

HW01_knn_kulikov

April 13, 2016

1 KNN – Digit Recognizer

1.1 Kulikov Alex, gr. 397

```
In [4]: import matplotlib
import numpy
import pandas
from knn import MatrixBasedKNearestNeighbor, KDBasedKNearestNeighbor

%pylab inline
%load_ext autoreload
%autoreload 2

pandas.options.display.max_colwidth = 0

from IPython.core.display import HTML
HTML("<style>.container { width:90% !important; }</style>")
```

Populating the interactive namespace from numpy and matplotlib

```
Out[4]: <IPython.core.display.HTML object>
```

1.2 Let's get some data!

```
In [5]: df = pandas.read_csv("kaggle_data/train.csv")
```

```
In [6]: df.head()
```

```
Out[6]:
```

	label	pixel0	pixel1	pixel2	pixel3	pixel4	pixel5	pixel6	pixel7	\
0	5	0	0	0	0	0	0	0	0	
1	0	0	0	0	0	0	0	0	0	
2	4	0	0	0	0	0	0	0	0	
3	1	0	0	0	0	0	0	0	0	
4	9	0	0	0	0	0	0	0	0	

	pixel8	...	pixel774	pixel775	pixel776	pixel777	pixel778	\
0	0	...	0	0	0	0	0	
1	0	...	0	0	0	0	0	
2	0	...	0	0	0	0	0	
3	0	...	0	0	0	0	0	
4	0	...	0	0	0	0	0	

	pixel779	pixel780	pixel781	pixel782	pixel783
0	0	0	0	0	0

```

1 0      0      0      0      0
2 0      0      0      0      0
3 0      0      0      0      0
4 0      0      0      0      0

```

[5 rows x 785 columns]

```

In [7]: print "Head:"
        print df.head()
        print "Shape:"
        print shape(df)

```

Head:

```

   label  pixel0  pixel1  pixel2  pixel3  pixel4  pixel5  pixel6  pixel7  \
0  5      0      0      0      0      0      0      0      0
1  0      0      0      0      0      0      0      0      0
2  4      0      0      0      0      0      0      0      0
3  1      0      0      0      0      0      0      0      0
4  9      0      0      0      0      0      0      0      0

```

```

   pixel8  ...  pixel774  pixel775  pixel776  pixel777  pixel778  \
0  0      ...  0      0      0      0      0
1  0      ...  0      0      0      0      0
2  0      ...  0      0      0      0      0
3  0      ...  0      0      0      0      0
4  0      ...  0      0      0      0      0

```

```

   pixel779  pixel780  pixel781  pixel782  pixel783
0  0      0      0      0      0
1  0      0      0      0      0
2  0      0      0      0      0
3  0      0      0      0      0
4  0      0      0      0      0

```

[5 rows x 785 columns]

Shape:

(20000, 785)

```

In [8]: X_train, y_train = df[df.columns[1:]].values, df["label"].values

```

1.2.1 OK, we have the initial data and we understand its structure

1.3 Visualizing it “as is”, binarized and with image centering

```

In [12]: def plot_image(img, im_size=28):
        pylab.imshow(img.reshape(im_size, im_size), cmap = "gray")

        def plot_grid(imgs, nrows, ncols, dataset = X_train, im_size = 28):
            fig = pyplot.gcf()
            fig.set_size_inches(17.5,15.5)
            for pylab_index, img in enumerate(imgs):
                pylab.subplot(nrows, ncols, pylab_index + 1)
                plot_image(img)
                pylab.axis('off')

```

```

In [24]: plot_grid(X_train[0:10], 1, 10)

```



```
In [25]: def binarize(img, bborder = 100):
    binarizator = MatrixBasedKNearestNeighbor(k = 3)
    img = img.reshape(binarizator.size, binarizator.size)
    img = binarizator.center_image(img)
    img = binarizator.binarize(img, black_border = bborder)

    img = img.reshape(binarizator.size * binarizator.size)

    return img

In [26]: def binarize_batch(img_set, bborder = 100):
    for index, img in enumerate(img_set):
        img_set[index] = binarize(img.copy(), bborder)
    return img_set

In [27]: def plot_grid_bin(imgs, nrows, ncols, bborder = 100, dataset = X_train, im_size = 28):
    fig = pyplot.gcf()
    fig.set_size_inches(17.5,15.5)
    binarizator = MatrixBasedKNearestNeighbor(k = 3)
    for pylab_index, img in enumerate(imgs):
        img = img.reshape(binarizator.size, binarizator.size)
        img = binarizator.binarize(img, bborder)
        pylab.subplot(nrows, ncols, pylab_index + 1)
        plot_image(img)
        pylab.axis('off')

In [28]: plot_grid_bin(X_train[0:20].copy(), 1, 20, bborder = 0)
```



```
In [29]: plot_grid_bin(X_train[0:20].copy(), 1, 20, bborder = 100)
```



```
In [385]: plot_grid_bin(X_train[0:20].copy(), 1, 20, bborder = 200)
```



```
In [386]: def plot_grid_bin_centered(imgs, nrows, ncols, bborder = 100, dataset = X_train, im_size = 28):
    fig = pyplot.gcf()
    fig.set_size_inches(17.5,15.5)
    for pylab_index, img in enumerate(imgs):
        img = binarize(img, bborder)
        pylab.subplot(nrows, ncols, pylab_index + 1)
        plot_image(img)
        pylab.axis('off')
```

```
In [387]: plot_grid_bin_centered(X_train[0:20].copy(), 1, 20, bborder = 0)
```



1.3.1 OK, now we can transform images in a simple way (binarization, centering) and draw them. Hopefully, this helps.

1.4 Plot means

```
In [388]: average_class_imgs = []

    figures = [[] for i in xrange(0, 10)]

    for cur_fig in xrange(0, 10):
        for image_id in xrange(1, len(X_train)):
            if (y_train[image_id] == cur_fig):
                figures[cur_fig].append(X_train[image_id])

        np_figures = np.array(figures[cur_fig])
        np_figures = np.mean(np_figures, axis = 0)
        average_class_imgs.append(np_figures)
        pass

    average_class_imgs = np.array(average_class_imgs)
```

```
In [389]: # Plot your means, note that is should be similar on to real smooth numbers -- done
    plot_grid(average_class_imgs, nrows = 1, ncols = 10)
```



```
In [390]: plot_grid_bin_centered(average_class_imgs.copy(), 1, 10, bborder = 50)
```



1.5 Matrix-based KNN

```
In [391]: # Code matrix-based KNN with L2 norm (see MatrixBasedKNearestNeighbor class)
          # Use predict on to X_train[:100] only for debug
```

```
In [392]: plot_grid(X_train[110:120], 1, 10)
```



```
In [393]: # KNN two loops
```

```
knn_clf_loop2 = MatrixBasedKNearestNeighbor(num_loops = 2, k = 3)
knn_clf_loop2 = knn_clf_loop2.fit(X_train[:110], y_train[:110])
%time knn_clf_loop2.calc_dist(X_train[110:120], metric="pixel_L1")
%time y_pred2 = knn_clf_loop2.predict_labels(X_train[110:120])
print y_pred2
```

CPU times: user 853 ms, sys: 43.3 ms, total: 897 ms

Wall time: 794 ms

[(9, 2)]

[(3, 2)]

[(1, 3)]

[(1, 3)]

[(0, 3)]

[(4, 2)]

[(9, 2)]

[(2, 2)]

[(0, 1)]

[(0, 3)]

CPU times: user 0 ns, sys: 0 ns, total: 0 ns

Wall time: 703 μ s

[9. 3. 1. 1. 0. 4. 9. 2. 0. 0.]

```
In [394]: # KNN one loop
```

```
knn_clf_loop1 = MatrixBasedKNearestNeighbor(num_loops = 1, k = 3)
knn_clf_loop1 = knn_clf_loop1.fit(X_train[:110], y_train[:110])
%time knn_clf_loop1.calc_dist(X_train[110:120], metric="pixel_L1")
%time y_pred1 = knn_clf_loop1.predict_labels(X_train[110:120])
print y_pred1
```

CPU times: user 787 ms, sys: 30 ms, total: 817 ms

Wall time: 763 ms

[(9, 2)]

[(3, 2)]

[(1, 3)]

[(1, 3)]

[(0, 3)]

[(4, 2)]

[(9, 2)]

[(2, 2)]

[(0, 1)]

[(0, 3)]

