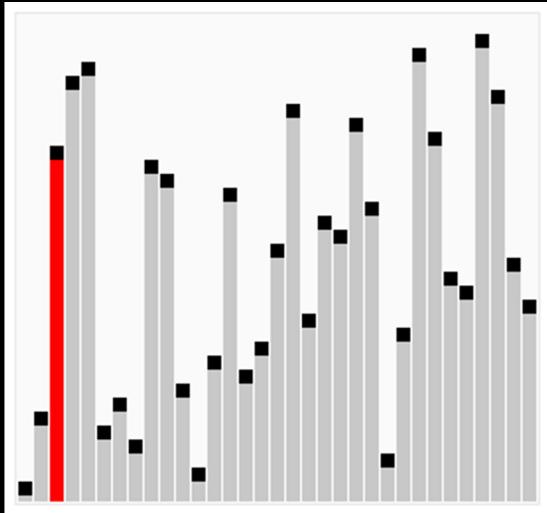


Which sorting algorithm is this?



Bubbles

In a file on your IDE, create a "person" struct with attributes name and age. Then, in int main(void), create an array of 2 persons. Iterate through the array and print each name and age.

```
typedef struct           int main (void)           int arr[5],  
{                           {                           ↳ integer array named arr w/ len 5  
    string name;           person people[2]; → person array named people w/ len 2  
    int age;               people[0].name = "Phyllis";  
}                           people[0].age = 19;  
person;                     people[1].name = "John";  
                            people[1].age = 20;  
                            for (int i=0; i<2; i++)  
                            {  
                                printf("%s/n", people[i].name);  
                            }
```

CS50 Section 3

- Searching and Running Times
- Structs
- Sorting
- Recursion

Runtime

- Best Case? Ω
 - $\Omega(1)$: constant
 - $\Omega(n)$: linear
- Worst Case? O
 - $O(n)$: constant

