

To prepare:

Check out the github directory for this module -
<https://github.com/alanrogers/agar22/tree/main/introgression>

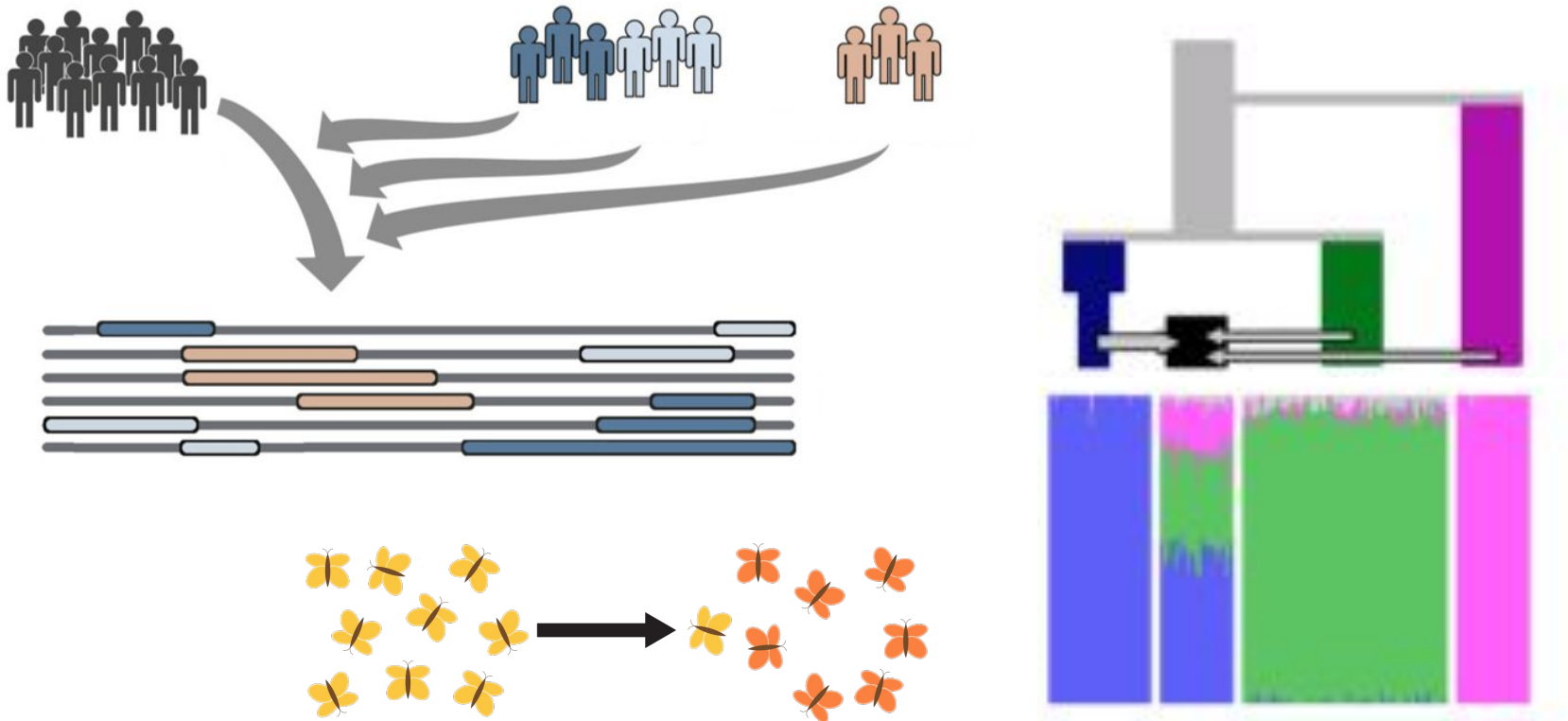
Download all necessary materials

- Exercise document
- All .R and .py scripts

Install all necessary software

- R and RStudio
- python3 (conda)
- msprime (conda)
- plink (conda)
- admixture (conda)
- vcftools (conda)
- rfmix (conda)

Module 4: Population genomics of admixture and introgression



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AGAR Workshop, July 28th 2022

Outline

Part 1:

Population genetics and evolutionary forces (~1 hr)

Part 2:

Gene flow (~2 hrs)

**** We will have two breaks ****

Part 1 objectives

- Understand **genetic drift** and its effects on patterns of **neutral diversity**
- Understand how **demographic parameters** impact drift and **population differentiation**
- Predict the effect of demography on F_{ST} between two populations

Population genetics examines patterns of **genetic variation** within and between populations to understand how they are shaped over time by **fundamental mechanisms of evolution**

Populations evolve by four main mechanisms:

1. Mutation
2. Selection
3. Drift
4. Migration

Mutation

- Generates **new variation** within a population
- Generally parametrized by a **single fixed rate**

