

# Package ‘rdecision’

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**Title** Decision Analytic Modelling in Health Economics

**Version** 1.0.1

**Description** Classes and functions for modelling healthcare interventions using cohort models (decision trees, Markov models and extended Markov models). It draws on terminology and examples from Briggs, Claxton and Sculpher, “Decision Modelling for Health Economic Evaluation”, Oxford University Press, 2006.

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grid

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Action	<i>Action</i>
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## Description

An R6 class to represent an action (choice) edge in a decision tree.

## Details

A specialism of class Arrow which is used in a decision tree to represent edges with source nodes joined to DecisionNodes.

## Super classes

`rdecision::Edge` -> `rdecision::Arrow` -> `Action`

## Methods

### Public methods:

- `Action$new()`
- `Action$modvars()`
- `Action$p()`
- `Action$cost()`
- `Action$benefit()`
- `Action$clone()`

**Method** `new()`: Create an object of type 'Action'. Optionally, a cost and a benefit may be associated with traversing the edge. A *payoff* (benefit-cost) is sometimes used in edges of decision trees; the parametrization used here is more general.

### Usage:

```
Action$new(source, target, label, cost = 0, benefit = 0)
```

### Arguments:

`source` Decision node from which the arrow leaves.

`target` Node which the arrow enters.

`label` Character string containing the arrow label. This

`cost` Cost associated with traversal of this edge.

**benefit** Benefit associated with traversal of the edge. must be defined for an action because the label is used in tabulation of strategies.

*Returns:* A new Action object.

**Method** `modvars()`: Find all the model variables of type `ModVar` that have been specified as values associated with this Action. Includes operands of these `ModVars`, if they are expressions.

*Usage:*

`Action$modvars()`

*Returns:* A list of `ModVars`.

**Method** `p()`: Return the current value of the edge probability, i.e. the conditional probability of traversing the edge.

*Usage:*

`Action$p()`

*Returns:* Numeric value equal to 1.

**Method** `cost()`: Return the cost associated with traversing the edge.

*Usage:*

`Action$cost()`

*Returns:* Cost.

**Method** `benefit()`: Return the benefit associated with traversing the edge.

*Usage:*

`Action$benefit()`

*Returns:* Benefit.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

`Action$clone(deep = FALSE)`

*Arguments:*

`deep` Whether to make a deep clone.

## Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

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Arborescence

*Arborescence*

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## Description

An R6 class to represent an arborescence (rooted directed tree).

## Details

Class to encapsulate a directed rooted tree specialization of a digraph. An arborescence must be a directed tree with exactly one root and the directed paths from the root must be unique.

**Super classes**

`rdecision::Graph -> rdecision::Digraph -> Arborescence`

**Methods****Public methods:**

- `Arborescence$new()`
- `Arborescence$is_parent()`
- `Arborescence$is_leaf()`
- `Arborescence$root()`
- `Arborescence$siblings()`
- `Arborescence$root_to_leaf_paths()`
- `Arborescence$postree()`
- `Arborescence$clone()`

**Method** `new()`: Create a new Arborescence object from sets of nodes and edges.

*Usage:*

`Arborescence$new(V, A)`

*Arguments:*

V A list of Nodes.

A A list of Arrows.

*Returns:* An Arborescence object.

**Method** `is_parent()`: Test whether the given node is a parent (has child nodes).

*Usage:*

`Arborescence$is_parent(v)`

*Arguments:*

v Node to test

*Returns:* TRUE if v has one or more child nodes, FALSE otherwise.

**Method** `is_leaf()`: Test whether the given node is a leaf. In an arborescence, `is_parent()` and `is_leaf()` will be mutually exclusive.

*Usage:*

`Arborescence$is_leaf(v)`

*Arguments:*

v Vertex to test.

*Returns:* TRUE if v has no child nodes, FALSE otherwise.

**Method** `root()`: Find the root vertex of the arborescence.

*Usage:*

`Arborescence$root()`

*Returns:* The root vertex.

**Method** `siblings()`: Find the siblings of a vertex in the arborescence.

*Usage:*

`Arborescence$siblings(v)`

*Arguments:*

*v* Vertex to test.

*Returns:* A (possibly empty) list of siblings.

**Method** `root_to_leaf_paths()`: Find all directed paths from the root of the tree to the leaves.

*Usage:*

```
Arborescence$root_to_leaf_paths()
```

*Returns:* A list of ordered node lists.

**Method** `postree()`: Implements function POSITIONTREE (Walker, 1989) to determine the coordinates for each node in an arborescence.

*Usage:*

```
Arborescence$postree(
  SiblingSeparation = 4,
  SubtreeSeparation = 4,
  LevelSeparation = 1,
  RootOrientation = "SOUTH"
)
```

*Arguments:*

*SiblingSeparation* Distance in arbitrary units for the distance between siblings.

*SubtreeSeparation* Distance in arbitrary units for the distance between neighbouring subtrees.

*LevelSeparation* Distance in arbitrary units for the separation between adjacent levels.

*RootOrientation* Must be one of "NORTH", "SOUTH", "EAST", "WEST". Defined as per Walker (1989), but noting that Walker assumed that y increased down the page. Thus the meaning of NORTH and SOUTH are opposite to his, with the default (SOUTH) having the child nodes at positive y value and root at zero, as per his example (figure 12).