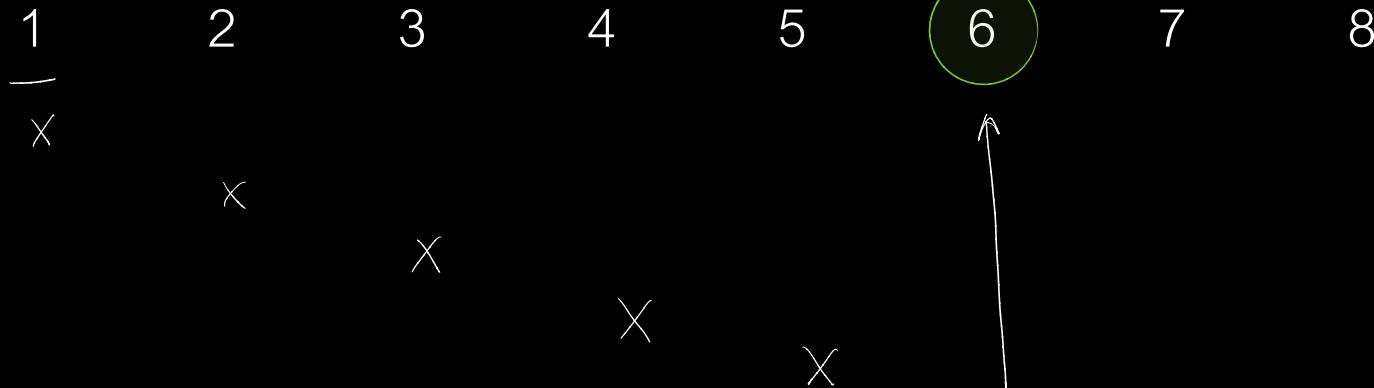
Searching

- Linear Search

go through array from beginning

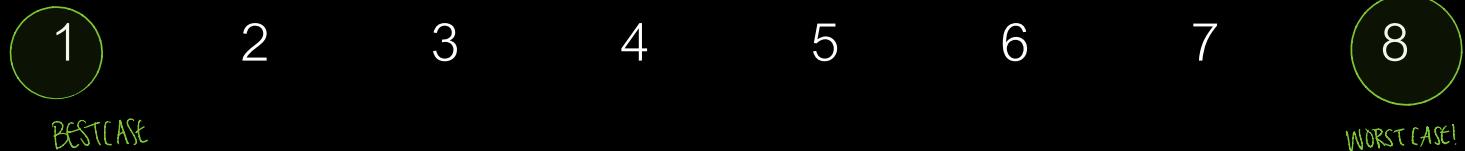
↳ return once you find the element

- some sort of output; fn returns output
- function stops



Searching and Run Times

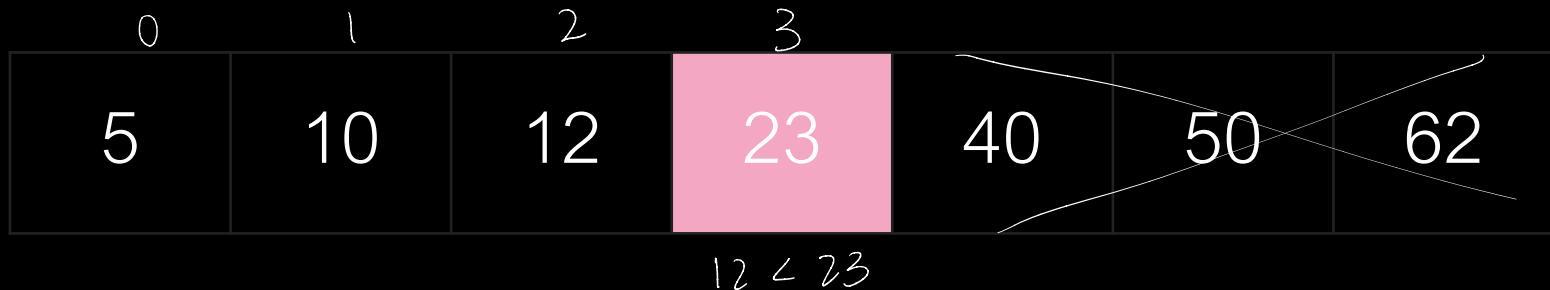
- Linear Search



- Best Case? $\mathcal{O}(1)$
- Worst Case? $\mathcal{O}(n)$

Searching and Run Times

- Binary Search – Let's look for the number 12.



$$\left(\frac{7 \text{ elements}}{2} \right) = 3$$

Searching and Run Times

- Binary Search – Let's look for the number 12.

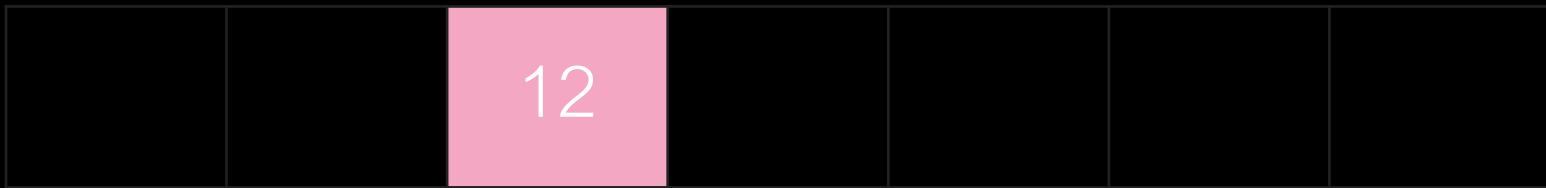


$12 > 10 \Rightarrow$ TO THE RIGHT

$$\frac{3 \text{ elements}}{2} = 1$$

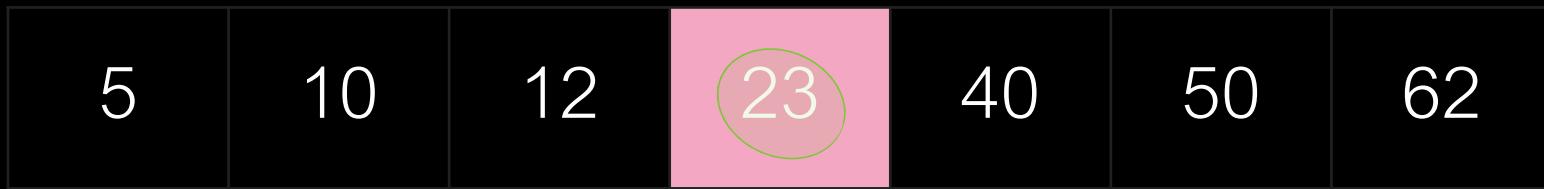
Searching and Run Times

- Binary Search – Let's look for the number 12.



Searching and Run Times

- Binary Search – Let's look for the number 12.



