

# Shale gas

## A decision tree example

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## Introduction

Kamiński *et al*<sup>1</sup> provide an example of a decision tree with multiple decision nodes, including some that are descendants of another decision node. This vignette illustrates how **rdecision** can be used to model a complex decision tree, using the example from Figure 7 of Kamiński *et al*.<sup>1</sup>

## The problem

Kamiński *et al*<sup>1</sup> state the problem as follows:

Consider an investor owning a plot of land, possibly (*a priori* probability amounting to 70%) hiding shale gas layers. The plot can be sold immediately (800, all prices in \$'000). The investor can build a gas extraction unit for a cost of 300. If gas is found, the profit will amount to 2,500 (if not there will be no profit, and no possibility of selling the land). Geological tests can be performed for a cost of 50, and will produce either a positive or negative signal. The sensitivity amounts to 90% and the specificity amounts to 70%. The installation can be built after the test or the land may be sold for 1000 (600) after a positive (negative) test result.

## Creating the model

The model, comprising three decision nodes, four chance nodes, nine leaf nodes and 15 edges, is constructed as follows. Costs, benefits and probabilities are associated with each edge, which must be an Action or a Reaction object.

```
# nodes
d1 <- DecisionNode$new("d1")
d2 <- DecisionNode$new("d2")
d3 <- DecisionNode$new("d3")
c1 <- ChanceNode$new("c1")
c2 <- ChanceNode$new("c2")
c3 <- ChanceNode$new("c3")
c4 <- ChanceNode$new("c4")
t1 <- LeafNode$new("t1")
t2 <- LeafNode$new("t2")
t3 <- LeafNode$new("t3")
t4 <- LeafNode$new("t4")
t5 <- LeafNode$new("t5")
t6 <- LeafNode$new("t6")
```

```

t7 <- LeafNode$new("t7")
t8 <- LeafNode$new("t8")
t9 <- LeafNode$new("t9")
# probabilities
p.sens <- 0.9
p.spec <- 0.7
p.gas <- 0.7
p.nogas <- 1-p.gas
p.ptest <- p.sens*p.gas + (1-p.spec)*p.nogas
p.ntest <- (1-p.sens)*p.gas + p.spec*p.nogas
p.gas.ptest <- p.sens*p.gas / p.ptest
p.gas.ntest <- (1-p.sens)*p.gas / p.ntest
# edges
E <- list(
  Action$new(d1,t1,"sell",benefit=800),
  Action$new(d1,c1,"dig",cost=300),
  Reaction$new(c1,t2,p=p.gas,benefit=2500,label="gas"),
  Reaction$new(c1,t3,p=p.nogas,label="no gas"),
  Action$new(d1,c2,"test",cost=50),
  Reaction$new(c2,d2,p=p.ntest,label="negative"),
  Action$new(d2,t4,"sell",benefit=600),
  Action$new(d2,c3,"dig",cost=300),
  Reaction$new(c3,t5,p=p.gas.ntest,benefit=2500,label="gas"),
  Reaction$new(c3,t6,p=(1-p.gas.ntest),label="no gas"),
  Reaction$new(c2,d3,p=p.ptest,label="positive"),
  Action$new(d3,t7,"sell",benefit=1000),
  Action$new(d3,c4,"dig",cost=300),
  Reaction$new(c4,t8,p=p.gas.ptest,benefit=2500,label="gas"),
  Reaction$new(c4,t9,p=(1-p.gas.ptest),label="no gas")
)
# tree
V <- list(d1,d2,d3, c1,c2,c3,c4, t1,t2,t3,t4,t5,t6,t7,t8,t9)
DT<-DecisionTree$new(V,E)

```

## Evaluating the strategies

There are a total of 12 possible strategies (3 choices from node d1  $\times$  2 choices at node d2  $\times$  choices at node d3). But some of these are not unique. For example if the choice at node d1 is “sell”, the choices at nodes d2 and d3 (4 possible combinations) are unimportant; all four such strategies are identical. In identifying strategies, `rdecision` discards non-unique strategies, and uses the labels of an arbitrarily chosen strategy within each identical group as the identifier for the strategy; i.e. “sell/sell/sell” also represents the identical “sell/sell/dig”, “sell/dig/sell” and “sell/dig/dig”.

Similarly, four strategies with choice “dig” at node d1 are identical. Removing the six repeated strategies leaves a total of six possible strategies to evaluate:

```

# strategies
S <- DT$strategies("label")
knitr::kable(S, row.names=FALSE)

```

d1	d2	d3
sell	sell	sell

d1	d2	d3
dig	sell	sell
test	sell	sell
test	dig	sell
test	sell	dig
test	dig	dig

```
# evaluate one strategy (test/sell/sell)
RES <- DT$evaluate_strategy(list(E[[5]],E[[7]],E[[12]]))
# find optimal strategies
RES <- DT$evaluate()
imax <- which.max(RES$Benefit-RES$Cost)
popt <- paste(RES$d1[imax], RES$d2[imax], RES$d3[imax], sep="/")
```

## References

1. Kamiński, B. M. J. & Szufel, P. A framework for sensitivity analysis of decision trees. *Central European Journal of Operational Research* **26**, 135–159 (2018).