*Returns:* A data frame with one row per node and three columns (n, x and y) where n gives the node index given by the `Graph::vertex_index()` function.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
Arborescence$clone(deep = FALSE)
```

*Arguments:*

*deep* Whether to make a deep clone.

**Author(s)**

Andrew Sims <andrew.sims@newcastle.ac.uk>

**References**

- Walker, John Q II. A node-positioning algorithm for general trees. University of North Carolina Technical Report TR 89-034, 1989.
- Tilford, J and Reingold, E. Tidier Drawings of Trees. IEEE Transactions on Software Engineering. 1981;7: 223–228. doi:10.1109/TSE.1981.234519

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 Arrow

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*Arrow*


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## Description

An R6 class to represent an directed edge in a digraph.

## Details

Arrows are the formal term for links between pairs of nodes in a directed graph. Inherits from class Edge.

## Super class

`rdecision::Edge` -> Arrow

## Methods

### Public methods:

- `Arrow$new()`
- `Arrow$source()`
- `Arrow$target()`
- `Arrow$clone()`

**Method** `new()`: Create an object of type 'Arrow'.

*Usage:*

`Arrow$new(source, target, label = "")`

*Arguments:*

`source` Node from which the arrow leaves.

`target` second Node to which the arrow enters.

`label` Character string containing the arrow label.

*Returns:* A new 'Arrow' object.

**Method** `source()`: Access source node.

*Usage:*

`Arrow$source()`

*Returns:* 'Node' from which the arrow leads.

**Method** `target()`: Access target node.

*Usage:*

`Arrow$target()`

*Returns:* 'Node' to which the arrow points.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

`Arrow$clone(deep = FALSE)`

*Arguments:*

`deep` Whether to make a deep clone.

**Author(s)**

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

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BetaModVar

*BetaModVar*

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**Description**

An R6 class for a model variable with Beta function uncertainty

**Details**

A model variable for which the uncertainty in the point estimate can be modelled with a Beta distribution. The hyperparameters of the distribution are the shape ('alpha') and the shape ('beta') of the uncertainty distribution.

**Super class**

`rdecision::ModVar` -> BetaModVar

**Methods****Public methods:**

- `BetaModVar$new()`
- `BetaModVar$is_probabilistic()`
- `BetaModVar$distribution()`
- `BetaModVar$mean()`
- `BetaModVar$mode()`
- `BetaModVar$SD()`
- `BetaModVar$r()`
- `BetaModVar$quantile()`
- `BetaModVar$clone()`

**Method** `new()`: Create an object of class BetaModVar.

*Usage:*

`BetaModVar$new(description, units, alpha, beta)`

*Arguments:*

`description` A character string describing the variable.

`units` Units of the variable, as character string.

`alpha` parameter of the Beta distribution.

`beta` parameter of the Beta distribution.

*Returns:* An object of class BetaModVar.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, some of which follow distributions.

*Usage:*

BetaModVar\$is\_probabilistic()

*Returns:* TRUE if probabilistic

**Method** distribution(): Accessor function for the name of the uncertainty distribution.

*Usage:*

BetaModVar\$distribution()

*Returns:* Distribution name as character string.

**Method** mean(): Return the expected value of the distribution.

*Usage:*

BetaModVar\$mean()

*Returns:* Expected value as a numeric value.

**Method** mode(): Return the mode of the distribution (if alpha, beta > 1)

*Usage:*

BetaModVar\$mode()

*Returns:* mode as a numeric value.

**Method** SD(): Return the standard deviation of the distribution.

*Usage:*

BetaModVar\$SD()

*Returns:* Standard deviation as a numeric value Draw a random sample from the model variable.

**Method** r():

*Usage:*

BetaModVar\$r(n = 1)

*Arguments:*

n Number of samples to draw.

*Returns:* Samples drawn at random.

**Method** quantile(): Return the quantiles of the Gamma uncertainty distribution.

*Usage:*

BetaModVar\$quantile(probs)

*Arguments:*

probs Vector of probabilities, in range [0,1].

*Returns:* Vector of quantiles.

**Method** clone(): The objects of this class are cloneable with this method.

*Usage:*

BetaModVar\$clone(deep = FALSE)

*Arguments:*

deep Whether to make a deep clone.

## Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>



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ChanceNode

*ChanceNode*

---

## Description

An R6 class to represent a chance node in a decision tree.

## Details

An R6 class to represent a chance node in a decision tree. The node is associated with at least two branches to other nodes, each of which has a conditional probability (the probability of following that branch given that the node has been reached) and a cost.

## Super class

`rdecision::Node` -> ChanceNode

## Methods

### Public methods:

- `ChanceNode$new()`
- `ChanceNode$clone()`

**Method** `new()`: Create a new ChanceNode object

*Usage:*

`ChanceNode$new(label = "")`

*Arguments:*

`label` An optional label for the chance node.

*Returns:* A new 'ChanceNode' object

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

`ChanceNode$clone(deep = FALSE)`

*Arguments:*

`deep` Whether to make a deep clone.

## Author(s)

Andrew Sims <andrew.sims@newcastle.ac.uk>

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ConstModVar

*ConstModVar*


---

## Description

An R6 class for a constant in a model

## Details

A ModVar with no uncertainty in its value. It has no distribution and there are no hyperparameters. Its benefit over using a regular 'numeric' variable in a model is that it will appear in automatic tabulations of the model variables associated with a model and therefore be explicitly documented as a model input.

## Super class

`rdecision::ModVar` -> ConstModVar

## Methods

### Public methods:

- `ConstModVar$new()`
- `ConstModVar$is_probabilistic()`
- `ConstModVar$distribution()`
- `ConstModVar$mode()`
- `ConstModVar$mean()`
- `ConstModVar$r()`
- `ConstModVar$SD()`
- `ConstModVar$quantile()`
- `ConstModVar$clone()`

**Method** `new()`: Create a new constant model variable

*Usage:*

`ConstModVar$new(description, units, const)`

*Arguments:*

`description` A character string description of the variable and its role in the model. This description will be used in a tabulation of the variables linked to a model.

`units` A character string description of the units, e.g. "GBP", "per year".

`const` The constant numerical value of the object.

*Returns:* A new ConstModVar object.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, some of which follow distributions.

*Usage:*

`ConstModVar$is_probabilistic()`

*Returns:* TRUE if probabilistic

**Method** `distribution()`: Accessor function for the name of the uncertainty distribution.

*Usage:*

```
ConstModVar$distribution()
```

*Returns:* Distribution name as character string.

**Method** `mode()`: Return the mode of the distribution.

*Usage:*

```
ConstModVar$mode()
```

*Returns:* Value of the constant.

**Method** `mean()`: Return the expected value of the distribution.

*Usage:*

```
ConstModVar$mean()
```

*Returns:* Expected value as a numeric value.

**Method** `r()`: Return a random sample from the distribution.

*Usage:*

```
ConstModVar$r(n = 1)
```

*Arguments:*

`n` Number of samples to draw.

*Returns:* Constant value as a numeric value.

**Method** `SD()`: Return the standard deviation of the distribution.

*Usage:*

```
ConstModVar$SD()
```

*Returns:* Standard deviation as a numeric value

**Method** `quantile()`: Quantiles of the uncertainty distribution; for a constant all quantiles are returned as the value of the constant.

*Usage:*

```
ConstModVar$quantile(probs)
```

*Arguments:*

`probs` Numeric vector of probabilities, each in range [0,1].

*Returns:* Vector of numeric values of the same length as ‘probs’.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
ConstModVar$clone(deep = FALSE)
```

*Arguments:*

`deep` Whether to make a deep clone.

## Author(s)

Andrew Sims <andrew.sims@newcastle.ac.uk>

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DecisionNode

*DecisionNode*


---

## Description

An R6 class for a decision node in a decision tree

## Details

A class to represent a decision node in a decision tree. The node is associated with one or more branches to child nodes.

## Super class

`rdecision::Node` -> DecisionNode

## Methods

### Public methods:

- `DecisionNode$new()`
- `DecisionNode$clone()`

**Method** `new()`: Create a new decision node.

*Usage:*

```
DecisionNode$new(label)
```

*Arguments:*

`label` A label for the node. Must be defined because the label is used in tabulation of strategies. The label is automatically converted to a syntactically valid (in R) name to ensure it can be used as a column name in a data frame.

