



# **Real-Time Bridge Monitoring Technical Documentation**

**Version 2.0**

Real-Time Bridge Monitoring	Version: 2.0
Technical Documentation	Date: 2013-12-20

## Revision History

Date	Version	Description	Author
2002-00-00	0.01	Initial Draft	
2013-12-12	1.0	First Setup of the document Filled all chapters, except the first, from Inputs_Conversion_Formulas_Calculation document	Andrea Bottoli
2013-12-20	2.0	Finalization of the document Filled the introduction section	Andrea Bottoli

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## 1. Introduction

### 1.1 Purpose of this document

The purpose of this document is to provide a precise description of the calculations performed by Real-Time Bridge Monitoring program, trying to be as detailed as possible and also as understandable as possible.

A first description of the calculations was taken by ing. Gianluca Crotti from Politecnico di Milano, and re elaborated by Lorenzo Pagliari, which is a member of this product development group.

### 1.2 Document organization

The document is organized as follows:

- The first section of this document describes the contents of this guide, used documentation during developing process; it defines also the scope and the intended audience of this document, and also some useful references.
- The second section of this document defines the type of the inputs for the program, taken by the local server on the bridge monitored, and on their contents.
- The third section of this document is about the conversion of the content of the input files.
- The fourth section of this document focuses on the forces acting on the bridge, first on the whole bridge and then, with more details, on the stack, on the pier and on the single pylon.
- The fifth section of this document describes the calculations needed to retrieving the forces needed to calculate a safety factor of the bridge structure.
- The sixth section is about all the possible combination of calculations, taken in consideration the presence of debris, traffic and also the type of traffic on the bridge.
- The last section, which is the more innovative one, is about the M-N domain, and describes the critical domain in which the pylons are secure, following NTC 08 and EU 305/2011 guide lines.

### 1.3 Intended Audience

The intended audience is:

- technical end users
- DSD staff
- DSD supervisors
- DSD customers
- Real-Time Bridge Monitoring group members

### 1.4 Scope

The major scope of this document is to explain in a detailed ways the calculations made by Real-Time Bridge Monitoring product. It is produced also to be referred by the other documents, trying to help a better understand of the documents.

### 1.5 References

- Real-Time Bridge Monitoring web site: <http://161.53.67.134/BridgeMonitoring/>
- User Guide: [http://www.fer.unizg.hr/\\_download/repository/User\\_Guide\\_v1.0.pdf](http://www.fer.unizg.hr/_download/repository/User_Guide_v1.0.pdf)
- Installation Guide: [http://www.fer.unizg.hr/\\_download/repository/Installation\\_Guide\\_v1.0.pdf](http://www.fer.unizg.hr/_download/repository/Installation_Guide_v1.0.pdf)
- Design: [http://www.fer.unizg.hr/\\_download/repository/Design\\_Description\\_v1.5.pdf](http://www.fer.unizg.hr/_download/repository/Design_Description_v1.5.pdf)
- Requirements: [http://www.fer.unizg.hr/\\_download/repository/Requirements\\_Definition\\_v1.3.pdf](http://www.fer.unizg.hr/_download/repository/Requirements_Definition_v1.3.pdf)

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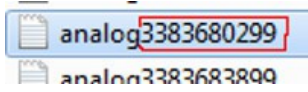
## 2. Type Of Inputs

### 2.1 Three Type of Inputs

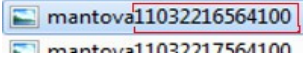

On the source folder there are three type of inputs:

- *analog\*\*\*\*\*.txt*
  - in this file there are the values measured by the *Anemometer* and the Hydrometer
- *sonar\*\*\*\*\*.txt*
  - in this file there are the values measured by the *Echo-sounder*
- *Modena\*\*\*\*\*.jpg* or *Mantova\*\*\*\*\*.jpg*
  - these are the pictures taken by the two camera on the Borgoforte bridge

### 2.2 How to interpret the ID/timestamp of a file

How to interpret the ID/timestamp of a file	
<p><i>analog*****.txt</i> <i>sonar*****.txt</i></p> <p><b>Example</b> File: <i>analog3383680299.txt</i></p>  <p>(fig. 1)</p>	<p>For this two kind of files the ID represents the Labview encoding and corresponds at the number of seconds that have elapsed sing 1th January 1904, without time zone so on the meridian of Greenwich (and at the same way for the timestamp of the all values in the file) <a href="http://www.ni.com/white-paper/7900/en/">http://www.ni.com/white-paper/7900/en/</a></p> $s = 3383680299 \leftarrow \text{fig. 1}$ $m = (3383680299 / 60) = 56394671$ $h = (56394671 / 60) = 939911$ $d = (939911 / 24) = 39162$ $y = (39162 / 365) = 107$ $\text{rest of days} = d - (y * 365) = 107$ $\text{rest of hours} = h - (d * 24) = 23$ $\text{rest of minutes} = m - (h * 60) = 11$ $\text{rest of seconds} = s - (m * 60) = 39$ <p>The rest of days is 107, and it corresponds at the month of April because 107 is between the sum of the days till March(that is 90) and the sum of days till April (that is 120). So mean that 107 days remaining corresponds at the month of April, the 4<sup>th</sup>; how many days in April? April begins after 90 days so 107-90=17days elapsed.</p> <p>Here we are:</p> <p><u>Day 0</u> + <u>results</u></p> $y = 1904 + 107y = 2011$ $m = 0 + 04m = 04$ $d = 0 + 17d = 17$ $h = 00 + 23 = 23 h$ $m = 00 + 11 = 11 m$ $s = 00 + 39 = 39 s$ <p>This is the “normal” conversion; then we have to consider the leap years and correct the result in the right one.</p>

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How to interpret the ID/timestamp of a file	
<p><b>Modena*****.jpg</b></p> <p><b>Mantova*****.jpg</b></p>	For the pictures the ID represents the exact date and time when the picture is taken
<p><u>Example</u></p> <p>File:</p> <p><i>mantova11032216564100.jpg</i></p>	<p>As you can see in fig. 3 this picture is taken on 22/03/2011 (DD/MM/YYYY) at 16:56:40 (hh:mm:ss)</p>
<p>This information is used to build the timestamp of the file, in this way:</p>	<p><i>Y = 2011 → 11 take only the last two number of the year</i></p> <p><i>M = 03</i></p> <p><i>D = 22</i></p>
<p>(fig. 2)</p>  <p>(fig. 3)</p> 	<p><i>h = 16</i></p> <p><i>m = 56</i></p> <p><i>s = 40</i></p> <p><i>concatenating all these numbers we obtain:</i></p> <p><i>Y M D h m s</i></p> <p><i>110322165640</i></p> <p><i>If we compare this result and the file ID</i></p> <p><i>110322165640 ← concatenation of values</i></p> <p><i>11032216564100 ← timestamp of the file</i></p> <p><i>it is the same value except for the last two numbers that we can discard; this file was saved just 1sec after the picture was taken.</i></p> <p><i>Concluding, we can extract the date&amp;time when a picture was taken, just reading the file ID.</i></p>

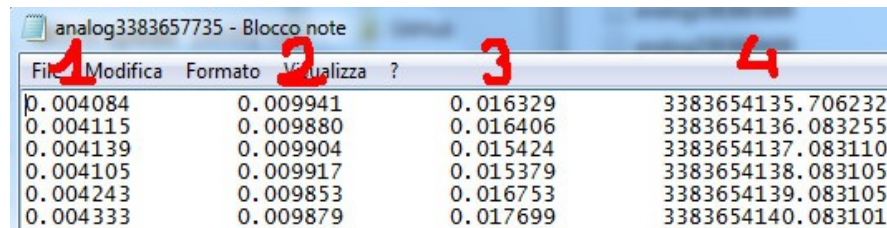
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### 3. Inputs Content

#### 3.1 Analog Files

The analog file contains 4 columns of values (*fig.4*):

1. **Wind speed** (unity measure Ampère)
2. **Distance between the Hydrometer and the level of water** (unity measure Ampère)
3. **Wind direction** (unity measure Ampère)
4. **Timestamp** of the detection of the sample (Labview encode → see before)[*decimals can be dropped*]



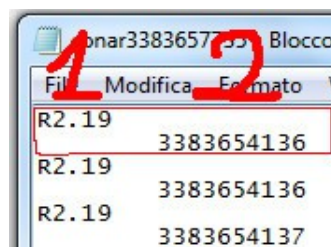
0.004084	0.009941	0.016329	3383654135.706232
0.004115	0.009880	0.016406	3383654136.083255
0.004139	0.009904	0.015424	3383654137.083110
0.004105	0.009917	0.015379	3383654138.083105
0.004243	0.009853	0.016753	3383654139.083105
0.004333	0.009879	0.017699	3383654140.083101

(*fig. 4*)

#### 3.2 Echo-sounder Files

The echo-sounder file contains 2 columns of values, offset of a line (*fig.5*):

1. **Distance between the sonar and the river bed** (unity measure meters)
2. **Timestamp** of the detection of the sample (Labview encode → see before)



R2.19	3383654136
R2.19	3383654136
R2.19	3383654137

(*fig.5*)

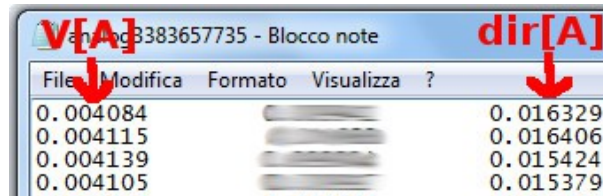


## 4. Conversion operations

### 4.1 Introduction

Every hour the system receives a packet in which there are an analog file and a sonar file, both files with at most 3600 values, and two images one for camera. All these values are to be converted from the parser into the db, in the table of *sensor\_raw\_data*. Each values has to fill one row of the table.

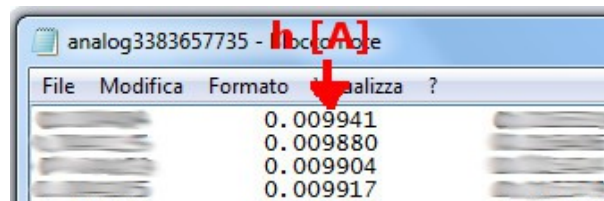
### 4.2 Anemometer



(fig.6)

- Speed  $V[m/s] = (((V[A] * 1000) - 4) * 3,75)$
- Direction  $dir[^\circ] = (((dir[A] * 1000) - 4) * 22,5)$

### 4.3 Hydrometer



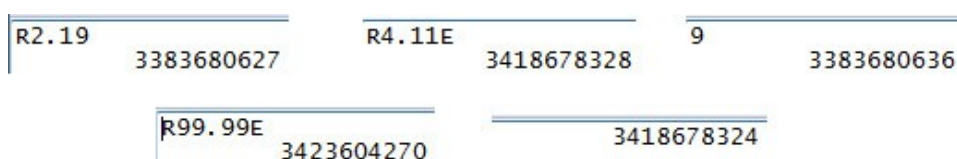
(fig.7)

- Distance hydrometer-water  $h[m] = 20 + (((h[A] * 1000) - 4) * (-1,25))$
- Water height  $h_{water}[m] = 29,86 - h[m]$

### 4.4 Echo-sounder

The sonar could produces five different kind of data

1. Correct data → Rxx.xx (can exist even one decimal)
2. Uncertain data → Rxx.xxE (can exist even one decimal)
3. Wrong data → xx.xx (can exist even one decimal)
4. Sonar out of water → R99.99E
5. Error → E1 or missing data



(fig.8)

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The generic xx.xx is the distance in *meter* between the sonar and the height of the bottom.

