

Homework 18, Section 4.3: 3, 7, 8, 15

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Homework

3. A)

It is invertible because the function is one-to-one and onto.

3. B)

One to one, but not onto

3. C)

One to one but not onto

3. D)

It is invertible because the function is one-to-one and onto.

7.

$$f(x_1) = f(x_2)$$

f is one-to-one

$$2x_1 = 2x_2$$

Therefore

$$x_1 = x_2$$

8.

Proof: since f is onto then there must be an $x \in \mathbb{R}$ with $f(x) = y$. If we take $z = \frac{x}{2} \in \mathbb{R}$ it follows that $h(z) = f(2z) = f(x)$

This shows that $h(z) = y$

15. A)

Proof

let x_1 and $x_2 \in \mathbb{R}$ be given.

Let it also be given that $y(x_1) = y(x_2)$. This means that given the function, $5x_1 = 7 = 5x_2 = 7$

This in turn means $x_1 = x_2$ meaning y is one to one.

15. B)

15. C)