*Returns:* A new DecisionNode object

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
DecisionNode$clone(deep = FALSE)
```

*Arguments:*

`deep` Whether to make a deep clone.

## Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

DecisionTree

*DecisionTree***Description**

An R6 class to represent a decision tree

**Details**

A class to represent a decision tree. An object contains a tree of decision nodes, chance nodes and leaf nodes, connected by edges (either actions or reactions) and which satisfies the following conditions:

1. Nodes and edges must form a tree with a single root and there must be a unique path from the root to each node. In graph theory terminology, the directed graph formed by the nodes and edges must be an *arborescence*.
2. Each node must inherit from one of DecisionNode, ChanceNode or LeafNode. Formally the set of vertices must be a disjoint union of sets of decision nodes, chance nodes and leaf nodes.
3. All and only leaf nodes must have no children.
4. Each edge must inherit from either Action or Reaction.
5. All and only edges that have source endpoints joined to decision nodes must inherit from Action.
6. All and only edges that have source endpoints joined to chance nodes must inherit from Reaction.
7. The sum of probabilities of each set of reaction edges with a common source endpoint must be 1.
8. Each DecisionNode must have a label, and the labels of all DecisionNodes must be unique within the model.
9. Each Action must have a label, and the labels of Actions that share a common source endpoint must be unique.

**Super classes**

`rdecision::Graph -> rdecision::Digraph -> rdecision::Arborescence -> DecisionTree`

**Methods****Public methods:**

- `DecisionTree$new()`
- `DecisionTree$decision_nodes()`
- `DecisionTree$chance_nodes()`
- `DecisionTree$leaf_nodes()`
- `DecisionTree$actions()`
- `DecisionTree$modvars()`
- `DecisionTree$modvar_table()`
- `DecisionTree$draw()`
- `DecisionTree$is_strategy()`

- `DecisionTree$strategy_table()`
- `DecisionTree$strategy_paths()`
- `DecisionTree$evaluate_walks()`
- `DecisionTree$evaluate()`
- `DecisionTree$tornado()`
- `DecisionTree$clone()`

**Method** `new()`: Create a new decision tree. The tree must consist of a set of nodes and a set of edges which satisfy the conditions given in the details section of this class.

*Usage:*

`DecisionTree$new(V, E)`

*Arguments:*

V A list of nodes.

E A list of edges.

*Returns:* A DecisionTree object

**Method** `decision_nodes()`: Find the decision nodes in the tree.

*Usage:*

`DecisionTree$decision_nodes(what = "node")`

*Arguments:*

what A character string defining what to return. Must be one of "node", "label" or "index".

*Returns:* A list of DecisionNode objects (for what="node"); a list of character strings (for what="label"); or a list of integer indexes of the decision nodes (for what="index").

**Method** `chance_nodes()`: Find the chance nodes in the tree.

*Usage:*

`DecisionTree$chance_nodes()`

*Returns:* A list of ChanceNode objects.

**Method** `leaf_nodes()`: Find the leaf nodes in the tree.

*Usage:*

`DecisionTree$leaf_nodes(what = "node")`

*Arguments:*

what One of "node" (returns Node objects), "label" (returns the leaf node labels) or "index" (returns the vertex index of the leaf nodes).

*Returns:* A list of LeafNode objects (for what="node"); a list of character strings (for what="label"); or a list of integer indexes of the decision nodes (for what="index").

**Method** `actions()`: Return the edges that have the specified decision node as their source.

*Usage:*

`DecisionTree$actions(d)`

*Arguments:*

d A decision node.

*Returns:* A list of Action edges.

**Method** `modvars()`: Find all the model variables of type ModVar that have been specified as values associated with the nodes and edges of the tree.

*Usage:*

DecisionTree\$modvars()

*Returns:* A list of ModVars.

**Method** modvar\_table(): Tabulate the model variables.

*Usage:*

DecisionTree\$modvar\_table(expressions = TRUE)

*Arguments:*

expressions A logical that defines whether expression model variables should be included in the tabulation.

*Returns:* Data frame with one row per model variable, as follows:

**Description** As given at initialization.

**Units** Units of the variable.

**Distribution** Either the uncertainty distribution, if it is a regular model variable, or the expression used to create it, if it is an ExprModVar.

**Mean** Mean; calculated from means of operands if an expression.

**E** Expectation; estimated from random sample if expression, mean otherwise.

**SD** Standard deviation; estimated from random sample if expression, exact value otherwise.

**Q2.5** p=0.025 quantile; estimated from random sample if expression, exact value otherwise.

**Q97.5** p=0.975 quantile; estimated from random sample if expression, exact value otherwise.

**Est** TRUE if the quantiles and SD have been estimated by random sampling.

**Method** draw(): Draw the decision tree to the current graphics output. Uses the algorithm of Walker (1989) to distribute the nodes compactly (see the [Arborescence](#) class help for details).

*Usage:*

DecisionTree\$draw(border = FALSE)

*Arguments:*

border If TRUE draw a light grey border around the plot area.

*Returns:* No return value.

**Method** is\_strategy(): Tests whether a strategy (a unanimous prescription of an action in each decision node, specified as a list of nodes) is a valid strategy for this decision tree.

*Usage:*

DecisionTree\$is\_strategy(strategy)

*Arguments:*

strategy A list of Action edges.

*Returns:* TRUE if the strategy is valid for this tree. Throws an exception if the argument is not a list of Action edges. Returns FALSE if the list of Action edges are not a valid strategy.

**Method** strategy\_table(): Find all potential strategies for the decision tree. A strategy is a unanimous prescription of the actions at each decision node. If there are decision nodes that are descendants of other nodes in the tree, the strategies returned will not necessarily be unique.

*Usage:*

DecisionTree\$strategy\_table(what = "index", select = NULL)

*Arguments:*

what A character string defining what to return. Must be one of "label" or "index".

**select** A single strategy (given as a list of action edges, with one action edge per decision node). If provided, only that strategy is selected from the returned table. Intended for tabulating a single strategy into a readable form.

**Returns:** A data frame where each row is a potential strategy and each column is a Decision Node. Values are either the index of each action edge, or their label.

**Method** `strategy_paths()`: Find all paths walked in each possible strategy. A strategy is a unanimous prescription of an action in each decision node. Some paths can be walked in more than one strategy, if there exist paths that do not pass a decision node.

*Usage:*

```
DecisionTree$strategy_paths()
```

**Returns:** A data frame, where each row is a path walked in a strategy. The structure is similar to that returned by `strategy_table` but includes an extra column, 'Leaf' which gives the leaf node index of each path, and there is one row for each path in each strategy.

**Method** `evaluate_walks()`: Evaluate the components of payoff associated with a set of walks in the decision tree. For each walk, probability, cost, benefit and utility are calculated.

*Usage:*

```
DecisionTree$evaluate_walks(W)
```

*Arguments:*

**W** A list of root-to-leaf walks. Each walk must start with the root node and end with a leaf node. Normally this is all the root to leaf paths in a tree.

**Returns:** A matrix (payoff table) with one row per path and columns organized as follows:

**Leaf** The unique identifier of the path, taken to be the index of the terminal (leaf) node.

**Probability** The probability of traversing the pathway.

**Path.Cost** The cost of traversing the pathway.

**Path.Benefit** The benefit derived from traversing the pathway.

**Path.Utility** The utility associated with the outcome (leaf node).

**Cost**  $\text{Path.Cost} * \text{probability of traversing the pathway}$ .

**Benefit**  $\text{Path.Benefit} * \text{probability of traversing the pathway}$ .

**Utility**  $\text{Path.Utility} * \text{probability of traversing the pathway}$ .

**Method** `evaluate()`: Evaluate each strategy. Starting with the root, the function works though all possible paths to leaf nodes and computes the probability, cost, benefit and utility of each, then aggregates by strategy.

*Usage:*

```
DecisionTree$evaluate(setvars = "expected", N = 1, by = "strategy")
```

*Arguments:*

**setvars** One of "expected" (evaluate with each model variable at its mean value), "random" (sample each variable from its uncertainty distribution and evaluate the model), "q2.5", "q50", "q97.5" (set each model variable to its 2.5, 50, 97.5 percentile and evaluate the model), "current" (leave each model variable at its current value prior to calling the function and evaluate the model).

**N** Number of replicates. Intended for use with PSA (`modvars="random"`); use with `modvars="expected"` will be repetitive and uninformative.

**by** One of "path", "strategy". If "path", the table has one row per path walked per strategy, per run, and includes the label of the terminating leaf node to identify each path. if "strategy" (the default), the table is aggregated by strategy, i.e. there is one row per strategy, per run and there is no "Leaf" column.



**Returns:** A data frame with one row per strategy per run and columns organized as follows:

**Leaf** The label of the leaf that terminates the path, for by='path'.

**Strategy** The strategy expressed as the values of the action edges emanating from each decision node.

**Run** The run number

**Probability** Probability (1 if by='strategy')

**Cost** Aggregate cost of the strategy.

**Benefit** Aggregate benefit of the strategy.

**Utility** Aggregate utility of the strategy.

**Method** `tornado()`: Create a "tornado" diagram to compare two strategies for traversing the decision tree. A strategy is a unanimous prescription of the actions at each decision node.

*Usage:*

```
DecisionTree$tornado(index, ref, outcome = "cost", exclude = NULL, draw = TRUE)
```

*Arguments:*

`index` The index strategy (option) to be evaluated.

`ref` The reference strategy (option) with which the index strategy will be compared.

`outcome` One of "cost" or "ICER". For "cost" (e.g. in cost consequence analysis), the x axis is cost saved (cost of reference minus cost of index), on the presumption that the new technology will be cost saving at the point estimate. For "ICER" the x axis is  $\Delta C/\Delta E$  and is expected to be positive at the point estimate (i.e. in the NE or SW quadrants of the cost-effectiveness plane), where  $\Delta C$  is cost of index minus cost of reference, and  $\Delta E$  is utility of index minus utility of reference.

`exclude` A list of descriptions of model variables to be excluded from the tornado.

`draw` TRUE if the graph is to be drawn; otherwise return the data frame silently.

**Returns:** A data frame with one row per input model variable and columns for: minimum value of the variable, maximum value of the variable, minimum value of the outcome and maximum value of the outcome.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
DecisionTree$clone(deep = FALSE)
```

*Arguments:*

`deep` Whether to make a deep clone.

## Note

There is minimal checking of the argument because this function is intended to be called repeatedly during tree evaluation, including PSA. The argument `P` is expected to be obtained from `root_to_leaf_paths`.

The extreme values of each input variable are the upper and lower 95 This ensures that the range of each input is defensible (Briggs 2012).

## Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

Digraph

*Digraph***Description**

An R6 class to represent a digraph (a directed graph).

**Details**

Encapsulates, and provides methods for computation and checking of directed graphs (digraphs). Inherits from class Graph.

**Super class**

`rdecision::Graph` -> Digraph

**Methods****Public methods:**

- `Digraph$new()`
- `Digraph$digraph_adjacency_matrix()`
- `Digraph$digraph_incidence_matrix()`
- `Digraph$topological_sort()`
- `Digraph$is_connected()`
- `Digraph$is_weakly_connected()`
- `Digraph$is_acyclic()`
- `Digraph$is_tree()`
- `Digraph$is_polytree()`
- `Digraph$is_arborescence()`
- `Digraph$direct_successors()`
- `Digraph$direct_predecessors()`
- `Digraph$paths()`
- `Digraph$walk()`
- `Digraph$clone()`

**Method** `new()`: Create a new Digraph object from sets of nodes and edges.

*Usage:*

`Digraph$new(V, A)`

*Arguments:*

V A list of Nodes.

A A list of Arrows.

*Returns:* A Digraph object.

**Method** `digraph_adjacency_matrix()`: Compute the adjacency matrix for the digraph. Each cell contains the number of edges from the row vertex to the column vertex, with the convention of self loops being counted once, unless 'boolean' is TRUE when cells are either FALSE (not adjacent) or TRUE (adjacent).

*Usage:*

```
Digraph$digraph_adjacency_matrix(boolean = FALSE)
```

*Arguments:*

`boolean` If TRUE, the adjacency matrix is logical, each cell is FALSE,TRUE.

*Returns:* A square numeric matrix with the number of rows and columns equal to the order of the graph. The rows and columns are in the same order as `V`. If the nodes have defined and unique labels the dimnames of the matrix are the labels of the nodes.

**Method** `digraph_incidence_matrix()`: Compute the incidence matrix for the graph. Each row is a vertex and each column is an edge. Edges leaving a vertex have value -1 and edges entering have value +1. if all vertexes have defined and unique labels and all edges have defined and unique labels, the dimnames of the matrix are the labels of the vertexes and edges.

*Usage:*

```
Digraph$digraph_incidence_matrix()
```

*Returns:* The incidence matrix.

**Method** `topological_sort()`: Attempt to topologically sort the vertexes in the directed graph using Kahn's algorithm (<https://doi.org/10.1145>)

*Usage:*

```
Digraph$topological_sort()
```

*Returns:* A list of vertexes, topologically sorted. If the digraph has cycles, the returned ordered list will not contain all the vertexes in the graph, but no error will be raised.

**Method** `is_connected()`: Test whether the graph is connected. For digraphs this will always return FALSE because "connected" is not defined. Function `weakly_connected` calculates whether the underlying graph is connected.

*Usage:*

```
Digraph$is_connected()
```

*Returns:* TRUE if connected, FALSE if not.

**Method** `is_weakly_connected()`: Test whether the digraph is weakly connected, i.e. if the underlying graph is connected.

*Usage:*

```
Digraph$is_weakly_connected()
```

*Returns:* TRUE if connected, FALSE if not.

**Method** `is_acyclic()`: Checks for the presence of a cycle in the graph by attempting to do a topological sort. If the sort does not contain all vertexes, the digraph contains at least one cycle. This method overrides 'is\_acyclic' in `Graph`.

*Usage:*

```
Digraph$is_acyclic()
```

*Returns:* TRUE if no cycles detected.

**Method** `is_tree()`: Compute whether the digraph's underlying graph is a tree (connected and acyclic).

*Usage:*

```
Digraph$is_tree()
```

*Returns:* TRUE if the underlying graph is a tree; FALSE if not.

**Method** `is_polytree()`: Compute whether the digraph's underlying graph is a tree (connected and acyclic). Synonymous with `'is_graph'`.

*Usage:*

`Digraph$is_polytree()`

*Returns:* TRUE if the underlying graph is a tree; FALSE if not.

**Method** `is_arborescence()`: Check whether the digraph is an arborescence (a tree with a single root and unique paths from the root).

*Usage:*

`Digraph$is_arborescence()`

*Returns:* TRUE if the digraph is an arborescence; FALSE if not.

**Method** `direct_successors()`: Find the direct successors of a node.

*Usage:*

`Digraph$direct_successors(v)`

*Arguments:*

`v` The index vertex.

*Returns:* A list of nodes or an empty list if the specified node has no successors.

**Method** `direct_predecessors()`: Find the direct predecessors of a node.

*Usage:*

`Digraph$direct_predecessors(v)`

*Arguments:*

`v` The index vertex.

*Returns:* A list of nodes or an empty list if the specified node has no predecessors.

**Method** `paths()`: Find all directed paths from source node 's' to target node 't'. In this definition, 'path' is a simple path, i.e. all vertexes are unique. Uses a recursive depth-first search algorithm.

*Usage:*

`Digraph$paths(s, t)`

*Arguments:*

`s` Source node.

`t` Target node.

*Returns:* A list of ordered node lists.

**Method** `walk()`: Construct the sequence of edges which joins the specified sequence of vertexes in this graph.

*Usage:*

`Digraph$walk(P)`

*Arguments:*

`P` A list of Nodes

*Returns:* A list of Edges

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

`Digraph$clone(deep = FALSE)`

*Arguments:*

`deep` Whether to make a deep clone.

**Author(s)**

Andrew Sims <andrew.sims@newcastle.ac.uk>

---

Edge

*Edge*

---

**Description**

An R6 class to represent an edge in a graph.

**Details**

Edges are the formal term for links between pairs of nodes in a graph.

**Methods****Public methods:**

- `Edge$new()`
- `Edge$is_same_edge()`
- `Edge$endpoints()`
- `Edge$label()`
- `Edge$clone()`

**Method** `new()`: Create an object of type 'Edge'.

*Usage:*

```
Edge$new(v1, v2, label = "")
```

*Arguments:*

v1 Node at one endpoint of the edge.

v2 Node at the other endpoint of the edge.

label Character string containing the edge label.

*Returns:* A new 'Edge' object.

**Method** `is_same_edge()`: Is this edge the same as the argument? (DOM-style)

*Usage:*

```
Edge$is_same_edge(e)
```

*Arguments:*

e edge to compare with this one

*Returns:* TRUE if 'e' is also this one.

**Method** `endpoints()`: Retrieve the endpoints of the edge.

*Usage:*

```
Edge$endpoints()
```

*Returns:* List of two nodes to which the edge is connected.

**Method** `label()`: Access label.

*Usage:*

Edge\$label()

*Returns:* Label of the edge; character string.

**Method** clone(): The objects of this class are cloneable with this method.

*Usage:*

Edge\$clone(deep = FALSE)

*Arguments:*

deep Whether to make a deep clone.

### Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

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ExprModVar	<i>ExprModVar</i>
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### Description

An R6 class for a model variable constructed from an expression involving other model variables.

### Details

A class to support expressions involving objects of base class ModVar, which itself behaves like a model variable. For example, if A and B are variables with base class ModVar and c is a variable of type numeric, then it is not possible to write, for example,  $x \leftarrow -42 \cdot A/B + c$ , because R cannot manipulate class variables using the same operators as regular variables. But such forms of expression may be desirable in constructing a model and this class provides a mechanism for doing so.

### Super class

`rdecision::ModVar` -> ExprModVar

### Methods

#### Public methods:

- `ExprModVar$new()`
- `ExprModVar$add_method()`
- `ExprModVar$is_probabilistic()`
- `ExprModVar$operands()`
- `ExprModVar$distribution()`
- `ExprModVar$r()`
- `ExprModVar$mean()`
- `ExprModVar$mode()`
- `ExprModVar$SD()`
- `ExprModVar$quantile()`
- `ExprModVar$mu_hat()`
- `ExprModVar$sigma_hat()`
- `ExprModVar$q_hat()`

- [ExprModVar\\$set\(\)](#)
- [ExprModVar\\$get\(\)](#)
- [ExprModVar\\$clone\(\)](#)

**Method** `new()`: Create a Model Variable formed from an expression involving other model variables.

*Usage:*

```
ExprModVar$new(description, units, quo)
```

*Arguments:*

`description` Name for the model variable expression. In a complex model it may help to tabulate how model variables are combined into costs, probabilities and rates.