CPU times: user 3.33 ms, sys: 0 ns, total: 3.33 ms

Wall time: 648 μ s

[9. 3. 1. 1. 0. 4. 9. 2. 0. 0.]

```
In [395]: print 'good' if np.linalg.norm(y_pred2 - y_pred1) < 1e-4 else 'fail'
```

good

```
In [396]: # KNN no loops
```

```
knn_clf_loop0 = MatrixBasedKNearestNeighbor(num_loops = 0, k = 3)
knn_clf_loop0 = knn_clf_loop0.fit(X_train[:110], y_train[:110])
%time knn_clf_loop0.calc_dist(X_train[110:120], metric="pixel_L1")
%time y_pred0 = knn_clf_loop0.predict_labels(X_train[110:120])
print y_pred0
```

CPU times: user 707 ms, sys: 30 ms, total: 737 ms

Wall time: 710 ms

[(9, 2)]

[(3, 2)]

[(1, 3)]

[(1, 3)]

[(0, 3)]

[(4, 2)]

[(9, 2)]

[(2, 2)]

[(0, 1)]

[(0, 3)]

CPU times: user 0 ns, sys: 0 ns, total: 0 ns

Wall time: 652 μ s

[9. 3. 1. 1. 0. 4. 9. 2. 0. 0.]

```
In [397]: print 'good' if np.linalg.norm(y_pred1 - y_pred0) < 1e-4 else 'fail'
```

good

1.5.1 It works sometimes!

1.5.2 Lets' try the clever IMED metric

<http://www.cis.pku.edu.cn/faculty/vision/wangliwei/pdf/IMED.pdf>

```
In [13]: def precalc_G(sigma, size = 28):
```

```
    G = numpy.zeros(size * size * size * size).reshape(size, size, size, size)
```

```

sigma_squared = math.pow(sigma, 2)

# fill G
for row_i in range(size):
    for col_i in range(size):
        for row_j in range(size):
            for col_j in range(size):
                G[row_i][col_i][row_j][col_j] = math.exp(((row_i - row_j) * (row_i - row_j)

return G

G_0p4 = precalc_G(0.4) # 0.04
G_0p5 = precalc_G(0.5) # 0.14
G_0p6 = precalc_G(0.6) # 0.25
G_0p9 = precalc_G(0.9) # 0.53
G_1p01 = precalc_G(1.01) #0.61

In [399]: from collections import Counter
          print(Counter(y_train[:110]).keys())
          print(Counter(y_train[:110]).values())


[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
[14, 17, 7, 12, 11, 6, 12, 12, 8, 11]

In [403]: knn_IMED = MatrixBasedKNearestNeighbor(num_loops = 2, k = 1)
          knn_IMED = knn_IMED.init_G(G_1p5)
          # print(knn_IMED.G) # prints the pixel distance matrix
          knn_IMED = knn_IMED.fit(knn_IMED.ST_batch(X_train[:510].copy()), y_train[:510])
          %time knn_IMED = knn_IMED.calc_dist(X_train[1110:1120], metric="IMED")
          %time y_predIMED = knn_IMED.predict_labels(X_train[1110:1120])
          print y_predIMED

CPU times: user 56.7 ms, sys: 0 ns, total: 56.7 ms
Wall time: 59 ms
[[4, 1]]
[[8, 1]]
[[9, 1]]
[[8, 1]]
[[7, 1]]
[[1, 1]]
[[9, 1]]
[[6, 1]]
[[1, 1]]
[[3, 1]]
CPU times: user 3.33 ms, sys: 0 ns, total: 3.33 ms
Wall time: 1.31 ms
[ 4.  8.  9.  8.  7.  1.  9.  6.  1.  3.]

In [356]: plot_grid(X_train[1110:1120], 1, 10)

```



1.5.3 Seems that this metric is also working

1.6 KDTree-based KNN

```
In [9]: # KNN kd_tree
```

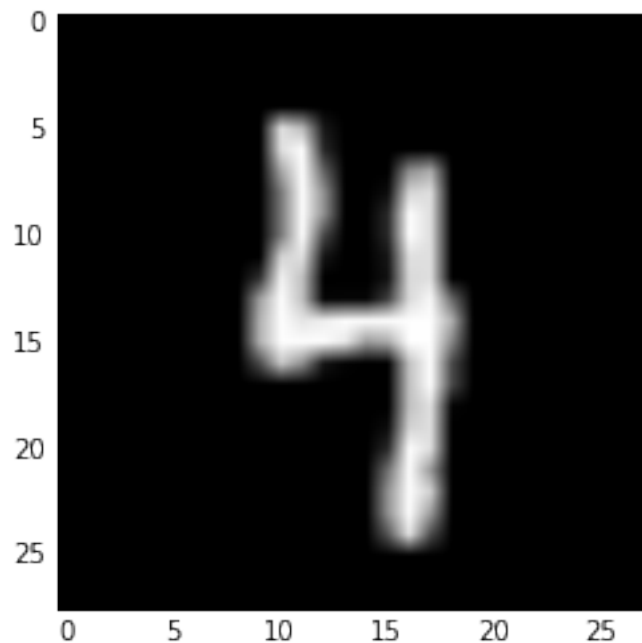
```
knn_clf_Tree = KDBasedKNearestNeighbor(k = 3)
knn_clf_Tree = knn_clf_Tree.fit(X_train[:110], y_train[:110])
knn_clf_Tree = knn_clf_Tree.calc_dist(X_train[1110:1120], "minkowski")
neighbors = knn_clf_Tree.get_neighbors(X_train[1110:1120])
%time y_pred = knn_clf_Tree.predict_labels(X_train[1110:1120])
print y_pred
print neighbors
```

CPU times: user 6.67 ms, sys: 0 ns, total: 6.67 ms

Wall time: 7.76 ms

```
[ 4.  5.  9.  6.  7.  1.  4.  1.  1.  0.]
[[ 26  92  48]
 [ 11  99  35]
 [ 26  84  54]
 [ 73  66  22]
 [ 52  84 103]
 [ 59  23   3]
 [ 58  92   4]
[105  77  59]
 [ 67  40  72]
 [  1  21   0]]
```

```
In [13]: plot_image(X_train[1110]) # one of the target images
```



```
In [14]: plot_grid(X_train[[26, 92, 48]], 1, 3) # and the 3 nearest neighbors (default 'minkowski' L2 m
```




1.7 It's time to test it 4real!

1.8 Code Accuracy score and Cross Validation Prosses

```
In [412]: # Accuracy
          from sklearn import metrics
```

```
def accuracy(y_true, y_predict):
    return metrics.accuracy_score(y_true, y_predict)
```

```
In [413]: print 'good' if accuracy([1, 1, 1, 0], [1, 1, 1, 5]) == 0.75 else 'fail'
```

good

```
In [442]: # Cross validation
```

```
from sklearn import cross_validation
from datetime import datetime
```

```
def my_cross_validation(X, y, predictor, metric, q_fold = 5, r_fold = 5):
    scores = []
```

```
    total_size = X.shape[0]
```

```
    seed = datetime.now().microsecond + datetime.now().second * 1000000
```

```
    shuffled_split = cross_validation.ShuffleSplit(total_size, n_iter=r_fold, test_size=1.0/q
```

```
    for train_index, test_index in shuffled_split:
```

```
        X_train = X[train_index]
```

```
        y_train = y[train_index]
```

```
        X_test = X[test_index]
```

```
        y_test = y[test_index]
```

```
        predictor = predictor.fit(X_train, y_train)
```

```
        predictor = predictor.calc_dist(X_test, metric)
```

```
        y_predicted = predictor.predict_labels(X_test)
```

```
        scores.append(accuracy(y_test, y_predicted))
```

```
    return np.mean(scores)
```

```
In [473]: # ShuffleSplit test using datetime.now() random seed
```

```
seed = datetime.now().microsecond + datetime.now().second * 1000000
shuffled_split = cross_validation.ShuffleSplit(10, n_iter=2, test_size=0.1, random_state=seed)
for train_index, test_index in shuffled_split:
    print(train_index)
    print(test_index)
```

```
[0 6 3 5 9 7 1 2 4]
```

```
[8]
```

```
[5 1 3 8 4 0 7 2 9]
```

```
[6]
```