AGAGTGCGGTCCGGGGCGCC



AGAGCGCGGTCCGGGGCGCC



AGAGCGCGGTCCGGGACGCC

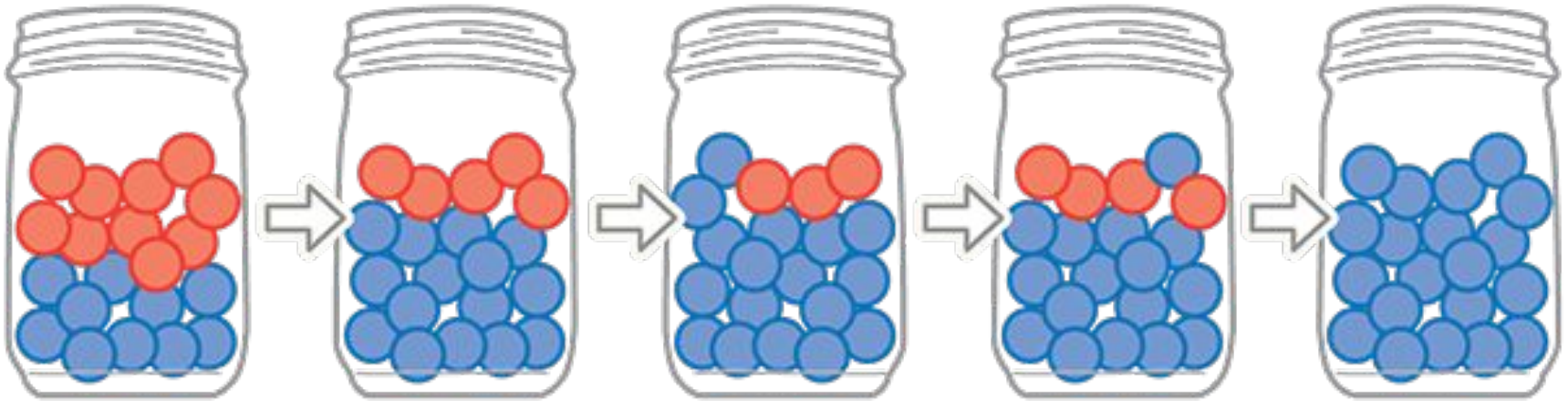
Selection

- Favours **certain alleles** over others, causing them to **increase in frequency**