`units` Units in which the variable is expressed.

`quo` A quosure (see package `rlang`), which contains an expression and its environment. The usage is `'quo(x+y)'` or `'rlang::quo(x+y)'`.

*Returns:* An object of type `ExprModVar`

**Method** `add_method()`: Create a new quosure from that supplied in `new()` but with each `ModVar` operand appended with `$x` where `x` is the argument to this function.

*Usage:*

```
ExprModVar$add_method(method = "mean()")
```

*Arguments:*

`method` A character string with the method, e.g. `"mean()"`.

*Returns:* A quosure whose expression is each `ModVar` `v` in the expression replaced with `v$method` and the same environment as specified in the quosure supplied in `new()`.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, at least one of which follows a distribution.

*Usage:*

```
ExprModVar$is_probabilistic()
```

*Returns:* TRUE if probabilistic

**Method** `operands()`: Return a list of operands that are themselves `ModVars` given in the expression.

*Usage:*

```
ExprModVar$operands()
```

*Returns:* A list of model variables.

**Method** `distribution()`: Accessor function for the name of the expression model variable.

*Usage:*

```
ExprModVar$distribution()
```

*Returns:* Expression as a character string with all control characters having been removed.

**Method** `r()`: Draw a random sample from the model variable.

*Usage:*

```
ExprModVar$r(n = 1)
```

*Arguments:*

*n* Number of samples to draw.

*Returns:* A sample drawn at random.

**Method** `mean()`: Return the value of the expression when its operands take their mean value (i.e. value returned by call to `mean` or their value, if numeric). See notes on this class for further explanation.

*Usage:*

`ExprModVar$mean()`

*Returns:* Mean value as a numeric value.

**Method** `mode()`: Return the mode of the variable. By default returns NA, which will be the case for most ExprModVar variables, because an arbitrary expression is not guaranteed to be unimodal.

*Usage:*

`ExprModVar$mode()`

*Returns:* Mode as a numeric value.

**Method** `SD()`: Return the standard deviation of the distribution as NA because the variance is not available as a closed form for all functions of distributions.

*Usage:*

`ExprModVar$SD()`

*Returns:* Standard deviation as a numeric value

**Method** `quantile()`: Find quantiles of the uncertainty distribution. Not available as a closed form, and returned as NA.

*Usage:*

`ExprModVar$quantile(probs)`

*Arguments:*

*probs* Numeric vector of probabilities, each in range [0,1].

*Returns:* Vector of numeric values of the same length as 'probs'.

**Method** `mu_hat()`: Return the estimated expected value of the expression variable. This is computed by numerical simulation because there is, in general, no closed form expressions for the mean of a function of distributions.

*Usage:*

`ExprModVar$mu_hat(nest = 1000)`

*Arguments:*

*nest* Sample size to be used to estimate the mean. Values less than 1000 (default) are unlikely to return meaningful estimates and will be rejected.

*Returns:* Expected value as a numeric value.

**Method** `sigma_hat()`: Return the estimated standard deviation of the distribution. This is computed by numerical simulation because there is, in general, no closed form expressions for the SD of a function of distributions.

*Usage:*

`ExprModVar$sigma_hat(nest = 1000)`

*Arguments:*



nest Sample size to be used to estimate the SD. Values less than 1000 (default) are unlikely to return meaningful estimates and will be rejected.

*Returns:* Standard deviation as a numeric value.

**Method** `q_hat()`: Return the estimated quantiles by sampling the variable. This is computed by numerical simulation because there is, in general, no closed form expressions for the quantiles of a function of distributions.

*Usage:*

```
ExprModVar$q_hat(probs, nest = 1000)
```

*Arguments:*

probs Vector of probabilities, in range [0,1].

nest Sample size to be used to estimate the SD. Values less than 1000 (default) are unlikely to return meaningful estimates and will be rejected.

*Returns:* Vector of quantiles.

**Method** `set()`: Sets the value of the ExprModVar that will be returned by subsequent calls to `get()` until `set()` is called again. Because an ExprModVar can be considered as a dependent variable, the idea of setting a value is meaningless, and calls to this method have no effect. To affect the value returned by the next call to `get`, call `set` for each of the operands of this expression.

*Usage:*

```
ExprModVar$set(what = "random")
```

*Arguments:*

what Character string; for compatibility with non-expression ModVars only; not used.

*Returns:* Updated ExprModVar.

**Method** `get()`: Gets the value of the ExprModVar that was set by the most recent call to `set()` to each operand of the expression.

*Usage:*

```
ExprModVar$get()
```

*Returns:* Value determined by last `set()`.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
ExprModVar$clone(deep = FALSE)
```

*Arguments:*

deep Whether to make a deep clone.

## Note

For many expressions involving model variables there will be no closed form expressions for the mean, standard deviation and the quantiles. Therefore they are obtained by simulation, via functions `mu_hat`, `sigma_hat` and `q_hat`.

For consistency with ModVars which are not expressions, the function `mean` returns the value of the expression when all its operands take their mean values. This will, in general, not be the mean of the expression distribution (which can be obtained via `mu_hat`), but is the value normally used in the base case of a model as the point estimate. As Briggs *et al* note (section 4.1.1) "in all but the

most nonlinear models, the difference between the expectation over the output of a probabilistic model and that model evaluated at the mean values of the input parameters, is likely to be modest."

Functions SD, mode and quantile return NA because they do not necessarily have a closed form. The standard deviation can be estimated by calling `sigma_hat` and the quantiles by `q_hat`. Because a unimodal distribution is not guaranteed, there is no estimator provided for the mode.

Method `distribution` returns the string representation of the expression used to create the model variable.

This method is mostly intended for internal use within the class and will not generally be needed for normal use of `ExprModVar` objects. The returned expression is *not* syntactically checked or evaluated before it is returned.

### Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

---

GammaModVar

*GammaModVar*

---

### Description

An R6 class for a model variable with Gamma function uncertainty

### Details

A model variable for which the uncertainty in the point estimate can be modelled with a Gamma distribution. The hyperparameters of the distribution are the shape ('alpha') and the rate ('beta') of the uncertainty distribution. Note that this is the conventional parametrization used in Bayesian statistics; in econometrics the shape/scale ('k'/'theta') parametrization is more common (and the one used in this implementation). Note, however, that although Briggs et al use the shape/scale formulation, they use 'alpha'/'beta' as parameter names.

### Super class

`rdecision:ModVar` -> `GammaModVar`

### Methods

#### Public methods:

- `GammaModVar$new()`
- `GammaModVar$is_probabilistic()`
- `GammaModVar$distribution()`
- `GammaModVar$mean()`
- `GammaModVar$mode()`
- `GammaModVar$SD()`
- `GammaModVar$r()`
- `GammaModVar$quantile()`
- `GammaModVar$clone()`

**Method** `new()`: Create an object of class `GammaModVar`.

*Usage:*

```
GammaModVar$new(description, units, shape, scale)
```

*Arguments:*

description A character string describing the variable.

units Units of the variable, as character string.

shape shape parameter of the Gamma distribution.

scale scale parameter of the Gamma distribution.

*Returns:* An object of class GammaModVar.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, some of which follow distributions.

*Usage:*

```
GammaModVar$is_probabilistic()
```

*Returns:* TRUE if probabilistic

**Method** `distribution()`: Accessor function for the name of the uncertainty distribution.

*Usage:*

```
GammaModVar$distribution()
```

*Returns:* Distribution name as character string.

**Method** `mean()`: Return the expected value of the distribution.

*Usage:*

```
GammaModVar$mean()
```

*Returns:* Expected value as a numeric value.

**Method** `mode()`: Return the mode of the distribution (if shape  $\geq 1$ )

*Usage:*

```
GammaModVar$mode()
```

*Returns:* mode as a numeric value.

**Method** `SD()`: Return the standard deviation of the distribution.

*Usage:*

```
GammaModVar$SD()
```

*Returns:* Standard deviation as a numeric value

**Method** `r()`: Draw a random sample from the model variable.

*Usage:*