1.9 Knn Matrix stats plotting

1.9.1 Dumb L1, L2, L3 metrics

Not a perfect metric for an image, frankly

```
In [475]: predictor = MatrixBasedKNearestNeighbor(k = 3)
print("L1: " + str(my_cross_validation(X_train[:100], y_train[:100], predictor, "pixel_L1", q
print("L2: " + str(my_cross_validation(X_train[:100], y_train[:100], predictor, "pixel_L2", q
```

```
L1: 0.74
```

```
L2: 0.48
```

```
In [447]: # without binarization
```

```
stats_k = [1, 3, 5, 7, 9]
stats_result_L1 = []
stats_result_L2 = []
stats_result_L3 = []

for k in stats_k:
    predictor = MatrixBasedKNearestNeighbor(k)
    stats_result_L1.append(my_cross_validation(X_train[:500], y_train[:500], predictor, "pixel_L1", q
    stats_result_L2.append(my_cross_validation(X_train[:500], y_train[:500], predictor, "pixel_L2", q
    stats_result_L3.append(my_cross_validation(X_train[:500], y_train[:500], predictor, "pixel_L3", q
```

```
print "L1 " + str(stats_result_L1)
print "L2 " + str(stats_result_L2)
print "L3 " + str(stats_result_L3)
```

```
from matplotlib import pyplot
```

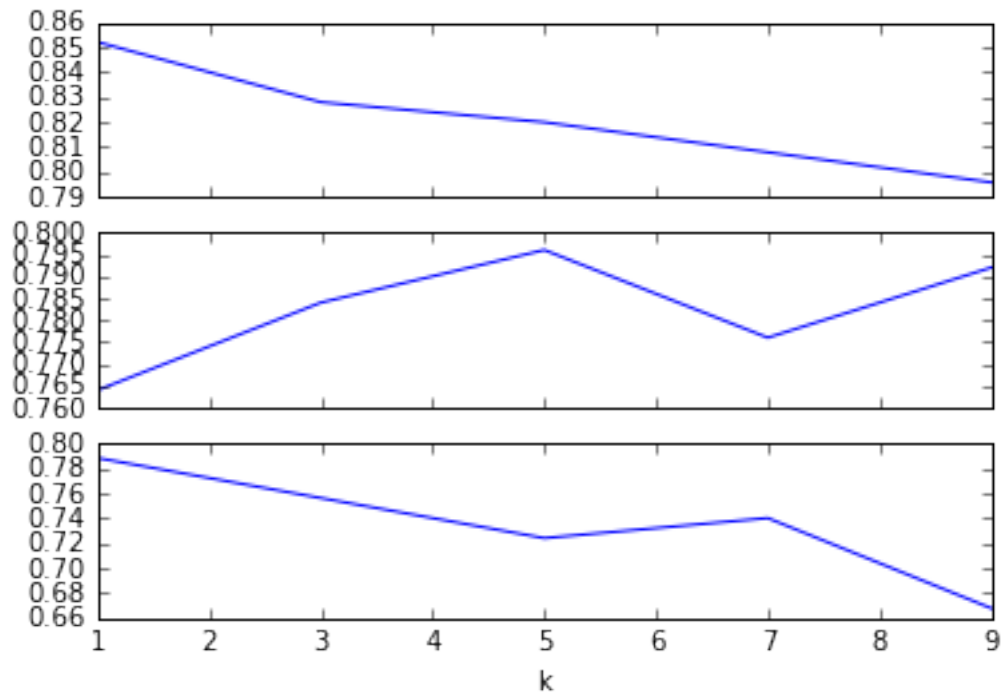
```
f, axarr = plt.subplots(3, sharex=True)
axarr[2].set_xlabel("k")
axarr[0].plot(stats_k, stats_result_L1)
axarr[1].plot(stats_k, stats_result_L2)
axarr[2].plot(stats_k, stats_result_L3)
```

```
L1 [0.8519999999999998, 0.82800000000000007, 0.82000000000000006, 0.80800000000000005, 0.79600000000000000]
```

```
L2 [0.76400000000000001, 0.78400000000000003, 0.79599999999999993, 0.77600000000000002, 0.79200000000000000]
```

```
L3 [0.78800000000000003, 0.75600000000000001, 0.72399999999999998, 0.73999999999999999, 0.66800000000000000]
```

```
Out[447]: [<matplotlib.lines.Line2D at 0x7fcee8d29710>]
```



```
In [448]: plot_grid(binarize_batch(X_train[:500].copy(), 10)[0:10], 1, 10)
```



```
In [449]: # with binarization
```

```
stats_k = [1, 3, 5, 7, 9]
borders = [10, 25, 50, 75, 100, 150]
stats_result_bin = []

for k in stats_k:
    this_result = []
    predictor = MatrixBasedKNearestNeighbor(k)

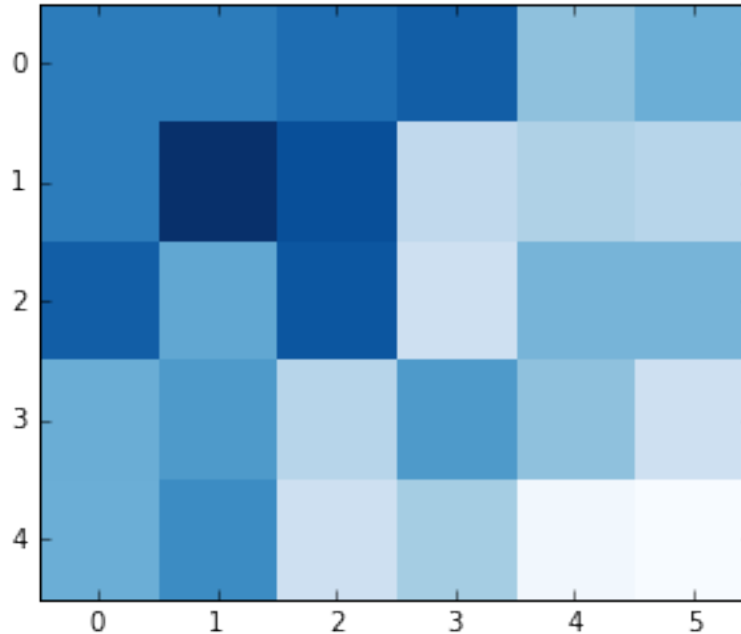
    for b in borders:
        this_result.append(my_cross_validation(binarize_batch(X_train[:500].copy(), b), y_train[:500]))
    stats_result_bin.append(this_result)

print "bin " + str(stats_result_bin)

from matplotlib import pyplot
```

```
plt.imshow(stats_result_bin,
            interpolation="nearest", cmap = "Blues")
plt.show()
```

```
bin [[0.8640000000000001, 0.8640000000000001, 0.8720000000000011, 0.8800000000000012, 0.8240000000000000,
```



```
In [450]: import pprint
```

```
pp = pprint.PrettyPrinter(indent=4)

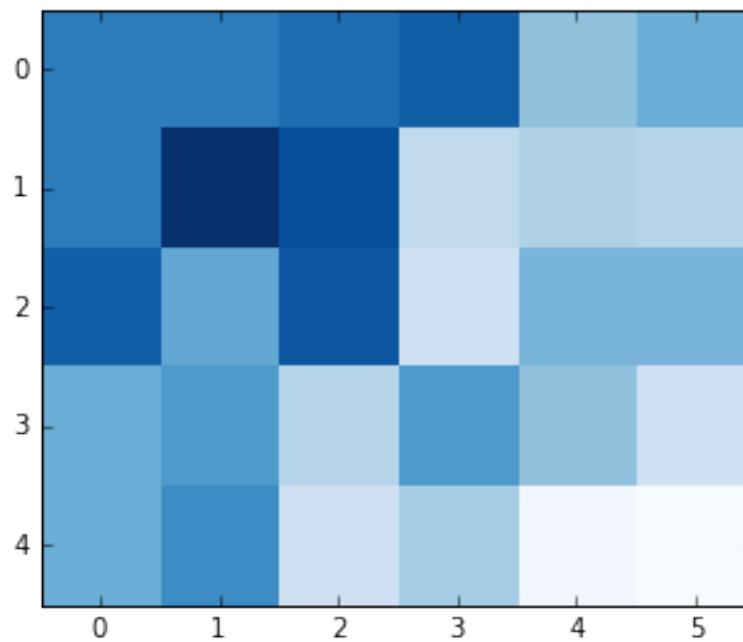
pp.pprint(stats_result_bin)

from matplotlib import pyplot

plt.imshow(stats_result_bin,
            interpolation="nearest", cmap = "Blues")
plt.show()
```

```
[ [ 0.8640000000000001,
    0.8640000000000001,
    0.8720000000000011,
    0.8800000000000012,
    0.8240000000000007,
    0.8359999999999997],
  [ 0.8640000000000001,
    0.9039999999999991,
    0.8880000000000012,
    0.8040000000000005,
    0.8120000000000006,
    0.8080000000000005],
```

```
[ 0.880000000000000012,
 0.840000000000000008,
 0.884000000000000001,
 0.796000000000000004,
 0.832000000000000007,
 0.832000000000000007],
[ 0.836000000000000008,
 0.847999999999999986,
 0.808000000000000005,
 0.848000000000000009,
 0.824000000000000007,
 0.796000000000000004],
[ 0.83599999999999997,
 0.856000000000000009,
 0.796000000000000004,
 0.816000000000000006,
 0.772000000000000002,
 0.768000000000000013]]
```



