Cellular Potts Model

f(x)

```
(∗ cross and moore neighbour indices within bounds of the canvas ∗)
In[62]:=
       crossneighbours[{p_, q_}] := DeleteCases[{
            {p, q-1},
            {p, q+1},
            {p-1, q},
            \{p+1, q\}\}, \{OrderlessPatternSequence[x_ /; x \le 0 | | x > n, _]\}, \{1\}];
       mooreneighbours[{p_, q_}] := DeleteCases[{
            {p, q-1},
            {p, q+1},
            {p-1, q-1},
            {p-1, q},
            {p-1, q+1},
            {p+1, q-1},
            {p+1, q},
            \{p+1, q+1\}\}, \{OrderlessPatternSequence[x_/; x \le 0 | | x > n, _]\}, \{1\}];
       (* boundary points of all cells together *)
In[64]:=
       boundarymerger[assoc_] := DeleteDuplicates[Cases[Normal@assoc, {__Integer} .., {-2}]]
```

```
(* total energy of the system *)
In[71]:=
       Clear@globalTotalEnergy;
       globalTotalEnergy[assoc_] :=
        Total[Map[springEnergy, assoc]] + globalAdhesionEnergy[assoc]
       Clear@fun; Clear@xx;
In[73]:=
       fun = Function[x,
          Which[Length[xx = Union@Extract[A, mooreneighbours@x]] > 1, x,
            Length[xx] = 1&& (Complement[xx, A[[x]]]) \neq {}, x,
            True, Nothing
         ];
```

params

```
n = 100; (* canvas size *)
In[75]:=
             (* adhesion strength *)
In[76]:=
            j_{00} = 0; j_{11} = 6; j_{22} = 6;
            j_{01} = j_{10} = 6;
            j_{02} = j_{20} = 6;
             j_{12} = j_{21} = 16;
            J = \begin{pmatrix} j_{00} & j_{01} & j_{02} \\ j_{10} & j_{11} & j_{12} \end{pmatrix};
             a0 = 100; p0 = 1; (* rest parameters *)
In[81]:=
             Kparam = \langle |1 \rightarrow \langle |ka \rightarrow 1|, kp \rightarrow 2| \rangle, 2 \rightarrow \langle |ka \rightarrow 1|, kp \rightarrow 2| \rangle | \rangle; (*stifness params*)
             T = 20; (*temperatures*)
             iter = 1000; (* number of iterations *)
In[191]:=
             A = ConstantArray[0, {n, n}]; (* empty canvas *)
In[85]:=
```

CPM lattice

```
ln[86]:= shift = {30, 30};
     pos = shift + # & /@ Position[DiskMatrix[20], 1];
     Scan (A[[Sequence@@#]] = 1) &, pos
In[89]:= ( *
     Table [shift={35+i,40+j};
       pos=shift+#&/@Position[DiskMatrix[2],1];
       Scan[(A[[Sequence@@#]]=2)&,pos],{i,Range[1,28,8]},{j,Range[1,20,8]}];
     *)
```