- Height of the bottom →  $h_{bottom}[m] = 12,3 - xx.xx[m]$

Data that are of type ① and ② can be convert in a real height; for the other types this conversion is not possible but is necessary to store these information anyway, to compute some statistics that will explain later.

The data of type ③, ④ and ⑤ are not used to make calculations but will be saved into the db and on these data in future could be made some statistics. For now, is only a report that says how good is the behavior of the echo-sounder.

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## 5. Kind of Calculations

### 5.1 Introduction

To aggregate data for 10 minutes (1 hour and/or 1 day), we have to manage 600 data as a single sample to calculate the needed information; these 600 data correspond to a sequence of 600 seconds starting from a given time instant.

### 5.2 Anemometer (10 min)

- [ANE1] mean wind speed
- [ANE2] maximum wind speed in the 10 minutes
- [ANE3] mean wind direction
- [ANE4] direction of the maximum wind speed in the 10 minutes

### 5.3 Hydrometer (10 min)

- [IDRO1] mean water height
- [IDRO2] variance of the sample

### 5.4 Echo-sounder (10 min)

- [SONAR1] mean value of the height of the bottom (only with data of type ① + ②)
- [SONAR2] variance of the sample (only with data of type ① + ②)
- [SONAR3] % of data of type “① + ②” used compared to the 600 elements of the sample
- [SONAR4] % of data of type “③” there are in the sample
- [SONAR5] % of data of type “④” there are in the sample
- [SONAR6] % of data of type “⑤” there are in the sample
- [SONAR7] % of data of type “②” there are, considering as sample the “① + ②” set of data (so not all the 600 data)

### 5.5 Images (10 min)

The images don't need any kind of elaboration, they have only to be displayed.

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## 6. Forcing Calculation

### 6.1 Introduction

The deck of the Borgoforte bridge is bore by many piers. Only one is monitored, number 30.

This pier is composed by 2 independent rows of 3 piles (the 3 piles of each row are connected by 2 horizontal structures, superior beam, called "pulvino", and an inferior beam called "traverso").

The structural analysis does not include the entire bridge but a piece of it: the pier (number 30) and the related part of the deck (for instance, every weight or force applied to this part of the deck must be totally "absorbed" by the pier, in particular by each 6 piles).



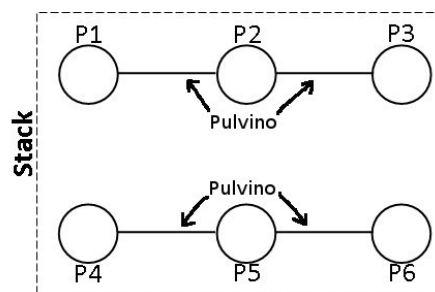
The logical steps are:

1. evaluate the force on the part of the bridge of pier 30 competence
2. transfer these forces from the deck to the pier
3. split this transferred force on the 2 independent rows
4. define the maximum stresses in each pile

For the most of the formulas, it is needed the use of parameters; these parameters are in a DB table that only who have a high level of authorization can change. The change of parameters causes the re-elaboration of the all data in the grouped tables (customers know it and accept it).

### 6.2 Pier/Stack compositions

The bridge is supported by various stacks/cells and each stack is composed by two line of three pylons connected together by a "pulvino" (fig. 9).



(fig.9)

The system has to calculate the forces acting on the stack and after, if is possible, has to divide these forces on the two lines of the stack and divide again on the three pylons of each line.

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### 6.3 Push of the wind

The push of the wind is divided in two components:

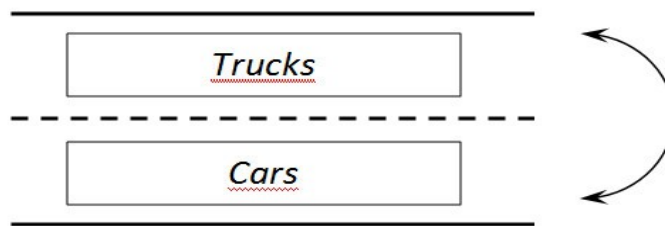
- $S_{V_{plank}}$ : is the push of wind on the planking
- $S_{V_{traf}}$ : is the push of wind on the traffic

Because the traffic is not monitored, we have to use a combination of possible traffic scenarios; in this model are modeled three scenarios, named A1, A2 and A3, and each scenario is itself divided into two or four scenarios dependent on the direction of the traffic; the scenarios are default scenarios that are used at design phase of any kind of structure of this type.

These are the traffic combinations:

#### A1

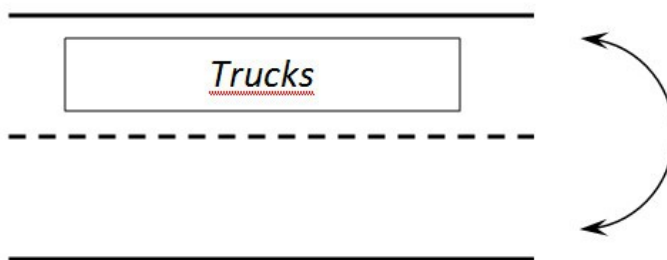
(A110 - A120)



*In this combination the push of wind on traffic is high because this is the combination that expected a huge amount of traffic in both directions and on the whole length of the plank.*

#### A2

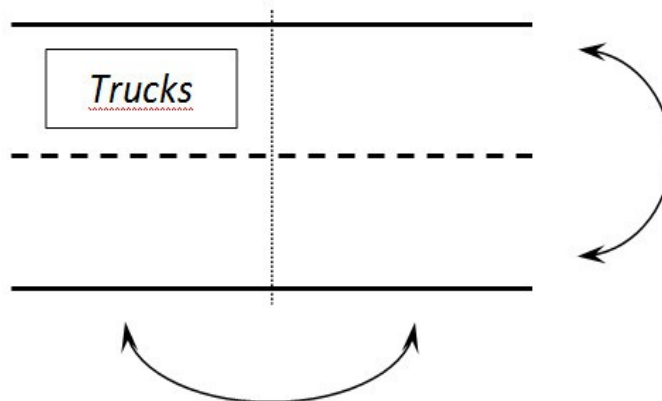
(A210 - A220)



*This combination that expected a traffic only in one direction but still for the whole length of the plank. Then the push is expected to be less than the previous one.*

#### A3

(A311 - A312  
A321 - A322)



*This combination expects the presence of traffic only in one direction and not for all the length of the plank portion on the pier. That mean the traffic is concentrated in one quarter, as you can see in the figure. That mean that wind push on the traffic will be minimum respects the other combinations but will have other major effects under other aspects that we will explain later in the document.*

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### 6.3.1 Effective Speed

Before start to calculate the push of the wind on the whole bridge system, we must consider the real relevant value of the wind speed and not the general one. Is defined *effective speed* ( $V_{EFFwind}$ ) the wind component orthogonal to the bridge and to calculate it are needed:

- Measured wind speed  $\rightarrow [ANE2]$
- Measured wind direction  $\rightarrow [ANE4]$
- Planimetric inclination of the bridge from the north  $\rightarrow \alpha$  (parameter)

$$V_{EFFwind} = [ANE2] * \sin([ANE4] + \alpha)$$

### 6.3.2 Push of the wind on the planking

For calculate this value are needed these information:

- “Drag planking” coefficient  $\rightarrow C_{Dwi}$  (parameter)
- Air density  $\rightarrow \rho$  (parameter)
- Planking area  $\rightarrow A_{PLANK}$  (parameter)
- Effective wind speed  $\rightarrow V_{EFFwind}$  (see previous point)

$$S_{Vplank} = \frac{1}{2} * C_{Dwi} * \rho_{air} * A_{plank} * V_{EFFwind}^2$$

### 6.3.3 Push of the wind on the traffic

For calculate this variable we must consider the three possible traffic scenarios, and also are needed:

- “Drag traffic” coefficient  $\rightarrow C_{Dwi}$  (the same of previous point)
- Air density  $\rightarrow \rho_{air}$  (the same of previous point)
- Surface of traffic  $\rightarrow A_{TRAF}$  (parameter)
- Aerial reduction coefficient  $\rightarrow \beta_1$  or  $\beta_2$  (parameters)
- Effective wind speed  $\rightarrow V_{EFFwind}$  (see previous point)

For traffic combination A1:

$$S_{V(A1 \text{ traf})} = \frac{1}{2} * C_{Dwi} * \rho_{air} * (\beta_1 * A_{traf}) * V_{EFFwind}^2$$

For traffic combination A2 (the same of A1):

$$S_{V(A2 \text{ traf})} = \frac{1}{2} * C_{Dwi} * \rho_{air} * (\beta_1 * A_{traf}) * V_{EFFwind}^2$$

For traffic combination A3:

$$S_{V(A3 \text{ traf})} = \frac{1}{2} * C_{Dwi} * \rho_{air} * (\beta_2 * A_{traf}) * V_{EFFwind}^2$$

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## 6.4 Hydrodynamic Load (on the whole pier)

### 6.4.1 Introduction

The water pressure on the pier depends on the presence or not of debris on the stack basement.

As the same way of the wind, will be calculate all the loads and then choose at a later which consider.

### 6.4.2 Water Speed

The hydrometer values provided by the customer, measure the height of the water, then we have to find a relation between the height of water and the water speed. To do this are needed:

- Scale of flow rates: correlates uniquely the water height ( $h_{\text{water}} \rightarrow [\text{IDRO1}]$ ) and the flow rate ( $Q$ )
- Two-dimensional analysis: allow to know for some flow rate value ( $Q$ ) the relative value of water speed ( $V_{\text{water}}$ )

#### 6.4.2.1 Scale of flow rates

The following table shows the relation between the flow rate ( $Q$ ) and the water height ( $h_{\text{water}}$ ), depending on the value of  $h_{\text{water}}$  the parameters  $a_i$ ,  $b_i$  and  $c_i$  changes

- $a_1, b_1, c_1$  (parameters) for  $h_{\text{water}} < 17\text{m}$
- $a_2, b_2, c_2$  (parameters) for  $17\text{m} < h_{\text{water}} < 22\text{m}$
- $a_3, b_3, c_3$  (parameters) for  $22\text{m} < h_{\text{water}} < h_{\text{MAXwater}}$

$h_{\text{MAXwater}} = 25,3 \text{ m}$

Scale of estimate flow rates with fixed section			
Parameters	[IDRO1] < 17m	17m < [IDRO1] < 22m	22m < [IDRO1] < $h_{\text{MAXwater}}$ (25,3m)
$a_i$	46	60	96
$b_i$	-902	-1350	-2800
$c_i$	4658	8000	22500

$$Q = a_i * h_{\text{water}}^2 + b_i * h_{\text{water}} + c_i$$

if  $h_{\text{water}} > h_{\text{MAXwater}}$  the river has overflowed.

