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Micromegas Trigger Processor Algorithm Performance in Nominal, Misaligned, and Misalignment Corrected Conditions

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5 Abstract

The Trigger Algorithm for the Micromegas detectors is an important component of the Level 1 New Small Wheel trigger. Updates to the algorithm simulation are described, and baseline performance measures of the algorithm under a variety of conditions are detailed. Additionally, the performance of the algorithm under chamber misalignment for the possible three translations and three rotations is shown, and corrections for each case are presented. Nominal resolutions for the fit quantities are 0.364 mrad for θ , 8.12 mrad for ϕ , and 1.47 mrad for $\Delta\theta$. For misalignments resulting from translations, nominal performance can be restored, and for misalignments resulting from rotations, the only non-negligible effect is a shift in $\Delta\theta$ bias of 0.12 mrad and a resolution degradation of 2% for 0.3 mrad (roughly corresponding to a 1 mm translation misalignment) rotation around the s axis.

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7 1. Introduction

In order to preserve key physics functionality by maintaining the ability to trigger on low p_T muons, the Phase I Upgrade to ATLAS includes a New Small Wheel (NSW) that will supply muon track segments to the Level 1 trigger. These NSW trigger segments will combine segments from the sTGC and Micromegas (MM) trigger processors (TP). This note will focus in particular on the algorithm for the MMTP, described in detail with initial studies in [1]. The goal of this note is to describe the MMTP algorithm performance under a variety of algorithm settings with both nominal and misaligned chamber positions, as well as addressing a number of performance issues.

This note is organized as follows: the algorithm and its outputs are briefly described in Section 2; Monte Carlo samples used are in Section 3; nominal algorithm performance and certain quantities of interest are described in Section 4; algorithm performance under misalignment, misalignment corrections, and corrected performance are shown in Section 5; and conclusions are presented in Section 6.

2. Algorithm Overview

The MMTP algorithm is shown schematically in Figure 1, taken from [1], where a more detailed description may be found. The algorithm begins by reading in hits, which are converted to slopes. These 31 slopes are calculated under the assumption that the hit originates from the IP; slopes calculated under 32 this assumption are denoted by a superscript g for global in order to distinguish them from local slopes 33 calculated using only hits in the wedge. In the algorithm simulation, events are screened at truth level 34 to make sure they pass certain requirements. The track's truth-level coordinates must place it with the 35 wedge since some generated tracks do not reach the wedge. These hits are stored in a buffer two bunch crossings (BCs) in time deep that separates the wedge into so-called "slope-roads." If any given sloperoad has sufficient hits to pass what is known as a coincidence threshold, a fit proceeds. A coincidence 38 threshold is a requirement for an event expressed as aX+bUV, which means that an slope-road must have 39 at least a hits in horizontal (X) planes and at least b hits in stereo (U or V (corresponding to positive and 40 negative stereo rotations)) planes. For coincidence thresholds with a 2X hit requirement there is the extra 41 requirement that, in the case of only 2X hits, one be on each quadruplet in order to ensure an adequate lever arm for the $\Delta\theta$ calculation. Note that less stringent (lower hit) coincidence thresholds are inclusive; i.e. a slope-road passing a 4X+4UV cut automatically passes 2X+1UV. The coincidence threshold, size of the slope-roads (denoted h), and the number of slope-roads into which each horizontal and stereo hits 45 get written centered upon their nominal value are configurable parameters of the algorithm. 46

An individual hit's slope is calculated as shown in Equation 1, where y_{base} is the local y coordinate (orthogonal to the beamline and direction of the horizontal strips) of a station's base, w_{str} is the strip pitch, n_{str} is the hit's strip number, and z_{plane} is the location of the hit's plane along the beamline.

$$M_{hit} = \frac{y}{z} = \frac{y_{base}}{z_{plane}} + \frac{w_{str}}{z_{plane}} \times n_{str}$$
 (1)

In the fit, individual hit slopes in a slope-road are used to calculate global slopes associated with each plane type, which are averages (e.g. M_X^g for the average slope of horizontal planes). These in turn are used to calculate the three composite slopes: slopes associated with the horizontal (m_X) and vertical coordinates (m_Y) and the local slope of hits in the horizontal planes (M_X^l) , all of which are shown in Equation 2. Note that the expression for M_X^l differs but is equivalent to the expression given in [1]. This

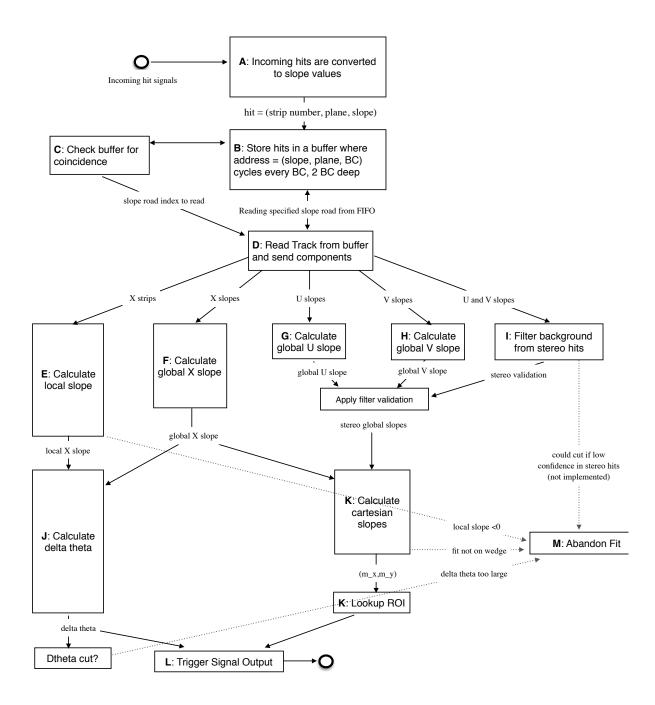


Figure 1: A flow chart describing the algorithm steps, taken from [1].

is due to a procedural change in the algorithm detailed in Appendix A. In Equation 2, θ_{st} is the stereo angle of 1.5 degrees; the sums are over relevant planes; \bar{z} is the average position in z of the horizontal planes; and y_i and z_i in the local slope expression refer to the y and z coordinates of hits in X planes.

$$m_{X} = \frac{1}{2} \cot \theta_{st} \left(M_{U}^{g} - M_{V}^{g} \right), \ m_{Y} = M_{X}^{g}, \ M_{X}^{l} = \frac{\bar{z}}{\sum_{i} z_{i}^{2} - 1/n \left(\sum_{i} z_{i} \right)^{2}} \sum_{i} y_{i} \left(\frac{z_{i}}{\bar{z}} - 1 \right)$$
(2)

From these composite slopes, the familiar expressions for the fit quantities θ (the zenith), ϕ (the azimuth¹), and $\Delta\theta$ (the difference in θ between the direction of the segment extrapolated back to the interaction point and its direction when entering the detector region; the following is an approximation) may be calculated, as noted in [1]:

$$\theta = \arctan\left(\sqrt{m_X^2 + m_y^2}\right), \ \phi = \arctan\left(\frac{m_X}{m_y}\right), \ \Delta\theta = \frac{M_X^l - M_X^g}{1 + M_X^l M_X^g}$$
 (3)

Looking at Equations 2 and 3, the dependence of fit quantities on input hit information becomes clear. $\Delta\theta$ relies exclusively on information from the horizontal (X) planes. Both θ and ϕ rely on both horizontal and stereo slope information. However, the sum in quadrature of m_x and m_y in the arctangent for θ means that θ is less sensitive to errors in stereo hit information than ϕ . Given that θ_{st} is small, $\cot\theta_{st}$ is large (\sim 38), so m_x multiplies small differences in M_U and M_V , where m_y is simply an average over slopes. This means that while errors in horizontal hit information will affect all three fit quantities, comparable errors in stereo hits will have a proportionately larger effect on θ and particularly on ϕ . The $\Delta\theta$ cut after step J in Figure 1 has been implemented, requiring all fits to have $|\Delta\theta| < 16$ mrad. This requirement ensures good quality fits but also slightly reduces algorithm efficiency.

3. Monte Carlo Samples

The Monte Carlo (MC) samples used for these studies were generated in Athena release 20.1.0.2 using simulation layout ATLAS-R2-2015-01-01-00 with muon GeoModel override version MuonSpectrometer-R.07.00-NSW and modifications to have two modules per multiplet and xxuvuvxx geometry with a stereo angle of 1.5 degrees. Muons of a single p_T were generated around the nominal IP with a smearing of 50 mm along the beam line and 0.015 mm orthogonal to it; these muons were pointed toward a single, large sector of the NSW. Each event consists of one muon fired towards the single NSW wedge separated by effectively infinite time from other events.

4. Nominal Performance

In order to evaluate algorithm performance, a number of quantities are evaluated, including the fit quantities θ , ϕ , and $\Delta\theta$ as well as algorithm efficiency. Unless otherwise stated, that algorithm is run with a 4X+4UV coincidence threshold, slope-road size of 0.0009, an X tolerance of two slope-roads (i.e. hits in horizontal planes are written into the two slope-roads closest to the hits' value), a UV tolerance of four

¹ Defined with respect to the center (y) axis and *not* the axis of the strips (x) as is sometimes typical, so a hit along the center of the wedge has $\phi = 0$

slope-roads², and a charge threshold requirement on hits of 1 (measured in units of electron charge) for a sample of 30 000 events with a muon p_T of 100 GeV. Samples were also generated for p_T values of 10 GeV, 20 GeV, 30 GeV, 50 GeV, and 200 GeV, which were used in some of the following studies.

7 4.1. Fit Quantities

In order to evaluate the performance of the algorithm's fit quantities θ , ϕ , and $\Delta\theta$, fit values are compared to truth-level MC values. The residual of the three fit quantities, $\theta_{fit} - \theta_{tru}$, $\phi_{fit} - \phi_{tru}$, and $\Delta\theta_{fit} - \Delta\theta_{tru}$, are recorded for every fitted track. The distributions of these quantities, in particular their biases and standard deviations, are then used to evaluate performance. In most cases, following [1], the mean and standard deviation of a 3σ Gaussian fit are quoted, as they capture the main features of the algorithm and generally behave like the raw mean and rms. Nevertheless, discussion of the raw quantities will be included when their behavior deviates markedly from that of the 3σ fit quantities.

The truth-level quantities used in residual distribution are taken from information in the MC. These come directly from the MC for θ , ϕ , and $\Delta\theta$. These quantities, along with the geometry of the (large) wedge, are then in turn used to calculate truth-level values for any intermediate quantities used in the algorithm. $m_{x,tru}$, for instance, is given by $\tan\theta_{tru} \sin\phi_{tru}$.

Residual distributions for fit quantities under the previously described default settings of the algorithm are shown in Figure 2. Both the $\theta_{fit} - \theta_{tru}$ and $\Delta\theta_{fit} - \Delta\theta_{tru}$ distributions feature a mostly Gaussian shape with more pronounced tails. The mean bias for these distributions is negligible at under one tenth of a milliradian, and the fitted (raw) rms values are 0.349 (0.614) mrad for θ and 1.03 (2.55) mrad for $\Delta\theta$. The case of the $\phi_{fit} - \phi_{tru}$ distribution is less straightforward, with both the shape and bias arising from the xxuvuvxx geometry and relatively large extent of one of the two η -stations, as explained in Appendix B. The fitted (raw) rms for the ϕ distribution is 8.67 (16.6) mrad.

