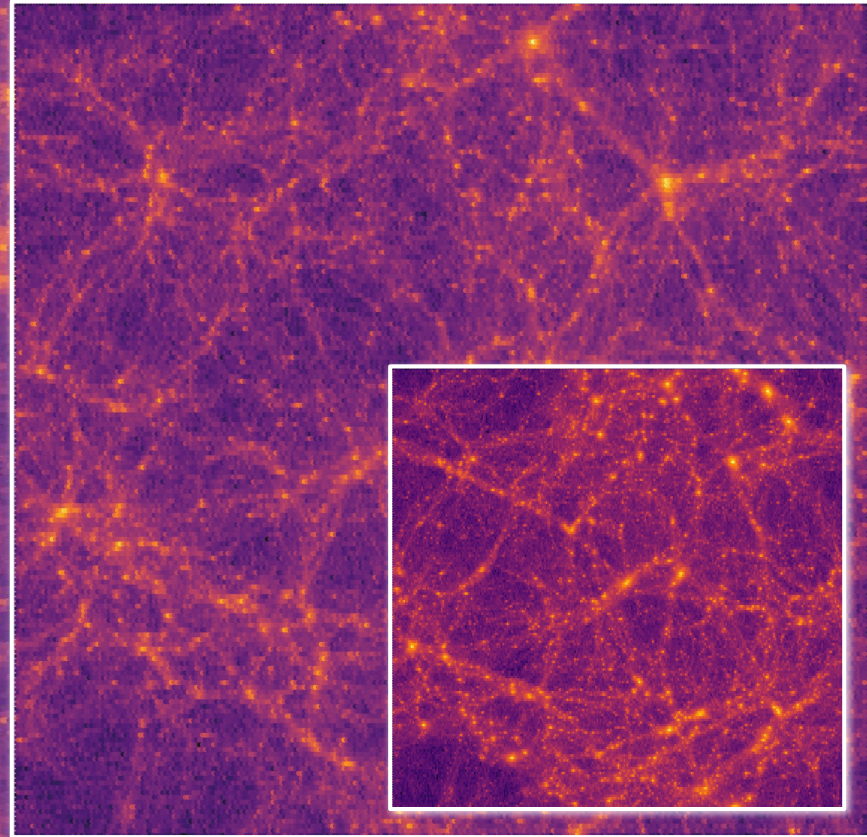


# Convergence of Cosmological N-body Simulations

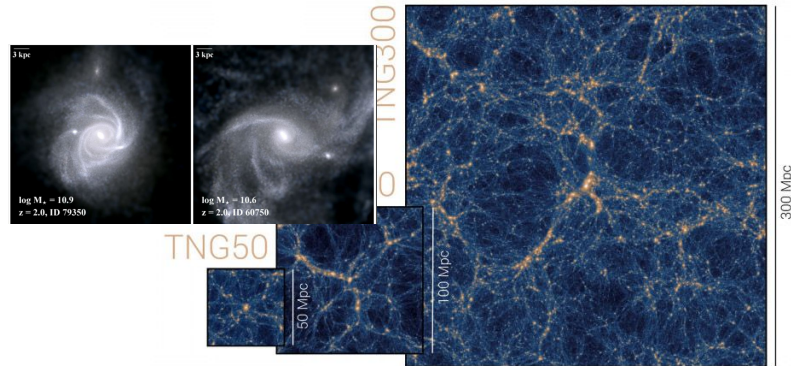
Aaron Ouellette  
May 4, 2022



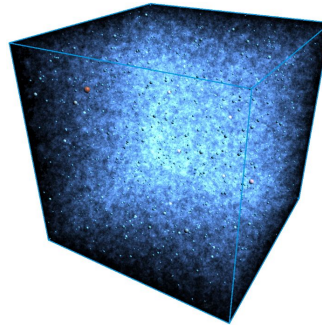
# Cosmological Simulations

- **Linear** structure formation (early times or large scales) - very easy to predict analytically
- **Non-linear** structure formation (late times, small scales) - practically impossible without direct simulation