#### 6.4.2.2 2D Analysis

The relation between the flow rate of water and its speed are in the following table. Depending on the flow rate of water, you can identify the range and interpolate linearly to get the speed of water.

$$V_{\text{water}} = a * h_{\text{water}}^3 + b * h_{\text{water}}^2 + c * h_{\text{water}}$$

2D analysis – fixed bottom		
$h_{\text{water}}$ [m]	$Q$ [ $\text{m}^3/\text{s}$ ]	$V_{\text{water}}$ [m/s]
3	510	0,24
10,5	5400	2,73
14	10000	3,54

**N.B.:** the parameters  $a$ ,  $b$  and  $c$  are different from the parameters  $a_i$ ,  $b_i$  and  $c_i$

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### 6.4.3 Water Thrust

To calculate the water thrust are needed these information:

- “Drag planking” coefficient  $\rightarrow C_{Dwa}$  (different parameter from that of the wind, see below)
- Water density  $\rightarrow \rho$  (parameter)
- Stack area  $\rightarrow A_{stack}$
- Water speed  $\rightarrow V_{water}$  (see point before)

The “Drag planking” coefficient depends on the presence ( $D=1$ ) or not ( $D=0$ ) of debris on the stack base; so the Drag Planking coefficient is split in:

- “Drag planking” coefficient ( $D=0$ )  $\rightarrow C_{D0wa}$  (parameter)
- “Drag planking” coefficient ( $D=1$ )  $\rightarrow C_{D1wa}$  (parameter)

The area of the stack invested by the flow of water depends on three factors:

- Presence ( $D=1$ ) or not ( $D=0$ ) of debris on the stack basement
- Height of the water  $\rightarrow [IDRO1]$
- Height of the bottom of the river  $\rightarrow [SONAR1]$
- Shape of the stack; with presence of debris the shape of the stack changes, because the debris offer a greater surface on which the water can push.

The area of the stack is calculated using always the same formula, but depending on the scenario the coefficients involved change.

$$A_s = B_s * h_s$$

The  $h_s$  is calculated independently by the presence or not of debris:

- $[SONAR1] < \text{bottom\_ref} \rightarrow h_s = [IDRO1] - \text{bottom\_ref}$
- $[SONAR1] > \text{bottom\_ref} \rightarrow h_s = [IDRO1] - [SONAR1]$

The  $\text{bottom\_ref}$  is a parameter.

The  $B_s$  depends instead on the presence or not of debris:

- $D=0 \rightarrow B_s = B_{s0} = 2 * D_{pylon}$
- $D=1 \rightarrow B_s = B_{s1} = c$

$c$  and  $D_{pile}$  are parameters

At the end we have this formulas:

(D = 0)	(D = 1)
$A_s = B_{s0} * h_s$ $S_{water} = \frac{1}{2} * C_{D0} * \rho_{water} * A_s * V_{water}^2$	$A_s = B_{s1} * h_s$ $S_{water} = \frac{1}{2} * C_{D1} * \rho_{water} * (A_s * \beta_A) * V_{water}^2$



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## 6.5 Weight of the structure (of the whole stack)

In this case we have to calculate the weight of the stack and the portion of planking which is competence of the pier. Most of the weight that will be considered are constant, the only variable is related about the portion of the pier exposed, so that portion that is measured as [SONAR1].

To calculate this value, are needed these information:

- Weight on the pier →  $P_p$  (parameter)
- Weight of pulvino →  $P_{pu}$  (parameter)
- Weight of trunk pylon →  $P_{tp}$  (parameter)
- Weight of the beam →  $P_b$  (parameter)
- Weight per meter of the single pylon →  $P_{py}$  (parameter)
- Height of the beam →  $h_{beam}$  (parameter)
- Height of stack portion exposed → to be evaluated with [SONAR1]

$$PP_{structure} = P_p + [(2 * P_{pu} + 6 * P_{tp} + 2 * P_b) + 6 * (P_{py} * (h_{beam} - [SONAR1]))]$$

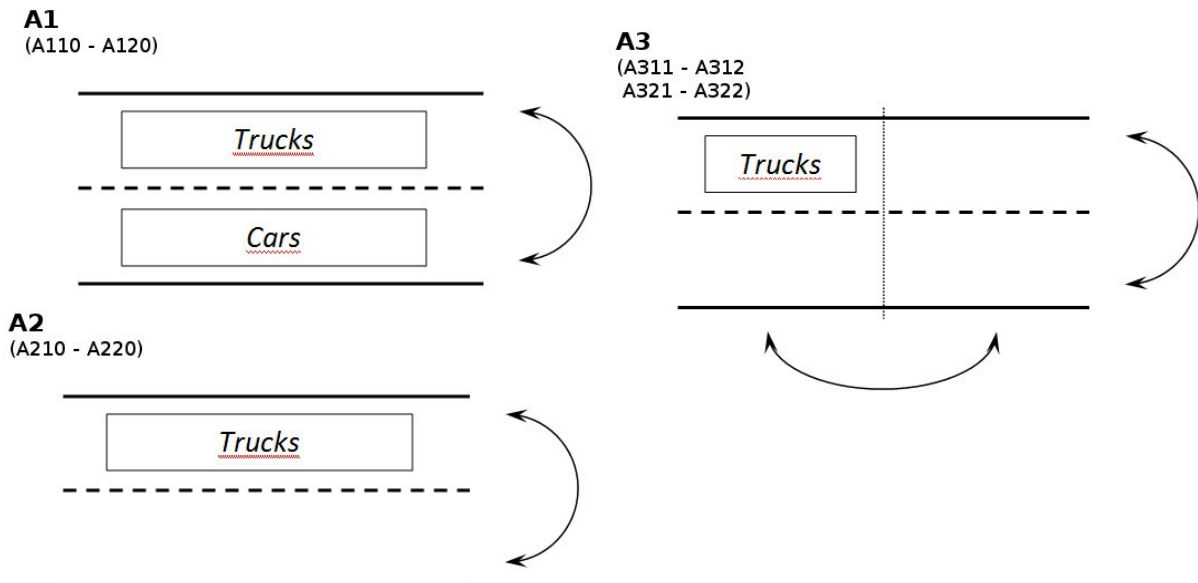
## 6.6 Mobile/Traffic Loads

The traffic is not monitored, so we have to use combinations of load to suite the common possible scenarios. The common combinations of loads used at design phase of a bridge are in general three and are A1, A2 and A3. At each combination was assigned a different contribute in terms of forces.

- A1 → N(A1), Mxx(A1) and Myy(A1)
- A2 → N(A2), Mxx(A2) and Myy(A2)
- A3 → N(A3), Mxx(A3) and Myy(A3)

The load combinations generate three kind of different forces: N is a vertical load, Mxx is the bending moment on the x-axis and Myy is the bending moment on the y-axis. The direction of the axes will be define later.

These are the traffic combinations:



We'll explain later the effects that each combination generates.

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## 6.7 Brake of Vehicles

In presence of traffic, there is the possibility of hard brakes by the vehicles that induce additional forces on the planking.

- $F_R \rightarrow$  vehicles braking (parameter)

## 6.8 Final Remark on the Forcing

The forcing that act on the stack 30 are:

- Push of wind
- Hydrodynamic thrust
- Weight of the structure
- Mobile loads
- Brake of vehicles

The descriptions and the formulas presented until here allow to evaluate the generic force but say nothing about where this force is applied, if to the planking or directly to the stack or to both.

The mainly purpose in to calculate the safety coefficient of the pier, all these generic forces must be transfer from the bridge to the pier.

During this “transferring” could born some new forces or some forces could transform in other forces and so on.

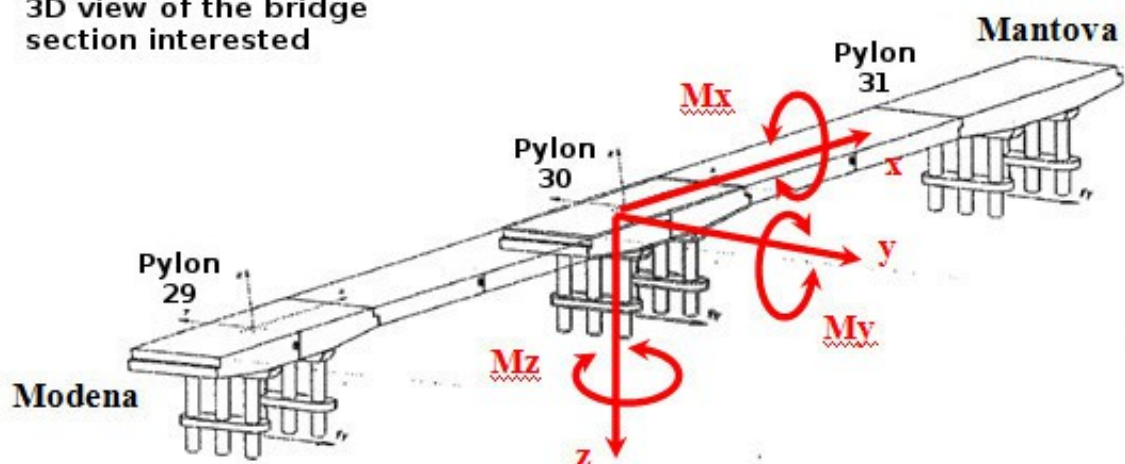
Moreover, all these forces and moments must be transferred also to the two lines of pylons that compose the single stack.

At the end, we have to transfer each force from the row to each single pylon.

## 6.9 Reference System

Below will be present a schema of the reference system and the naming of forcing still transferred to

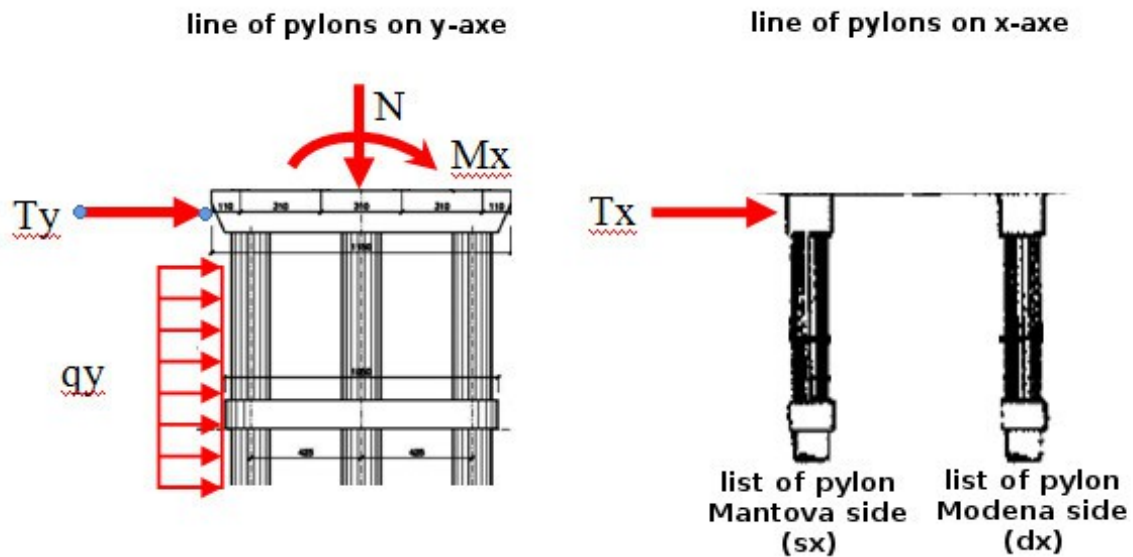
### 3D view of the bridge section interested



the single line of pylon.

