

# Homework 3, Section 1.3: 1-11 odd, 17-25 odd

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## Homework

1.

$$u = \begin{bmatrix} -1 & 2 \end{bmatrix} \quad v = \begin{bmatrix} -3 & -1 \end{bmatrix}$$

3.

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5.

$$3x_1 + 5x_2 = 2 \quad -2x_1 + 0x_2 = -3 \quad 8x_1 + -9x_2 = 8$$

7.

$$a = u - 2v \quad b = 2u - 2v \quad c = 2u - 2.5v \quad d = 3u - 4v$$

9.

$$x_1 \begin{bmatrix} 0 & 4 & -1 \end{bmatrix} + x_2 \begin{bmatrix} 1 & 6 & 3 \end{bmatrix} + x_3 \begin{bmatrix} 5 & -1 & -8 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}$$

11.

The linear system corresponding to M has a solution so 1 has a solution and b is therefore a linear combination of  $a_1, a_2$  and  $a_3$ .

17.

The weights are 1 and -1

19.

If  $v_1$  and  $v_2$  are nonzero vectors then  $\text{Span}\{v_1, v_2\}$  for the given vectors is the set of points on a line through  $v_1$  and 0.

21.

The matrix corresponds to a consistent system for all  $h$  and  $k$ , so  $y$  is in Span of  $\{u, v\}$

**23.**

$$\text{Span } \{u, v\} = \text{span } \{u\}$$

**25. A)**

There are only three vectors in the set of columns  $\{a_1, a_2, a_3\}$  in  $A$  and  $b$  is not one of them.

**25. B)**

There are infinitely many vectors in  $W = \text{Span}\{a_1, a_2, a_3\}$

**25. C)**

$a_1$  is in  $W$ .