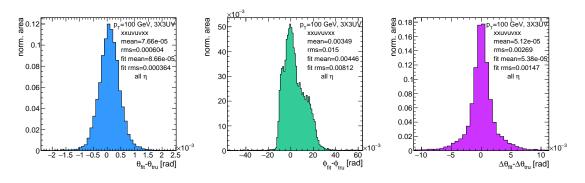


Figure 2: Nominal residual plots; θ , ϕ , $\Delta\theta$ for $p_T = 100$ GeV muons

Both increasing muon p_T and increasing muon η for a fixed p_T imply increasing muon energy. As muons become more energetic, two effects compete in affecting the quality of fit. On the one hand, higher energy muons are deflected less by the ATLAS magnetic field, which should tend to improve the quality of the fit, since the fitted θ (upon which $\Delta\theta$ also relies) and ϕ values are calculated under the infinite momentum muon (straight track) assumption. However, as muon energy increases, the likelihood that

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² The larger tolerance on stereo hits takes into account the particulars of the m_x calculation mentioned in Section 2.

the muon will create additional secondaries increases, which creates extra hits that degrade the quality of the fit. While the geometry of the multiplet is such that there is very good resolution in the direction orthogonal to the horizontal strip direction, the shallow stereo angle of 1.5 degrees means that early hits caused by secondaries can have an outsize impact on m_x . $\Delta\theta$, which does not rely upon stereo information should feel the effect of secondaries the least and benefit from straighter tracks the most and hence benefit from higher muon energies; ϕ , relying upon stereo information the most, would be most susceptible to secondaries and benefit the least from straighter tracks and hence least likely to benefit from higher muon energy; θ relies upon both horizontal and vertical slope information, though small errors are less likely to seriously affect the calculation, so the two effects are most likely to be in conflict for this fit quantity.

The interplay of these effects on the residual standard deviations can be seen in their dependencies on η (Figure 3; note that the final point in each of these plots is the rms of the distribution overall η) and p_T (Figure 4). For $p_T = 100$ GeV muons, $\Delta\theta$ performance increases with η (energy), and ϕ performance decreases, as expected³; for θ , the two effects appear to compete, with performance first increasing with η until the effects of secondaries begins to dominate. Integrated over all η , the effects are less clearly delineated. Both $\Delta\theta$ and θ performance increases with increasing p_T , suggesting straighter tracks with increasing energy are the dominant effect for these quantities, while ϕ performance appears to improve and then deteriorate (the slight improvement at high p_T is due to the addition of the $\Delta\theta$ cut into the algorithm, which filters out very poor quality fits).

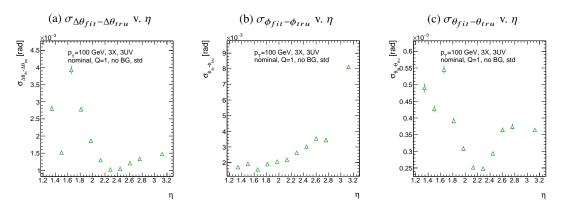


Figure 3: The rms distributions of $\Delta\theta$, ϕ , and θ as a function of η for $p_T=100$ GeV; the final point in each plot is the rms obtained from a fit obtained from a fit to the fill distribution including all η bins.

The rms of the three benchmark quantities as a function of algorithm set (i.e. slope-road) coincidence threshold are shown in Figure 5 using Gaussian fits and in Figure 6 for the raw quantities. The fitted σ 's for θ and ϕ are fairly stable across coincidence threshold. $\Delta\theta$, on the other hand, performs better particularly for the most stringent coincidence threshold; this is a result of the fact that additional information for more hits greatly improves the quality of the local slope fit calculation. The raw rms is a different story. Naïvely, one would expect the performance to get better with more stringent coincidence threshold, but this is not the case in Figure 6. As the coincidence threshold gets more stringent, fewer and fewer tracks are allowed to be fit. When moving from 2X hits to 3X hits, the tracks that get vetoed populate the tails of the distribution outside the 3σ fit range but are not in the very extremes of the distribution. While tracks with 2X hits are of lower quality than those with 3 and 4 X hits, tracks with the very worst fit values pass even the most stringent coincidence threshold requirements (e.g. as a result of many hits arising from

³ The much worse overall performance for ϕ is due to the η dependent bias and other effects described in Appendix B.

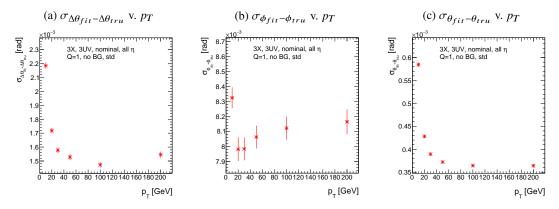


Figure 4: The rms distributions of $\Delta\theta$, ϕ , and θ as a function of p_T .

a shower of secondaries). This is best illustrated when comparing the 2X+1UV $\Delta\theta$ residual distribution with the 4X+4UV distribution in Figure 7. As both the overlayed normalized curves and ratio distribution show, while the most central regions are fairly similar, the 2X+1UV distribution is much more prominent in the tails but not the extreme tails, which means that, though the overall 2X+1UV raw rms goes down, the overall quality of algorithm fits is worse.

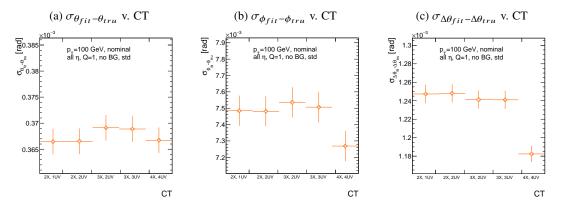


Figure 5: The fitted rms of residual distributions for θ , ϕ , and $\Delta\theta$ as a function of coincidence threshold for $p_T = 100$ GeV.

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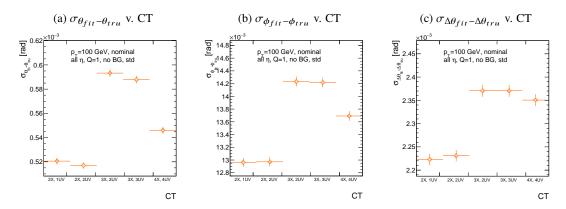


Figure 6: The raw rms of residual distributions for θ , ϕ , and $\Delta\theta$ as a function of coincidence threshold for $p_T=100$ GeV.

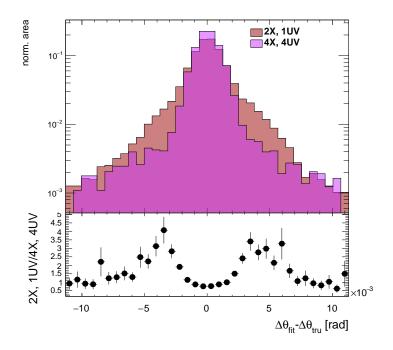


Figure 7: Nominal $\Delta\theta$ residual distribution for $p_T=100$ GeV muons with coincidence thresholds 2X+1UV and 4X+4UV normalized to the same area and plotted together (top) as well as the ratio of the 2X+1UV distribution and the 4X+4UV per bin.

4.2. Efficiencies

Two general efficiencies have been formulated to study the performance of the MMTP algorithm. The first, denoted ε_{alg} , is the fraction of tracks that pass some (slope-road) coincidence threshold configuration that are successfully fit. An event that passes a slope-road coincidence but does not fit fails because some of the hits included are of sufficiently poor quality to throw off the fit. This efficiency answers the question of how often the algorithm performs fits when technically possible, giving a measure of overall algorithm performance for a given configuration. For example, $\varepsilon = 95\%$ for 3X+2UV means that 95% of tracks that produce at least 3X hits and 2UV hits in at least one slope-road will be successfully fitted 95% of the time. The performance of this efficiency as a function of coincidence threshold, η (with the final point once again being the efficiency integrated over all η), and p_T is shown in Figure 8. ε_{alg} is fairly constant in η and decreases with increased p_T , which can be attributed to the increased likelihood of secondaries introducing lower quality hits that cause the fit to fail.

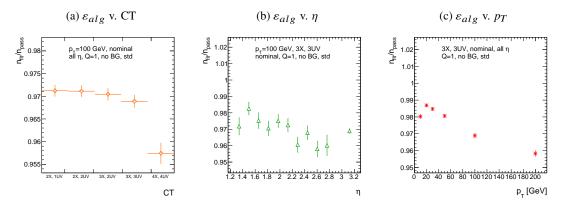


Figure 8: ε_{alg} and as a function of coincidence threshold, η (final point is ε_{alg} integrated over all η), and p_T .

The second efficiency type, denoted ε_{fit} , is the fraction of tracks that enter the wedge whose fits (if any) satisfy a given coincidence threshold. This efficiency can be used to help establish an optimal coincidence threshold setting in the algorithm, balancing the improved overall fit quality of higher thresholds with the greater number of fits for lower thresholds. Hence, an ε_{fit} of 95% at 3X+2UV means that 95% of tracks entering the wedge are fit and that these fits include at least 3X and 2UV hits. ε_{fit} as a function of coincidence threshold is shown in Figure 9 (a), which shows that the majority of fits having at most 3X+3UV hits. That there is a marked drop to 4X+4UV is not surprising, as there is a substantial population outside the 4X+4UV bin in Figure 10. The behavior of ε_{fit} with η in Figure 9 (b) (with the final point once again being the efficiency integrated over all η) is much more varied, with geometric effects of detector acceptance coming into play. The performance of ε_{fit} as a function of p_T , shown in Figure 9 (c), is similar to that of ε_{alg} coincidence threshold, again consistent with the effects of secondaries at higher energies.

In order to better understand efficiency behavior with coincidence threshold, the distribution of highest slope-road coincidence thresholds in events is shown in Figure 10, with the 0,0 bin containing events that did not meet requirements for the minimum 2X+1UV coincidence threshold for a fit to occur. That the efficiency is lower at higher coincidence threshold suggests that most of the fits that fail have high hit multiplicity (i.e. a similar number fails in each of the coincidence threshold bins in Figure 8 (a)), which is consistent with the interpretation that the primary source of fit failures is bad hits originating from secondaries created by higher energy muons.

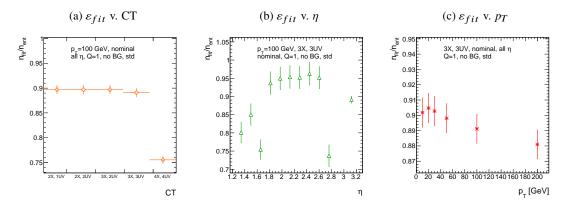


Figure 9: ε_{fit} and as a function of coincidence threshold, η (final point is ε_{fit} integrated over all η), and p_T .