(fig. 10)

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(fig. 11)

In these pictures, fig.10 and fig.11, are represented the generic forces acting on the stack, then each generic force contains the contributes of many forces.

The following table explain how the contributes are distributed into the generic force.

Chassis	Forces				
Action	Weight	Mobile weight	Brake	Wind	Water
N	X	X	X		
Ty				X	
Tx			X		
qy					X
Mx		X		X	
My					
Mz					

(table 1)

To clarify this concept, for example think about the Mobile weights. Before was said that the Mobile weights, independently from the combination of traffic, exercise three kind of forces: N, Mxx and Myy. These three forces are applied to the planking and in their transfer to the single line of pylon, become N and Mx.

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## 7. Forcing: from planking to the single line of pylons

### 7.1 Introduction

Now we will take a look at each force acting on the bridge and how these forces are transferred from the planking to the single line of pylons.

The signs of the values are all related with the reference system described in the previous chapter (*fig.10 and fig.11*).

### 7.2 Weight of the planking

The weight of the structure is composed by the weight of the planking that are on the stack ( $P_p$ ) and the weight of the stack itself.

To calculate how the weight of the structure is split on the two lines of pylons we consider only the weight of the planking on the stack.

The own weight of the stack will be added at the end.

In the following table there are the values of the forces resulting from the analysis.

Description	Line of pylons Mantova side (sx)	Line of pylons Modena side (sx)	Unity measure
[N] $R1 = P_p / 2$	+5355	+5355	kN
[N] $R2 = Mt/c_{span}$	+1023	-1023	kN
<b>[N]</b>	<b>+6378</b>	<b>+4332</b>	<b>kN</b>

$Mt, c_{span}$  are both parameters.

#### Observations:

- The bridge structure is not symmetric respect the y-axis and that involves that the “plank + pier” system is not split equally on the pier structure, so not split equally on the two rows of pylons
- The first **[N]** R1 contribute is made by the weight of the plank portion on the pier. This vertical load is a symmetric force
- The second **[N]** R2 contribute is generated by the asymmetry of the bridge that generate a constant vertical load R2 with different sign on the two row; this because this R2 factor is generated by a bending moment and obviously is a row is loaded, the other is unloaded by the R2 contribute
- At the end, the generic effects on the structure, on the single row on pylon is a resulting of sums between symmetric contributes and asymmetric contributes; as in this first table the **[N]** total force is a sum of a symmetric component R1 and an asymmetric component R2.

### 7.3 Mobile Loads (traffic combinations)

#### 7.3.1 Introduction

For the traffic combinations are reported the three final tables in which are described the decomposition of the forces in the three components.

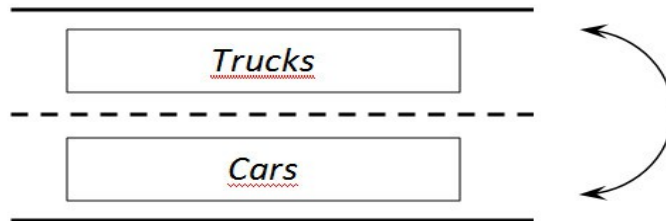
Each combination will be duplicated in the next calculations due to the fact that the specific combination represents a double scenario because the traffic can be symmetrical (for example cars in left lane and trucks in right lane; but also the vice versa, so trucks in left lane and cars in right lane).

This stuff is represented by the possibility to the variables to change their sign.

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### 7.3.2 A1 Combination

#### **A1** (A110 - A120)



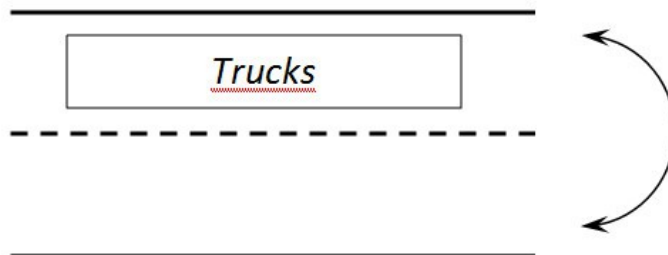
In this combination we have the most height vertical load, due by the presence of traffic in both directions for the whole length of the plank portion of competence of the pier.

In this combination we have a medium bending moment generated on x-axis by the traffic weight, due by the presence of traffic in both directions for the whole length of the plank portion of competence of the pier; the bending moment generated by one direction is balanced by the bending moment generated by the opposite direction, then the resulting is not the highest.

The bending moment generated on y-axis is quite low because the traffic is distributed on the whole length of the plank portion.

### 7.3.3 A2 Combination

#### **A2** (A210 - A220)



In this combination we have less vertical load respect the A1 combinations, due by the presence of traffic only in one of the two directions, always for the whole length of the plank portion of competence of the pier.

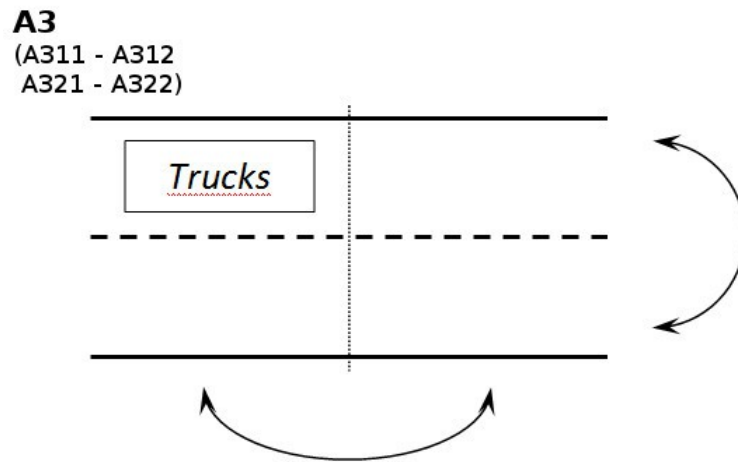
In this combination we have the highest bending moment generated on x-axis by traffic weight, due by the presence of traffic only in one direction for the whole length of the plank portion of competence of the pier; the bending moment generated is not balanced by the opposite direction, then the resulting is the highest.

The bending moment generated on y-axis is quite low because the traffic is distributed on the whole length of the plank portion.

A little bit lower then the previous but still quite low.

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#### 7.3.4 A3 Combination



In this combination we have the minimum vertical load respect others combinations, due by the presence of traffic only in one of the two directions and only in half length of the plank portion of competence of the pier; so only one quarter of the road has traffic. For this reason the A3 combination has 4 sub-scenarios, one for each quarter.

In this combination we have the minimum bending moment generated on x-axis by traffic weight, due by the presence of traffic only in one direction and concentrated into a quarter of the plank portion; the bending moment generated is not balanced by the opposite direction but since there is less traffic, the result is not high.

The bending moment generated on y-axis is the highest of all, because the traffic is not distributed on the whole length of the plank portion and that accentuates the asymmetry of the structure, generating a big bending moment on y-axis.

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#### 7.4 Traffic Tables

ID	Combination	N (Wsl)	Mxx	Myy
		[kN]	[kNm]	[kNm]
A1	1-a	4024	4368	3908
Description		Line of pylon Mantova side (sx)	Line of pylon Modena side (dx)	Unity Measure
[N]	$R1 = (N/2)$	+ 2012	+ 2012	kN
[N]	$R2 = (Myy/c_{span})$	+ 411	- 411	kN
[Mx]	$M1 = (Mxx/2)$	± 2184	± 2184	Knm

ID	Combination	N (Wsl)	Mxx	Myy
		[kN]	[kNm]	[kNm]
A2	1-b	3166	8077	3015
Description		Line of pylon Mantova side (sx)	Line of pylon Modena side (dx)	Unity Measure
[N]	$R1 = (N/2)$	+ 1583	+ 1583	kN
[N]	$R2 = (Myy/c_{span})$	± 317	∓ 317	kN
[Mx]	$M1 = (Mxx/2)$	± 4038.5	± 4038.5	kNm

ID	Combination	N (Wsl)	Mxx	Myy
		[kN]	[kNm]	[kNm]
A3	2-a	1979	2121	25756
Description		Line of pylon Mantova side (sx)	Line of pylon Modena side (dx)	Unity Measure
[N]	$R1 = (N/2)$	+ 989.5	+ 989.5	kN
[N]	$R2 = (Myy/c_{span})$	± 2711	∓ 2711	kN
[Mx]	$M1 = (Mxx/2)$	± 1060.5	± 1060.5	kNm

#### 7.5 Vehicle braking

At the same way of the mobile loads, we can't know the direction the brake, then we have report the values in the following table with the corresponding signs.

Description		Line of pylons Mantova side (sx)	Line of pylons Modena side (sx)	Unity measure
[Tx]	$T1 = F_R / 2$	± 103	± 103	kN
[N]	$R1 = F_R * n/c_{span}$	± 72	∓ 72	kN

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## 7.6 Wind

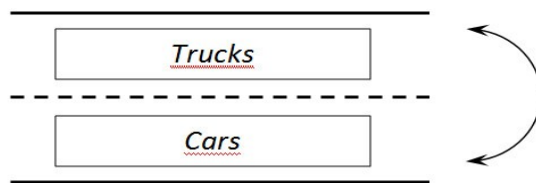
For the wind are still valid the considerations made before on the direction. The only different is that the wind direction is a value measured by monitoring, so we can know if its contribution is positive or negative.

Description	Line of pylons Mantova side (sx)	Line of pylons Modena side (sx)	Unity measure
[Ty] $F_v = (S_v / 2)$	$\pm F_v$	$\pm F_v$	kN
[Ty] $R_{av} = (S_{vplank} * r / c_{span})$	$\pm R_{av}$	$\mp R_{av}$	kN
[Mx] $M_{xv} = [(S_{vplank} * e_{plank} + S_{vtraf} * e_{traf}) / 2]$	$\pm M_{xv}$	$\pm M_{xv}$	kNm

For the [Ty] the  $S_v$  is the sum of  $S_{vplank} + S_{vtraf}$ , while  $r$ ,  $e_{plank}$  and  $e_{traf}$  are parameters.