```
GammaModVar$r(n = 1)
```

*Arguments:*

n Number of samples to draw.

*Returns:* Samples drawn at random.

**Method** `quantile()`: Return the quantiles of the Gamma uncertainty distribution.

*Usage:*

```
GammaModVar$quantile(probs)
```

*Arguments:*

probs Vector of probabilities, in range [0,1].

*Returns:* Vector of quantiles.

**Method** clone(): The objects of this class are cloneable with this method.

*Usage:*

```
GammaModVar$clone(deep = FALSE)
```

*Arguments:*

deep Whether to make a deep clone.

## Note

The Gamma model variable class can be used to model the uncertainty of the mean of a count quantity which follows a Poisson distribution. The Gamma distribution is the conjugate prior of a Poisson distribution, and the shape and scale relate directly to the number of intervals from which the mean count has been estimated. Specifically, the shape ( $k$ ) is equal to the total count of events in  $1/\theta$  intervals, where  $\theta$  is the scale. For example, if 200 counts were observed in a sample of 100 intervals, setting shape=200 and scale=1/100 gives a Gamma distribution with a mean of 2 and a 95

## Author(s)

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Graph

*Graph*

---

## Description

An R6 class to represent a graph (from discrete mathematics).

## Details

Encapulates and provides methods for computation and checking of undirected graphs. Graphs are systems of vertices connected in pairs by edges.

## Methods

### Public methods:

- [Graph\\$new\(\)](#)
- [Graph\\$vertex\\_index\(\)](#)
- [Graph\\$has\\_vertex\(\)](#)
- [Graph\\$edge\\_index\(\)](#)
- [Graph\\$has\\_edge\(\)](#)
- [Graph\\$order\(\)](#)
- [Graph\\$size\(\)](#)
- [Graph\\$graph\\_adjacency\\_matrix\(\)](#)
- [Graph\\$is\\_simple\(\)](#)

- `Graph$is_connected()`
- `Graph$is_acyclic()`
- `Graph$is_tree()`
- `Graph$degree()`
- `Graph$neighbours()`
- `Graph$clone()`

**Method** `new()`: Create a new Graph object from sets of nodes and edges.

*Usage:*

`Graph$new(V, E)`

*Arguments:*

V A list of Nodes.

E A list of Edges.

*Returns:* A Graph object.

**Method** `vertex_index()`: Find the index of a vertex in the graph.

*Usage:*

`Graph$vertex_index(v)`

*Arguments:*

v Subject vertex

*Returns:* Index of v. The vertexes are normally stored in the same order they are specified in new, but this cannot be guaranteed. This function returns the same index as used in the adjacency matrix and NA if the vertex is not in the graph.

**Method** `has_vertex()`: Test whether a vertex is an element of the graph.

*Usage:*

`Graph$has_vertex(v)`

*Arguments:*

v Subject vertex.

*Returns:* TRUE if v is an element of V(G).

**Method** `edge_index()`: Find the index of an edge in a graph.

*Usage:*

`Graph$edge_index(e)`

*Arguments:*

e Subject edge.

*Returns:* Index of e. The edges are normally stored in the same order they are specified in new, but this cannot be guaranteed. This function returns the same index returned in other functions and NA if the edge is not in the graph.

**Method** `has_edge()`: Test whether an edge is element of the graph.

*Usage:*

`Graph$has_edge(e)`

*Arguments:*

e Subject edge.

*Returns:* TRUE if  $e$  is an element of  $E(G)$ .

**Method** `order()`: Return the order of the graph (number of vertices).

*Usage:*

`Graph$order()`

*Returns:* Order of the graph (integer).

**Method** `size()`: Return the size of the graph (number of edges).

*Usage:*

`Graph$size()`

*Returns:* Size of the graph (integer).

**Method** `graph_adjacency_matrix()`: Compute the adjacency matrix for the graph. Each cell contains the number of edges joining the two vertexes, with the convention of self loops being counted twice, unless 'binary' is TRUE when cells are either 0 (not adjacent) or 1 (adjacent).

*Usage:*

`Graph$graph_adjacency_matrix(bootstrap = FALSE)`

*Arguments:*

`bootstrap` If TRUE, the adjacency matrix is logical, each cell is FALSE,TRUE.

*Returns:* A square numeric matrix with the number of rows and columns equal to the order of the graph. The rows and columns are in the same order as `V`. If the nodes have defined and unique labels the dimnames of the matrix are the labels of the nodes.

**Method** `is_simple()`: A simple graph has no self loops or multi-edges.

*Usage:*

`Graph$is_simple()`

*Returns:* TRUE if simple, FALSE if not.

**Method** `is_connected()`: Test whether the graph is connected. Graphs with no vertices are considered unconnected; graphs with 1 vertex are considered connected. Otherwise a graph is connected if all nodes can be reached from an arbitrary starting point. Uses a depth first search.

*Usage:*

`Graph$is_connected()`

*Returns:* TRUE if connected, FALSE if not.

**Method** `is_acyclic()`: Checks for the presence of a cycle in the graph using a depth-first search from each node to detect the presence of back edges. A back edge is an edge from the current node joining a previously detected (visited) node, that is not the parent node of the current one.

*Usage:*

`Graph$is_acyclic()`

*Returns:* TRUE if no cycles detected.

**Method** `is_tree()`: Compute whether the graph is connected and acyclic.

*Usage:*

`Graph$is_tree()`

*Returns:* TRUE if the graph is a tree; FALSE if not.

**Method** `degree()`: The degree of a vertex in the graph, or number of incident edges.

*Usage:*

Graph\$degree(v)

*Arguments:*

v The subject node.

*Returns:* Degree of the vertex, integer.

**Method** neighbours(): Find the neighbours of a node. A property of the graph, not the node. Does not include self, even in the case of a loop to self.

*Usage:*

Graph\$neighbours(v)

*Arguments:*

v The subject node.

*Returns:* A list of nodes which are joined to the subject.

**Method** clone(): The objects of this class are cloneable with this method.

*Usage:*

Graph\$clone(deep = FALSE)

*Arguments:*

deep Whether to make a deep clone.

## Author(s)

Andrew Sims <andrew.sims@newcastle.ac.uk>

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LeafNode

*LeafNode*

---

## Description

An R6 class for a leaf node in a decision tree representing a clinical state.

## Details

It represents a state of being, and is associated with an incremental utility.

## Super class

`rdecision::Node` -> LeafNode

## Methods

### Public methods:

- `LeafNode$new()`
- `LeafNode$modvars()`
- `LeafNode$utility()`
- `LeafNode$clone()`

**Method** new(): Create a new LeafNode object; synonymous with a clinical outcome.

*Usage:*

```
LeafNode$new(
  label,
  utility = 1,
  interval = as.difftime(365.25, units = "days")
)
```

*Arguments:*

**label** Character string; a label for the state; must be defined because it is used in tabulations. The label is automatically converted to a syntactically valid (in R) name to ensure it can be used as a column name in a data frame.

**utility** The incremental utility that a user associates with being in the health state (range -Inf to 1) for the interval. Intended for use with cost benefit analysis.

**interval** The time interval over which the utility parameters apply, expressed as an R difftime object; default 1 year.

*Returns:* A new LeafNode object

**Method** `modvars()`: Find all the model variables of type ModVar that have been specified as values associated with this LeafNode. Includes operands of these ModVars, if they are expressions.

*Usage:*

```
LeafNode$modvars()
```

*Returns:* A list of ModVars.

**Method** `utility()`: Return the incremental utility associated with being in the state for the interval.

*Usage:*

```
LeafNode$utility(expected)
```

*Arguments:*

**expected** Parameter passed to the value method of the model variable used to define utility; ignored otherwise.

*Returns:* Incremental utility (numeric value).

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
LeafNode$clone(deep = FALSE)
```

*Arguments:*

**deep** Whether to make a deep clone.

**Author(s)**

Andrew J. Sims <andrew.sims@newcastle.ac.uk>



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LogNormModVar	LogNormModVar
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## Description

An R6 class for a model variable with Log Normal uncertainty

## Details

A model variable for which the uncertainty in the point estimate can be modelled with a Log Normal distribution. [ProbOnto \(2017\)](#) defines seven parametrizations of the log normal distribution. These are linked, allowing the parameters of any one to be derived from any other. All 7 parametrizations require two parameters; their meanings are as follows:

**LN1**  $p_1 = \mu, p_2 = \sigma$ , where  $\mu$  and  $\sigma$  are the mean and standard deviation, both on the log scale.