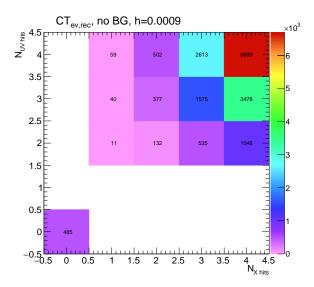


Figure 10: The distribution of highest slope-road coinicidence thresholds in events; the 0,0 bin is the number of events passing selection requirements that fail to form the minimum 2X+1UV coincidence threshold necessary for a fit.

4.3. Incoherent Background

The default slope-road size and tolerances associated with horizontal and stereo hits used in the above studies were configured to optimize algorithm performance, similar to studies in [1]. In order to evaluate algorithm performance under conditions with more limited resources, as might be expected at run-time, additional studies were conducted with the slope-road size and hit tolerances set equivalent to the sensitive area of a single VMM chip⁴ both with and without generation of incoherent background. The specifics of incoherent background generation may be found in Appendix C. The effects of incoherent background and larger slope road size are summarized in Figure 11 for efficiencies and in Figure 13 and Table 1 for residual of fit quantities.

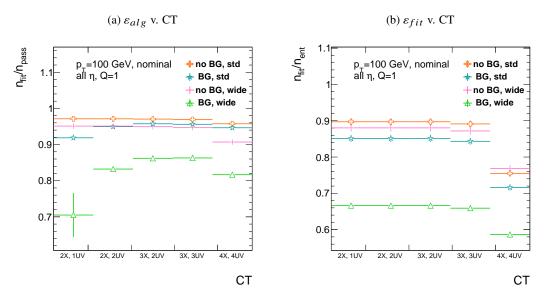


Figure 11: The algorithm and total efficiencies as a function of coincidence threshold for different background settings and slope-road sizes (standard and wide (one slope road as 1 VMM chip)).

Figure 11 show the effect of both wider slope-roads and the introduction of background on efficiencies. The introduction of wider slope-roads increases the chance that an early errant hit (either from secondaries/ionization or background) will be introduced into the fit, and the presence of incoherent background greatly increases the number of such errant hits. Both wider slope-roads and background drive down the number of fits (numerator) in both efficiencies, and background can artificially inflate the denominator of ε_{alg} , a reco-level, slope-road coincidence threshold. The shape of the ε_{fit} versus coincidence threshold distributions remains fairly constant with each complicating factor (standard, wider slope-roads, background, both wider slope-roads and background), suggesting many muons will simply not be fit with any number of hits; ε_{fit} does not take into account the coincidence threshold of tracks that are not fit, so the effect appears uniform across coincidence threshold. The effects seen for ε_{alg} , which are not uniform across coincidence threshold can be better understood when examining the distribution of event highest coincidence thresholds, shown for wide slope-roads both without and with background in Figure 12. Take, for example the 2X+1UV case. The 2X+1UV bin in particular has a marked increase when background is introduced. No new, good tracks are introduced between the no backgrond and backround

⁴ One VMM is assumed to cover 64 MM strips at 0.445 mm each.

cases, so the increase is entirely due to bad, background hits; hence, these events do not (and should not) fit, causing the particularly pronounced drop in this bin between these two cases in Figure 11.

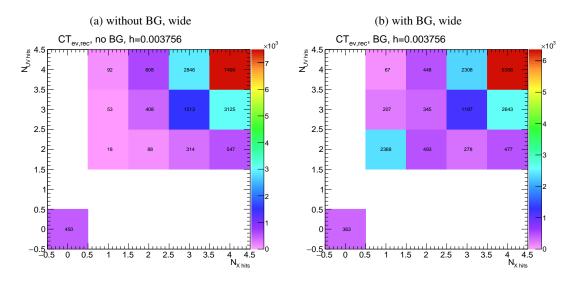


Figure 12: The distribution of highest slope-road coinicidence thresholds in events for the algorithm with wide slope-roads (width of 1 VMM) both without (a) and with (b) incoherent background; the 0,0 bin is the number of events passing selection requirements that fail to form the minimum 2X+1UV coincidence threshold necessary for a fit.

The effect of increasing slope-road size and incoherent background on fit quantity residual rms values as a function of p_T is shown in Figure 13. As the figure shows, the fitted rms values are fairly robust against increased slope-road size and background. This does not hold for all of the raw rms values, however, as shown in Table 1. Just as with the efficiencies, the introduction of background has a larger effect than that of increased slope-road size, which does not seem to have an overly large impact on any of the fit quantities on its own. While $\Delta\theta$ remains robust to both increased slope-road size and background (likely due to the $\Delta\theta$ cut of 16 mrad built into the algorithm), θ shows some degradation in performance, and the ϕ residual raw rms shows a very large increase upon the introduction of background. Nevertheless, the contrasting behavior of the fitted and raw rms values suggests that tracks that drive up the raw rms values already had very poor fit quality even before the introduction of background, so the impact on fit quantities should remain fairly limited.

Table 1: The fitted (absolute) σ of fit quantity residuals in mrad under different algorithm settings.

	No BG, std	No BG, wide	BG, std	BG, wide
θ	0.364 (0.604)	0.363 (0.542)	0.379 (0.886)	0.380 (1.07)
ϕ	8.12 (15.0)	7.93 (13.2)	8.20 (24.6)	7.63 (24.8)
$\Delta \theta$	1.47 (2.69)	1.40 (2.66)	1.50 (2.89)	1.43 (2.90)

As Table 1 shows, rms values appear to be robust to an increase in slope-road size. Nevertheless, though the fitted σ residual values are also fairly robust to the introduction of background, the raw rms values are not. While the raw $\Delta\theta$ rms stays stable, both θ and ϕ suffer noticeable degradation, which suggests

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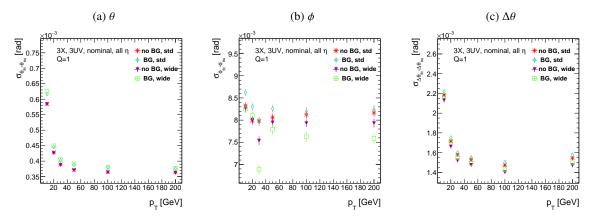


Figure 13: The three fit quantity residual rms values as a function of p_T for different background settings and slope-road sizes (standard and wide (one slope road as 1 VMM chip)).

that the introduction of background has a detrimental effect on horizontal slope residual (i.e. on stereo strips in particular). This level of degradation is likely acceptable for θ , though further steps may need to be taken to address ϕ .

4.3.1. BCID

A fitted track's BCID is determined by the most common BCID associated with its hits. Concerns were raised that this might cause incorrect BCID association for fitted tracks. In order to address this, the rate of successful BCID association for fitted tracks was recorded. Figure 14 shows the dependence of this success rate as a function of p_T and coincidence threshold in the different background and resource conditions used in the previous section. The successful BCID identification rate is always over 99.5%, demonstrating that this issue is not a concern with the state-of-the-art detector simulation.

4.4. Charge Threshold

The MMTP uses the first hits registered passing a charge threshold requirement given in units of electron charge. In principle, it would be beneficial to be able to use any hits that are registered regardless of deposited charge, but in the high rate environment envisioned for the NSW, this requirement might need to be raised. Nominal algorithm settings have this charge threshold requirement set to 1, and studies were conducted on algorithm performance for charge threshold values of 0, 1, and 2. Efficiencies as a function of coincidence threshold for different charge thresholds are shown in Figure 15. Increasing the charge threshold lowers both efficiencies, particularly at high coincidence threshold, which suggests that energetic muons with secondaries create both very many hits and hits with higher charge. While the shapes of the fit quantity distributions as a function of p_T in Figure 16 are fairly constant across charge threshold, performance is not. θ and $\Delta\theta$ show some improvement with higher charge threshold, particularly at low p_T , suggesting that resolution improves in the vertical direction, but ϕ shows degradation at higher charge threshold, which is a symptom of more highly charged particles experiencing greater bending in the ATLAS magnetic field in the ϕ direction.

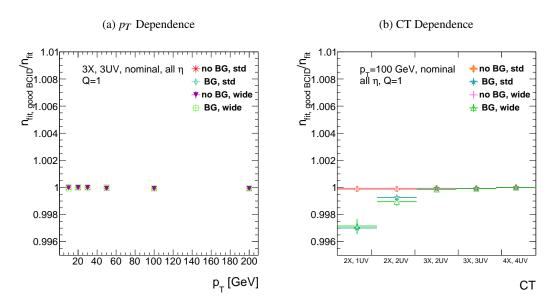


Figure 14: The rate of good BCID association based majority hit BCID as a function of p_T and coincidence threshold.

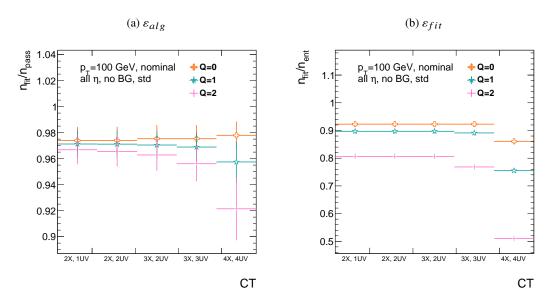


Figure 15: The efficiencies as a function of coincidence threshold for charge thresholds of 0, 1, and 2.

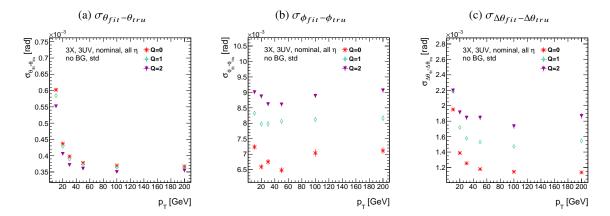


Figure 16: The fit quantity residual rms values as a function of p_T for charge thresholds of 0, 1, and 2.

5. Misalignments and Corrections

The performance of the trigger algorithm under misalignment has been studied for each of the six alignment quantities (three translations and three rotations all along the principal axes) described in [2] and [2], whose convention we will follow here. For the simulated wedge studied here the local coordinates described in [2] are taken to be centered at the center of the base of the wedge⁵, the local t axis corresponds to the axis of the beam line, the local t axis corresponds to the direction orthogonal to both the beam line and the horizontal strips, and the local t axis completes the right-handed coordinate system. The rotation angles t0, and t1 correspond to rotations around the local t1, and t2 axes, respectively. Note that the local t2, and t3 axes correspond to the usual global t4, axes. Misalignments were studied in twenty evenly spaced increments from nominal positions to misalignments of 1.5 mrad for the rotations (-1.5 mrad to +1.5 mrad for the t2 case), and of 5 mm (a roughly corresponding linear shift) for the translations. In all cases, the front quadruplet is misaligned while the rear quadruplet remains in its nominal position. While only the front quadruplet of a single wedge is misaligned, the framework for misalignment presented below could be used to study generic local and global misalignments. The six misalignments are schematically represented in Figure 17.

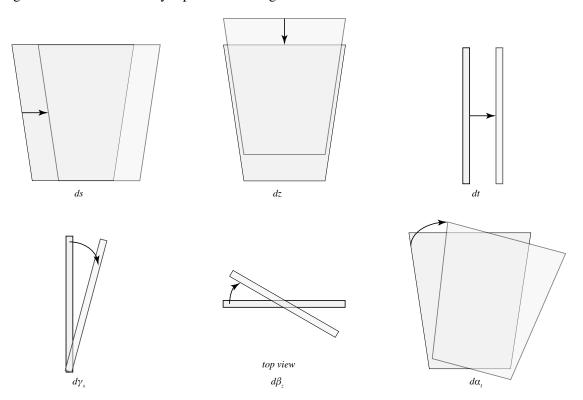


Figure 17: The different misalignment cases as defined in the AMDB manual.