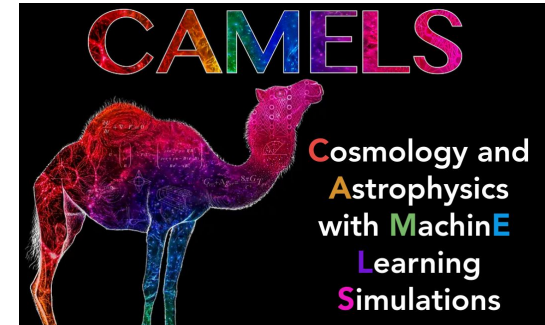
→ Need very large N-body simulations to study anything  $< \sim 10$  Mpc



IllustrisTNG collaboration



Outer Rim simulation  
Heitmann+ 2019



Villaescusa-Navarro+ 2021



# Initial Conditions

Use info from CMB to generate initial conditions

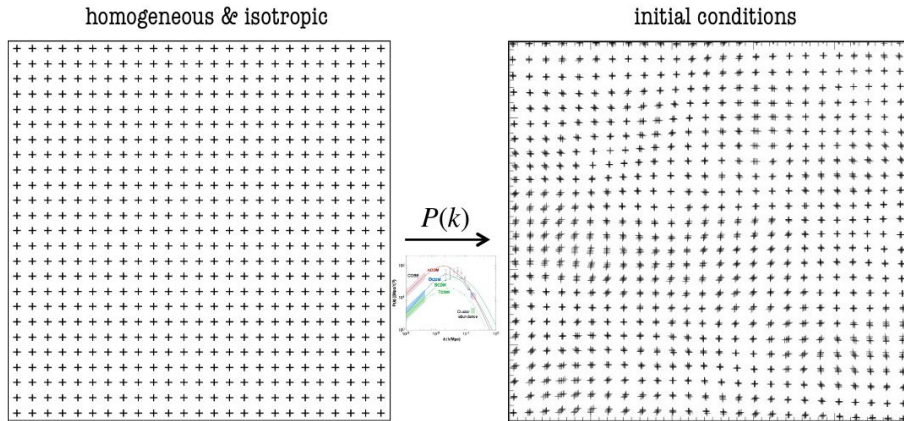


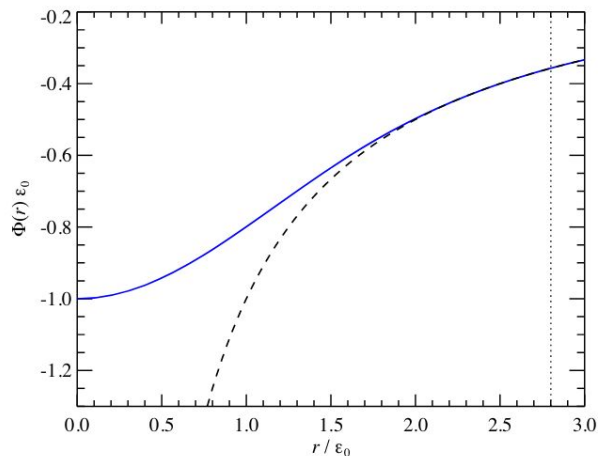
Image from lecture by  
Alexander Knebe

- Zel'dovich Approximation (ZA) - only linear order
- Second-order Lagrangian perturbation theory (2LPT)

Generate initial particle  
displacements and  
velocities from an initial  
power spectrum

# Discretization Parameters

- Number of particles ( $N$ ) and box length ( $L$ ) directly control the mass resolution ( $m_p$ ) of the simulation
  - Computational cost directly related to  $N$
  - Trade-off between needing large  $L$  and small  $m_p$
- Softening length ( $\epsilon$ ) - very important to avoid artificial close encounters, but puts limit on length resolution
  - Typically specified as a fraction of  $L / N^{1/3}$



Gravitational softening in  
GADGET (Springel+ 2021)