**LN2**  $p_1 = \mu, p_2 = v$ , where  $\mu$  and  $v$  are the mean and variance, both on the log scale.

**LN3**  $p_1 = m, p_2 = \sigma$ , where  $m$  is the median on the natural scale and  $\sigma$  is the standard deviation on the log scale.

**LN4**  $p_1 = m, p_2 = c_v$ , where  $m$  is the median on the natural scale and  $c_v$  is the coefficient of variation on the natural scale.

**LN5**  $p_1 = \mu, p_2 = \tau$ , where  $\mu$  is the mean on the log scale and  $\tau$  is the precision on the log scale.

**LN6**  $p_1 = m, p_2 = \sigma_g$ , where  $m$  is the median on the natural scale and  $\sigma_g$  is the geometric standard deviation on the natural scale.

**LN7**  $p_1 = \mu_N, p_2 = \sigma_N$ , where  $\mu_N$  is the mean on the natural scale and  $\sigma_N$  is the standard deviation on the natural scale.

## Super class

`rdecision::ModVar` -> LogNormModVar

## Methods

### Public methods:

- `LogNormModVar$new()`
- `LogNormModVar$is_probabilistic()`
- `LogNormModVar$distribution()`
- `LogNormModVar$r()`
- `LogNormModVar$mean()`
- `LogNormModVar$mode()`
- `LogNormModVar$SD()`
- `LogNormModVar$quantile()`
- `LogNormModVar$clone()`

**Method** `new()`: Create a model variable with log normal uncertainty.

*Usage:*

```
LogNormModVar$new(description, units, p1, p2, parametrization = "LN1")
```

*Arguments:*

description A character string describing the variable.  
 units Units of the quantity; character string.  
 p1 First hyperparameter, a measure of location. See 'Details'.  
 p2 Second hyperparameter, a measure of spread. See 'Details'.  
 parametrization A character string taking one of the values 'LN1' (default) through 'LN7' (see 'Details').

*Returns:* A LogNormModVar object.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, some of which follow distributions.

*Usage:*

```
LogNormModVar$is_probabilistic()
```

*Returns:* TRUE if probabilistic

**Method** `distribution()`: Accessor function for the name of the uncertainty distribution.

*Usage:*

```
LogNormModVar$distribution()
```

*Returns:* Distribution name as character string (LN1, LN2 etc).

**Method** `r()`: Draw a random sample from the model variable.

*Usage:*

```
LogNormModVar$r(n = 1)
```

*Arguments:*

n Number of samples to draw.

*Returns:* A sample drawn at random.

**Method** `mean()`: Return the expected value of the distribution.

*Usage:*

```
LogNormModVar$mean()
```

*Returns:* Expected value as a numeric value.

**Method** `mode()`: Return the point estimate of the variable.

*Usage:*

```
LogNormModVar$mode()
```

*Returns:* Point estimate (mode) of the LN distribution.

**Method** `SD()`: Return the standard deviation of the distribution.

*Usage:*

```
LogNormModVar$SD()
```

*Returns:* Standard deviation as a numeric value

**Method** `quantile()`: Return the quantiles of the logNormal uncertainty distribution.

*Usage:*

```
LogNormModVar$quantile(probs)
```

*Arguments:*

`probs` Vector of probabilities, in range [0,1].

*Returns:* Vector of quantiles.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
LogNormModVar$new(clone(deep = FALSE))
```

*Arguments:*

`deep` Whether to make a deep clone.

## Note

The log normal distribution may be used to model the uncertainty in an estimate of relative risk (Briggs 2006, p90). If a relative risk estimate is available with a 95 allows the uncertainty distribution to be specified directly. For example, if  $RR = 0.67$  with 95 can be modelled with `LogNormModVar$new("rr", "RR", p`

## Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

## References

- Briggs A, Claxton K and Sculpher M. Decision Modelling for Health Economic Evaluation. Oxford 2006, ISBN 978-0-19-852662-9.
- Leaper DJ, Edmiston CE and Holy CE. Meta-analysis of the potential economic impact following introduction of absorbable antimicrobial sutures. British Journal of Surgery 2017;104:e134-e144.
- Swat MJ, Grenon P and Wimalaratne S. Ontology and Knowledge Base of Probability Distributions. EMBL-EBI Technical Report (ProbOnto 2.5), 13th January 2017, <https://sites.google.com/site/probonto/doc>

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ModVar

*ModVar*

---

## Description

An R6 class for a variable in an health economic model

## Details

Base class for a variable used in a health economic model. The base class, which is not intended to be directly instantiated by model applications, wraps a numerical value which is used in calculations. The base class provides a framework for creating classes of model variables whose uncertainties are described by statistical distributions parametrized with hyperparameters.

## Methods

### Public methods:

- `ModVar$new()`
- `ModVar$is_expression()`
- `ModVar$is_probabilistic()`
- `ModVar$description()`
- `ModVar$units()`
- `ModVar$distribution()`
- `ModVar$r()`
- `ModVar$mean()`
- `ModVar$mode()`
- `ModVar$SD()`
- `ModVar$quantile()`
- `ModVar$set()`
- `ModVar$get()`
- `ModVar$clone()`

**Method** `new()`: Create an object of type 'ModVar'

*Usage:*

```
ModVar$new(description, units)
```

*Arguments:*

`description` A character string description of the variable and its role in the model. This description will be used in a tabulation of the variables linked to a model.

`units` A character string description of the units, e.g. 'GBP', 'per year'.

*Returns:* A new ModVar object.

**Method** `is_expression()`: Is this ModVar an expression?

*Usage:*

```
ModVar$is_expression()
```

*Returns:* TRUE if it inherits from ExprModVar, FALSE otherwise.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, some of which follow distributions.

*Usage:*

```
ModVar$is_probabilistic()
```

*Returns:* TRUE if probabilistic

**Method** `description()`: Accessor function for the description.

*Usage:*

```
ModVar$description()
```

*Returns:* Description of model variable as character string.

**Method** `units()`: Accessor function for units.

*Usage:*

```
ModVar$units()
```

*Returns:* Description of units as character string.

**Method** `distribution()`: Accessor function for the name of the uncertainty distribution.

*Usage:*

```
ModVar$distribution()
```

*Returns:* Distribution name as character string.

**Method** `r()`: Draw a random sample from the model variable.

*Usage:*

```
ModVar$r(n = 1)
```

*Arguments:*

`n` Number of samples to draw.

*Returns:* A sample drawn at random.

**Method** `mean()`: Return the mean value of the distribution.

*Usage:*

```
ModVar$mean()
```

*Returns:* Mean value as a numeric value.

**Method** `mode()`: Return the mode of the variable. By default returns NA, which will be the case for most ExprModVar variables, because an arbitrary expression is not guaranteed to be unimodal.

*Usage:*

```
ModVar$mode()
```

*Returns:* Mode as a numeric value.

**Method** `SD()`: Return the standard deviation of the distribution.

*Usage:*

```
ModVar$SD()
```

*Returns:* Standard deviation as a numeric value

**Method** `quantile()`: Find quantiles of the uncertainty distribution.

*Usage:*

```
ModVar$quantile(probs)
```

*Arguments:*

`probs` Numeric vector of probabilities, each in range [0,1].

*Returns:* Vector of numeric values of the same length as 'probs'.

**Method** `set()`: Sets the value of the ModVar that will be returned by subsequent calls to `get()` until `set()` is called again.

*Usage:*