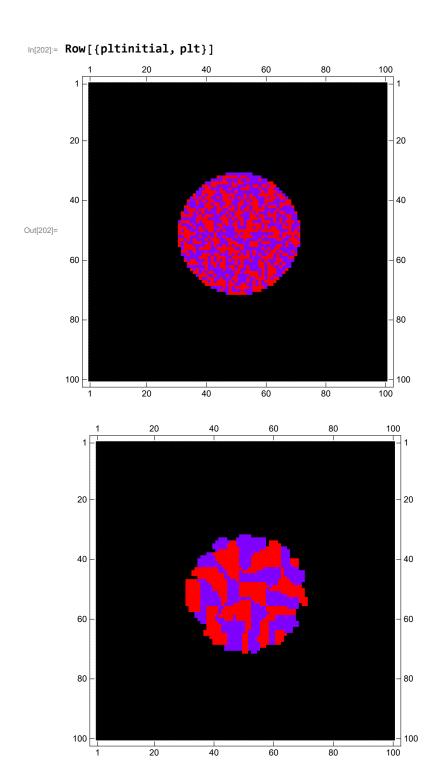
initial properties

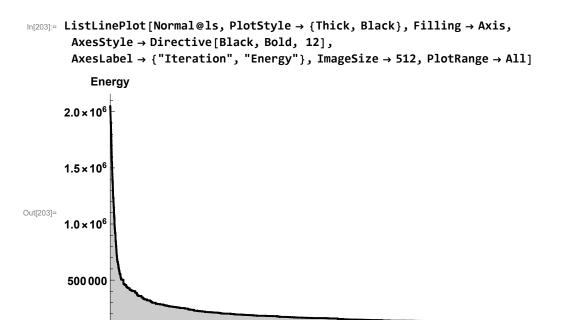
```
components, newtotalE, T = T, componentsprev = components, assocprev = assoc,
 assocTprev = assocT, assoc = assoc, assocT = assocT, p, newlatticesite, neighbours,
 cellnum, pixToCellAssoc = pixToCellAssoc, pixToTypeAssoc = pixToTypeAssoc},
t = 0;
Monitor|
While [t < iter,
  (* pick a random boundary pt and get its 4-neighbours for mutation *)
  p = assocT[RandomChoice@*Range@*Length@assocT][[2, 1]];
  If | p ≠ {},
   randpt = RandomChoice[p]; (*random boundary pt*)
   prevtype = A[[Sequence@@randpt]];
   cellnum = pixToCellAssoc[randpt];
   neighbours = crossneighbours[randpt];
   opts = Position[Lookup[pixToCellAssoc, neighbours] /. _Missing → 0,
     Except[cellnum], {1}, Heads → False];
   (*Pick[neighbours,KroneckerDelta@@@Thread[{pixToCellAssoc[randpt],
         Lookup[pixToCellAssoc,neighbours]/. _Missing→0}],0];*)
   If[opts # {},
    newlatticesite = RandomChoice@Extract[neighbours, opts];
    newcelltype = Extract[A, newlatticesite];
    A[[Sequence@@randpt]] = newcelltype;
    (* compute local energy change *)
    components = MapAt[
      Values@ComponentMeasurements[MorphologicalComponents[#,
           CornerNeighbors → False], {"Mask", "Area", "PerimeterLength"}] &,
      ComponentMeasurements[A, "Mask"], {All, 2}];
    assoc = <|MapIndexed[</pre>
        First[#2] \rightarrow {#[[1]], #1[[2]]} &, Flatten@Map[Thread, components]]|>;
    assocT = MapAt [Map[fun]@* (Position[ImageData@MorphologicalPerimeter@Image[#],
           1] &), assoc, {All, 2, 1}];
    newtotalE = globalTotalEnergy[assocT];
    pixToCellAssoc = AssociationMap[Thread[#[[2, 2, 1]] → First[#]] &, assocT];
     (*pixToTypeAssoc=AssociationMap[Thread[#[[2,2,1]]→ #[[2,1]]]&,assocT];*)
     (* acceptance, rejection step *)
    If | newtotalE < prevEnergy,</pre>
      (*accept it*)
     ls["Append", newtotalE];
     prevEnergy = newtotalE,
     If[RandomReal[1] < Exp[- (newtotalE - prevEnergy) / T],</pre>
       (*accept it by probability*)
      ls["Append", newtotalE];
      prevEnergy = newtotalE,
       (*return to the previous state*)
      A[[Sequence@@randpt]] = prevtype;
      components = componentsprev;
      assoc = assocprev;
      assocT = assocTprev;
      pixToCellAssoc = AssociationMap[Thread[#[[2, 2, 1]] → First[#]] &, assocT];
       (*pixToTypeAssoc=AssociationMap[Thread[#[[2,2,1]]→ #[[2,1]]]&,assocT];*)
      ls["Append", prevEnergy];
```

```
componentsprev = components;
      assocprev = assoc;
      assocTprev = assocT;
      plt =
       MatrixPlot[A, ColorFunction \rightarrow Hue, ColorRules \rightarrow \{0 \rightarrow Black\}, ImageSize \rightarrow Medium];
      (*Export["C:\\Users\\aliha\\Desktop\\save\\"<>ToString[t]<>".jpg",plt];*)
      t += 1
   ], {t, plt}]
On[General::munf1];
```

results

```
In[201]:= 1s["Length"]
Out[201]= 14 670
```





Iteration