# Simulation Runs

Simulations run with GADGET-4

DM only - no hydro

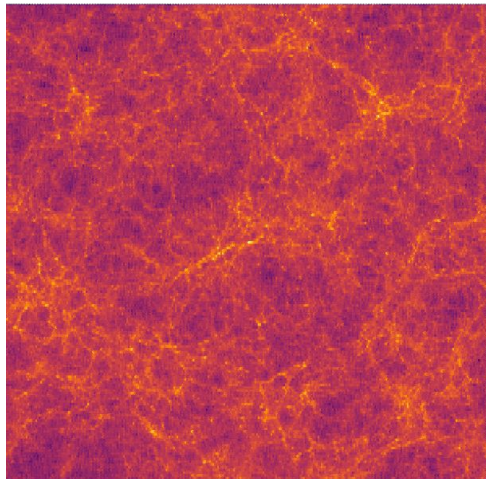
Assume Planck 2018 cosmology and same random seed for each run

Simulation outputs: particle snapshots and halo catalogs (FoF and subhalos)

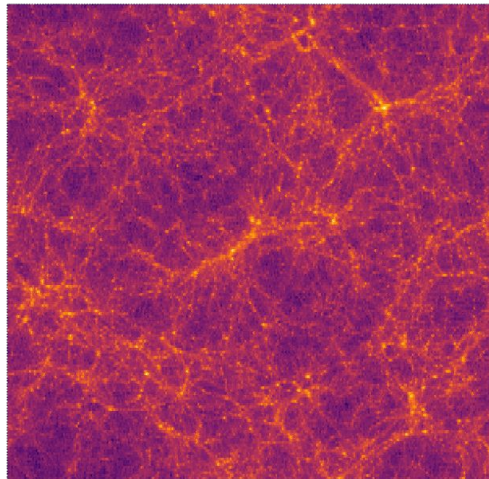
**Table 1.** Run parameters of the N-body simulations. Parameters that are not listed (e.g. the cosmology) are listed in the text and are kept constant between all of the runs.

Run #	$L(h^{-1} \text{ Mpc})$	$N$	$m_p(h^{-1} \text{ M}_\odot)$	IC type	$\epsilon (L/N^{1/3})$	$\epsilon (h^{-1} \text{ kpc})$
1	256	$64^3$	$5.6 \times 10^{12}$	2LPT	1/42	95
2	256	$128^3$	$7.0 \times 10^{11}$	2LPT	1/42	48
3	256	$256^3$	$8.7 \times 10^{10}$	2LPT	1/42	24
4	256	$512^3$	$1.1 \times 10^{10}$	2LPT	1/42	12
5	256	$64^3$	$5.6 \times 10^{12}$	ZA	1/42	95
6	256	$128^3$	$7.0 \times 10^{11}$	ZA	1/42	48
7	256	$256^3$	$8.7 \times 10^{10}$	ZA	1/42	24
8	256	$256^3$	$8.7 \times 10^{10}$	2LPT	1/200	5
9	256	$256^3$	$8.7 \times 10^{10}$	2LPT	1/67	15
10	256	$256^3$	$8.7 \times 10^{10}$	2LPT	1/29	35
11	256	$256^3$	$8.7 \times 10^{10}$	2LPT	1/22	45
13	512	$256^3$	$7.0 \times 10^{11}$	2LPT	1/42	48
14	128	$256^3$	$1.1 \times 10^{10}$	2LPT	1/42	12
15	64	$256^3$	$1.4 \times 10^9$	2LPT	1/42	6