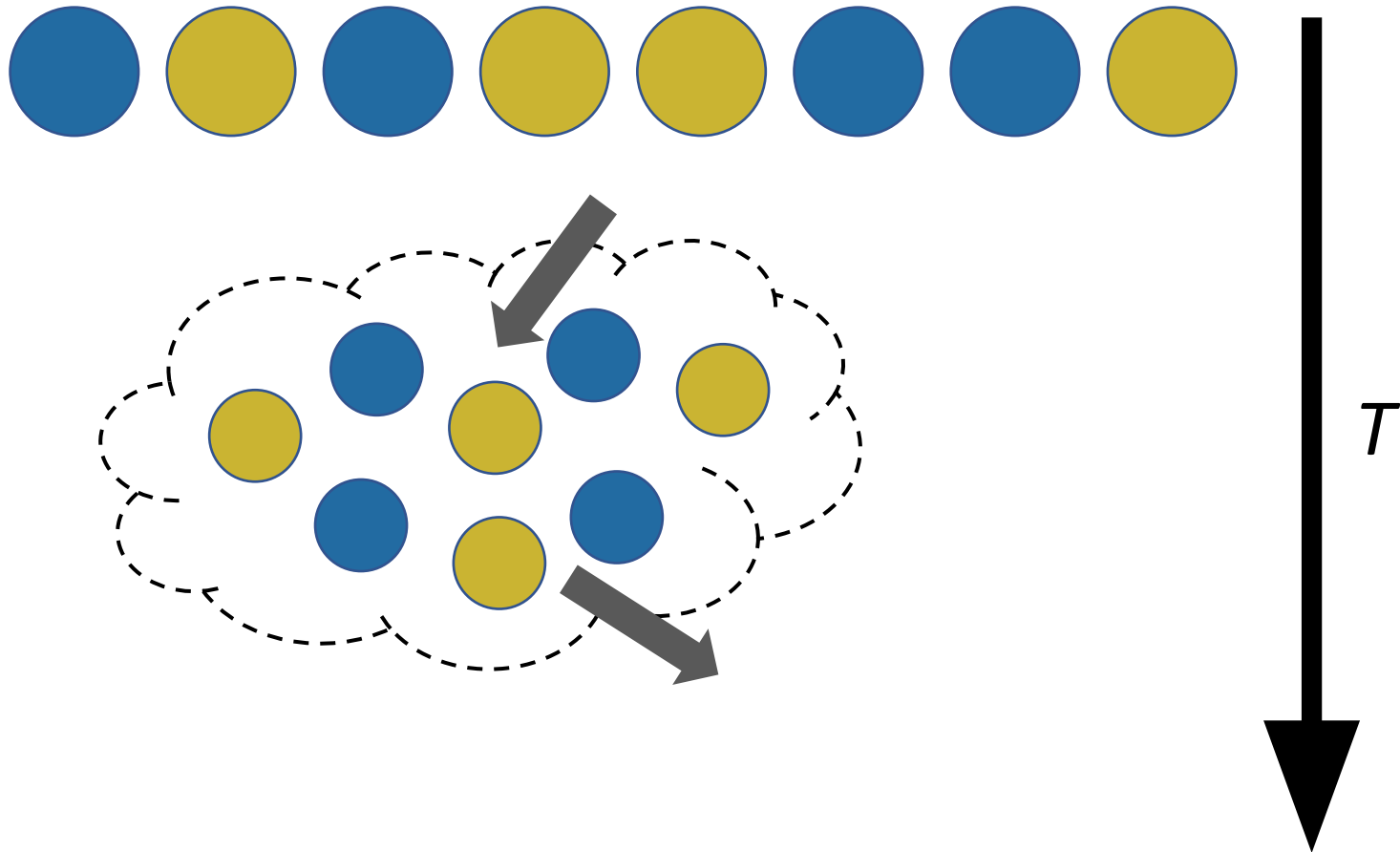


Genetic drift

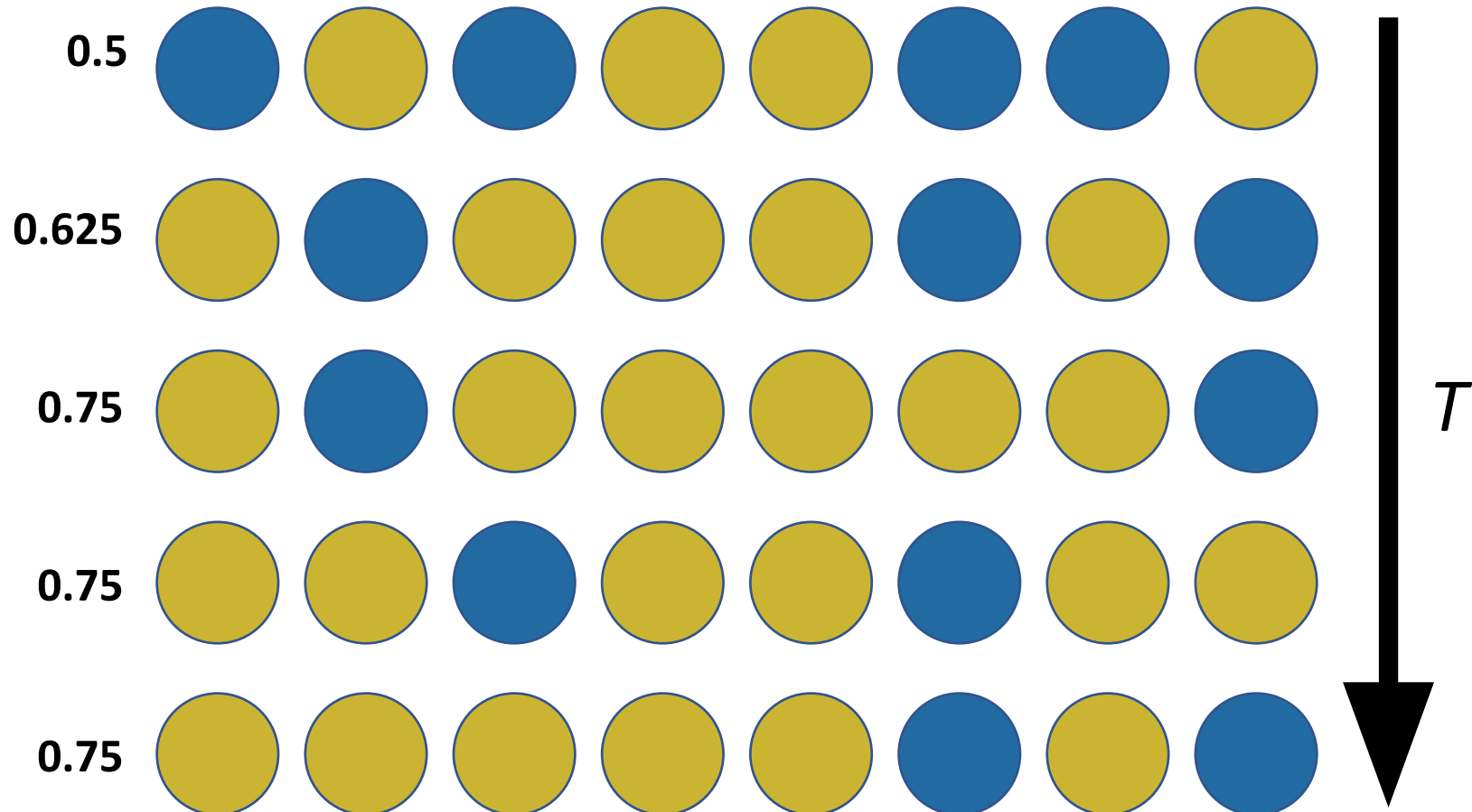
- **Stochastic change** in allele frequency due to the effect of sampling a **finite population**
- A completely **neutral** process