- Best Case? $O(1)$
- Worst Case? $O(\log n)$
 $n=7$
 $\log_2 n \sim 3$

Structs

```
typedef struct          typedef struct
{                      {
    type var1;
    type var2;
    ...
    string name;      }
    var3; //name of structure
    int age;
}

person;
```

Structs

```
typedef struct
```

int i; $\xrightarrow{\text{int} \rightarrow \text{person}}$ person p;

```
{
```

```
p.name = "Phyllis";
```

```
string name;
```

```
p.age = 19;
```

```
int age;
```

```
}
```

Why a struct?

```
person;
```

group together properties
of an item

Exercise 1: Struct Practice

```
typedef struct  
{  
    string name;  
  
    int age;  
}  
  
person;
```

Construct a struct called “birthday” that contains a variable *name* as a *string*, the variable *month* as an *int*, and the variable *day* as an *int*.

Create an array storing birthdays, initialize your contents, and print the contents of your array.

- Searching and Running Times
- Structs
- Sorting
- Recursion

Bubble Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

ITERATION 1

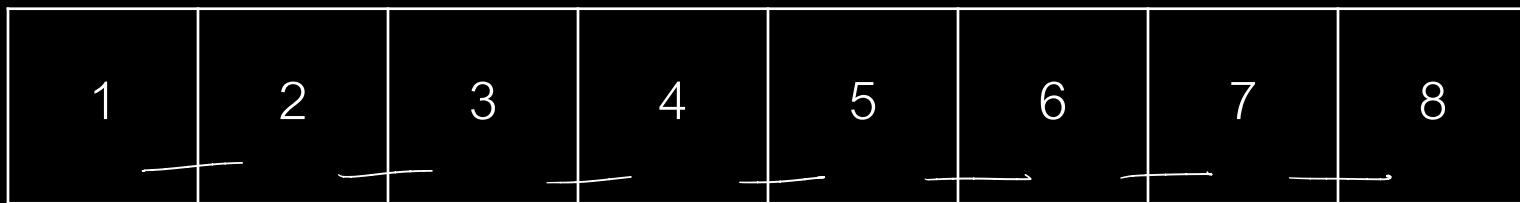
3 6 1 4 7 8 2 5
3 1 6 4 7 8 2 5
3 1 4 6 7 8 2 5
3 1 4 6 7 8 2 5
3 1 4 6 7 8 2 5
3 1 4 6 7 2 8 5
3 1 4 6 7 2 5 8

ITERATION 2

3 1 4 6 7 2 5 8
3 1 3 4 6 7 2 5 8
3 1 3 4 6 7 2 5 8
3 1 3 4 6 7 2 5 8
3 1 3 4 6 7 2 5 8
3 1 3 4 6 2 7 5 8
3 1 3 4 6 2 7 5 8
3 1 3 4 6 2 5 7 8

KEEP ITERATING
UNTIL NO SWAPS

Bubble Sort



already sorted: bubble sort makes 1 pass

1 2 3 4 5 6 7 8
1 2 3 4 5 6 7 8
1 2 3 4 5 6 7 8

} look through
all n elements

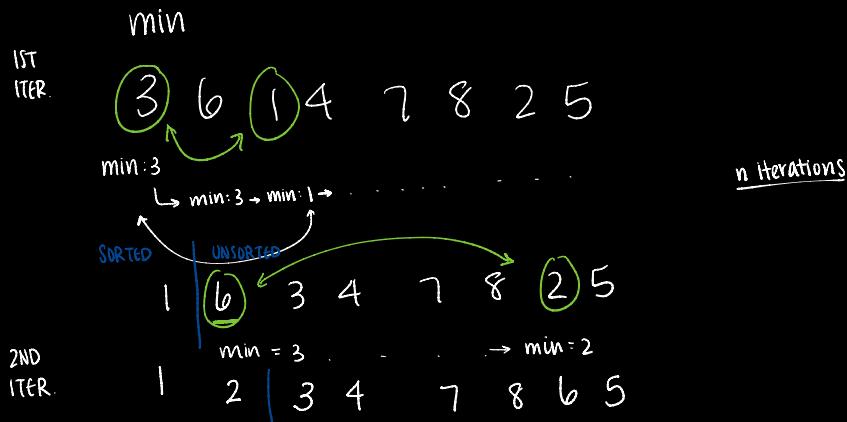
Bubble Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