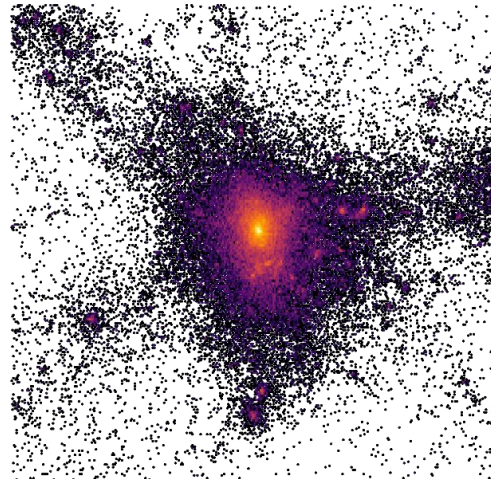
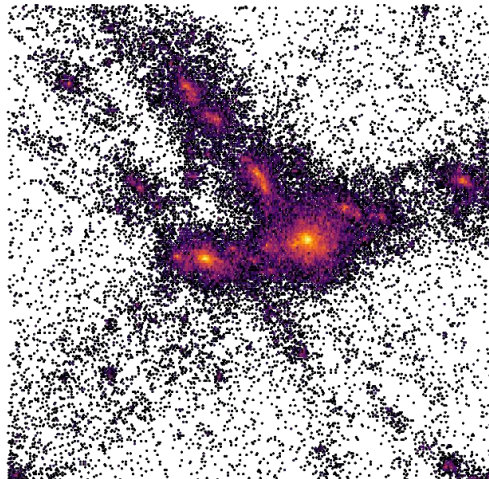
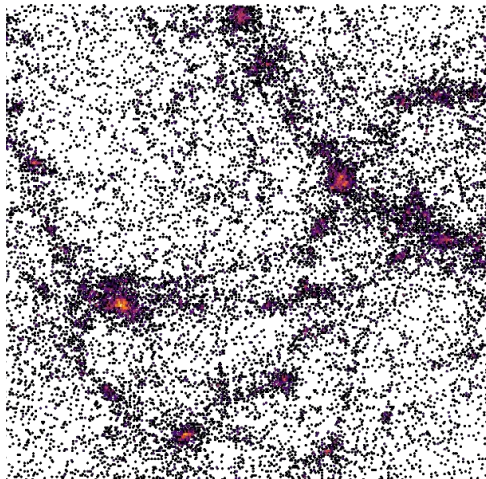
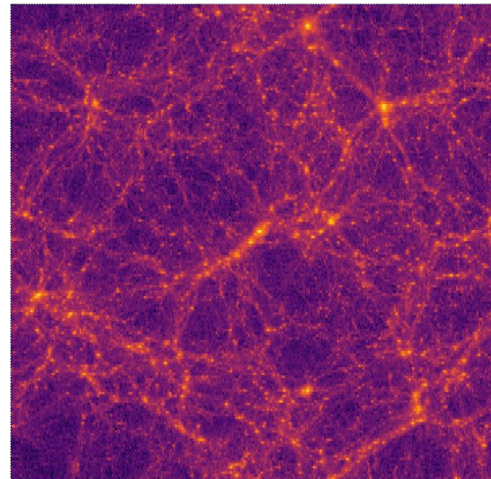
$a = 0.2, z = 3.0$



$a = 0.5, z = 1.0$

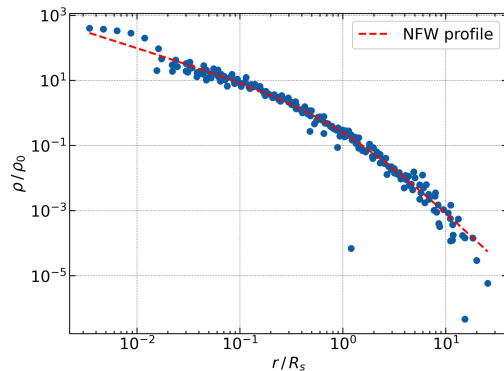
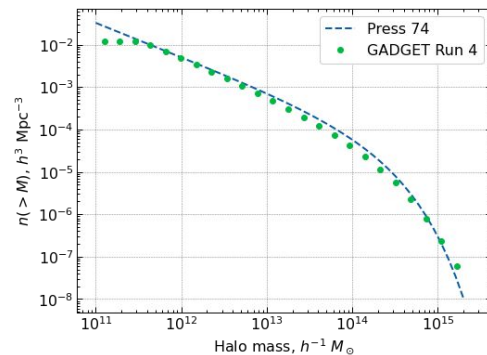
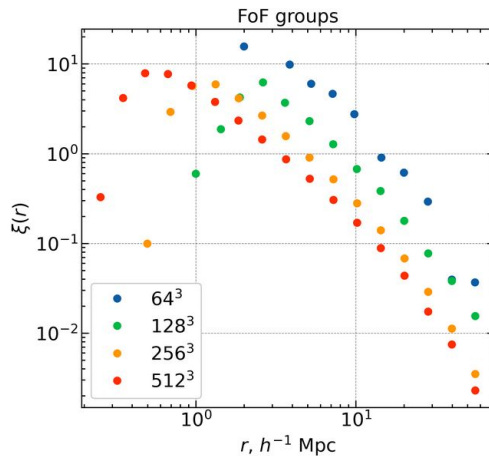
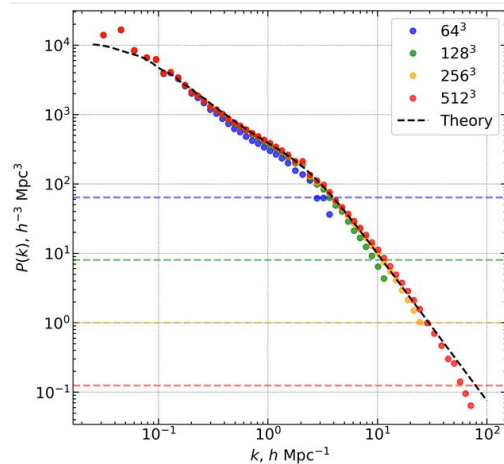