Genetic drift

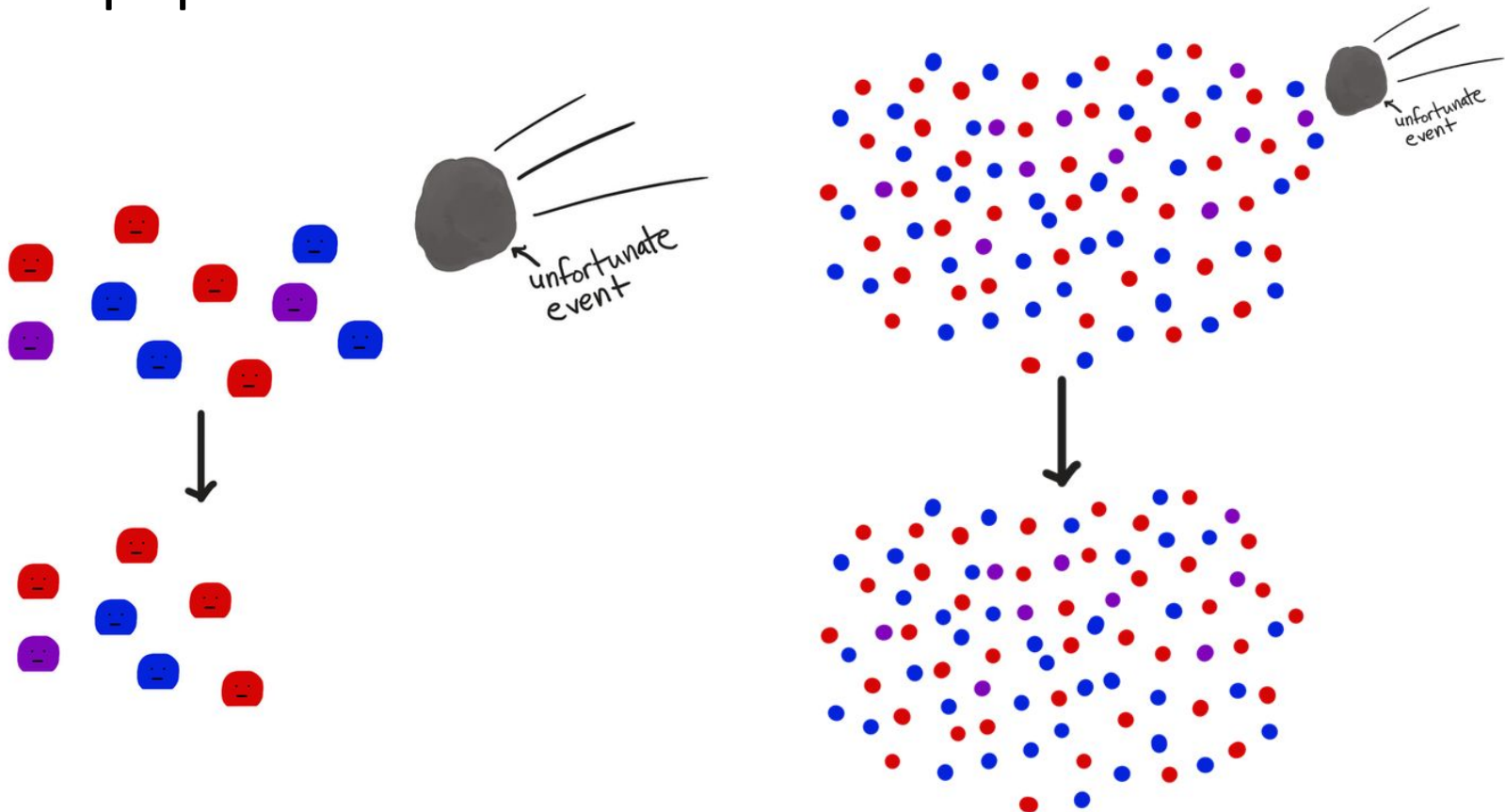


Genetic drift



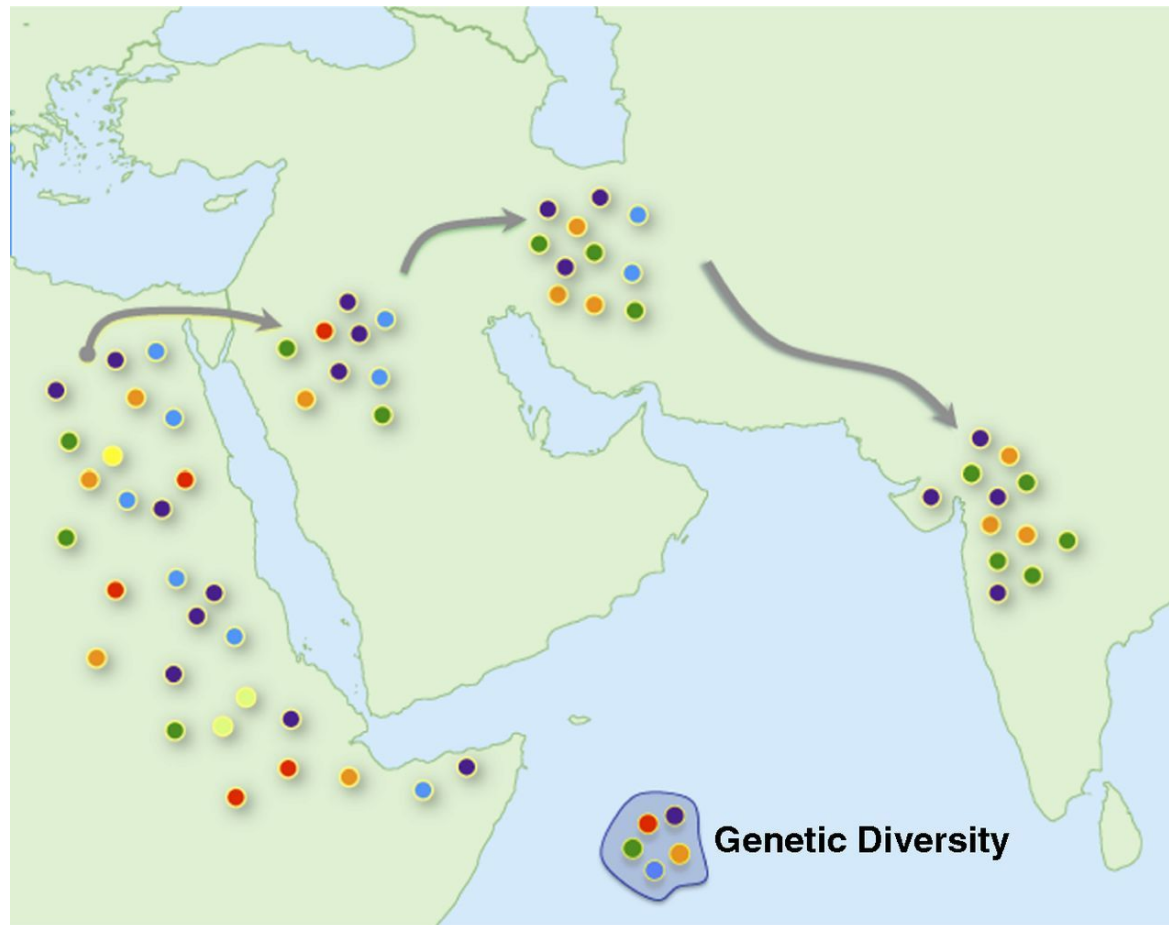
Genetic drift

- The effect of drift is **stronger** in **smaller** populations



Genetic drift

- Founder effects and bottlenecks



From Henn et al.
2012, PNAS

What is effective population size (N_e)?

- A **theoretical** population parameter