- A1 Combination**

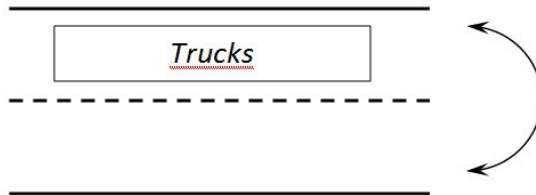
**A1**  
(A110 - A120)



*In this combination we have a the presence of traffic in both directions, so the wind push on traffic is very high because there is the most surface of traffic on which the wind can push.*

- A2 Combination**

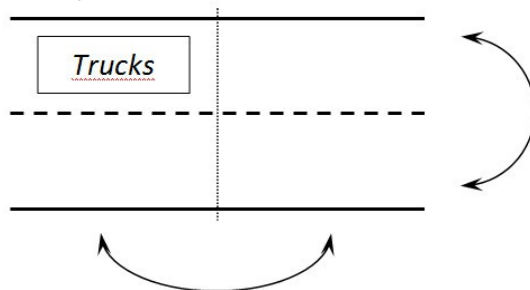
**A2**  
(A210 - A220)



*In this combination we have a the presence of traffic only in one direction, so the wind push on traffic contribute is less than the previous, because we lost a whole line of surface traffic.*

- A3 Combination**

**A3**  
(A311 - A312  
A321 - A322)



*In this combination we have a the presence of traffic only in one direction and only in half of plank length, so the wind push on traffic contribute is lesser than the previous, because we lost also half traffic respect the A2 combination.*



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## 7.7 Water

The water thrust acts only on the stack, since the planking is at a higher level of riverbank; that is to say that the water can never reach the planking, so this force don't need to be transferred to from the planking to the pylons. The only operation is to transform a concentrated force on a distributed load, and split it equally on the two lines of pylons. The values sign is defined because the water can flow only in one direction.

Description	Line of pylons Mantova side (sx)	Line of pylons Modena side (sx)	Unity measure
[qy] $qy = (S_{\text{WATER}} / h_s) / 2$	+ qy	+ qy	kN/m

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## 8. Load Combinations on the Stack

### 8.1 Introduction

Since some forces are not monitored, is not possible to know their direction and then the verse of these forces, that depending on the situations can stabilize or destabilize the whole structure.

To define in each moment the maximum stress scenario, we have to define load combinations which enclose all the possible situations.

In this table is reported, for each force, its contribution to the four generic resultant forces.

	Line of pylons MANTOVA side (sx)					Line of pylons MODENA side (dx)				
	N	Tx	Ty	qy	Mx	N	Tx	Ty	qy	Mx
<b>P<sub>p</sub></b>	+R1 +R2	0	0	0	0	+R1 -R2	0	0	0	0
<b>A110</b>	+R1 +R2	0	0	0	+M1	+R1 -R2	0	0	0	+M1
<b>A120</b>	+R1 +R2	0	0	0	-M1	+R1 -R2	0	0	0	-M1
<b>A210</b>	+R1 +R2	0	0	0	+M1	+R1 -R2	0	0	0	+M1
<b>A220</b>	+R1 +R2	0	0	0	-M1	+R1 -R2	0	0	0	-M1
<b>A311</b>	+R1 +R2	0	0	0	+M1	+R1 -R2	0	0	0	+M1
<b>A312</b>	+R1 -R2	0	0	0	+M1	+R1 -R2	0	0	0	+M1
<b>A321</b>	+R1 +R2	0	0	0	-M1	+R1 -R2	0	0	0	-M1
<b>A322</b>	+R1 -R2	0	0	0	-M1	+R1 -R2	0	0	0	-M1
<b>FR01</b>	+R1	+T1	0	0	0	-R1	+T1	0	0	0
<b>FR02</b>	-R1	-T1	0	0	0	-R1	-T1	0	0	0
<b>VT0</b>	0	0	$\pm (Fv0 + Rav)$	0	$\pm Mxv0$	0	0	$\pm (Fv0 - Rav)$	0	$\pm Mxv0$
<b>VT1A1</b>	0	0	$\pm (FvA1 + Rav)$	0	$\pm MxvA1$	0	0	$\pm (FvA1 - Rav)$	0	$\pm MxvA1$
<b>VT1A2</b>	0	0	$\pm (FvA2 + Rav)$	0	$\pm MxvA2$	0	0	$\pm (FvA2 - Rav)$	0	$\pm MxvA2$
<b>VT1A2</b>	0	0	$\pm (FvA3 + Rav)$	0	$\pm MxvA3$	0	0	$\pm (FvA3 - Rav)$	0	$\pm MxvA3$
<b>AQD0</b>	0	0	0	qy	0	0	0	0	qy	0
<b>AQD1</b>	0	0	0	qy	0	0	0	0	qy	0

Notes:

In the combination VT0 the bridge is ideally closed, so there is no traffic. The Fv0 identify the component of the wind force that acts only on the planking and the same thing with for the Mxv0.

- VT0 : wind thrust without traffic on the bridge
- VT1Ax: wind thrust with traffic of type A1 or A2 or A3 on the bridge
- AQDx: water thrust in presence or not of debris.

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## 8.2 Combinations

<b>comb_01A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT0</b>	
<b>comb_01B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT0</b>	

<b>comb_02A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A1</b>	<b>A110</b>	<b>FR01</b>
<b>comb_02B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A1</b>	<b>A110</b>	<b>FR01</b>
<b>comb_03A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A1</b>	<b>A110</b>	<b>FR02</b>
<b>comb_03B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A1</b>	<b>A110</b>	<b>FR02</b>
<b>comb_04A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A1</b>	<b>A120</b>	<b>FR01</b>
<b>comb_04B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A1</b>	<b>A120</b>	<b>FR01</b>
<b>comb_05A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A1</b>	<b>A120</b>	<b>FR02</b>
<b>comb_05B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A1</b>	<b>A120</b>	<b>FR02</b>

<b>comb_06A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A2</b>	<b>A210</b>	<b>FR01</b>
<b>comb_06B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A2</b>	<b>A210</b>	<b>FR01</b>
<b>Comb_07A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A2</b>	<b>A210</b>	<b>FR02</b>
<b>comb_07B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A2</b>	<b>A210</b>	<b>FR02</b>
<b>comb_08A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A2</b>	<b>A220</b>	<b>FR01</b>
<b>comb_08B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A2</b>	<b>A220</b>	<b>FR01</b>
<b>comb_09A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A2</b>	<b>A220</b>	<b>FR02</b>
<b>comb_09B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A2</b>	<b>A220</b>	<b>FR02</b>

<b>comb_10A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A311</b>	<b>FR01</b>
<b>comb_10B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A311</b>	<b>FR01</b>
<b>comb_11A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A311</b>	<b>FR02</b>
<b>comb_11B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A311</b>	<b>FR02</b>
<b>comb_12A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A312</b>	<b>FR01</b>
<b>comb_12B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A312</b>	<b>FR01</b>
<b>comb_13A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A312</b>	<b>FR02</b>
<b>comb_13B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A312</b>	<b>FR02</b>
<b>comb_14A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A321</b>	<b>FR01</b>
<b>comb_14B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A321</b>	<b>FR01</b>
<b>comb_15A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A321</b>	<b>FR02</b>
<b>comb_15B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A321</b>	<b>FR02</b>
<b>comb_16A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A322</b>	<b>FR01</b>
<b>comb_16B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A322</b>	<b>FR01</b>
<b>comb_17A</b>	→	<b>Pp</b>	<b>AQD0</b>	<b>VT1A3</b>	<b>A322</b>	<b>FR02</b>
<b>comb_17B</b>	→	<b>Pp</b>	<b>AQD1</b>	<b>VT1A3</b>	<b>A322</b>	<b>FR02</b>

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### 8.3 Combinations Explanation

Each of these combinations will provide a set of values N, Tx, Ty, qy and Mx with their specific signs that identify the forces direction.

At each combinations must be add the weight of the stack because, as said before, was “ignored” in the calculations of the force due by the weight of the structure.

This mean that the generic resultant force N must be increased to a  $N_{ps}$ .

Defined

$$PP_s = [(2 * P_{pu} + 6 * P_{tp} + 2 * P_b) + 6 * (P_p * (h_{beam} - [SONARI]))] \rightarrow N_{ps} = + \frac{PP_s}{2}$$

Now, using the structural model is possible to determine the stresses in the six pylons and be able to choose the most stressed pylon, identifying the load combination that generates it.

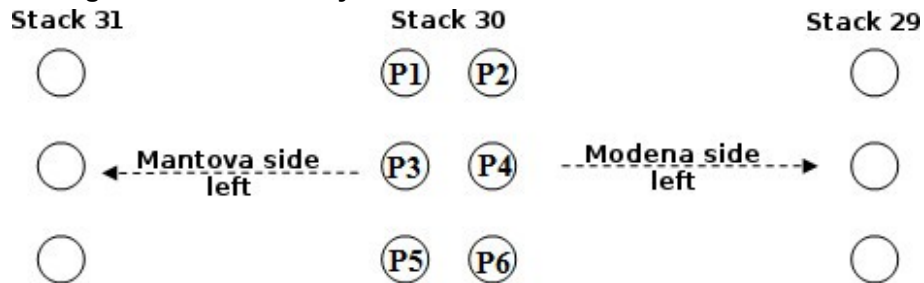
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## 9. Stress to the Level 4/Basis

### 9.1 Introduction

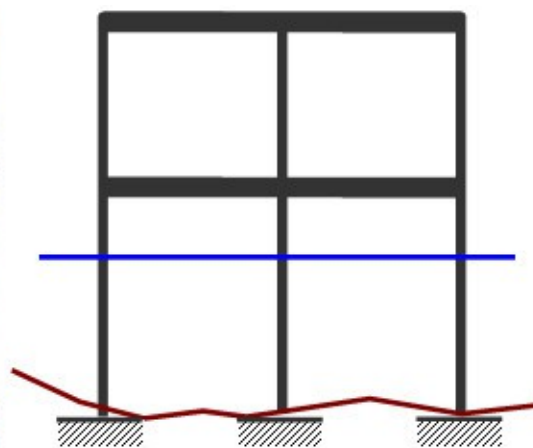
Before provide the formulas that allow to determine the stresses at the bases of the six pylons that compose the stack n.30, is needed to introduce some information and schemes.