Seems that `black_border = 20` is close to the best one

In [451]: `plot_grid(binimize_batch(X_train[:500].copy(), 15)[0:10], 1, 10)`



```
In [452]: plot_grid(binarize_batch(X_train[:500].copy(), 20)[0:10], 1, 10)
```



```
In [453]: plot_grid(binarize_batch(X_train[:500].copy(), 25)[0:10], 1, 10)
```



1.9.2 IMED metric – time to set up some parameters

```
In [456]: stats_k = [1, 3, 5, 7, 9]
          stats_result_IMED = []

          for k in stats_k:
              predictor = MatrixBasedKNearestNeighbor(k)
              predictor = predictor.init_G(G_0p5)
              stats_result_IMED.append(my_cross_validation(predictor.ST_batch(X_train[:500].copy()), y_

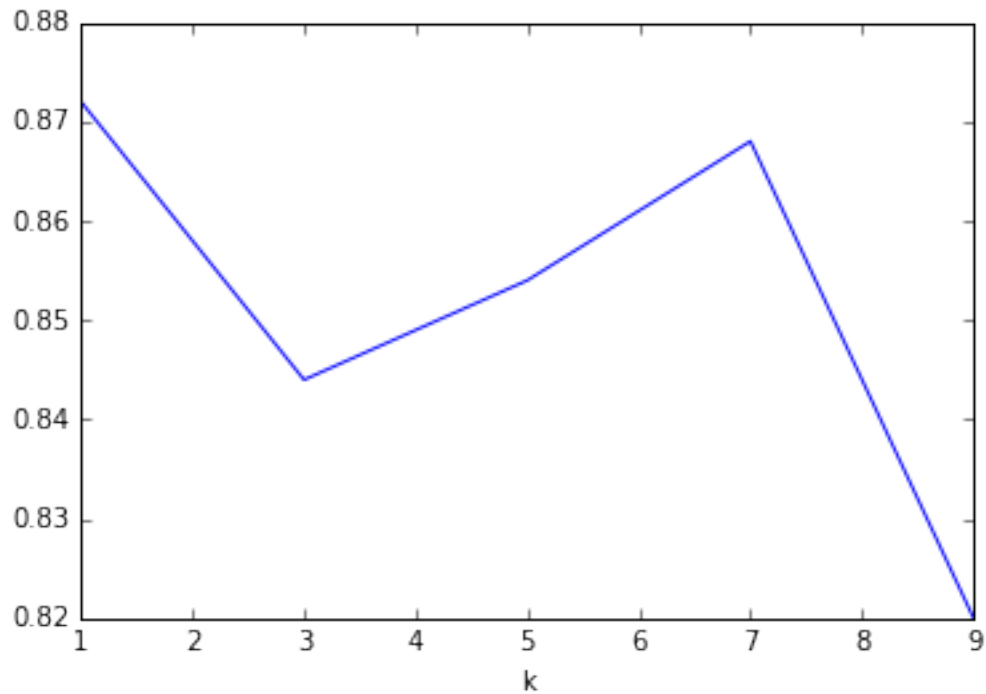
          print "IMED " + str(stats_result_IMED)

          from matplotlib import pyplot

          f, ax = plt.subplots()
          ax.set_xlabel("k")
          ax.plot(stats_k, stats_result_IMED)
```

```
IMED [0.87200000000000011, 0.84400000000000008, 0.85400000000000009, 0.8679999999999999, 0.82000000000000009]
```

```
Out[456]: [<matplotlib.lines.Line2D at 0x7fcee8f58f10>]
```



```
In [458]: stats_k = [1, 3, 5, 7, 9]
stats_result_IMED = []

for k in stats_k:
    predictor = MatrixBasedKNearestNeighbor(k)
    predictor = predictor.init_G(G_0p6)
    stats_result_IMED.append(my_cross_validation(predictor.ST_batch(X_train[:1000].copy()), y))

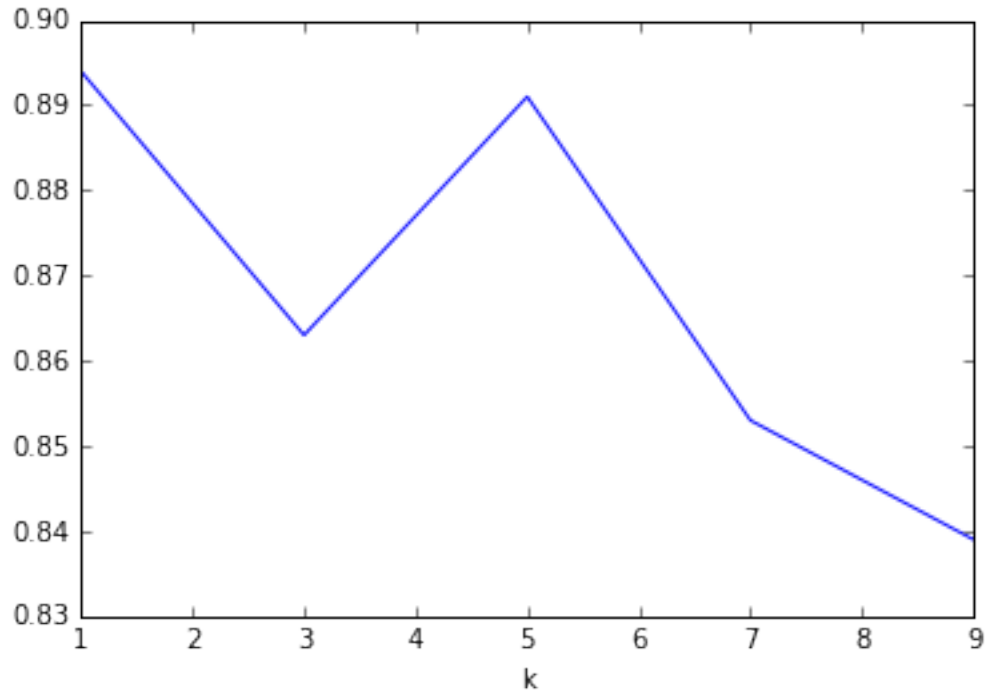
print "IMED " + str(stats_result_IMED)

from matplotlib import pyplot

f, ax = plt.subplots()
ax.set_xlabel("k")
ax.plot(stats_k, stats_result_IMED)

IMED [0.89400000000000013, 0.86299999999999988, 0.89100000000000001, 0.8529999999999998, 0.8389999999999998]

Out[458]: [<matplotlib.lines.Line2D at 0x7fcee9d28f90>]
```



```
In [460]: G_0p4 = precalc_G(0.4) # 0.04
          G_0p6 = precalc_G(0.6) # 0.25
          G_0p9 = precalc_G(0.9) # 0.53
          G_1p01 = precalc_G(1.01) #0.61
          G_1p3 = precalc_G(1.3) #0.74
          G_1p5 = precalc_G(1.5) #0.8
          G_2 = precalc_G(2) #0.88
          G_10 = precalc_G(10) #0.99 -- bad

stats_G = [G_0p4, G_0p5, G_0p6, G_0p9, G_1p01, G_1p3, G_1p5, G_2, G_10]
stats_result_IMED_G = []

for G in stats_G:
    predictor = MatrixBasedKNearestNeighbor(k=3)
    predictor = predictor.init_G(G)
    %time stats_result_IMED_G.append(my_cross_validation(predictor.ST_batch(X_train[:500]).copy(), X_test[:500]).copy())

CPU times: user 2.61 s, sys: 0 ns, total: 2.61 s
Wall time: 2.62 s
CPU times: user 2.62 s, sys: 0 ns, total: 2.62 s
Wall time: 2.62 s
CPU times: user 2.61 s, sys: 0 ns, total: 2.61 s
Wall time: 2.61 s
CPU times: user 3.81 s, sys: 0 ns, total: 3.81 s
Wall time: 3.81 s
CPU times: user 3.33 s, sys: 0 ns, total: 3.33 s
Wall time: 3.33 s
CPU times: user 3.2 s, sys: 0 ns, total: 3.2 s
```



```

Wall time: 3.2 s
CPU times: user 3.12 s, sys: 0 ns, total: 3.12 s
Wall time: 3.12 s
CPU times: user 3.6 s, sys: 0 ns, total: 3.6 s
Wall time: 3.6 s
CPU times: user 3.54 s, sys: 0 ns, total: 3.54 s
Wall time: 3.54 s