- The size that an **idealised** (i.e. Wright-Fisher) population would need to be in order to exhibit the **same qualities** as the real population
- These qualities generally derive from patterns of **neutral genetic diversity**, such as nucleotide diversity

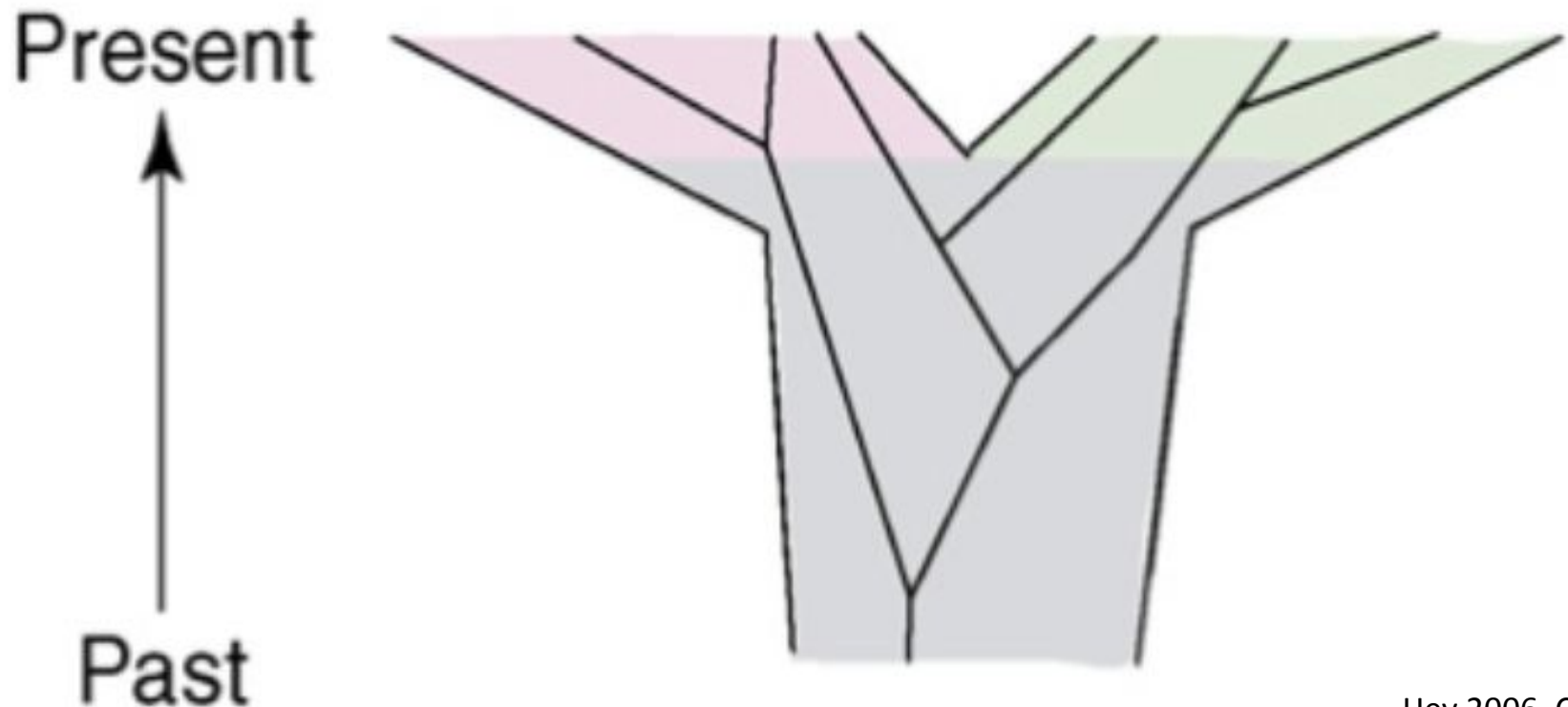
Exercise 1

~20 min.