### 9.2 Numbering of the Individual Pylon

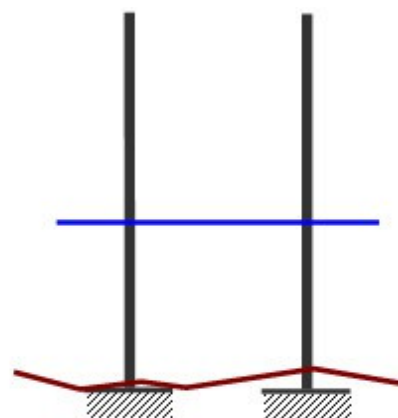


### 9.3 Introduction to the structural model

#### 9.3.1 Y Direction: flat frame

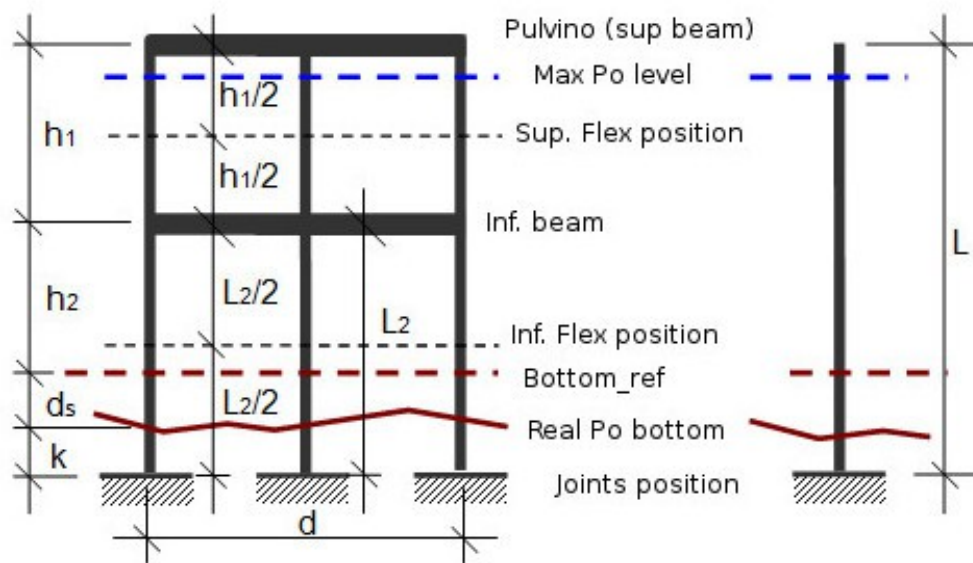


#### 9.3.2 X Direction



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#### 9.4 Geometry of the Structural Model (parameters from the parameters table)



(fig. 15)

Distance	Value	Notes
L	variable	Depends by $ds$
$L_2$	variable	Depends by $ds$
$h_1$	7.30 [m]	Parameter
$h_2$	7.50 [m]	Parameter
$(h_1)/2$	3.65 [m]	Parameter
$(L_2)/2$	variable	Depends by $ds$
$ds$	variable	Depends by the monitoring
$d$	8.5	Parameter (frame width)
$k$	0 [m]	Parameter (by hypothesis)

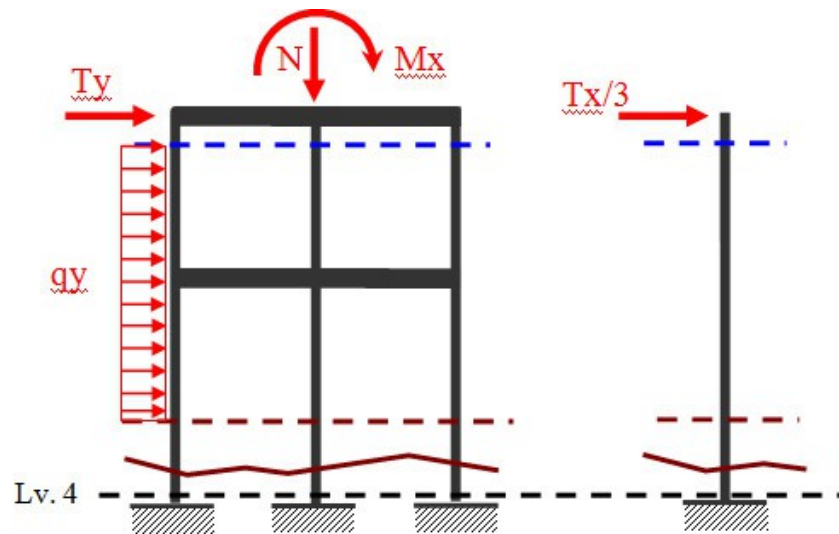
#### Notes:

The geometry provided in the pictures before, defined some distances that are present in the final formulas. All these parameters must be put into the parameters table.

The formulas reported below contain many parameters that up to day are set to zero (or to a default value) due to a lack of specific information.

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## 9.5 Summary of Kind of Forces Acting on the Frame



(fig. 16)

At this point the generic force is not more directly related to an external load (wind, water, traffic...), but at the sum of the all external forces contributions. Is reminded that the vertical force  $N$ , has not inside the pier weight.

All these forces are calculated and split in three parts for a single row, but is reminded that the two row are **not** loaded in the same way, so is needed to double the reasoning and the calculations during the implementation.

Last note is for **Level 4**: we'll use this call name to refer to the joints/base level of the pylons. So when we write *Level 4* we mean at joints /base level of the structure or the single pylon.

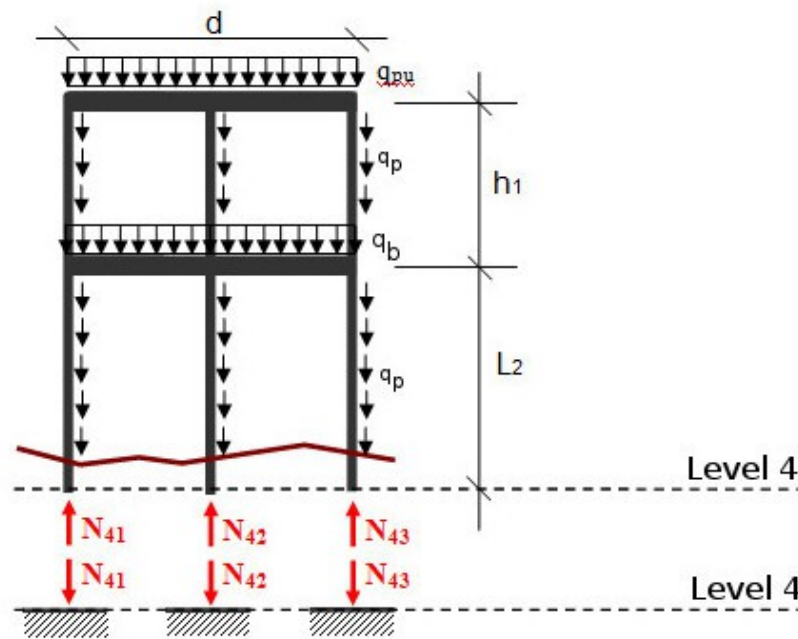
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## 9.6 Structure Weight

In the figure below are represented only the stack weight and how it is distributed; the pier weight is not an external load by definition, so we didn't unify it with the external load  $N$  even if acts in the same direction. For this reason we calculate this term separated by the external load  $N$ ; at the end of course we have to sum these two contributions, but is logical correct to kept these two terms separated until the end of calculations because mean different things.

The picture shows how the weight of the frame is distributed on itself. The weights of the pier split in pulvino weight ( $q_{pu}$ ), pylon weight ( $q_p$ ) and beam weight ( $q_b$ ); all these weight are “*weight/meter*”, so each weight has to be multiplied by the length on which it is distributed.

As said before, the section at the pylon base is named “**Level 4**” and we'll use this term to refer to the base of the pylon structure.



(fig. 17)

$$N_{41} = N_{42} = N_{43} = \frac{(q_{pu} + q_b) * d}{3} + q_p * (h_1 + L_2)$$

The weight of the truck stack ( $p_{ts}$ ) is equal to  $q_p * h_1$

The generic formula is the previous, but we have calculate that value yet before with this other formula:

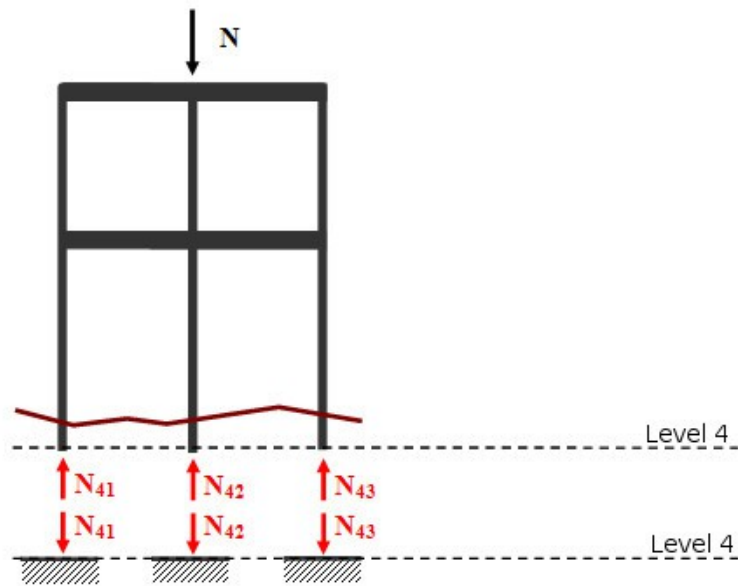
$$PP_s = [(2 * P_{pu} + 6 * P_{tp} + 2 * P_b) + 6 * (P_p * (h_{beam} - [SONAR]))]$$

So in own calculation flow process we calculate this value with the second formula that is specific for this structure.



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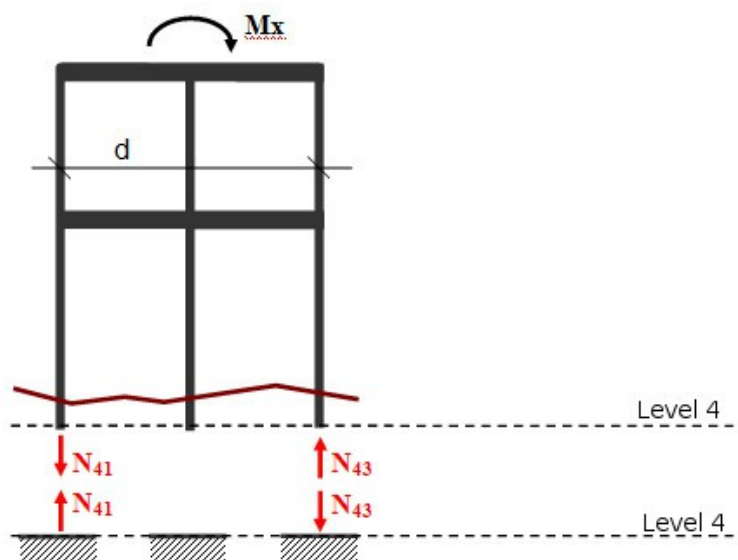
### 9.7 Vertical Load N