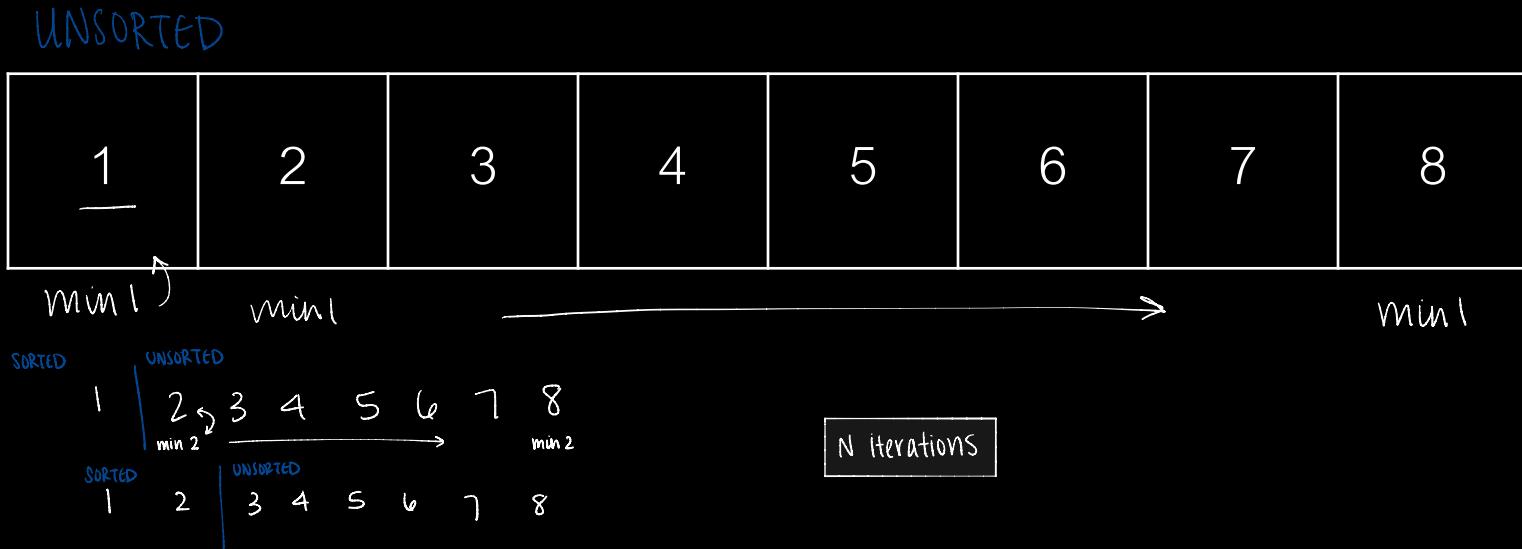
- Best Case? $\mathcal{O}(n)$
- Worst Case? n iterations
each iteration: n $\left. \right\} \mathcal{O}(n^2)$

Selection Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|



Selection Sort



Selection Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

- Best Case? $\mathcal{O}(n^2)$
- Worst Case? $\mathcal{O}(n^2)$

Selection Sort

$\text{arr} = [3, 5, 2, 6, 1, 7]$



Go through
n iterations

```

for (int i=0; i<6; i++)
{
    min = arr[i];
    idx = i;
    for (int j=i; j<6; j++)
    {
        if (min > arr[j])
        {
            min = arr[j];
            idx = j;
        }
    }
    temp = arr[i];
    arr[i] = min;
    arr[idx] = temp;
}
  
```

$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

$\text{int temp} = \text{arr}[0] \Rightarrow \text{temp}=1$
 $\text{arr}[0]=\text{arr}[2] \Rightarrow [3, 2, 1]$
 $\text{arr}[2]=\text{temp} \Rightarrow [3, 2, 1]$