github.com/alanrogers/agar22/tree/main/introgression

Population divergence

- A single population **splitting** into multiple populations and **evolving independently**



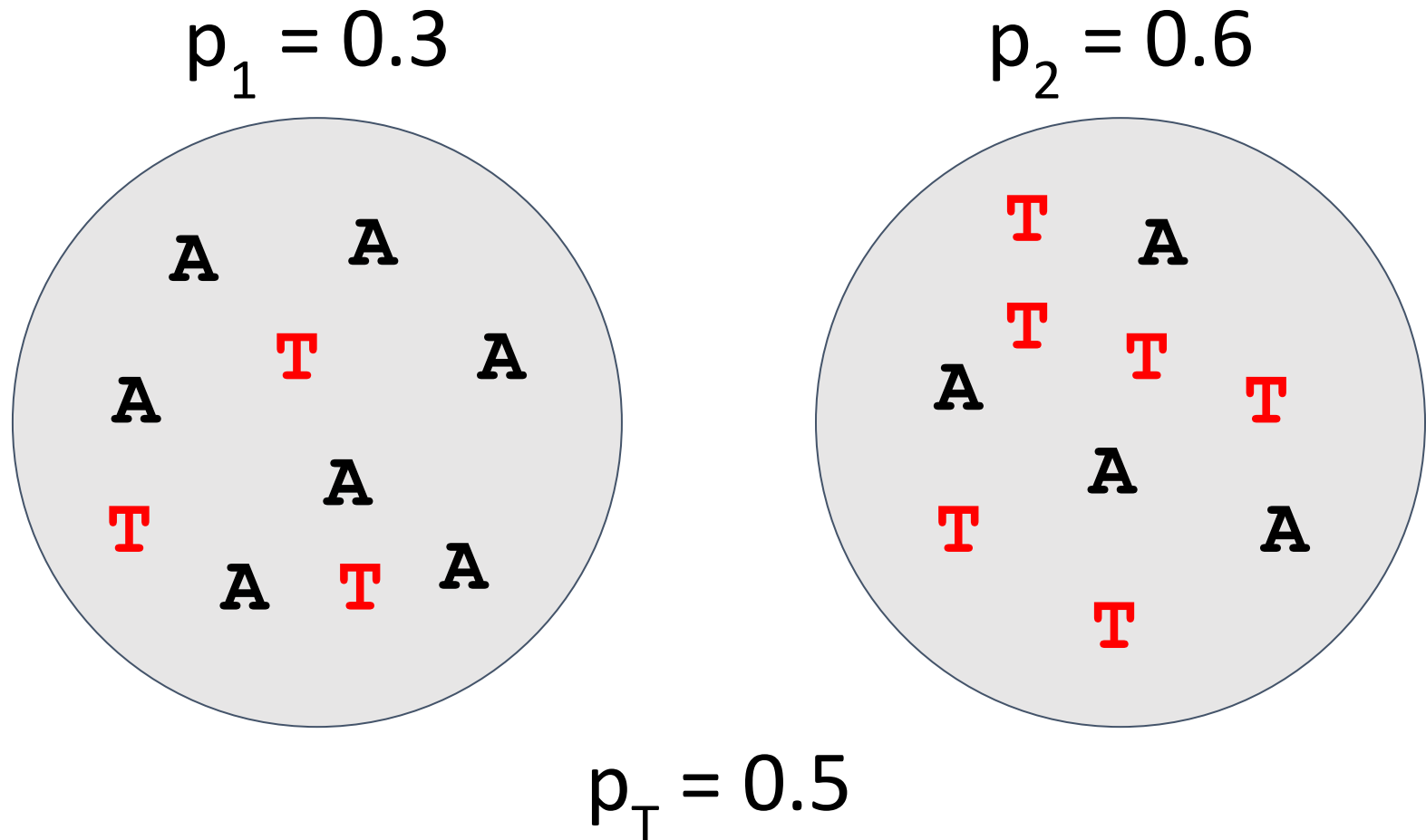
Population divergence

- F_{ST} is a measure of divergence calculated from allele frequencies across populations

$$F_{ST} = \frac{\text{total variance} - \text{within-pop variance}}{\text{total variance}}$$