Chamber misalignments manifest themselves as altered strips in algorithm input. In order to simulate the effects of misalignment, the change in the local y coordinate—the distance from the bottom wedge center in the direction perpendicular to both the beamline and the strip direction—is calculated for a

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⁵ Not, as is sometimes the case, the centroid position for simplicity's sake, as the agreed upon geometry of the detector changed several times while studies were in progress; any transformation in a centroid-origin coordinate system can of course be formed by a combination of the six transformations examined.

Table 2: A summary of corrections with additional constants/operations (written as $n_{const}c/n_{ops}$ op; n_X is the number of X hits in a fit) necessary for analytic corrections. Yes means a correction exists but might not entirely remove misalignment effects, while yes+ means a quality of correction is only limited by knowledge of misalignment and memory

	Δs	Δz	Δt	γ_s	β_z	α_t
Analytic	yes+	yes+	yes+	yes	no	yes
Resources	11c/2op	0c/0op	0c/0op	56c/1op		$400c/2n_X op$,
						$32c/12n_X$ op
Simulation	yes+	no	no	no	yes+	yes+

track coming straight from the interaction point defined by the truth-level θ and ϕ angles for generic misalignment; details can be found in Appendix D. This displacement in y is then added to input hit information and the algorithm is then run normally.

In order to evaluate algorithm performance under misalignment and corrections for misalignment, the absolute means and relative resolutions of the fit quantities θ , ϕ , and $\Delta\theta$ are measured as a function of misalignment. In the following, results will only be shown for which the effects of misalignment are significant. "Significant," for misalignments of 1 mm (0.3 mrad) for translations (rotations) means more than a 5% degradation in rms and/or bias shifts in θ , ϕ , and $\Delta\theta$ of 0.01 mrad, 1 mrad, and 0.1 mrad, respectively. A full set of plots may be found in Appendix F.

While corrections are typically done on a case-by-base basis, they fall under two general categories, analytic and simulation based. Analytic corrections rely upon specific knowledge of the misalignment, with each case being handled separately; as such, the additional resources required, both extra constants and operations, if any, vary accordingly. Simulation based corrections are all done in the same manner. The algorithm is run over a training MC sample (same setup but with $p_T = 200$ GeVinstead of the normal 100 GeV sample so as not to overtrain the corrections), and the mean biases for θ , ϕ , and $\Delta\theta$ are saved for different, equally spaced regions in the $\eta - \phi$ plane over the wedge based on the fitted θ and ϕ values. Currently, these values are saved for 10 η and 10 ϕ bins (100 η , ϕ bins total), with the number of bins in each direction being a configurable parameter. When the algorithm runs with simulation based correction, this table of constant corrections is saved in a LUT before runtime, and corrections are added to final fit quantities based on the (uncorrected) θ and ϕ fit values. With the settings mentioned, this is 300 extra constants $(10\eta - bins \times 10 - \phi bins \times 3)$ fit quantities) and two extra operations (a lookup and addition for each quantity done in parallel). The simulation correction can, in principle, also be applied to the algorithm in nominal conditions with non-trivial improvements, as detailed below in Section 5.1. Depending on the misalignment case in question, different approaches work better. A summary of correction methods, including resources necessary for the individual analytic cases, is shown in Table 2.

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5.1. Simulation Correction of the Algorithm Under Nominal Conditions

In addition to using simulation based correction to counter the effects of several classes of misalignment, the correction can be applied at to the algorithm under nominal conditions. The main effect of this correction is to mitigate the effects of the bias in stereo strips discussed in Appendix B. As such, the correction has a larger effect on quantities that rely on the aggregate slope m_y , as can be seen in in Figure 18, improving $\sigma_{\theta_{fit}-\theta_{tru}}$ resolution by about 25%, and reducing $\sigma_{\phi_{fit}-\phi_{tru}}$ by over 50% and restoring a largely Gaussian shape. The slight, apparent degradation in $\Delta\theta$ is due to a more mild version of the effect seen in Figure 7.

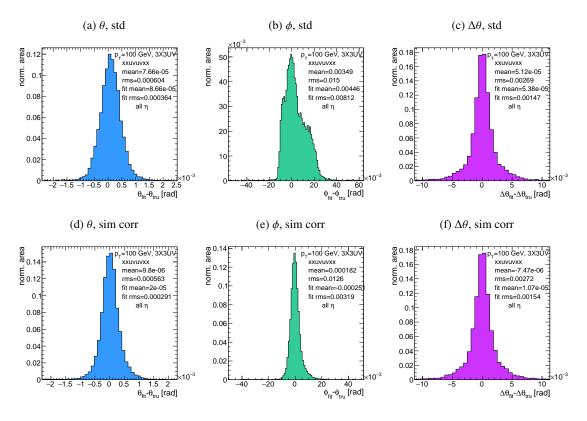


Figure 18: Nominal residual plots for both uncorrected and simulation corrected cases; θ , ϕ , $\Delta\theta$ for $p_T=100$ GeV muons

As can be seen in Figure 19, the simulation based correction also removes the η dependence to fit quantity resolution distributions, as expected. One consequence of this is that simulation-based corrections applied to the misalignment cases below will restore performance to the "sim" and not the "std" distributions of Figure 18. Hence, when making comparisons between simulation corrected curves and the nominal performance point, simulation-corrected distributions of benchmark quantities versus misalignment will often look generally better.

That the improvements from a simulation-based correction improve performance of the algorithm in nominal conditions most for the quantities that depend most on stereo information (ϕ and θ) and remove the η dependence of fit quantity resolutions suggests that there could, in principle, be analytic corrections that could be applied to the nominal algorithm. One possible solution is to introduce an additional set of

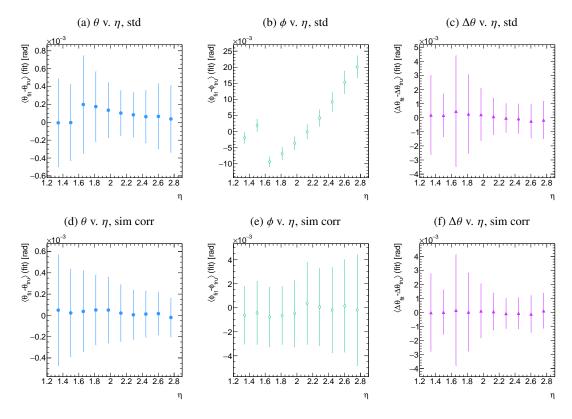


Figure 19: Nominal residual plots as a function of η with points as means and error bars as rms values in each η bin for the angles θ , ϕ , $\Delta\theta$ for $p_T = 100$ GeV muons in the uncorrected and simulation corrected cases.

constants, having the y_{base} depend on the strip number, similar to the γ_s correction for z_{plane} described in Section 5.5, which would add a lookup per hit and $8 \times n_{bins,y}$ extra constants that would be optimized as the γ_s correction was.

$$M_{hit} = \frac{y}{z} = \frac{y_{base}}{z_{plane}} (n_{str}) + \frac{w_{str}}{z_{plane}} n_{str}$$
 (4)

The simulation correction residual rms values suggest a limit on the quality of an such correction and could perhaps be implemented generically on their own regardless of misalignment for rms values on fit quantities of 0.291 mrad for θ , 3.19 mrad for ϕ , and 1.54 for $\Delta\theta$, which represent a 20% improvement for θ , a 62% improvement for ϕ , and a slight degradation in $\Delta\theta$ of 4.7%, again owing to an effect similar to the one in 7.

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5.2. Translation Misalignments Along the Horizontal Strip Direction (Δs)

A translation in s (i.e. along the direction of a horizontal strip) only affects the stereo strips, and, since the stereo angle is small, a very large misalignment is necessary for effects to be noticeable (a misalignment of roughly 17 mm corresponds to one strip's misalignment in the stereo planes). The only quantity to show any meaningful deviation with misalignments with translations in s is the ϕ residual bias (a change of 0.4 mrad at $\Delta s = 1$ mm), as can be seen in the uncorrected curve of Figure 20.

A translation in s induces a constant shift in the calculated horizontal slope, m_x in Equation 2. This constant shift should only depend on which stereo planes included in a fit are misaligned and how misaligned they are. Hence, the correction to m_x , for a sum over misaligned stereo planes i, with their individual misalignments in s and plane positions in z is:

$$\Delta m_x = \frac{1}{N_{stereo}} \sum_{i \text{ misal stereo}} \frac{\Delta s_i}{z_{i,plane}}$$
 (5)

Given prior knowledge of misalignment, these corrections to m_x can be performed ahead of time and saved in a lookup table (LUT), similar to the LUT used for constants in the X local slope (M_X^l) calculation. The added overhead of this analytic correction is hence eleven constants in memory, a lookup, and one addition. The correction perfectly corrects the effects of misalignment, as can be seen in Figure 20. The simulation based correction described above can also be used to correct for Δs misalignments, with the results of that correction also shown in Figure 20. The apparent discrepancy between the simulated and analytic correction is a natural consequence of the fact that the simulation correction, as previously mentioned, restores the ϕ residual distribution to an overall more Gaussian shape.

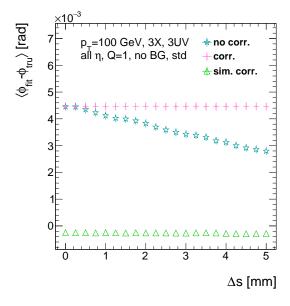


Figure 20: The mean of the ϕ residual as a function of misalignment for the uncorrected case and the analytic and simulation correction cases.

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5.3. Translation Misalignments Orthogonal to the Beamline and Horizontal Strip Direction (Δz)

A translation in AMDB z, the direction orthogonal to both the beamline and the horizontal strip direction, corresponds to a translation in the y of Equation 1, affecting all slope calculations. This has a large impact on the θ residual bias and both the bias and rms of $\Delta\theta$ residual, as can be seen in Figures 21 (a)–(c). The marked degradation and non-linear behavior in performance at very high levels of misalignments is a result of low statistics; there are fewer fits at high level of misalignments since for $\Delta z \gtrsim 3$ mm, most fits will fail the $\Delta\theta$ cut⁶. The θ bias shifts by about 0.075 mrad at $\Delta z = 1$ mm, and $\Delta\theta$ shifts by about 5 mrad for the same level of misalignment. While the fitted rms of the $\Delta\theta$ residual remains fairly stable for $\Delta z < 1$ mm or so, between $\Delta z = 2$ mm and $\Delta z = 3$ mm, the rms increases by 15% before the $\Delta\theta$ cut issue mentioned above intervenes.

Fortunately, these misalignments are straightforward to correct with knowledge of the misalignment. The only modification necessary for this correction is to change the definitions of y_{base} in Equation 1 for the individual hit slope addressing. This is done before runtime and adds no overhead to the algorithm, and the correction quality is only limited by knowledge of the misalignment. The results of this correction are also shown in Figures 21 (a)–(c) and restore nominal performance.