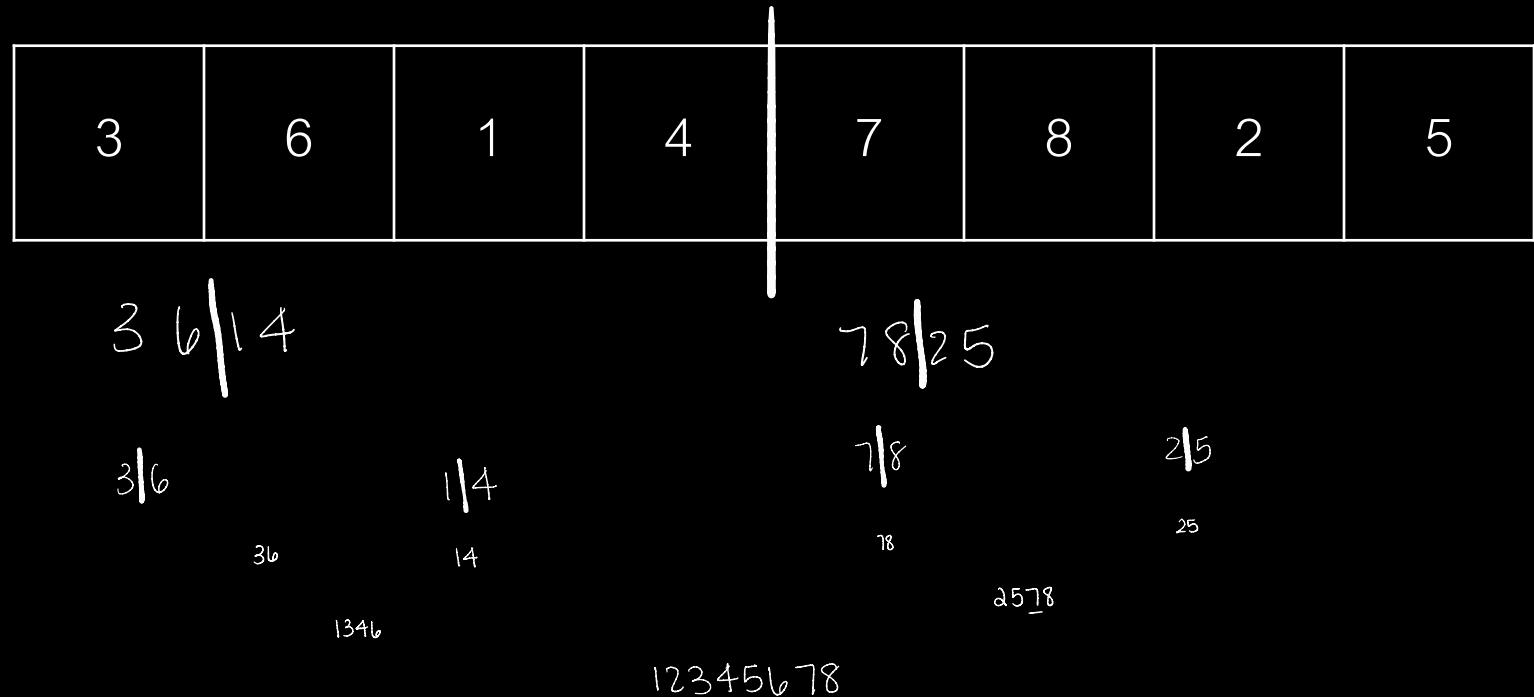
$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 3, 5, 2, 6, 1, 7 \end{matrix}$
 FOUND MIN OF UNSORTED ARRAY!
 $i=0$
 $\min=3$
 $\text{idx}=0$
 $j=0 \dots 2 \dots 4 \dots 5$
 if $(3 > \text{arr}[2])$
 $\min=2$
 $\text{idx}=2$
 $\min=1$
 $\text{idx}=4$

$\text{arr}[0] = \text{arr}[2] \Rightarrow \text{arr}[0]=3$
 $\text{arr}[2] = \text{arr}[0] \Rightarrow [3, 2, 3]$
 $\text{arr}[0]=3$
 $\text{arr}[2]=3$
 $\text{temp}=3$
 $\text{arr}[0]=1$
 $\text{arr}[4]=3$

$\begin{matrix} 3 & 5 & 1 & 6 & 7 & 2 \\ \overset{\text{min}}{\circ} & & & & & \\ \overset{i}{\circ} & \overset{j}{\circ} & & & & \\ \overset{\text{idx}}{\circ} & & & & & \end{matrix}$
 $\text{temp} = \text{arr}[0]$
 $\text{arr}[0] = \text{arr}[2]$
 $\text{arr}[2] = \text{temp}$

$3, 5, 2, 6, 1, 7$
 $1, 5, 2, 6, 3, 7$

Merge Sort



Merge Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|---|---|---|---|---|

1234

5678

12 34

56 78

1 2 3 4

1234

5 6 7 8

56

78



5678

Merge Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

- Best Case? $\Omega(n \log n)$
- Worst Case? $O(n \log n)$

Fun Sorts :D

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

Stalin Sort (fake sort vibes)

n size array

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

3

6

7

8

3 6 7 8

Stalin Sort (fake sort vibes)