$$F_{ST} = \frac{H_T - H_S}{H_T}$$

Population divergence



Population divergence

Hardy-Weinberg equilibrium for biallelic locus

$$p + q = 1$$

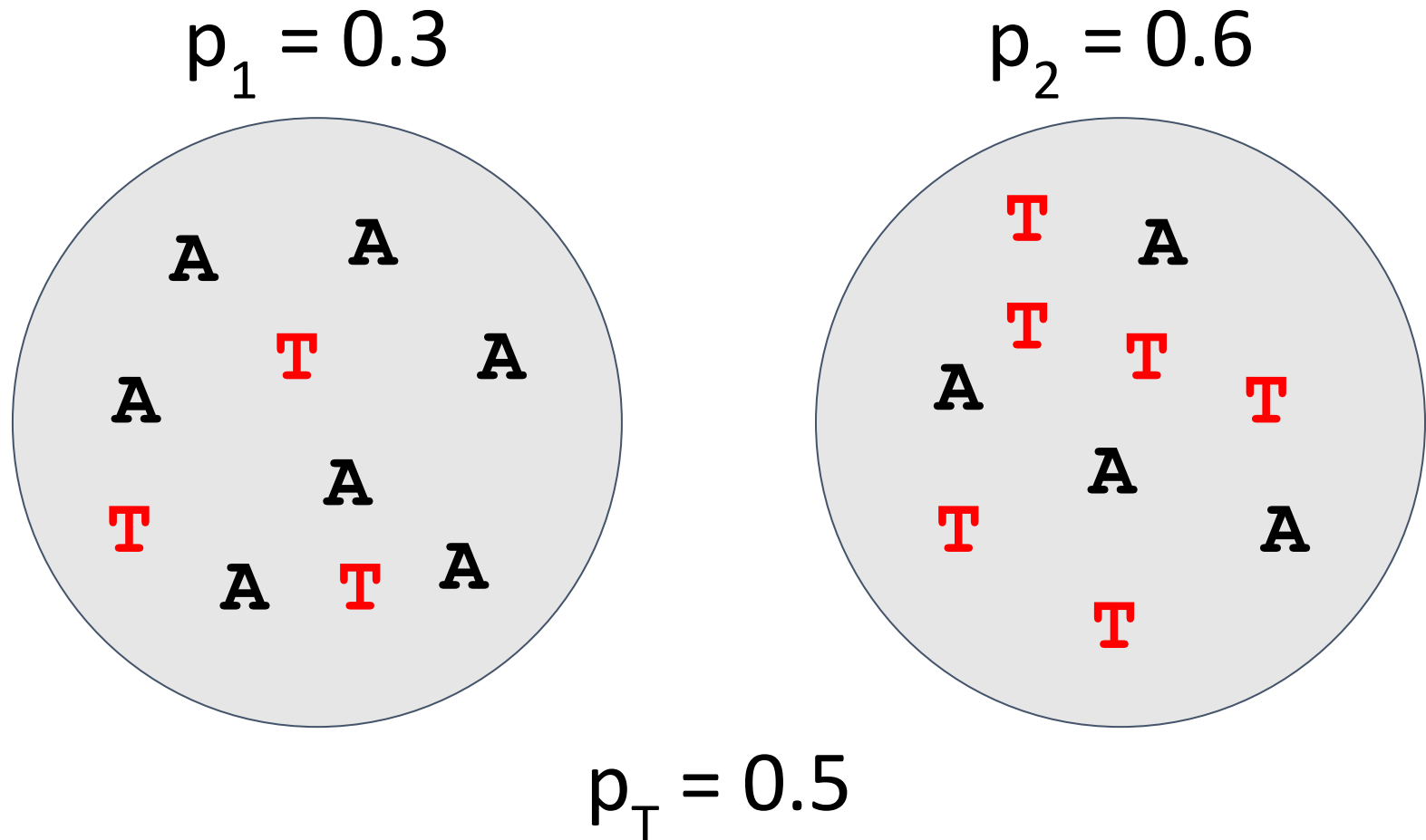
$$f_{AA} + f_{Aa} + f_{aa} = 1$$

$$f_{AA} = p^2$$

$$f_{aa} = q^2$$

$$f_{Aa} = 2pq$$

Population divergence



Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

$$H_1 = 2(0.3)(0.7)$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

$$H_1 = 2(0.3)(0.7)$$

$$H_1 = 0.42$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

$$H_2 = 2p_2q_1$$

$$H_1 = 2(0.3)(0.7)$$

$$H_2 = 2(0.6)(0.4)$$

$$H_1 = 0.42$$

$$H_2 = 0.48$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

$$H_2 = 2p_2q_1$$

$$H_1 = 2(0.3)(0.7)$$

$$H_2 = 2(0.6)(0.4)$$

$$H_1 = 0.42$$

$$H_2 = 0.48$$

$$H_s = (0.42 + 0.48) / 2 = 0.45$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