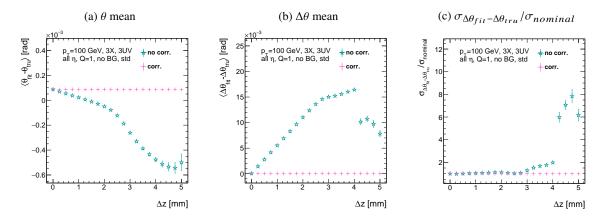


Figure 21: The affected quantities of Δz misalignments: θ bias, $\Delta \theta$ bias, and $\sigma_{\Delta \theta_{fit}-\Delta \theta_{tru}}/\sigma_{nominal}$ for both the misaligned and corrected cases.

⁶ Since $\Delta\theta = \frac{M_X^l - M_X^g}{1 + M_X^l M_X^g}$ and $M_X^l = B_k \sum y_i (z/\bar{z} - 1)$, a shift Δy translates (with typical slope values of ~ 0.3) to $5B_k (z_1 + z_2)/\bar{z}$ (with B_k in units of inverse mm); set equal to 16 mrad ($\Delta\theta$ is centered at zero), this corresponds to $\Delta y = 2.7$ mm

5.4. Translation Misalignments Parallel to the Beamline (Δt)

The effects of misalignment due to translations in t are very similar to those due to translations in t without the complication of the t0 cut, affecting the t2 instead of the t2 coordinate that enters into hit slope calculations. Again, t3 bias, t4 bias, and t5 bias shifts by just under 2 mrad, and t6 bias shifts by about 0.02 mrad, t7 bias shifts by just under 2 mrad, and t8 degrades by about 20%. The correction for this misalignment once again costs no overhead and consists of changing stored constants in the algorithm, in this case the positions along the beamline of the misaligned planes, with results similarly limited by knowledge of the misalignment. The slight improvement with correction to t8 cut to the real effect of a larger lever arm. Both the misaligned and corrected distributions of affected quantities of interest are shown in Figure 22.

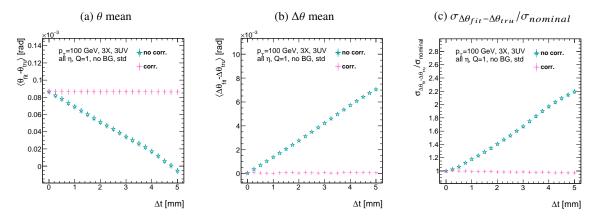


Figure 22: The affected quantities of Δt misalignments: θ bias, $\Delta \theta$ bias, and $\sigma_{\Delta \theta_{fit}-\Delta \theta_{tru}}/\sigma_{nominal}$ for both the misaligned and corrected cases.

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5.5. Chamber Tilts Towards and Away from the IP (γ_s Rotation)

Chamber misalignment due to rotations around the s axis act effectively like a translation in t that depends on strip number. These rotations tilt misaligned chambers away from (towards) the IP for positive (negative) values of γ_s . Since, unlike for the other two rotation cases that will be studied, positive and negative rotation values are not symmetric, this misalignment is studied for both positive and negative γ_s values. The divergent effect at the tails is a result of a large population of fits not having fit quantities within the cores, and so not appearing in the fit rms. Once again, affected quantities of interest θ bias, $\Delta\theta$ bias, and $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$. The effects of misalignment can be seen in Figures 23 (a)–(c). The relationship between biases and γ_s is roughly linear with $\Delta\gamma_s=0.3$ mrad (the angular scale corresponding to linear shifts of ~ 1 mm) corresponding to 0.005 mrad (0.12 mrad) for θ ($\Delta\theta$). For $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$, degradation is not symmetric. For negative (positive) γ_s , with the quadruplet tilted towards (away from) the IP, slope-roads are artificially expanded (shrunk), decreasing (increasing) the granularity of the trigger, explaining the asymmetry in Figure 23 (c), with the degradation being a 10% (25%) effect for γ_s of +(-)0.3 mrad.

Corrections are less simple in this case. In principle, corrections of the same accuracy of the translations could be calculated per strip, but the overhead of one correction per strip (many thousands of constants) is prohibitive. Instead, each plane was divided into eight equal segments with a t value (z in the slope calculation) assigned to strips in each region to correct for the misalignment. This amounts to 56 extra constants and a 2D instead of a 1D LUT for z positions while the algorithm runs. The corrected distributions can also be seen in Figures 23 (a)–(c). The corrections, while not as effective as for the simple translation cases, are still very effective with the quoted misalignment values for bias shifts down to 0.001 mrad (0.25 mrad) for θ ($\Delta\theta$) and no more than a 2% degradation in $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$ for $|\gamma_s| = 0.3$ mrad.

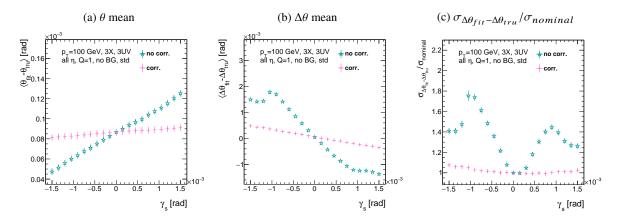


Figure 23: The noticeable effects of rotations in the s axis and the behavior of these quantities (θ and $\Delta\theta$ bias shifts and $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}/\sigma_{nominal}$) with and without misalignment correction.

5.6. Rotation Misalignments Around the Wedge Vertical Axis (β_z)

While misalignments coming from rotations around the z axis (the direction orthogonal to both the beamline and the horizontal strip direction) foreshorten the strips as seen from the IP and add a deviation in t, the long lever arm largely washes out any effects of this misalignment. Only the $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$ is noticeably affected, though only at severe misalignments, with only about a 1% degradation in performance at $\beta_z = 0.3$ mrad (corresponding to a linear shift of ~ 1 mm). A simulation based correction works well to cancel out the effects of this misalignment, and the $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$ as a function of misalignment with and without corrections are shown in Figure 24. The apparent 2% effect in the simulation corrected curve is a result of a more mild version of the effect shown in Figure 7.

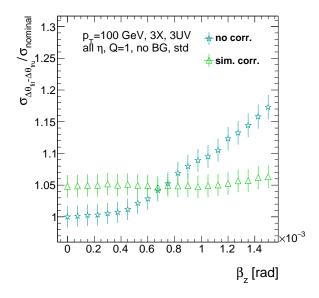


Figure 24: The effects of rotations in the z axis on $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}/\sigma_{nominal}$ a function of β_z both with and without misalignment corrections.

5.7. Rotation Misalignments Around the Axis Parallel to the Beamline (α_t)

Misalignments arising from rotations around the t axis (parallel to the beamline at the center of the base of the wedge) are essentially rotations in the ϕ direction. The quantities of interest most affected are the ϕ bias and $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$, as shown in Figures 25 (a) and (b), respectively, and correspond to a shift in ϕ bias of 0.2 mrad and a 10% degradation in $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}$ for $\alpha_t=0.3$ mrad (corresponding to a linear shift of ~ 1 mm). The raw instead of fitted mean ϕ biases is used in Figure 25 (a) to better illustrate the effect of misalignment.

Since the effect of misalignment is dependent on horizontal (along the strip direction, \hat{s}) in addition to vertical information, corrections cannot be applied before a fit takes place. The ϕ bias shift is uniform over the entire wedge, so a constant additive correction to ϕ based on the level of misalignment can be applied to all fits depending on how many misaligned stereo planes enter in the fit. $\Delta\theta$ is less straightforward, but corrections to the y and z information used in the local slope calculation in Equation 2 can be applied once θ_{fit} and ϕ_{fit} are known. These corrections are calculated ahead of time in bins of uniform η and ϕ as with the simulation corrections using the same framework as the misalignment calculation in Appendix D. The results of both types of correction can be seen in Figure 22. The apparent discrepancy between the simulation and analytic corrections in the ϕ bias happens for the same reason as in the Δs misalignment correction cases, as simulation correction restores a more Gaussian shape to the ϕ residual distribution opposed to the uncorrected nominal case, as discussed in Section 5.1.

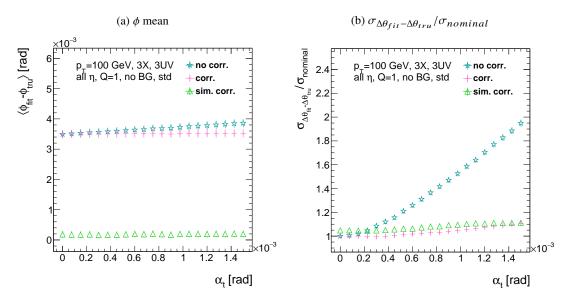


Figure 25: The effects of rotation misalignments around the t axis for ϕ bias and $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}/\sigma_{nominal}$ as a function of misalignment. The uncorrected and both the analytic and simulation correction cases are shown.

6. Conclusion

The algorithm for Micromegas detectors in the NSW Trigger Processor performs well in a variety of conditions and has proven robust to a number of effects to deliver measurements on muon tracks of the three angles θ , ϕ , $\Delta\theta$. Under nominal conditions, the rms values for the residuals of these quantities are 0.364 402 mrad for θ , 8.12 mrad for ϕ , and 1.47 mrad for $\Delta\theta$. Algorithm performance was found to be largely inde-403 pendent of the charge threshold setting, and a hit majority BCID association was found to provide proper 404 timing information over 99.7% even in the most relaxed settings (2X+1UV coincidence threshold require-405 ment+wide slope-road+background). The introduction of wide slope-roads to better mimic potentially 406 limited algorithm resources at run time and the introduction of incoherent background was found to have 407 a manageable effect on fit quantity residual rms values and on total algorithm efficiency for sufficiently 408 stringent coincidence threshold. The effects of the three translation and three rotation misalignments 409 specified by AMDB convention were studied, and correction methods for each of the six cases was de-410 veloped. Simulation-based corrections were found to improve nominal algorithm performance to residual 411 rms value of 0.291 mrad for θ , 3.19 mrad for ϕ , and 1.54 for $\Delta\theta$, which represent improvements of 20%, 62%, and -4.7%, respectively. Misalignment corrections were found to restore nominal performance for all but the rotation around the s axis, and a summary of tolerances may be found in Table 3.

Table 3: A summary of levels of misalignment corresponding to a 10% degradation in any residual rms or, for biases shifts of, 0.01 mrad for θ , 1 mrad for ϕ , and 0.25 mrad for $\Delta\theta$ for both the uncorrected and corrected cases; > 5 mm and > 1.5 mrad mean that such a degradation does not occur for the range of misalignment studied. Most affected quantity in parentheses.

