Homework 21, Section 4.3: 3, 4, 7, 10, 15, 25

Alex Gordon

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Homework

3.

This set does not form a basis for R^3 . The set is linearly dependent and does not span R^3

4.

The determinant equals 1, so these vectors are linearly independent. These vectors form a basis for R^3 .

7.

This set does not form a basis for R^3 because it is linearly independent and $m \ge n$.

10.

The RREF is
$$\begin{bmatrix} 1 & 0 & 0 & 2 & 3 & 0 \\ 0 & 1 & 0 & -1 & -2 & 0 \\ 0 & 0 & 1 & 0 & -2 & 0 \end{bmatrix}$$
. The span is then $\begin{bmatrix} -2 \\ 1 \\ 0 \\ 1 \\ 0 \end{bmatrix}$, $\begin{bmatrix} -3 \\ 2 \\ 2 \\ 0 \\ 1 \end{bmatrix}$

15. The RREF is
$$\begin{bmatrix} 1 & 0 & 2 & 2 & 3 \\ 0 & 1 & -2 & -1 & -1 \\ -2 & 2 & -8 & 10 & -6 \\ 3 & 3 & 0 & 3 & 9 \end{bmatrix}$$
. This reduces to
$$\begin{bmatrix} 1 & 0 & 2 & 2 & 3 \\ 0 & 1 & -2 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 2 & 2 & 3 \\ 0 & 1 & -2 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

25.

Yes it is a basis a typical element in H is sv1 + (t - s)v2 + sv3. we can re-write this as s(v1+v3)+(t-s)(v2), $so\{v1+v3,v2\}$ is a basis for H. the problem is that the span of $\{v1,v2,v3\}$ is much bigger than H, it is all of R^3 . This means that just because it is linearly independent, it is not the basis for H. Since the basis of the subspace is not isomorphic to R or R^2 , it's too big for the span.