$$H_2 = 2p_2q_1$$

$$H_1 = 2(0.3)(0.7)$$

$$H_2 = 2(0.6)(0.4)$$

$$H_1 = 0.42$$

$$H_2 = 0.48$$

$$H_s = (0.42 + 0.48) / 2 = 0.45$$

$$H_T = 2(0.5)(0.5) = 0.5$$

Population divergence

$$p_1 = 0.3$$

$$p_2 = 0.6$$

$$p_T = 0.5$$

$$H_1 = 2p_1q_1$$

$$H_2 = 2p_2q_1$$

$$H_1 = 2(0.3)(0.7)$$

$$H_2 = 2(0.6)(0.4)$$

$$H_1 = 0.42$$

$$H_2 = 0.48$$

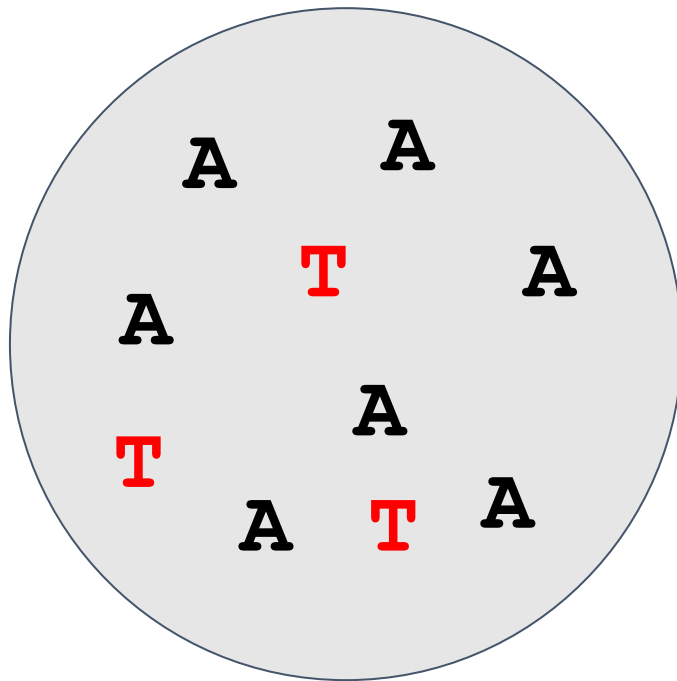
$$H_s = (0.42 + 0.48) / 2 = 0.45$$

$$H_T = 2(0.5)(0.5) = 0.5$$

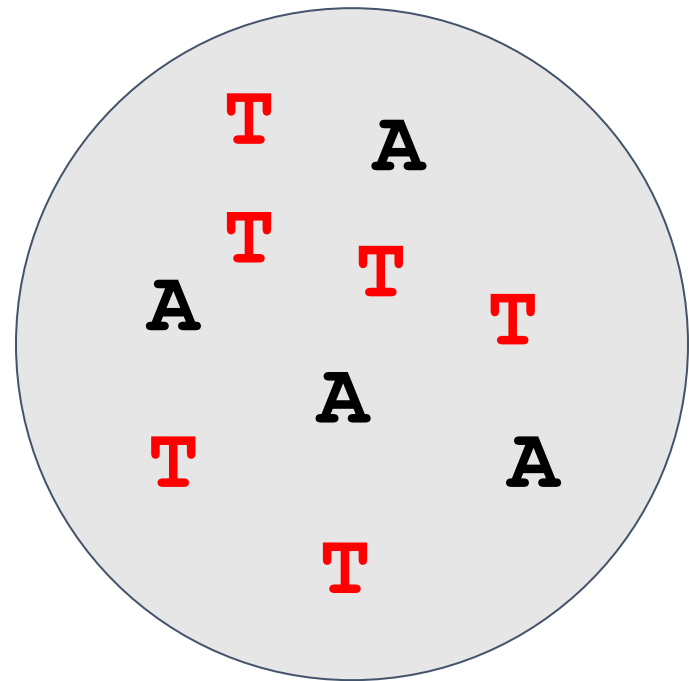
$$F_{ST} = (0.5 - 0.45) / 0.5 = 0.1$$

Population divergence

$$p_1 = 0.3$$

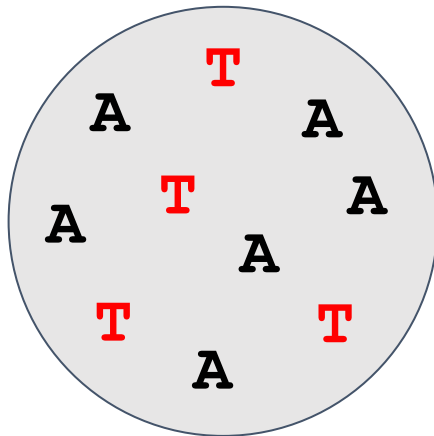
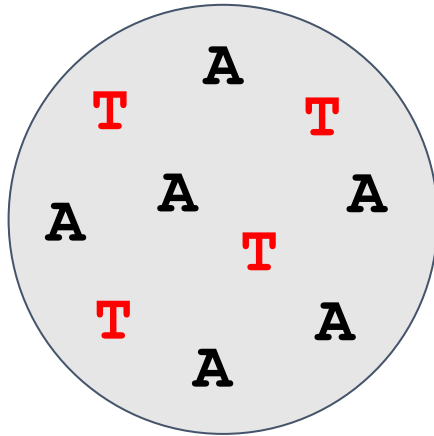


$$p_2 = 0.6$$

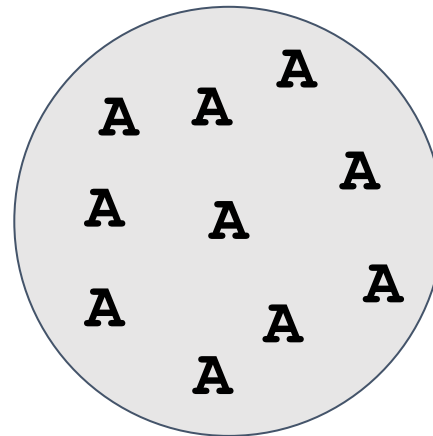
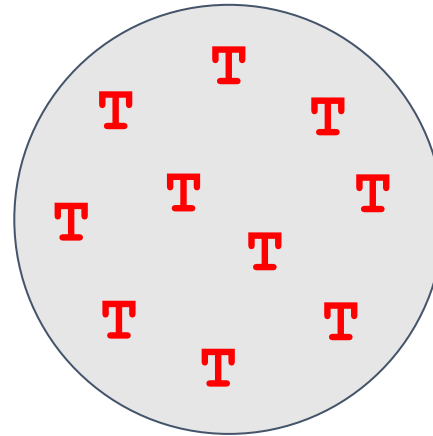


$$p_T = 0.5, F_{ST} = 0.1$$

Population divergence



$$F_{ST} = 0$$



$$F_{ST} = 1$$

Exercise 2

~20 min.

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