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

- Best Case? $\mathcal{O}(n)$
- Worst Case? $\mathcal{O}(n)$

Bogosort Sort

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 3 | 6 | 1 | 4 | 7 | 8 | 2 | 5 |
|---|---|---|---|---|---|---|---|

$O((n+1)!)$

Summary

Selection Sort : BEST n^2 WORST

Bubble Sort : BEST n WORST n^2

Merge Sort : BEST $n \log n$ WORST

- Searching and Running Times
- Structs
- Sorting
- Recursion

```
int hi()
{
    1. printf("%s\n", "hi");
    2. hi(); //calls the hi function
}

hi();
→ 1. print hi
→ 2. hi();
    → 1. print hi
    → 2. hi();
```

Recursion

- Base Case

- Recursive Call

Write a function that prints integers starting from n line by line, subtracting one for each line until zero is reached using recursion.

Recursion

```
void count(n)
{
    if (n == 0)
    {
        return;
    }
    count(n - 1(n - 1); } RECURSIVE CALL
    printf("%i\n", n);
}
```

```
count(3)
if 3==0 X
count(2);
if 2==0 X
count(1);
if 1==0 X
count(0);
if 0==0 ✓
print(1)
print(2)
print(3)
```

Recursion

- Base Case

- Recursive Call

Write a function that determines the factorial of an integer n using recursion. Prompt the user for an integer and print out its factorial.

```
int x = get_int("give int!");
int factorialX = fact(x),
printf("%d\n", factorialX);
```

```
int fact      (int x)
{
    if (x <= 1)
        return 1;
    return x * fact(x-1);
}
```

$$\begin{aligned} x! &= x \cdot (x-1) \cdot (x-2) \dots \\ x! &= x \cdot (x-1)! \quad \xrightarrow{\text{fact}(x) = x \cdot \text{fact}(x-1)} \\ &\qquad\qquad\qquad \text{function returning} \\ &\text{if we know } (x-1)!, \text{ then we} \\ &\text{can mult by } x \text{ to get } x! \end{aligned}$$

```
factorial (3)
if 3 >= x
    return 3 * fact(2)  $\leq 6$ 
else
    if 2 >= x
        return 2 * fact(1)  $\leq 2$ 
    else
        if 1 >= x
            return 1  $\leq 1$ 
```

$$\begin{aligned} (x-1)! &= (x-1) \cdot (x-2)! \\ (x-2)! &= (x-2) \cdot (x-3)! \end{aligned}$$

Exercise 2: Fibonacci Numbers

Write a recursive function *fib* that computes the nth Fibonacci number. The 0th Fibonacci number is 0, the 1st Fibonacci number is 1, and every subsequent Fibonacci number is the sum of the two preceding Fibonacci numbers.

fib(7) returns 13

$$\begin{aligned} \text{fib}(3) &= \text{fib}(2) + \text{fib}(1) \\ &\downarrow \quad \downarrow \\ &\text{fib}(1) + \text{fib}(0) \\ &\downarrow \quad \downarrow \\ &1 + 0 \\ &\quad \swarrow \quad \curvearrowright \\ &1 \end{aligned}$$

BST (AST: n==1 return 1)

$$\begin{aligned} \text{fib}(2) &= \text{fib}(1) + \text{fib}(0) \\ &\downarrow \quad \downarrow \\ &1 + \text{fib}(-1) + \text{fib}(-2) \end{aligned}$$

return-type name (arguments)
type name1, type name2...
{
}
{
}

```
int fib(int n); // tells computer fib fcn exists!
int main(void)
{
    int input = get_int("int: ");
    printf("%i\n", fib(input));
}

int fib(int n)
{
    if (n == 0)
    {
        return 0;
    }
    if (n == 1)
    {
        return 1;
    }
    return fib(n-1) + fib(n-2);
}
```

Lab

| | reversed [5, 4, 3, 2, 1] | sorted [1, 2, 3, 4, 5] | random [3, 2, 5, 1, 4] | |
|-----------|-----------------------------|---------------------------|---------------------------|-----------|
| Selection | n^2 | <u>n^2</u> | n^2 | BUBBLE |
| Bubble | n^2 | <u>n</u> | n^2 | MERGE |
| Merge | $n \log n$ | $n \log n$ | $n \log n$ | SELECTION |

```
time ./sort1 reversed10000.txt
```

USER TIME

CS50 Section 3