$a = 1.0, z = 0.0$



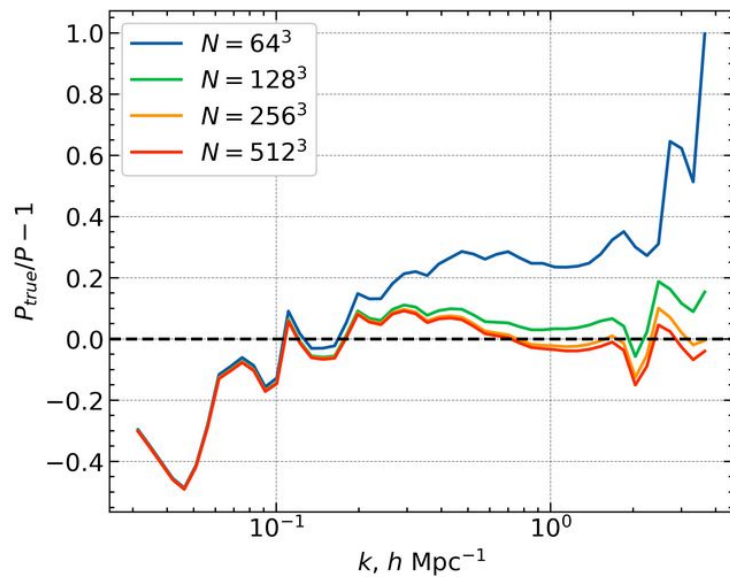
# Summary Statistics

- Power spectra
  - Compare to predictions using LSSTDESC Core Cosmology Library
- Correlation functions
- Halo mass functions (HMFs)
  - Compare to Press-Schechter HMF
- Halo density profiles
  - Fit to NFW profile