	No Correction	Correction
Δs	4 mm (ϕ bias)	> 5 mm
Δz	$0.25 \text{ mm } (\Delta \theta)$	> 5 mm
Δt	$0.25 \text{ mm } (\Delta \theta)$	> 5 mm
γ_s	$0.15 \text{ mrad } (\Delta \theta \text{ bias})$	0.75 mrad
β_z	$0.9 \text{ mrad } (\Delta\theta \text{ rms})$	> 1.5 mrad
α_t	$0.375 \text{ mrad } (\Delta\theta \text{ rms})$	> 1.5 mrad

Appendix

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416 A. Changes to Local Slope Calculation for Fixed Point

The local X slope is expressed in [1] as:

$$M_X^{local} = A_k \sum_i y_i z_i - B_k \sum_i y_i, \ B_k = \frac{1}{n} \sum_i z_i A_k = \bar{z} A_k \tag{6}$$

Procedurally, this entails doing the sums over y_i and $y_i z_i$, multiplying the sums by A_k , B_k , and then subtracting both of these numbers, $O\left(10^3\right)$, to get local slopes, $O\left(10^{-1}\right)$, while requiring precision on these numbers on the order of $O\left(10^{-3}\right)$. This requires precision in the sums $O\left(10^{-7}\right)$, and with 32 bit fixed point numbers, there are deviations with respect to the floating point calculations at the level of $O\left(10^{-5}\right)$, which is enough to introduce a significant bias in the $\Delta\theta$ calculation.

In order to prevent these errors, we do the subtraction first

$$M_X^{local} = A_k \sum_i y_i z_i - B_k \sum_i y_i = A_k \sum_i (y_i z_i - y_i \bar{z}) = B_k \sum_i y_i \left(\frac{z_i}{\bar{z}} - 1\right)$$
 (7)

Thus, we change the order of operations and store $1/\bar{z}$ instead of A_k in addition to B_k . We also change the units of y_i and z_i in the calculation by dividing the millimeter lengths by 8192.⁷ With these changes, a 32 bit fixed point based algorithm has essentially identical performance to that of an algorithm based on the usual C++ 32 floating point numbers. Future work includes converting the 32 bit fixed point arithmetic to 16 bit where possible in the algorithm. While introducing 16 bit numbers uniformly might seem preferable, since simple 16-bit operations in the firmware can be done in a single clock tick, and a larger number of bits increases the algorithm latency, some numbers in the algorithm will require a larger number of bits, in particular in the local slope calculation, which is the single calculation in the algorithm requiring the largest numeric range.

⁷ Chosen since it is a perfect power of 2 and of order the length scale of z in millimeters

B. Biases in the ϕ Calculation

While the θ and $\Delta\theta$ distributions have a mostly Gaussian shape, the ϕ resolution distribution has a markedly non-Gaussian shape. In order to verify the algorithm was performing correctly, all of the algorithm slope inputs were verified to match up to their truth-level values (calculated using truth-level angles). Some such plots are shown in Figure 26, and, as can be seen from the figure, all input quantities have some η dependence.

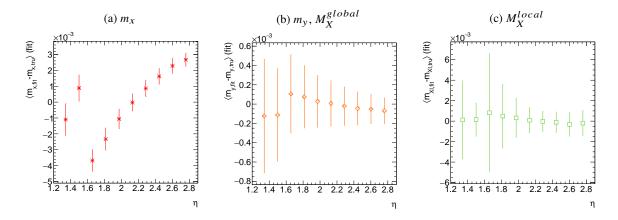


Figure 26: The mean of the residuals (fit value less truth value) of algorithm input slopes as a function of η . Note that the discontinuity in all three plots is a feature of the fact that each plane is divided into two stations in η , the positions of which are configured independently. Error bars are the rms in each bin.

This dependence is limited for both M_X^{global} and M_X^{local} but is noticeable for m_x , the slope corresponding to the horizontal coordinate used in fit angle calculations. This quantity depends heavily on information from hits in the stereo planes. The geometry of detector setup used in this simulation explains both the η dependence of all the quantities in Figure 26 and the stronger dependence for m_x in particular. A cartoon of a muon track moving through an octuplet in the NSW with its resulting ionization is shown in Figure 27.

As the figure shows, the geometry is such that hits in stereo U (V) planes tend to be biased downwards (upwards), while biases among the horizontal hits will tend to cancel. The size of this effect depends on the slope of the track and, hence, on η . This η dependent bias can be seen in Figure 26. Recalling Equation 3, ϕ depends most heavily on the stereo strip information, while θ and $\Delta\theta$ depend much more heavily on the horizontal strip information. This can be seen in Figure 28, where the relative shift in θ and $\Delta\theta$ is similar to that of the two M_X slopes in Figure 26, and that of ϕ is similar to m_X .

As to the overall accuracy of the ϕ calculation given the non-trivial overall bias of about 0.5 mrad, geometric parameters of the wedge (not properly defined in the software release) were tuned so that biases of input reconstructed means truth slope distributions were centered at zero. Example distributions of such quantities can be seen in Figure 29. The size of the bias can be attributed to the large smear that arises from the larger station at higher η , which causes the features in Figures 26 (a), 28 (a), and ultimately the overall shape in the ϕ residual distribution.

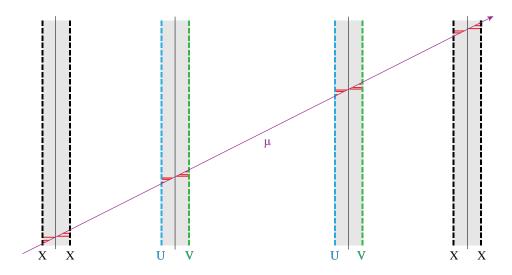


Figure 27: A cartoon of a muon (purple) passing through the NSW. Gaseous regions are shown in gray, horizontal plane strips shown in black, U (V) stereo plane strips shown in blue (green), and ionization in red.

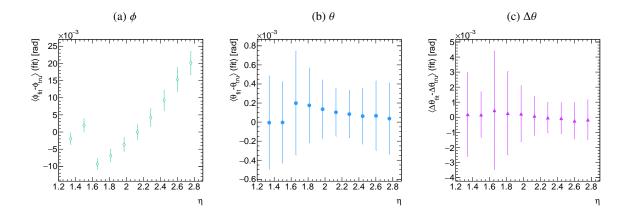


Figure 28: The resolutions (fit value less truth value) of algorithm output angles as a function of η . Note that the discontinuity in all three plots results from the fact that each plane is divided into two stations in η , the positions of which are configured independently. Error bars are the rms in each bin.

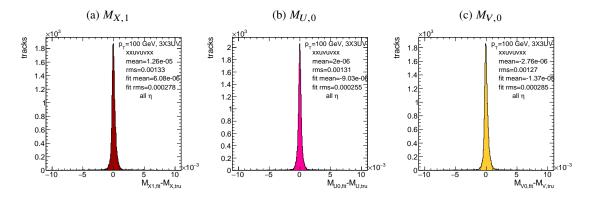


Figure 29: Example calibration plots for input slopes—in these cases resolutions for the X (a), U (b), and V (c) planes in a row in the first quadruplet.

57 C. Background Rates Normalization

Incoherent background is generated based on the assumption that the intensity only varies as a function of the distance from a point to the beamline, r. The number of hits per unit area per unit time as a function of r is given in Equation 8 and taken from [1].

$$I = I_0 (r/r_0)^{-2.125}$$
(8)

where $r_0 = 1000 \text{ mm}$ and $I_0 = 0.141 \text{ kHz/mm}^2$

Background generation happens per event as follows:

- 1. Determine the total number of hits to be generated in this event according to a Poisson distribution
- 2. Assign a time to hits uniformly in $[t_{start} t_{VMM}, t_{end}]$ where start and end are for the event clock and t_{VMM} is the VMM chip deadtime (100 ns)
- 3. Assign a plane to hits uniformly

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- 4. Assign a ϕ value to hits uniformly
- 5. Assign an r to hits according to Equation 8
- 6. Calculate hit information according to these values.

The expectation value for the Poisson distribution is determined by integrating Equation 8 over the surface area of the wedge to get the total hit rate for the wedge, Γ , and then multiplying this by the length of the time window over which hits may be generated. With H = 982 mm, $h_1 = 3665$ mm, and $\theta_w = 33\pi/180$, we find8:

$$\Gamma = 2I_0 r_0^{2.125} \int_0^{\theta_w/2} d\phi \int_{H \sec \phi}^{(H+h_1) \sec \phi} r \, dr \, r^{-2.125} = 98.6657 \,\text{MHz}$$
(9)

In this case, we have taken the nominal values of the MM sector geometry for H (wedge base), h_1 (the wedge height), and θ_w (the wedge opening angle).

 $^{^8}$ Using Mathematica and the extra factor of r from the volume element

D. Generic Calculation of Misalignment

Table 4: A summary of notation used in this section: note that non-AMDB notation is used in this section.

Symbol	Definition
S_X, S_Y, S_Z, \vec{S}	Position of the muon hit in ATLAS global coordinates; the infinite momentum muon
	track
ĥ	Vector normal to the plane; taken to be \hat{z} (the beamline) in the nominal case
$\mathscr{O}_{IP}^{g,l}$	Position of the interaction point in ATLAS global (g) or wedge local (l) coordinates
\mathcal{O}_{base}^{IP}	Position of the plane base in ATLAS global (g) or wedge local (l) coordinates;
buse	$(0, y_{base}, z_{pl})$ ((0,0,0)) for the nominal case in global (local) coordinates
ζ	$\vec{s} - \vec{\mathcal{O}}_{base}$
primed quant.	quantities after misalignment

Generically speaking, a hit is the intersection of a line (the muon track) with a plane (the individual plane in the multiplet). We assume the muon moves in a straight line defined by the origin and the truth-level 478 θ_{pos} and ϕ_{pos} (i.e. the infinite momentum limit) and that the MM plane is rigid and defined by a point, which we take to be the center of the bottom edge of the plane, and a normal vector, which we take to the z axis in the nominal case. 481

The coordinate axes x, y, z axes used here correspond to the usual AMDB s, z, -t axes. Since the direction does not really matter when studying misalignment or corrections thereof, the major difference is the 483 choice of origin. 484

The muon track we denote \vec{s} , the bottom point of the plane \mathcal{O}_{base} , and the normal vector \hat{n} . The muon track will always be given as (the wedge gets moved, not the muon): 486

$$\vec{s} = \mathcal{O}_{IP} + k\hat{s} \tag{10}$$

$$\hat{s} = \sin \theta_{pos} \sin \phi_{pos} \hat{x} + \sin \theta_{pos} \cos \phi_{pos} \hat{y} + \cos \theta_{pos} \hat{z}$$
 (11)

$$\hat{s} = \sin \theta_{pos} \sin \phi_{pos} \hat{x} + \sin \theta_{pos} \cos \phi_{pos} \hat{y} + \cos \theta_{pos} \hat{z}$$

$$\vec{s}^g = k \hat{s} = \frac{z_{pl}}{\cos \theta_{pos}} \hat{s} = z_{pl} (\tan \theta \sin \phi \hat{x} + \tan \theta \cos \phi \hat{y} + 1)$$
(12)

where $k \in \mathbb{R}$, along with the unit vector \hat{s} , defines the point where the track intersects the wedge.