```

```
In [462]: # best G = (G_1p01) -- 0.61
```

```

print "IMED " + str(stats_result_IMED_G)

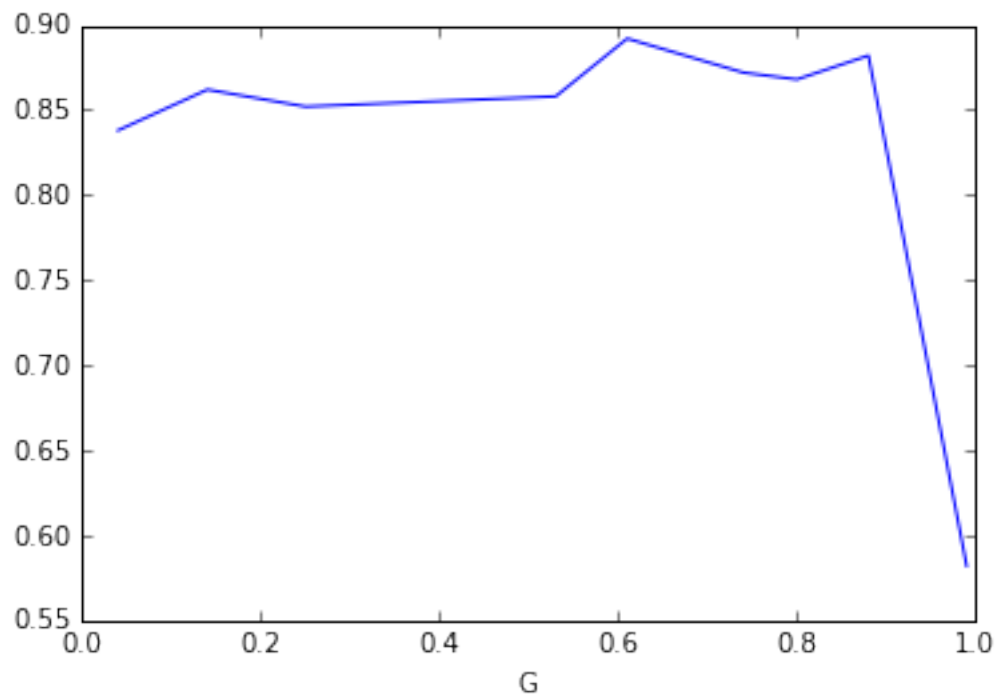
from matplotlib import pyplot

f, ax = plt.subplots()
ax.set_xlabel("G")
ax.plot([0.04, 0.14, 0.25, 0.53, 0.61, 0.74, 0.8, 0.88, 0.99], stats_result_IMED_G)

```

```
IMED [0.83800000000000008, 0.8619999999999998, 0.8519999999999998, 0.8579999999999998, 0.8920000000000000,
```

```
Out[462]: [<matplotlib.lines.Line2D at 0x7fcee9c8ad50>]
```



```
In [463]: ##### Binarize!
```

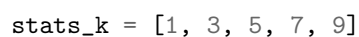
```

stats_k = [1, 3, 5, 7, 9]
borders = [0, 10, 15, 20, 50, 80, 100, 120]
stats_result_bin_IMED = []

for k in stats_k:

```

```
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 5.01  $\mu$ s
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 26  $\mu$ s
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 5.96  $\mu$ s
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 5.96  $\mu$ s
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 5.96  $\mu$ s
bin [[0.89200000000000002, 0.88000000000000012, 0.91199999999999992, 0.88000000000000012, 0.88200000000000002]]
```



```

stats_result_IMED = []

for k in stats_k:
    predictor = MatrixBasedKNearestNeighbor(k)
    predictor = predictor.init_G(G_1p01)
    %time stats_result_IMED.append(my_cross_validation(predictor.ST_batch(binarize_batch(X_tr

print "IMED " + str(stats_result_IMED)

from matplotlib import pyplot

f, ax = plt.subplots()
ax.set_xlabel("k")
ax.plot(stats_k, stats_result_IMED)

```

CPU times: user 4min 25s, sys: 223 ms, total: 4min 26s

Wall time: 4min 26s

CPU times: user 4min 17s, sys: 257 ms, total: 4min 17s

Wall time: 4min 17s

CPU times: user 4min 4s, sys: 337 ms, total: 4min 5s

Wall time: 4min 5s

CPU times: user 4min 8s, sys: 163 ms, total: 4min 8s

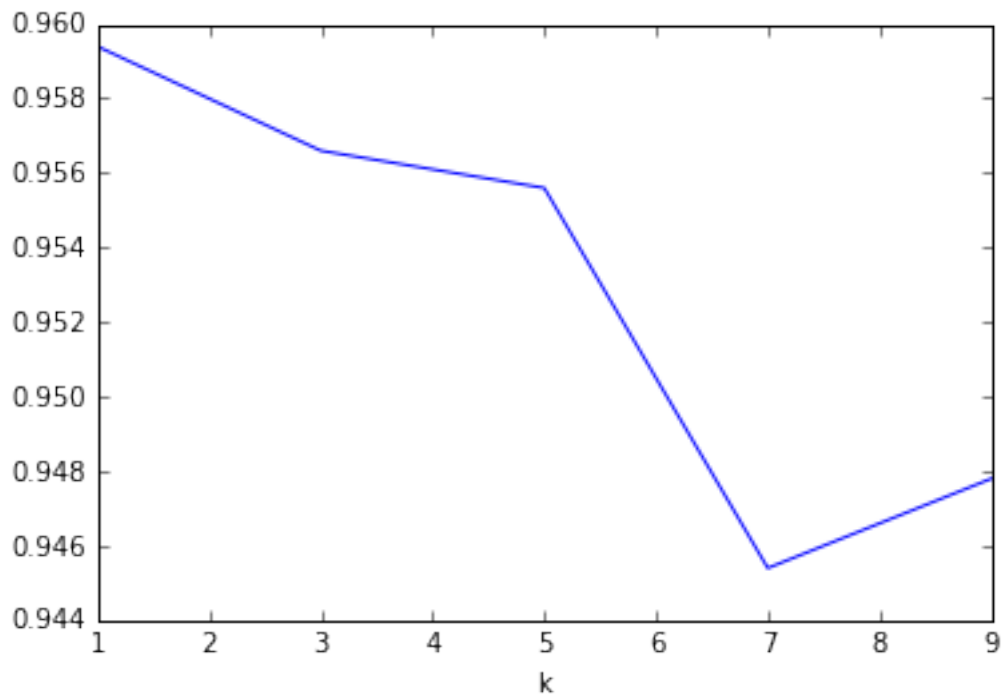
Wall time: 4min 8s

CPU times: user 4min 9s, sys: 233 ms, total: 4min 9s

Wall time: 4min 9s

IMED [0.95939999999999992, 0.956600000000000012, 0.95559999999999989, 0.94539999999999991, 0.94779999999999991, 0.94779999999999991, 0.94779999999999991, 0.94779999999999991, 0.94779999999999991]

Out[465]: [<matplotlib.lines.Line2D at 0x7fcee8f9b3d0>]