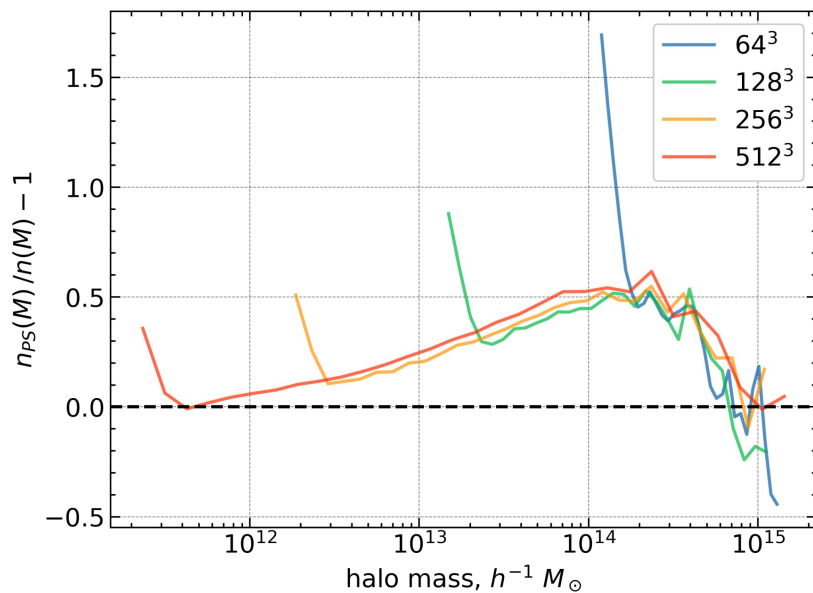




# Results: Mass Resolution



Power spectra

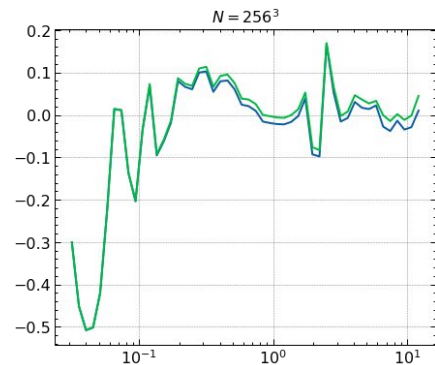
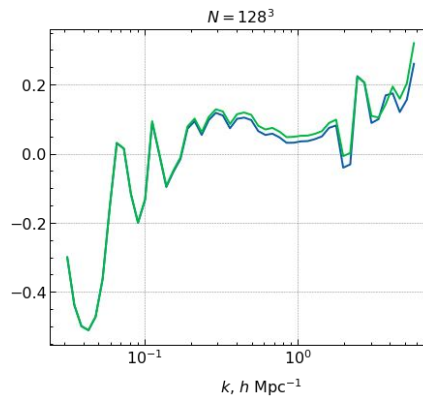
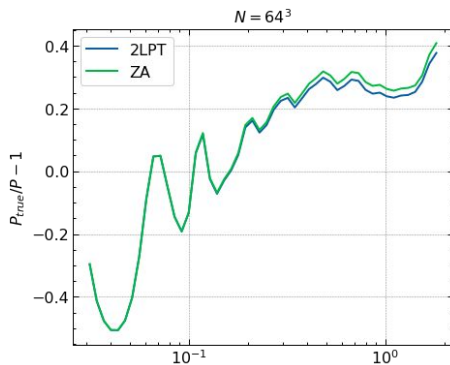


HMFs

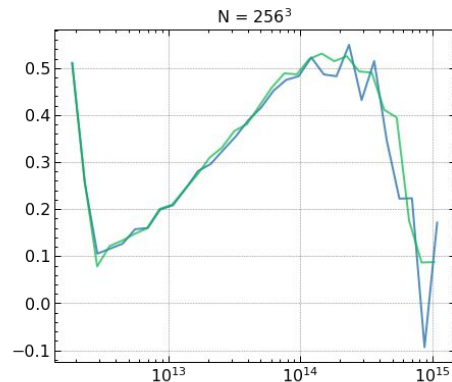
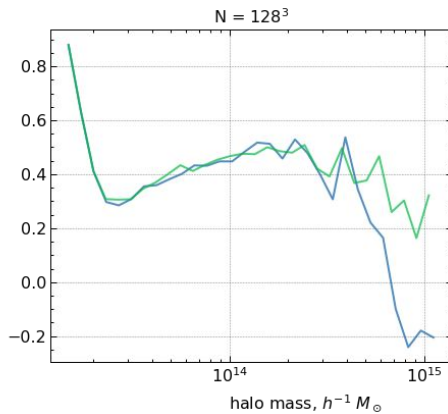
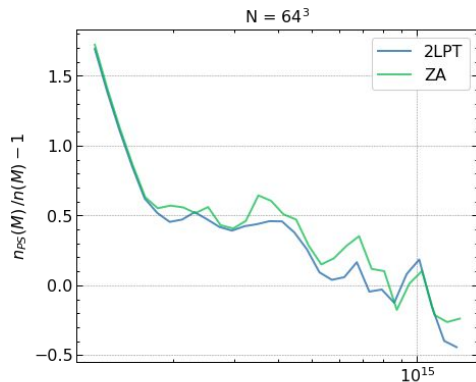