(fig. 18)

$$N_{41} = N_{42} = N_{43} = \frac{N}{3}$$

### 9.8 Bending Moment M



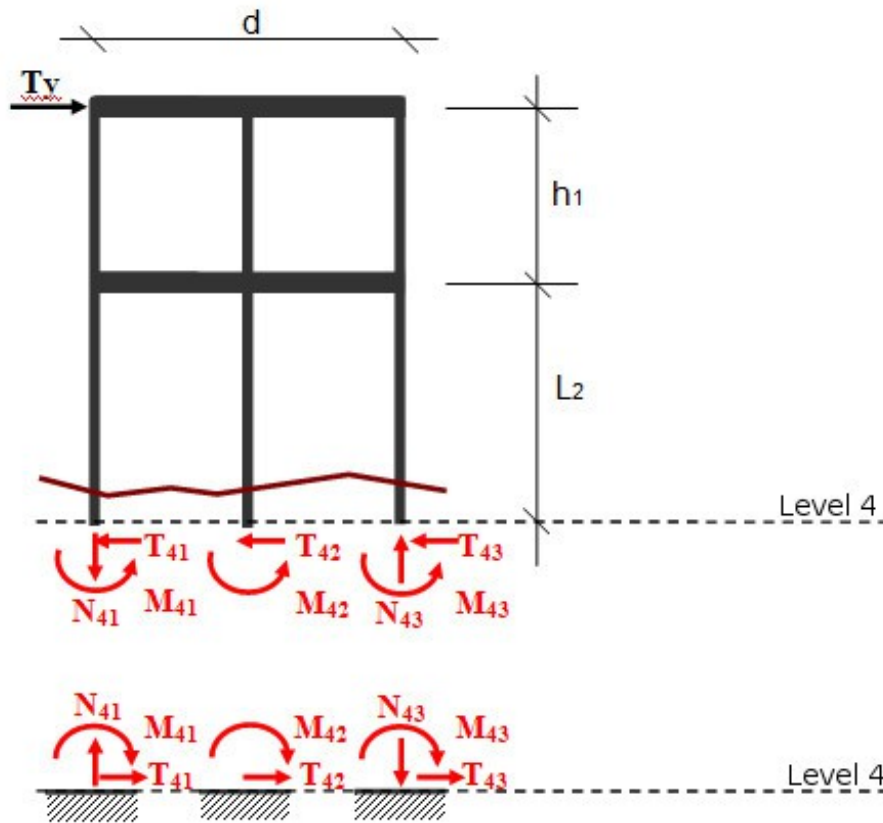
(fig. 19)

$$N_{41} = -N_{43} = \frac{M_x}{d}$$

$$N_{42} = 0$$

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### 9.9 Cutting Force $T_y$



(fig. 20)

$$N_{41} = -N_{43} = \left[ \frac{T_y}{d} \left( h_1 + \frac{L_2}{2} \right) \right]$$

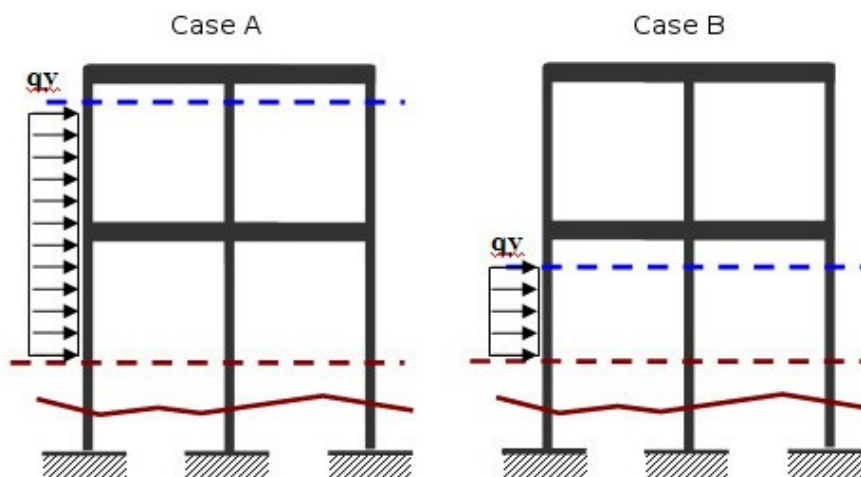
$$M_{41} = M_{42} = M_{43} = \frac{T_y * L_2}{6}$$

$$T_{41} = T_{42} = T_{43} = \frac{T_y}{3}$$

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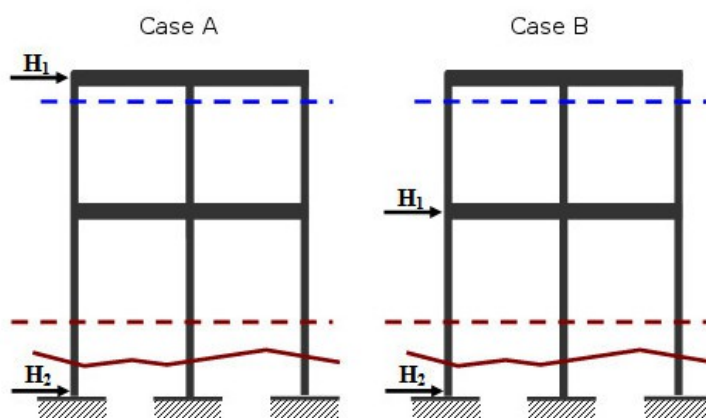
### 9.10 Distributed Load $qy$

This topic is not easy to discuss at the level 4, because the area of interest is variable since depends on the level of the river. For simplicity are evaluated only two cases: case A in which the level of the river is higher than the inferior beam and case B in which the level of the river is lesser than the inferior beam, like in the figure below.



(fig. 21)

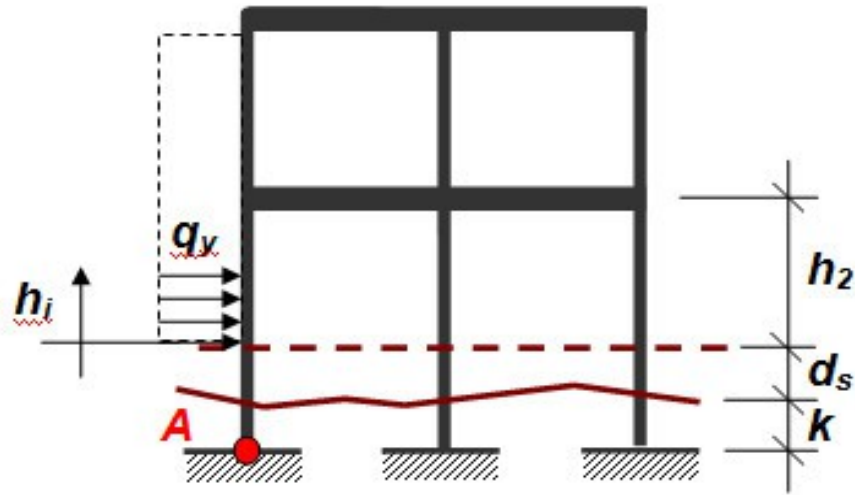
Later, is replaced the generic distributed load with a system of concentrated equivalent forces. For a better understanding, are reported the all steps to determine the equivalent concentrated forces.



(fig. 22)

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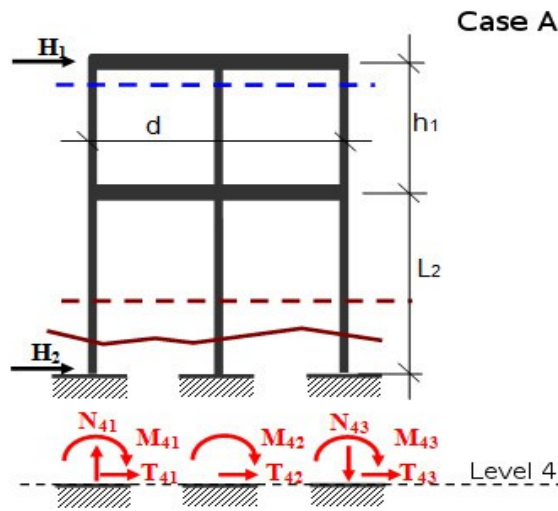
Once determined the resulting  $H$ , its moment is balanced respect at level 4 / base, point A fig23, with the component  $H_1$  that is the only component that generates a moment; the other component  $H_2$  is obtained by difference.



(fig. 23)

<i>Case A</i> $h_i \geq h_2$	<i>Case B</i> $h_i < h_2$
Calculation of the resulting $H$	
$H = q_y * h_i$	$H = q_y * h_i$
Calculation of the moment of $H$ , respect to point A	
$M_{(H)} = H * \left( \frac{h_i}{2} + d_s + k \right)$	$M_{(H)} = H * \left( \frac{h_i}{2} + d_s + k \right)$
Calculation of $H_1$ , equaling the moment of $H$	
$H_1 = \frac{M_{(H)}}{h_1 + L_2}$	$H_1 = \frac{M_{(H)}}{L_2}$
Calculation of $H_2$ by difference	
$H_2 = H - H_1$	$H_2 = H - H_1$

Even if the concentrated forces for both configurations have the same encoding ( $H_1$  and  $H_2$ ), their values are different, since derive from a different distribution of  $q_y$ .

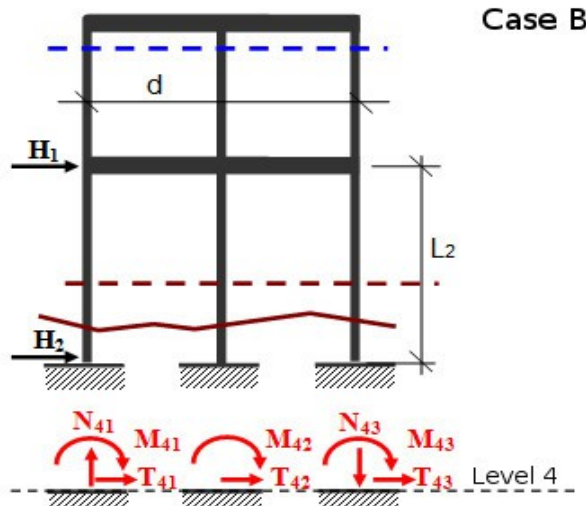


(fig. 24)

$$N_{41} = -N_{43} = \left[ \frac{H_1}{d} \left( h_1 + \frac{L_2}{2} \right) \right]$$

$$T_{41} = T_{42} = T_{43} = \frac{H_1 + H_2}{3}$$

$$M_{41} = M_{42} = M_{43} = \frac{H_1 L_2}{6}$$



(fig. 25)

$$N_{41} = -N_{43} = \frac{H_1 * L_2}{2d}$$

$$T_{41} = T_{42} = T_{43} = \frac{H_1 + H_2}{3}$$

$$M_{41} = M_{42} = M_{43} = \frac{H_1 L_2}{6}$$

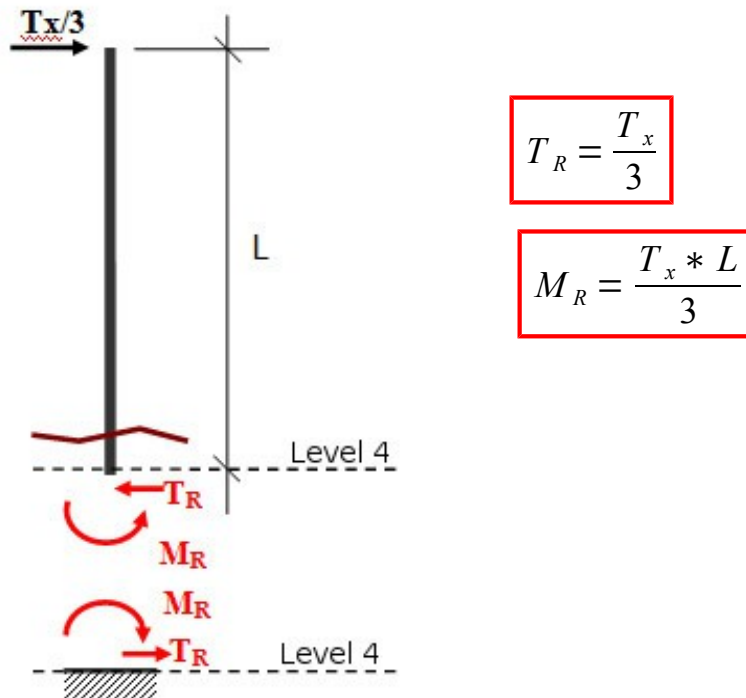
This note allow to define the case B as a particular case of case A: if the Po level was lower than the beam, the formula of the axial stress of case A should reset the h1 height. Next are identify the end formulas in their range of use.

