This is an individual project: no cooperation is allowed.

Problem 1: E-R (10 points)

```
You are given the following relational schema (keys underlined):

Employee(SSN, Name)

Faculty(SSN)
(Faculty(SSN) references Employee(SSN))

Staff(SSN, ManagerSSN)
(Staff(SSN) references Employee(SSN);
Staff(ManagerSSN) references Staff(SSN))

Student(PersonNo, Name)

Course(CourseNo, Title)

Offering(CourseNo, Semester, InstructorSSN, Credit)
(Offering(CourseNo) references Courses(CourseNo);
Offering(InstructorSSN) references Faculty(SSN))

Enrolls(CourseNo, Semester, PersonNo, Grade)
(Enrolls(CourseNo, Semester) references Offering(CourseNo, Semester);
Enrolls(PersonNo) references Student(PersonNo))
```

Decompile the above schema into an E-R schema representing the same information.

Problem 2: Relational design(10 points)

```
You are given the following relational schema (keys underlined):

Faculty(SSN,Name)

Student(PersonNo, Name)

Course(CourseNo, Title)

Offering(CourseNo, Semester, InstructorSSN, Credit)

Enrolls(CourseNo, Semester, PersonNo, Grade)
```

To do:

1. Represent the above schema as a single relation schema R with a set of functional dependencies F.

- 2. Is the resulting schema R in BCNF? Prove your answer using the appropriate definitions.
- 3. If R is not in BCNF, provide its lossless join decomposition into BCNF and determine whether it preserves the dependencies in F.

Problem 3: Extra credit (5 points)

Notation: A, B, C and D are distinct attributes a relation schema R(ABCD). MVDs are defined over R.

Are the following inferences correct? Prove or disprove them using formal definitions.

- 1. If A woheadrightarrow B and A woheadrightarrow C, then A woheadrightarrow BC.
- 2. If $A \rightarrow BC$, then $A \rightarrow B$.
- 3. If $AB \to C$, then $A \to C$.