1.9.3 Perfect result! About 95.9% based on a quarter of the set!

1.10 KDTree stats plotting

1.10.1 Chebyshev, Manhattan, Minkowski $p=2$ metrics

```
In [466]: stats_k = [1, 3, 5, 7, 9]
          stats_result_Ch = []
          stats_result_Ma = []
          stats_result_Mi = []

          for k in stats_k:
              predictor = KDBasedKNearestNeighbor(k)
              stats_result_Ch.append(my_cross_validation(X_train[:500], y_train[:500], predictor, "chebyshev"))
              stats_result_Ma.append(my_cross_validation(X_train[:500], y_train[:500], predictor, "manhattan"))
              stats_result_Mi.append(my_cross_validation(X_train[:500], y_train[:500], predictor, "minkowski"))

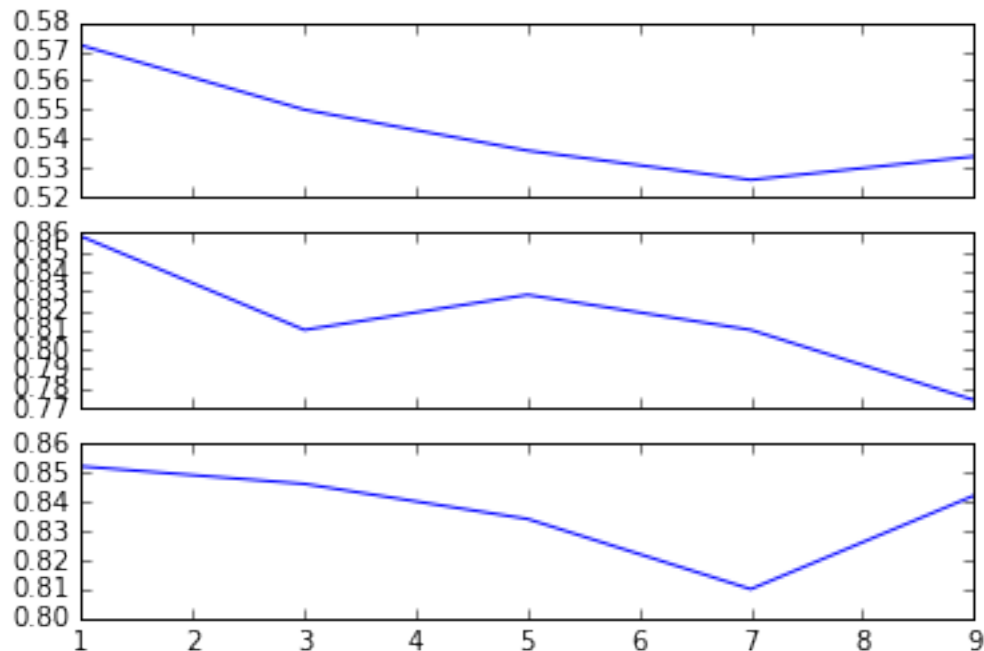
          print "Cheb " + str(stats_result_Ch)
          print "Manh " + str(stats_result_Ma)
          print "Mink " + str(stats_result_Mi)

          from matplotlib import pyplot

          f, axarr = plt.subplots(3, sharex=True)
          axarr[0].plot(stats_k, stats_result_Ch)
          axarr[1].plot(stats_k, stats_result_Ma)
          axarr[2].plot(stats_k, stats_result_Mi)

Cheb [0.57200000000000006, 0.55000000000000004, 0.53600000000000003, 0.52600000000000002, 0.5340000000000000]
Manh [0.85799999999999998, 0.80999999999999994, 0.82800000000000007, 0.80999999999999994, 0.7740000000000000]
Mink [0.85199999999999998, 0.84600000000000009, 0.83399999999999996, 0.80999999999999994, 0.8419999999999999]

Out[466]: [<matplotlib.lines.Line2D at 0x7fcee8d2ff10>]
```



```

In [467]: stats_k = [1, 3, 5, 7, 9]
          stats_result_Ch = []
          stats_result_Ma = []
          stats_result_Mi = []

          for k in stats_k:
              predictor = KDBasedKNearestNeighbor(k)
              stats_result_Ch.append(my_cross_validation(X_train[:1000], y_train[:1000], predictor, "cheb"))
              stats_result_Ma.append(my_cross_validation(X_train[:1000], y_train[:1000], predictor, "manh"))
              stats_result_Mi.append(my_cross_validation(X_train[:1000], y_train[:1000], predictor, "mink"))

          print "Cheb " + str(stats_result_Ch)
          print "Manh " + str(stats_result_Ma)
          print "Mink " + str(stats_result_Mi)

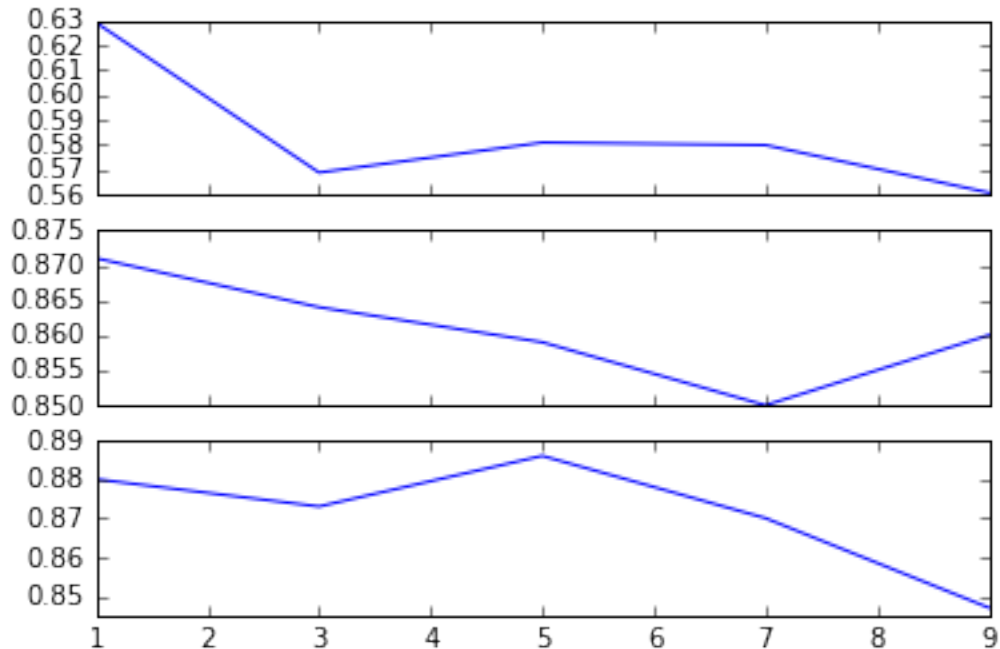
          from matplotlib import pyplot

          f, axarr = plt.subplots(3, sharex=True)
          axarr[0].plot(stats_k, stats_result_Ch)
          axarr[1].plot(stats_k, stats_result_Ma)
          axarr[2].plot(stats_k, stats_result_Mi)

Cheb [0.6289999999999999, 0.5690000000000001, 0.5809999999999999, 0.5800000000000001, 0.5610000000000001]
Manh [0.8710000000000001, 0.8640000000000001, 0.8589999999999999, 0.8499999999999998, 0.8599999999999999]
Mink [0.8800000000000001, 0.873, 0.8859999999999999, 0.8700000000000001, 0.8469999999999998]

Out[467]: [<matplotlib.lines.Line2D at 0x7fcee91704d0>]

```



```

In [471]: stats_k = [1, 3, 5, 7, 9]
          stats_result_Ch = []
          stats_result_Ma = []
          stats_result_Mi = []

          for k in stats_k:
              predictor = KDBasedKNearestNeighbor(k)
              stats_result_Ch.append(my_cross_validation(X_train[:5000], y_train[:5000], predictor, "ch")
              stats_result_Ma.append(my_cross_validation(X_train[:5000], y_train[:5000], predictor, "ma")
              stats_result_Mi.append(my_cross_validation(X_train[:5000], y_train[:5000], predictor, "mi")

          print "Cheb " + str(stats_result_Ch)
          print "Manh " + str(stats_result_Ma)
          print "Mink " + str(stats_result_Mi)

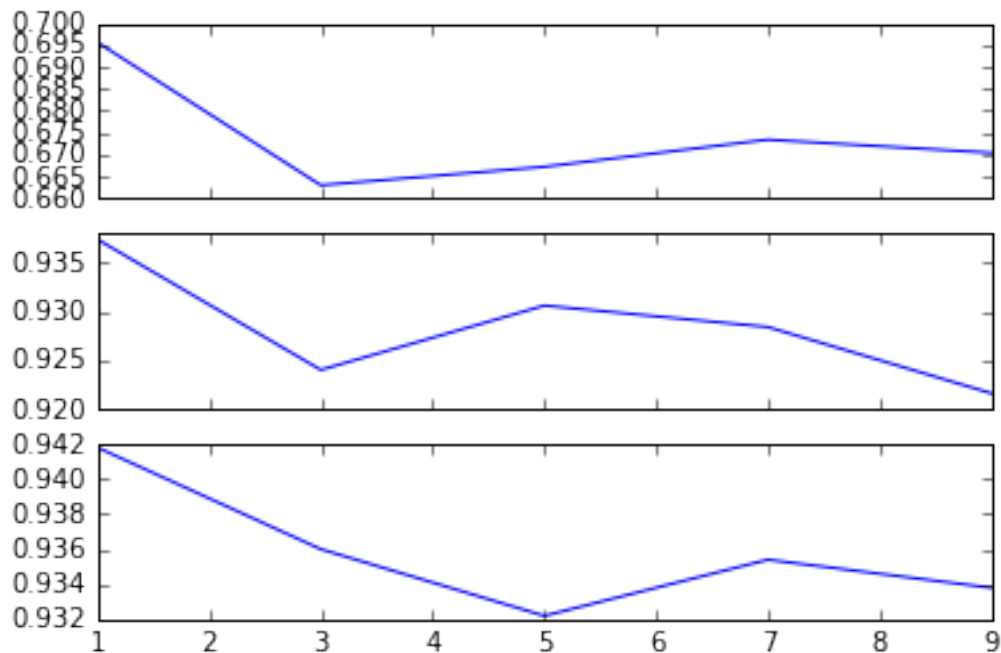
          from matplotlib import pyplot

          f, axarr = plt.subplots(3, sharex=True)
          axarr[0].plot(stats_k, stats_result_Ch)
          axarr[1].plot(stats_k, stats_result_Ma)
          axarr[2].plot(stats_k, stats_result_Mi)

Cheb [0.69560000000000011, 0.66300000000000003, 0.66720000000000002, 0.6734, 0.6704]
Manh [0.93740000000000001, 0.92400000000000015, 0.93060000000000009, 0.92840000000000011, 0.92160000000000000]
Mink [0.94179999999999997, 0.93600000000000017, 0.93219999999999992, 0.93539999999999999, 0.93379999999999999]

Out[471]: [<matplotlib.lines.Line2D at 0x7fcee90fad10>]

