

# Homework 4, Section 1.5: 3, 4(b,f), 5(d), 11, 14, 15, 22, 25

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## Homework

3.

q	p $\wedge$ q are lying	$\neg$ p (A is lying)
T	T	F
F	F	F
T	F	T
F	F	T

4. B)

p	q	p $\vee$ q	$\neg$ p $\vee$ q	$\neg$ p $\rightarrow$ (p $\vee$ q)
T	T	F	T	F
T	F	F	T	F
F	T	T	T	T
F	F	T	F	T

4. F)

p	q	r	p $\vee$ q	$\neg$ p $\vee$ q	$\neg$ p $\rightarrow$ (p $\vee$ q)
T	T	F	T	F	F
T	F	F	T	F	F
F	T	T	T	T	T
F	F	T	F	T	T

**5. D)**

p	q	r	$p \rightarrow (q \rightarrow r)$	$p \wedge q \rightarrow r$
T	T	T	T	T
T	T	F	F	F
T	F	T	T	T
T	F	F	T	T
F	T	T	T	T
F	T	F	F	F
F	F	T	T	T
F	F	F	T	T

These statements are equivalent

**11. A)**

True

**11. B)**

False. If  $x = 11$ , then  $x$  is not  $< 10$

**11. C)**

True

**11. D)**

True

**11. E)**

True, because it is not False.

**14. A)**

D= All integers that end in 5

$$B(n) = 5 \pmod{n} = 0$$

$$\forall_n \in D, B(n)$$

**14. B)**

D= All integers that end in 3

$$B(m) = 3 \pmod{n} = 0$$

$$\forall_m \in D, B(m)$$

**14. C)**

D= Multiples of 5  $B(n) = n^2 - 1 = \text{multiple of 3}$

$$\forall_n \in D, B(n)$$

**14. D)**

D= Positive real numbers greater than  $\sqrt{2}$

$$B(x) = 2/x > \sqrt{2}$$

$$\forall x \in D, B(x)$$

**15.**

A and D are true.

**22. A)**

If n is a positive integer and n is even then for all n  $\frac{1}{n} < 1$

**22. B)**

If a and b are positive integers and  $a - b$  is odd then for all a and b  $a^2 \neq 2b^2$

**22. C)**

If a and b are positive integers and a and b are even then for all a and b  $a/b \neq 1 + b/a$

**22. D)**

If there is a right triangle with perimeter equal to three times the length of one leg, then for all triangles that have a perimeter not equal to three times the length of one leg, they are not right triangles.

**25. A)**

If you do attend the concert you won't get and F for the course.

**25. B)**

We won't go if you go.

**25. C)**

If you do eat your breakfast, you won't go hungry.

**25. D)**

If a quadrilateral is not a square, then it does not have four equal sides and four equal angles.

**25. E)**

If a triangle does not either have two equal sides or two equal angles, then it is not an isosceles triangle.