Rotations are done before translations, according to the order prescribed in the AMDB guide for chamber 488 alignment, so the axes the principal axes of the plane are rotated according to the following matrix (where s, c, and t are the obvious trigonometric substitutions)

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c\gamma & -s\gamma \\ 0 & s\gamma & c\gamma \end{pmatrix} \begin{pmatrix} c\beta & 0 & s\beta \\ 0 & 1 & 0 \\ -s\beta & 0 & c\beta \end{pmatrix} \begin{pmatrix} c\alpha & -s\alpha & 0 \\ s\alpha & c\alpha & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c\gamma & -s\gamma \\ 0 & s\gamma & c\gamma \end{pmatrix} \begin{pmatrix} c\alpha c\beta & -s\alpha c\beta & s\beta \\ s\alpha & c\alpha & 0 \\ -c\alpha s\beta & s\alpha s\beta & c\beta \end{pmatrix}$$

$$= \begin{pmatrix} c\alpha c\beta & -s\alpha c\beta & s\beta \\ s\alpha c\gamma + c\alpha s\beta s\gamma & c\alpha c\gamma - s\alpha s\beta s\gamma & -c\beta s\gamma \\ s\alpha s\gamma - c\alpha s\beta c\gamma & c\alpha s\gamma + s\alpha s\beta c\gamma & c\beta c\gamma \end{pmatrix} = A$$

$$(13)$$

⁹ Recall ϕ_{pos} is defined with respect to the y axis instead of the x axis, as might otherwise be typical.

The thing that matters is what the new strip hit is—i.e. what the new y value is since this, along with a plane number, is all that is fed into the algorithm. To find this, we must solve for the new point of intersection with the rotated plane and then apply the effects of translations. The path connecting the base of the wedge with the intersection of the muon track will always be orthogonal to the normal vector of the plane. Our quantities after misalignment, denoted by primed quantities, will look like

$$\mathcal{O}_{base} \to \mathcal{O}_{base} + ds\hat{x} + dz\hat{y} + dt\hat{z} = \mathcal{O}'_{base}, \ \hat{n} \to A\hat{n} = A\hat{z} = \hat{z}', \ \vec{s} \to k'\hat{s} + \mathcal{O}_{IP} = \vec{s}'$$
 (14)

so, moving to explicit, global coordinates in the last line so we can do the computation (relying on the fact that any vector in the wedge, namely $\vec{\zeta} = \vec{s} - \mathcal{O}$ the local coordinates of the interaction point, is necessarily orthogonal to \hat{n}):

$$0 = \hat{n} \cdot (\vec{\mathcal{O}}_{base} - \vec{s}) \to 0 = A\hat{z}' \cdot (\vec{\mathcal{O}}'_{base} - (k'\hat{s} + \vec{\mathcal{O}}_{IP}))$$
 (15)

$$\rightarrow k' = \frac{s\beta\mathcal{O}'_{base-IP,x} - c\beta s\gamma\mathcal{O}'_{base-IP,y} + c\beta c\gamma\mathcal{O}'_{base-IP,z}}{\hat{s}\cdot\hat{z}'}$$
(16)

$$= \frac{s\beta ds - c\beta s\gamma \left(y_{base} + dz\right) + c\beta c\gamma \left(z_{pl} + dt\right)}{s\beta s\theta s\phi - c\beta s\gamma s\theta c\phi + c\beta c\gamma c\theta}$$
(17)

To find our new y coordinate, we need to evaluate $s'_{y} = \hat{y}' \cdot k'\vec{s}$ to find the final correction of:

$$\Delta y = \vec{\zeta}' \cdot \hat{y}' - \vec{\zeta} \cdot \hat{y} = \left(k'\hat{s} - \vec{\mathcal{O}}'_{base}\right) \cdot \hat{y}' - \left(s_y - y_{base}\right)$$
(18)

The correction will be plane dependent since (denoting the stereo angle ω):

$$\hat{y}_X = \hat{y} \to \hat{y}_X' = -s\alpha c \beta \hat{x} + (c\alpha c \gamma - s\alpha s \beta s \gamma) \hat{y} + (c\alpha s \gamma + s\alpha s \beta c \gamma) \hat{z}$$
(19)

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$$\begin{split} \hat{y}_{U,V} &= \pm s\omega \hat{x}' + c\omega \hat{y}_{U,V}' = \left[\pm c\alpha c\beta s\omega - s\alpha c\beta c\omega \right] \hat{x} + \left[\pm \left(s\alpha c\gamma + c\alpha s\beta s\gamma \right) s\omega \right. \\ &+ \left. \left(c\alpha c\gamma - s\alpha s\beta s\gamma \right) c\omega \right] \hat{y} + \left[\pm \left(s\alpha s\gamma - c\alpha s\beta c\gamma \right) s\omega + \left(c\alpha s\gamma + s\alpha s\beta c\gamma \right) c\omega \right] \hat{z} \end{split}$$

D.1. Individual Cases

Currently we only study the cases where one misalignment parameter is not zero. We examine these in detail below, calculating the most pertinent quantities in the misalignment calculation, k'/k and the new horizontal and stereo y axes. Before setting out, we simplify the expressions for the transformed \hat{y}' 's, removing any terms with the product of two sines of misalignment angles, which will be zero.¹⁰

$$\hat{y}_X' = -s\alpha c \beta \hat{x} + c\alpha c \gamma \hat{y} + c\alpha s \gamma \hat{z} \tag{21}$$

$$\hat{y}'_{U,V} = \left[\pm c\alpha c\beta s\omega - s\alpha c\beta c\omega\right] \hat{x} + \left[\pm s\alpha c\gamma s\omega + c\alpha c\gamma c\omega\right] \hat{y} + \left[\mp c\alpha s\beta c\gamma s\omega + c\alpha s\gamma c\omega\right] \hat{z}$$
(22)

If the translations are zero.

$$k' = \frac{-c\beta s\gamma y_{base} + c\beta c\gamma z_{pl}}{s\beta s\theta s\phi - c\beta s\gamma s\theta c\phi + c\beta c\gamma c\theta}, \ k'/k = \frac{-c\beta s\gamma y_{base}/z_{pl} + c\beta c\gamma}{s\beta t\theta s\phi - c\beta s\gamma t\theta c\phi + c\beta c\gamma}$$
(23)

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 $^{^{10}}$ If only one misalignment parameter is non-zero, then two or more sines will contain at least one term will contain $\sin 0 = 0$.

D.1.1. $ds \neq 0$

k'/k = 1 (the point of intersection does not move closer or further from the IP), and only the stereo planes are affected. Note that only relevant term in Equation 18, for the stereo strip \hat{y} for $\hat{\mathcal{O}}'_{base} = ds\hat{x}$ is:

$$\pm \sin \omega ds \approx \pm 0.0261 ds \tag{24}$$

meaning that a displacement in x of 17 mm, more than three times the range of misalignments studied, would be necessary for a shift in the stereo planes corresponding to one strip width.

D.1.2. $dz \neq 0$

k'/k = 1 (the point of intersection does not move closer or further from the IP). This case is the trivial one (cf. Equation 18 with $\vec{\mathcal{O}}'_{base} = dz\hat{y}$). y just gets moved in the opposite direction as the wedge. Correction is an additive constant.

D.1.3. $dt \neq 0$

 $k'/k = (z_{pl} + dt)/z_{pl}$. y gets modified by a simple scale factor. Correct by storing changing definitions of plane positions in algorithm to match the misaligned values.

D.1.4. $\alpha \neq 0$

k'/k = 1 and

$$\hat{\mathbf{y}}_{\mathbf{X}}' = -s\alpha\hat{\mathbf{x}} + c\alpha\hat{\mathbf{y}} \tag{25}$$

$$\hat{y}'_{X} = -s\alpha\hat{x} + c\alpha\hat{y}$$

$$\hat{y}'_{U,V} = [\pm c\alpha s\omega - s\alpha c\omega] \hat{x} + [\pm s\alpha s\omega + c\omega] \hat{y}$$
(25)

D.1.5. $\beta \neq 0$

We have $k'/k = (1 + \tan \beta \tan \theta \sin \phi)^{-1}$, and

$$\hat{\mathbf{y}}_X' = \hat{\mathbf{y}} \tag{27}$$

$$\hat{y}'_{U,V} = \hat{y} \pm (c\beta\hat{x} - s\beta\hat{z})s\omega \tag{28}$$

D.1.6. $\gamma \neq 0$

$$k'/k = \frac{1 - \tan \gamma \frac{y_{base}}{z_{pl}}}{1 - \tan \gamma \tan \theta \cos \phi}$$

$$\hat{y}'_{X} = c\gamma \hat{y} + s\gamma \hat{z}$$
(29)

$$\hat{\mathbf{y}}_{\mathbf{X}}' = c\gamma\hat{\mathbf{y}} + s\gamma\hat{\mathbf{z}} \tag{30}$$

$$\hat{y}'_{U,V} = \pm s\omega \hat{x} + c\omega \hat{y} - s\gamma c\omega \hat{z}$$
 (31)

E. Addressing MM Chamber Deformations Due to Gravity

Preliminary studies by the Saclay group have indicated that the Micromegas chambers will undergo continuous deformations at the scale of approximately half a millimeter due to the 0.7 degree tilt of the LHC ring combined with gravity. We have modeled the deformation as a combination of a twist β_z around the vertical axis orthogonal to the beamline and horizontal strip direction and a tilt γ_s around the horizontal axis in the strip direction at the chamber base, using the above misalignment and correction studies as a benchmark in each case. In addition to the two angular displacements, concerns have been raised over the effect of the non-planarity of the chambers, as misalignment studies were done under the assumption that chambers are rigid planes. One of the large sectors with the most severe deformations can be seen in Figure 30 taken from [3].

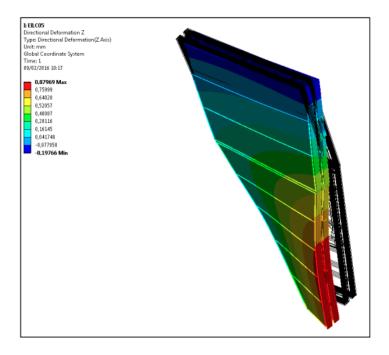


Figure 30: Large sector deformations

Before giving estimates of the impact of deformation on performance, it should be noted that in all of the cases examined, the quantity most affected is $\Delta\theta$ through the local slope calculation. Misalignment studies had one quadruplet in its nominal position and the other misaligned. This means that the bias in the local slope calculation has as non-trivial dependence on track θ, ϕ , which induces a larger total rms when integrated over an entire sector. If all planes (i.e. both quadruplets) experience the same misalignment/deformation, such systematic, position dependent bias is largely mitigated (though an overall average bias may not be). Since the recently reported deformations appear to have both quadruplets in a given chamber affected in the same way, we likely find ourselves in the latter, less severe case for $\Delta\theta$ rms, so the numbers quoted for degradation should be considered a conservative upper limit.

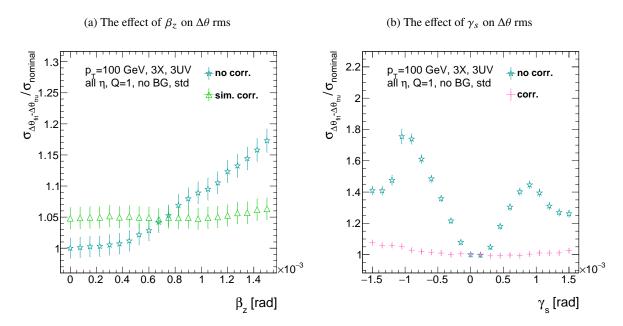


Figure 31: The effects of rotations in the z and (s) axes on $\sigma_{\Delta\theta_{fit}-\Delta\theta_{tru}}/\sigma_{nominal}$ a function of β_z (γ_s) in (a) ((b)) both with and without misalignment corrections.

