$$\text{Let } q = 1, p = 0 \text{ and } T^n_{pq} : \begin{cases} a_n = b_{n-1}q + a_{n-1}q + a_{n-1}p \\ b_n = b_{n-1}p + a_{n-1}q \end{cases}$$
 
$$\Rightarrow T^{n+1}_{pq} : \begin{cases} a_{n+1} = b_{n-1}(2pq + q^2) + a_{n-1}(q^2 + 2pq) + a_{n-1}(p^2 + q^2) \\ b_{n+1} = b_{n-1}(p^2 + q^2) + a_{n-1}(2pq + q^2) \end{cases}$$
 
$$\text{Let } q' = 2pq + q^2 \text{ and } p' = p^2 + q^2$$
 
$$\Rightarrow T^n_{pq} = (T^{\frac{n}{2}}_{p'q'})$$