```



```

In [ ]: stats_k = [1, 3, 5, 7, 9]
        stats_result_Ch = []

```

```

stats_result_Ma = []
stats_result_Mi = []

for k in stats_k:
    predictor = KDBasedKNearestNeighbor(k)
    stats_result_Ch.append(my_cross_validation(X_train, y_train, predictor, "chebyshev", q_fold
    stats_result_Ma.append(my_cross_validation(X_train, y_train, predictor, "manhattan", q_fold
    stats_result_Mi.append(my_cross_validation(X_train, y_train, predictor, "minkowski", q_fold

print "Cheb " + str(stats_result_Ch)
print "Manh " + str(stats_result_Ma)
print "Mink " + str(stats_result_Mi)

from matplotlib import pyplot

f, axarr = plt.subplots(3, sharex=True)
axarr[0].plot(stats_k, stats_result_Ch)
axarr[1].plot(stats_k, stats_result_Ma)
axarr[2].plot(stats_k, stats_result_Mi)

In [469]: # let's binarize! -- 15 topping

stats_k = [1, 3, 5, 7, 9]
borders = [0, 10, 15, 20, 50, 80, 100, 120]
stats_result_bin = []

for k in stats_k:
    this_result = []
    predictor = KDBasedKNearestNeighbor(k)

    for b in borders:
        this_result.append(my_cross_validation(binarize_batch(X_train[:500].copy(), b), y_train))
    %time stats_result_bin.append(this_result)

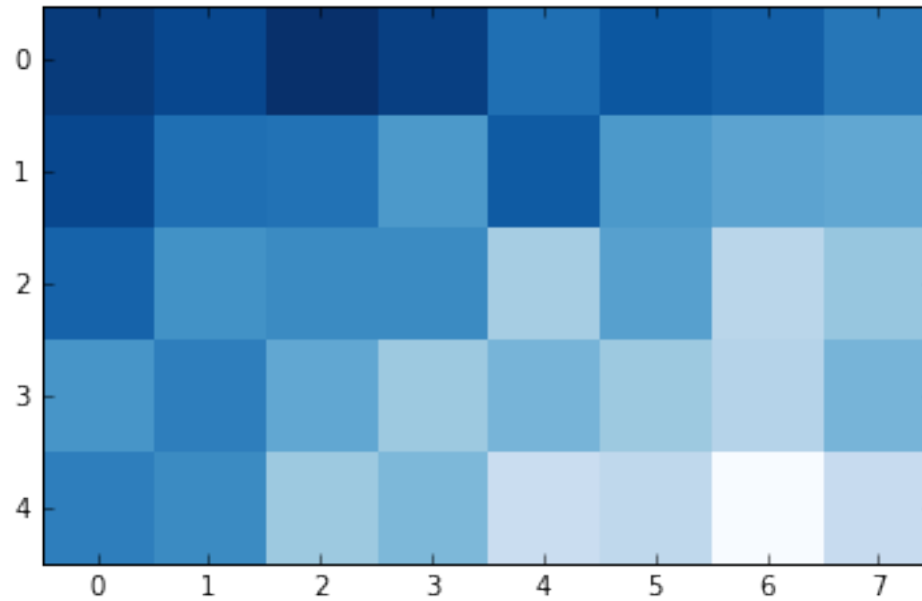
print "bin " + str(stats_result_bin)

from matplotlib import pyplot

plt.imshow(stats_result_bin,
            interpolation="nearest", cmap = "Blues")
plt.show()

CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 6.91 µs
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 9.06 µs
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 6.91 µs
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 5.96 µs
CPU times: user 0 ns, sys: 0 ns, total: 0 ns
Wall time: 5.96 µs
bin [[0.8899999999999999, 0.88400000000000001, 0.89600000000000013, 0.8879999999999999, 0.8640000000000000

```



```
In [470]: import pprint
```

```
pp = pprint.PrettyPrinter(indent=4)
```

```
pp.pprint(stats_result_bin)
```

```
from matplotlib import pyplot
```

```
plt.imshow(stats_result_bin,
            interpolation="nearest", cmap = "Blues")
plt.show()
```

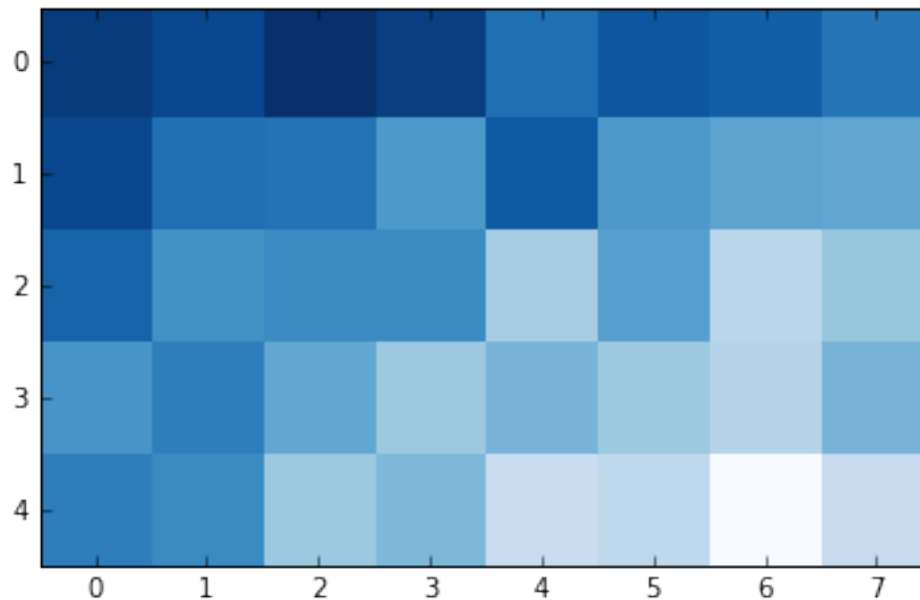
```
[ [ 0.8899999999999999,
    0.884000000000000001,
    0.896000000000000013,
    0.8879999999999999,
    0.864000000000000001,
    0.876,
    0.872000000000000011,
    0.8599999999999999],
  [ 0.884000000000000001,
    0.864000000000000001,
    0.86199999999999988,
    0.8419999999999997,
    0.874,
    0.8419999999999997,
    0.8359999999999997,
    0.8339999999999996],
  [ 0.86999999999999988,
    0.846000000000000009,
    0.8499999999999998,
```



```

0.8499999999999998,
0.8099999999999994,
0.83800000000000008,
0.80200000000000016,
0.81600000000000006],
[ 0.8439999999999997,
0.85600000000000009,
0.8339999999999996,
0.81400000000000006,
0.8259999999999996,
0.81400000000000006,
0.8039999999999994,
0.8259999999999996],
[ 0.8559999999999997,
0.8499999999999998,
0.81400000000000006,
0.82400000000000007,
0.7939999999999993,
0.80000000000000004,
0.76400000000000001,
0.79600000000000004]]

```



1.11 As long as IMED does really good, here are the final tests of IMED on the whole dataset

```

In [493]: predictor = MatrixBasedKNearestNeighbor(k=1)
           predictor = predictor.init_G(G_1p01)
           %time final_result = my_cross_validation(predictor.ST_batch(binimize_batch(X_train.copy(), 15)

```

CPU times: user 57min 16s, sys: 4.92 s, total: 57min 21s
Wall time: 57min 21s

```
In [264]: print(final_result)
```

```
0.967166666667
```