# Results: Initial Conditions

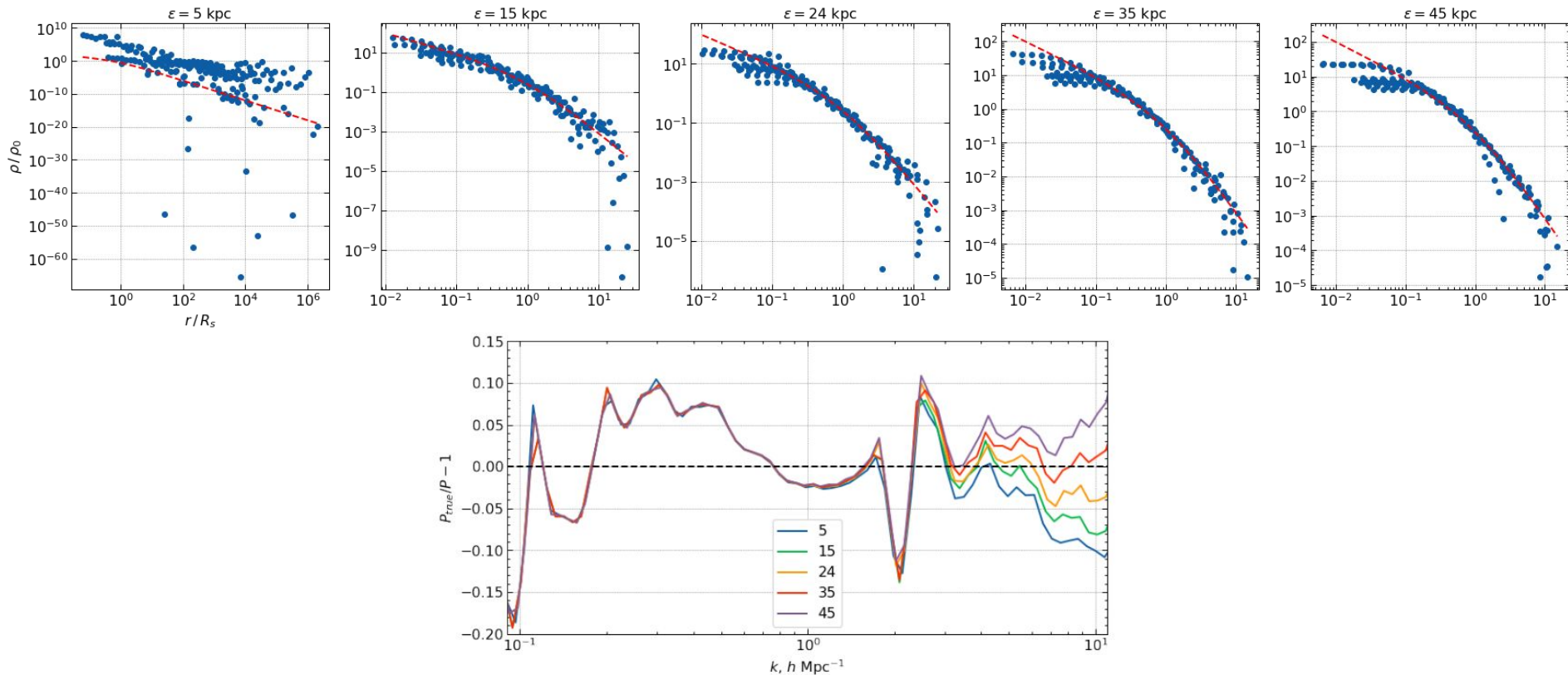
Power spectra



HMFs



# Results: Softening Length



# Conclusions

- Parameter choices for cosmological simulations:
  - Use 2LPT instead of ZA to generate initial conditions
  - $N$  and  $L$  directly affect the regimes the simulation can probe, secondary concern: accuracy
  - Softening length should usually be  $\sim 1/40$  to  $1/30$  x mean interparticle separation
- For current and upcoming surveys, huge computational effort is required to produce simulations that can be compared to observations