```
ModVar$set(what = "random")
```

*Arguments:*

`what` Character: one of "random" (samples from the uncertainty distribution), "expected" (mean), "q2.5" (lower 95 "q50" (median), "q97.5" (upper 95 the value unchanged). The "current" option is provided to support having common functions to set (or leave alone) sets of model variables, depending on their use case.

*Returns:* Updated ModVar.

**Method** `get()`: Gets the value of the ExprModVar that was set by the most recent call to `set()`.

*Usage:*

`ModVar$get()`

*Returns:* Value determined by last `set()`.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

`ModVar$clone(deep = FALSE)`

*Arguments:*

`deep` Whether to make a deep clone.

### Author(s)

Andrew Sims <andrew.sims@newcastle.ac.uk>

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Node	<i>Node</i>
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### Description

An R6 class to represent a node in a decision tree

### Details

Base class to represent a single node in a decision tree. Objects of base class Node are not expected to be created as model objects.

### Methods

#### Public methods:

- [Node\\$new\(\)](#)
- [Node\\$label\(\)](#)
- [Node\\$type\(\)](#)
- [Node\\$clone\(\)](#)

**Method** `new()`: Create new Node object.

*Usage:*

`Node$new(label = "")`

*Arguments:*

`label` An optional label for the node.

*Returns:* A new Node object.

**Method** `label()`: Return the label of the node.

*Usage:*

`Node$label()`

*Returns:* Label as a character string.

**Method** type(): node type

*Usage:*

Node\$type()

*Returns:* Node class, as character string

**Method** clone(): The objects of this class are cloneable with this method.

*Usage:*

Node\$clone(deep = FALSE)

*Arguments:*

deep Whether to make a deep clone.

### Author(s)

Andrew Sims <andrew.sims@newcastle.ac.uk>

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NormModVar	<i>NormModVar</i>
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### Description

An R6 class for a model variable with Normal uncertainty

### Details

A model variable for which the uncertainty in the point estimate can be modelled with a Normal distribution. The hyperparameters of the distribution are the mean ('mu') and the standard deviation ('sd') of the uncertainty distribution. The value of 'mu' is the expected value of the variable.

### Super class

`rdecision::ModVar` -> NormModVar

### Methods

#### Public methods:

- NormModVar\$new()
- NormModVar\$is\_probabilistic()
- NormModVar\$distribution()
- NormModVar\$r()
- NormModVar\$mean()
- NormModVar\$SD()
- NormModVar\$quantile()
- NormModVar\$clone()

**Method** new(): Create a model variable with normal uncertainty.

*Usage:*

NormModVar\$new(description, units, mu, sigma)

*Arguments:*

*description* A character string describing the variable.

*units* Units of the quantity; character string.

*mu* Hyperparameter with mean of the Normal distribution for the uncertainty of the variable.

*sigma* Hyperparameter equal to the standard deviation of the normal distribution for the uncertainty of the variable.

*Returns:* A NormModVar object.

**Method** `is_probabilistic()`: Tests whether the model variable is probabilistic, i.e. a random variable that follows a distribution, or an expression involving random variables, some of which follow distributions.

*Usage:*

```
NormModVar$is_probabilistic()
```

*Returns:* TRUE if probabilistic

**Method** `distribution()`: Accessor function for the name of the uncertainty distribution.

*Usage:*

```
NormModVar$distribution()
```

*Returns:* Distribution name as character string.

**Method** `r()`: Draw a random sample from the model variable. Normally accessed by a call to `value(what="r")`.

*Usage:*

```
NormModVar$r(n = 1)
```

*Arguments:*

*n* Number of samples to draw.

*Returns:* A sample drawn at random.

**Method** `mean()`: Return the mean value of the distribution.

*Usage:*

```
NormModVar$mean()
```

*Returns:* Expected value as a numeric value.

**Method** `SD()`: Return the standard deviation of the distribution.

*Usage:*

```
NormModVar$SD()
```

*Returns:* Standard deviation as a numeric value

**Method** `quantile()`: Return the quantiles of the Normal uncertainty distribution.

*Usage:*

```
NormModVar$quantile(probs)
```

*Arguments:*

*probs* Vector of probabilities, in range [0,1].

*Returns:* Vector of quantiles.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
NormModVar$clone(deep = FALSE)
```

*Arguments:*

*deep* Whether to make a deep clone.



**Author(s)**

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

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rdecision

*rdecision: Decision Analytic Modelling in Health Economics.*


---

**Description**

Classes and functions for modelling healthcare interventions using cohort models (decision trees, Markov models and extended Markov models). It draws on terminology from Briggs, Claxton and Sculpher, "Decision Modelling for Health Economic Evaluation", Oxford University Press, 2006.

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Reaction

*Reaction*


---

**Description**

An R6 class to represent a reaction (chance) edge in a decision tree.

**Details**

A specialism of class Arrow which is used in a decision tree to represent edges with source nodes joined to ChanceNodes.

**Super classes**

`rdecision::Edge` -> `rdecision::Arrow` -> `Reaction`

**Methods****Public methods:**

- `Reaction$new()`
- `Reaction$modvars()`
- `Reaction$p()`
- `Reaction$cost()`
- `Reaction$benefit()`
- `Reaction$clone()`

**Method** `new()`: Create an object of type 'Reaction'. A probability must be assigned to the edge. Optionally, a cost and a benefit may be associated with traversing the edge. A *payoff* (benefit-cost) is sometimes used in edges of decision trees; the parametrization used here is more general.

*Usage:*

```
Reaction$new(source, target, p, cost = 0, benefit = 0, label = "")
```

*Arguments:*

source Chance node from which the arrow leaves.

target Node which the arrow enters.

p Probability

**cost** Cost associated with traversal of this edge.

**benefit** Benefit associated with traversal of the edge.

**label** Character string containing the arrow label.

*Returns:* A new Reaction object.

**Method** `modvars()`: Find all the model variables of type `ModVar` that have been specified as values associated with this Action. Includes operands of these `ModVars`, if they are expressions.

*Usage:*

`Reaction$modvars()`

*Returns:* A list of `ModVars`.

**Method** `p()`: Return the current value of the edge probability, i.e. the conditional probability of traversing the edge.

*Usage:*

`Reaction$p()`

*Returns:* Numeric value in range [0,1].

**Method** `cost()`: Return the cost associated with traversing the edge.

*Usage:*

`Reaction$cost()`

*Returns:* Cost.

**Method** `benefit()`: Return the benefit associated with traversing the edge.

*Usage:*

`Reaction$benefit()`

*Returns:* Benefit.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

`Reaction$clone(deep = FALSE)`

*Arguments:*

**deep** Whether to make a deep clone.

### Author(s)

Andrew J. Sims <andrew.sims@newcastle.ac.uk>

---

Stack	A stack class.
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---

## Description

An R6 class to represent a stack of objects of any type.

## Details

Conventional implementation of a stack. Used extensively in graph algorithms and offered as a separate class for ease of programming and to ensure that implementations of stacks are optimized. By intention, there is only minimal checking of method arguments. This is to maximize performance and because the class is mainly intended for use internally to 'rdecision'.

## Methods

### Public methods:

- `Stack$new()`
- `Stack$push()`
- `Stack$pop()`
- `Stack$size()`
- `Stack$as_list()`
- `Stack$clone()`

**Method** `new()`: Create a stack.

*Usage:*

`Stack$new()`

*Returns:* A new Stack object.

**Method** `push()`: Push an item onto the stack.

*Usage:*

`Stack$push(x)`

*Arguments:*

x The item to push onto the top of the stack. It should be of the same class as items previously pushed on to the stack. It is not checked.

*Returns:* An updated Stack object

**Method** `pop()`: Pop an item from the stack. Note that stack underflow is not checked.

*Usage:*

`Stack$pop()`

*Returns:* The item previously at the top of the stack.

**Method** `size()`: Gets the number of items on the stack.

*Usage:*

`Stack$size()`

*Returns:* Number of items.

**Method** `as_list()`: Inspect items in the stack.

*Usage:*

```
Stack$as_list()
```

*Returns:* A list of items.

**Method** `clone()`: The objects of this class are cloneable with this method.

*Usage:*

```
Stack$clone(deep = FALSE)
```

*Arguments:*

`deep` Whether to make a deep clone.

**Author(s)**

Andrew Sims <andrew.sims@newcastle.ac.uk>

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