545 E.1. The twist β_z

This effect, while the most dramatic in the pictures, probably does not have any noticeable effect on performance, as a 10% degradation in performance corresponds to $\beta_z = 1$ mrad, equivalent to a more than 3 mm linear translation, much greater than scales currently under consideration. At the maximal 1 mm levels quoted, this is a 1% effect, as can be seen in Figure 31 (a), reproduced from Section 5.5.

550 E.2. The tilt γ_s

The tilt is the deformation that is the most concerning, as detailed in 5.5. The 1 mm level of maximal deformation corresponds to $\gamma_s = 0.3$ mrad, while the intermediate deformation value of 0.5 mm corresponds to $\gamma_s = 0.15$ mrad. In the misalignment studies, this could correspond to a 20% (10%) degradation in $\Delta\theta$ resolution for 1 mm (0.5 mm) level deformations, as seen in Figure 31 (b). While the two quadruplets having equivalent deformations should mitigate this effect somewhat, corrections might be necessary here. These corrections, also outlined in Section 5.5, consist of dividing up each plane into eight equal segments in y (AMDB z) for a total of 64 constants (56 extra). While 64 total constants was more than sufficient for the studies in this note, if the deformations were severe and localized to one half of the chamber, then additional constants (naïvely twice as many) would probably be necessary to ensure the same level of performance. As Figure 31 (b) also, shows, these corrections make this deformation/misalignment a < 5% effect.

E.3. Non-planarity

Studies by Saclay have non-planarity effects inducing a 0.25 mm RMS to using the naïve rigid plane assumption. Misalignments of this order have the largest effect in the directions orthogonal to the horizontal strip direction (Δz and Δt), for which there was a 10% effect. Again, this figure is most certainly very conservative, as the effect of a general smearing would not be as deleterious as systematic shift of only one quadruplet. A summary of studies of these effects can be found in [3].

E.4. Estimate of Upper Limit of Overall Effect

In order to estimate the total effect of the deformations, we assume that only γ_s contributes. We take the γ_s corresponding to the peak to peak deformation value to affect half of each chamber. We also take the worse case for the sign of γ_s . Both of these assumptions are conservative, and so the figure presented here should be considered an **upper limit**.

Table 5: A summary of the deformation upper limit effect calculation. Even though both the positive and negative γ_s numbers are given, only the more severe (negative) numbers are used in the calculation.

$\gamma_s \left(l_{pk-to-pk} \right)$	- (+) $\gamma_s \% \Delta \theta$ degradation	$n_{chambers}$	
0.1 mrad (0.33 mm)	5 (0)%	5 (EISC06, 08, 10, 12)	
0.15 mrad (0.5–0.6 mm)	8 (0)%	6 (EISC02, 14, 15; EILC07, 09)	
0.3 mrad (0.8–1.0 mm)	20 (6)%	3 (EILC01, 03, 15)	
0.375 mrad (1.25 mm)	28 (15)%	2 (EISC05, 13)	
TOTAL	(25 + 48 + 6)	$50 + 56)\% \times \frac{1}{2} \times \frac{1}{16} = 6\%$	

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E.5. Conclusions

If nothing is done to correct for the deformations in the MM chambers, the above calculation shows that we can expect the effect to be at most 6% assuming the worst conditions from misalignment studies. Hence, the statement that this will be no more than a 10% effect seems more than reasonable. Nevertheless, corrections for the deformations presented do seem possible using the formalism and techniques presented in the note, and the case of most concern, the γ_s correction, can be addressed with the addition of 56 constants and two operations.

F. All Misalignment/Correction Plots

All plots for misalignment and all relevant misalignment correction types for fit quantities θ , ϕ , $\Delta\theta$ bias means and standard deviations for each of the six misalignment cases studied Δs (Figure 32), Δz (Figure 33), Δt (Figure 34), γ_s (Figure 35), β_s (Figure 36), and α_t (Figure 37)

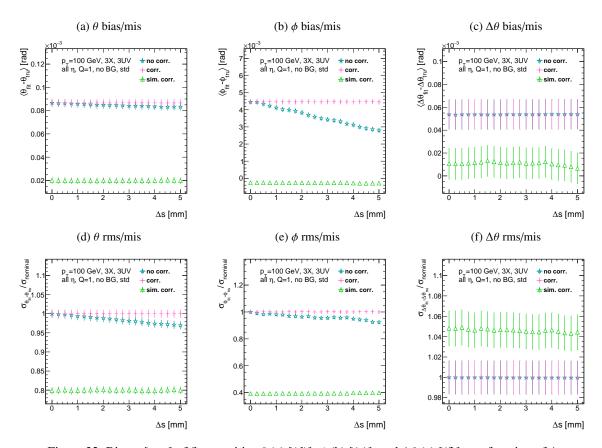


Figure 32: Biases [rms] of fit quantities θ (a) [(d)], ϕ (b) [(e)], and $\Delta\theta$ (c) [(f)] as a function of Δs .

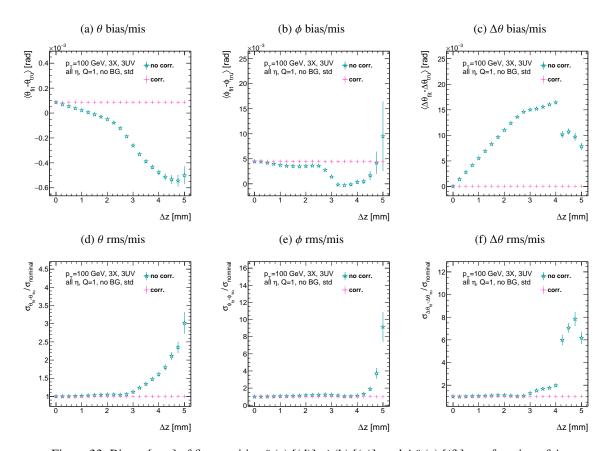


Figure 33: Biases [rms] of fit quantities θ (a) [(d)], ϕ (b) [(e)], and $\Delta\theta$ (c) [(f)] as a function of Δz .

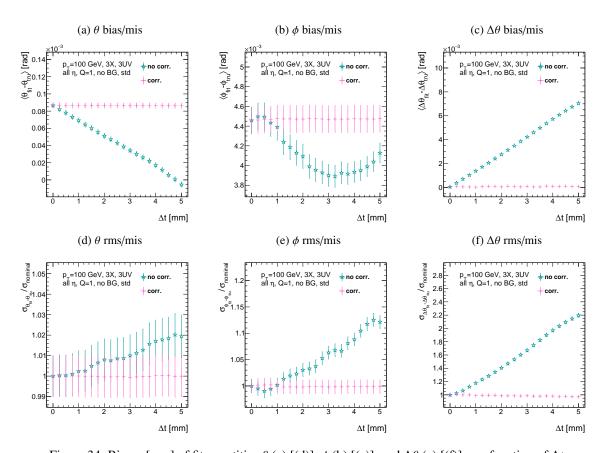


Figure 34: Biases [rms] of fit quantities θ (a) [(d)], ϕ (b) [(e)], and $\Delta\theta$ (c) [(f)] as a function of Δt .

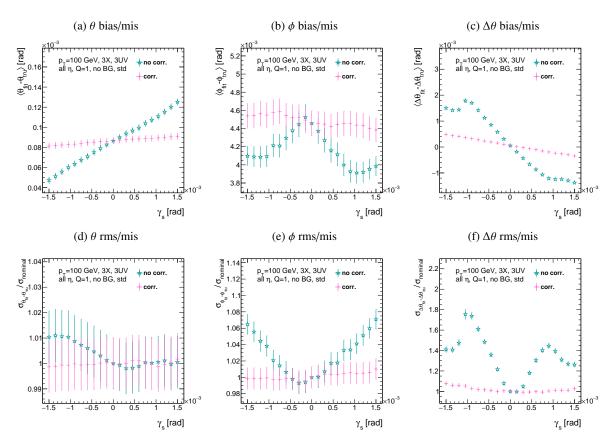


Figure 35: Biases [rms] of fit quantities θ (a) [(d)], ϕ (b) [(e)], and $\Delta\theta$ (c) [(f)] as a function of γ_s .

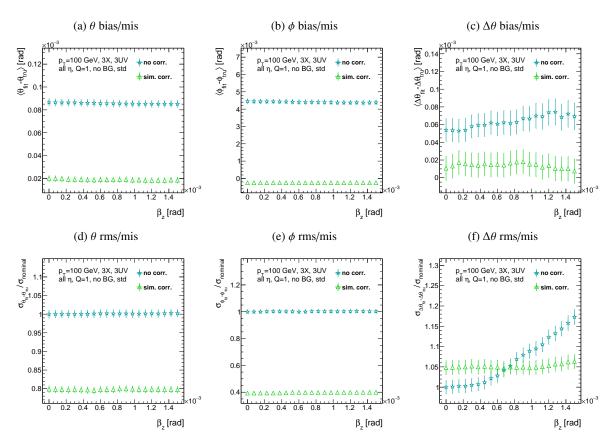


Figure 36: Biases [rms] of fit quantities θ (a) [(d)], ϕ (b) [(e)], and $\Delta\theta$ (c) [(f)] as a function of β_z .

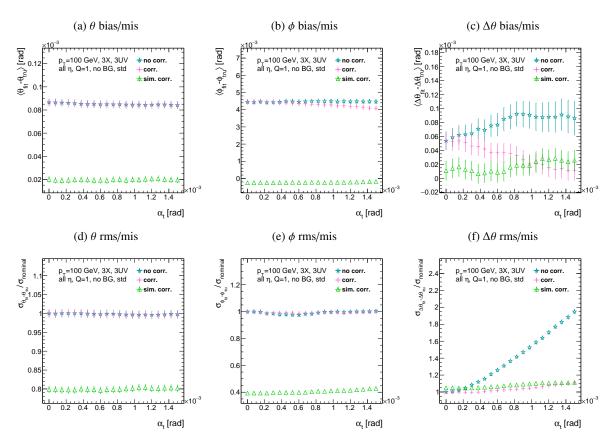


Figure 37: Biases [rms] of fit quantities θ (a) [(d)], ϕ (b) [(e)], and $\Delta\theta$ (c) [(f)] as a function of α_t

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References

- B Clark et al., 'An Algorithm for Micromegas Segment Reconstruction in the Level-1 Trigger of the New Small Wheel', tech. rep. ATL-UPGRADE-INT-2014-001, CERN, 2014, URL: https://cds.cern.ch/record/1753329.
- L Chevalier,

 'AMDB_SIMREC: A Structured data base for the ATLAS Spectrometer Simulation Program',

 tech. rep. ATL-MUON-97-148. ATL-M-PN-148, CERN, 1997,

 URL: https://cds.cern.ch/record/684070.
- [3] P Ponsot, ATLAS-NSW Sector Deformations: Impact of a twist on MM detectors, 2016.