2 WOW that is WORTH it.

2.1 Getting the final results

```
In [477]: df = pandas.read_csv("kaggle_data/train.csv")
          df_test = pandas.read_csv("kaggle_data/test.csv")
          df_random = pandas.read_csv("kaggle_data/test_random_label.csv")
```

```
In [478]: df_test.head()
```

```
Out[478]:
```

	pixel0	pixel1	pixel2	pixel3	pixel4	pixel5	pixel6	pixel7	pixel8	\
0	0	0	0	0	0	0	0	0	0	
1	0	0	0	0	0	0	0	0	0	
2	0	0	0	0	0	0	0	0	0	
3	0	0	0	0	0	0	0	0	0	
4	0	0	0	0	0	0	0	0	0	

	pixel9	...	pixel774	pixel775	pixel776	pixel777	pixel778	\
0	0	...	0	0	0	0	0	
1	0	...	0	0	0	0	0	
2	0	...	0	0	0	0	0	
3	0	...	0	0	0	0	0	
4	0	...	0	0	0	0	0	

	pixel779	pixel780	pixel781	pixel782	pixel783
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	0	0	0	0
4	0	0	0	0	0

[5 rows x 784 columns]

```
In [479]: df.head()
```

```
Out[479]:
```

	label	pixel0	pixel1	pixel2	pixel3	pixel4	pixel5	pixel6	pixel7	\
0	5	0	0	0	0	0	0	0	0	
1	0	0	0	0	0	0	0	0	0	
2	4	0	0	0	0	0	0	0	0	
3	1	0	0	0	0	0	0	0	0	
4	9	0	0	0	0	0	0	0	0	

	pixel8	...	pixel774	pixel775	pixel776	pixel777	pixel778	\
0	0	...	0	0	0	0	0	
1	0	...	0	0	0	0	0	
2	0	...	0	0	0	0	0	
3	0	...	0	0	0	0	0	
4	0	...	0	0	0	0	0	

	pixel779	pixel780	pixel781	pixel782	pixel783
0	0	0	0	0	0

```

1 0      0      0      0      0
2 0      0      0      0      0
3 0      0      0      0      0
4 0      0      0      0      0

```

```
[5 rows x 785 columns]
```

```
In [515]: df_random["label"].head()
```

```

Out[515]: 0      4
          1      1
          2      5
          3      6
          4      6
          Name: label, dtype: int64

```

```

In [544]: X_train, y_train = df[df.columns[1:]].values, df["label"].values
          X_test = df_test[df_test.columns].values
          y_random = df_random[df_random.columns].values

```

```

In [486]: predictor = MatrixBasedKNearestNeighbor(k=1)
          predictor = predictor.init_G(G_1p01)
          %time predictor = predictor.fit(predictor.ST_batch(binarize_batch(X_train.copy(), 15)), y_train)

```

```

CPU times: user 2min 57s, sys: 610 ms, total: 2min 57s
Wall time: 2min 57s

```

```

In [494]: predictor = predictor.calc_dist(predictor.ST_batch(binarize_batch(X_test.copy(), 15)), "IMED")
          %time y_final = predictor.predict_labels(X_test)

```

```

CPU times: user 3.33 s, sys: 0 ns, total: 3.33 s
Wall time: 3.41 s

```

```
In [497]: print(y_final[0:20]) #looks good
```

```

[ 7.  2.  1.  0.  4.  1.  4.  9.  5.  9.  0.  6.  9.  0.  1.  5.  9.  7.
  3.  4.]

```

```
In [496]: plot_grid(X_test[0:20], 1, 20)
```



2.1.1 Let's do some checking

Statistically

```
In [530]: # random_label, strange..
```

```

y_test = y_random[:, 1]

numpy.unique(y_test, return_counts = True)

```

```

Out[530]: (array([0, 1, 2, 3, 4, 5, 6, 7, 8]),
          array([297, 270, 277, 292, 276, 277, 283, 259, 269]))

```

```
In [499]: # predicted

from collections import Counter
print(Counter(y_final).keys())
print(Counter(y_final).values())

[0.0, 1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0]
[222, 300, 265, 266, 259, 221, 229, 250, 227, 261]
```

Manually

```
In [535]: #quite good

start = 2000

print(y_final[start:start + 20])

plot_grid(X_test[start:start + 20], 1, 20)

[ 6.  5.  6.  5.  8.  4.  6.  4.  3.  9.  1.  3.  4.  1.  9.  1.  7.  1.
 1.  9.]
```



2.1.2 Looks good, time to submit. :)

2.1.3 Result output

```
In [541]: for val in y_final:
           open("prediction.txt", "a").write(str(int(y_final[val])) + '\n')
```

/usr/lib/python2.7/site-packages/ipykernel/_main_.py:2: DeprecationWarning: using a non-integer number
from ipykernel import kernelapp as app

2.2 Extra: Official kaggle results – not yet submitted

```
In [15]: kaggle_df = pandas.read_csv("kaggle_data/4real/train.csv")
         kaggle_df_test = pandas.read_csv("kaggle_data/4real/test.csv")

In [16]: X_traink, y_traink = kaggle_df[kaggle_df.columns[1:]].values, kaggle_df["label"].values
         X_testk = kaggle_df_test[kaggle_df_test.columns].values

In [30]: predictork = MatrixBasedKNearestNeighbor(k=1)
         predictork = predictork.init_G(G_1p01)
         %time predictork = predictork.fit(predictork.ST_batch(binarize_batch(X_traink.copy(), 15)), y_

CPU times: user 5min 29s, sys: 540 ms, total: 5min 30s
Wall time: 5min 29s

In [31]: print(X_testk.shape)

(28000, 784)
```

```
In [32]: predictork = predictork.calc_dist(predictork.ST_batch(binarize_batch(X_testk[:7000]).copy(), 15),
      %time y_finalk1 = predictork.predict_labels(X_testk[:7000])
```

KeyboardInterrupt

Traceback (most recent call last)

```
<ipython-input-32-c316438ab545> in <module>()
----> 1 predictork = predictork.calc_dist(predictork.ST_batch(binarize_batch(X_testk[:7000]).copy(), 15),
      2 get_ipython().magic(u'time y_finalk1 = predictork.predict_labels(X_testk[:7000])'))

/home/aq/workspace/diht/ML/symbols/knn.pyc in calc_dist(self, X_test, metric, k)
226         # Fill matrix self.dist_mt by using 0 loops
227         #####
--> 228         self.dist_mt = numpy.apply_along_axis(set_row, 1, X_test)
229
230         # print(self.dist_mt)

/usr/lib/python2.7/site-packages/numpy/lib/shape_base.pyc in apply_along_axis(func1d, axis, arr, n, indlist, ind)
126         n -= 1
127         i.put(indlist, ind)
--> 128         res = func1d(arr[tuple(i.tolist())], *args, **kwargs)
129         outarr[tuple(i.tolist())] = res
130         k += 1

/home/aq/workspace/diht/ML/symbols/knn.pyc in set_row(X_test_i)
205
206     def set_row(X_test_i):
--> 207         return numpy.apply_along_axis(self.dist, 1, self.X_train, X_test_i, metric=metric)
208
209         if self.num_loops == 2:

/usr/lib/python2.7/site-packages/numpy/lib/shape_base.pyc in apply_along_axis(func1d, axis, arr, n, indlist, ind)
105         n -= 1
106         i.put(indlist, ind)
--> 107         res = func1d(arr[tuple(i.tolist())], *args, **kwargs)
108         outarr[tuple(ind)] = res
109         k += 1

/home/aq/workspace/diht/ML/symbols/knn.pyc in dist(self, img1, img2, metric)
176         return self.dist_pixel_L3(img1, img2)
177         elif metric == "IMED":
--> 178         return self.dist_IMED(img1, img2)
179     else:
180         print("Unknown metric")

/home/aq/workspace/diht/ML/symbols/knn.pyc in dist_IMED(self, img_x, img_y, G)
```

```

156         http://www.cis.pku.edu.cn/faculty/vision/wangliwei/pdf/IMED.pdf
157         """
--> 158         dist = (numpy.transpose(img_x - img_y)).dot(img_x - img_y)
159         # for row_i in range(self.size):
160         #     for col_i in range(self.size):

```

KeyboardInterrupt:

```
In [3]: print(y_finalk[0:20])
```

```

9
2
3
2
0
3
2
0
2
0

```

```
In [24]: plot_grid(X_testk[0:20], 1, 20)
```



```
In [6]: for index in range(len(y_finalk)):
        open("predictionkaggle.csv", "a").write(str(index) + ", " + str(y_finalk[index]) + '\n')
```

```
In [9]: f = open("predictionkaggle.txt", "r")
        numpy.loadtxt(f)
```

```
Out[9]: array([ 9.,  2.,  3., ...,  0.,  3.,  9.])
```

```
In [ ]:
```