	Case A ( $h_1 \geq h_2$ )	Case B ( $h_1 < h_2$ )
N	$N_{41} = -N_{43} = \left[ \frac{H_1}{d} \left( h_1 + \frac{L_2}{2} \right) \right]$	$N_{41} = -N_{43} = \frac{H_1 * L_2}{2d}$
T	$T_{41} = T_{42} = T_{43} = \frac{H_1 + H_2}{3}$	
M	$M_{41} = M_{42} = M_{43} = \frac{H_1 L_2}{6}$	

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### 9.11 Cutting Force Tx

The chassis subject to a force Tx, has a structural behaves like a “shelf”. The figure below defines the stresses that this Tx force make on the level 4. Remember that Tx/3 is the force that acts on the single pylon.



(fig. 26)

### 9.12 Superposition Principle

The stresses that each force generates at the level 4 can be simply added, determining the total stresses.

The representation of this process will be show separating the stresses at the level 4 and explaining this stress for each of the three pylons.

To be general, the formulas will be refer to the three pylons of the generic line not with the encoding of page 19 (fig. 12) but with the simple encoding of 1, 2 and 3. So the formulas are valid for both of the lines of the stack.

Moreover the generic stress will have a subscript that identify the direction (x or y) and the reference section, the number 4.

In the following tables, from 2 to 6 are defined respectively the stresses at the level 4: axial force N, cutting force Tx, cutting force Ty, bending moment Mx and bending moment My.

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### Axial stress N

	Pylon 1	Pylon 2	Pylon 3
P.P.	$N_4 = \frac{\left(\frac{P_s}{2}\right)}{3}$	$N_4 = \frac{\left(\frac{P_s}{2}\right)}{3}$	$N_4 = \frac{\left(\frac{P_s}{2}\right)}{3}$
N	$N_4 = -\frac{N}{3}$	$N_4 = -\frac{N}{3}$	$N_4 = -\frac{N}{3}$
Ty	$N_4 = -\left[\frac{T_y}{d}\left(h_1 + \frac{L_2}{2}\right)\right]$		$N_4 = \left[\frac{T_y}{d}\left(h_1 + \frac{L_2}{2}\right)\right]$
Mc	$N_4 = -\frac{M_x}{3}$		$N_4 = \frac{M_x}{3}$
qy	$N_4 = -\left[\frac{H_1}{d}\left(h_1 + \frac{L_2}{2}\right)\right]$		$N_4 = \left[\frac{H_1}{d}\left(h_1 + \frac{L_2}{2}\right)\right]$
Tx			

Tab.2: contributions of singles forces to the axial stress N

### Cutting force Tx

	Pylon 1	Pylon 2	Pylon 3
P.P.			
N			
Ty			
Mc			
qy			
Tx	$T_{x4} = \frac{Tx}{3}$	$T_{x4} = \frac{Tx}{3}$	$T_{x4} = \frac{Tx}{3}$

Tab.3: contributions of singles forces to the cutting action Tx

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### Cutting force Ty

	Pylon 1	Pylon 2	Pylon 3
P.P.			
N			
Ty	$T_{y4} = \frac{Ty}{3}$	$T_{y4} = \frac{Ty}{3}$	$T_{y4} = \frac{Ty}{3}$
Mc			
qy	$T_{y4} = \frac{q_y * h_i}{3}$	$T_{y4} = \frac{q_y * h_i}{3}$	$T_{y4} = \frac{q_y * h_i}{3}$
Tx			

Tab.4: contributions of singles forces to the cutting action Ty

### Blending stress Mx

	Pylon 1	Pylon 2	Pylon 3
P.P.			
N			
Ty	$M_{x4} = \frac{T_y * L_2}{6}$	$M_{x4} = \frac{T_y * L_2}{6}$	$M_{x4} = \frac{T_y * L_2}{6}$
Mc			
qy	$M_{x4} = \frac{H_1 * L_2}{6}$	$M_{x4} = \frac{H_1 * L_2}{6}$	$M_{x4} = \frac{H_1 * L_2}{6}$
Tx			

Tab.5: contributions of singles forces to the stress Mx



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### Blending stress $M_y$

	Pylon 1	Pylon 2	Pylon 3
<b>P.P.</b>			
<b>N</b>			
<b>Ty</b>			
<b>Mc</b>			
<b>qy</b>			
<b>Tx</b>	$M_{y^4} = \frac{T_x * L}{3}$	$M_{y^4} = \frac{T_x * L}{3}$	$M_{y^4} = \frac{T_x * L}{3}$

Tab.6: contributions of singles forces to the stress  $M_y$

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## 10. Verification “Pressoflessione”

**Pressoflessione:** combined compression and bending

### 10.1 M-N Domain

#### 10.1.1 Parameter Data

External radius	75	cm
Internal radius	0	cm
Number of identical bars	12	--
Bars diameter	2,4	cm
Barycentric concrete cover	4,2	cm
Steel class	FeB44K	--
Concrete class	C25/30	--

tab. 7

These are other parameters (tab. 7) to add at the parameters tables in the DB. This parameters are used to calculate the M-N domains and is not important how is the calculation because we receive directly the table with the values to can draw the domain graph/graphs.

The value M of a pylon is easily calculated with:  $M = \sqrt{Mx^2 + My^2}$

The idea is that each pylon has at the end 2 resulting forces: N and M. Then we can “put” each pylon into the graph to see if the pylon is in or not into the domain. If the pylon is in, the pylon is “ok”, but if the pylon is out it is in a very dangerous situation from a structural point of view.

So, pylon in → ok, pylon out → danger.

The safety factor (critical factor) is the expression of the pylon position into the domain, I mean that a pylon close to the axes origin represents a minor dangerous situation than a pylon that still is in the domain but is close to the domain bound because with a little variations of the conditions this pylon could cross the domain border and transforms in a dangerous situations.

So, the safety factor is a value that represents this “proximity” to the domain bounds, more a pylon is close to the domain bound more dangerous is the situation.

However, the calculation of this “proximity” is not an easy calculation and we proceed with two way in parallel:

1. Approximation thought linearization of the proximity
2. Representations of the six pylons of the worst load combination selected with the approximation at previews point, into the M-N domain as the EU 305/2011 Regulation requires.

The following table (tab.8) contains the values that describe the M-N domain, and also these values have to be stored into the db, maybe in another table. In this way also the View part can reads these value to be able to plot them.

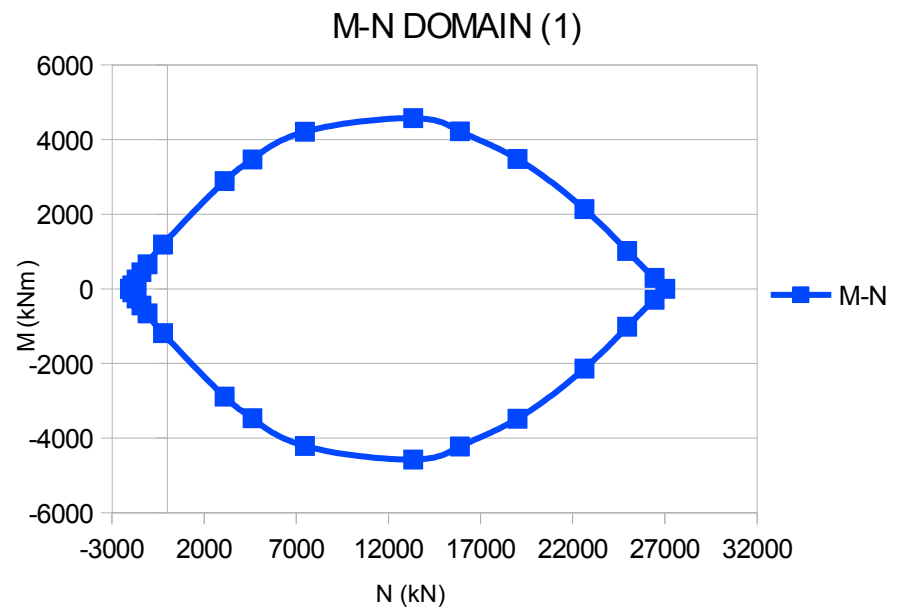
Into graph M-N DOMAIN (1) is represented the more simple M-N domain with the values in tables, but we could add other M-N domain into DB to define different work areas of the structure. For instance the other graph M-N DOMAIN (2) represents two different domains: into the pink one all is “ok”, between pink and blue → “attention” and then if out of blue → “fast reaction or good bye bridge”.

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### 10.1.2 M-N Domain Values

Point	N1 (kN)	M1 (kNm)
1	-2029,78	0
2	-1895,17	96,4807
3	-1673,87	254,95
4	-1401,65	446,55
5	-1078,88	660,403
6	-241,319	1188,31
7	3104,27	2887,33
8	4622,78	3468,79
9	7466,71	4210,28
10	13342,2	4572,35
11	15880,5	4222,35
12	18998,7	3480,02
13	22632,8	2136,98
14	24958,6	1016,27
15	26441	293,541
16	27023	0
17	26441	-293,541
18	24958,6	-1016,27
19	22632,8	-2136,98
20	18998,7	-3480,02
21	15880,5	-4222,35
22	13342,2	-4572,35
23	7466,71	-4210,28
24	4622,78	-3468,79
25	3104,27	-2887,33
26	-241,319	-1188,31
27	-1078,88	-660,403
28	-1401,65	-446,55
29	-1673,87	-254,95
30	-1895,17	-96,4807
31	-2029,78	0

Tab.8



**Observation:** we don't know the formulas to calculate the domain values.

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### 10.1.3 M-N Domain Table

The M-N domain table in the database has this schema:

*m\_n\_domain*

Field	Type	Null	Key	Default	Extra
ID	int(10)	NO	PRI	NULL	auto_increment
N	float	NO		NULL	
M	float	NO		NULL	

## 10.2 New tables in the DB

### 10.2.1 Tables of “Grouped Data”

sensor\_data\_10\_min /sensor\_data\_1\_hour /sensor\_data\_1\_day

Field	Type	Null	Key	Default	Extra
ID	int(10)	NO	PRI	NULL	auto_increment
wind_speed	float	NO		NULL	
wind_direction	float	NO		NULL	
wind_speed_max	float	NO		NULL	
wind_direction_max	float	NO		NULL	
hydrometer	float	NO		NULL	
hydrometer_variance	float	NO		NULL	
sonar	float	NO		NULL	
sonar_variance	float	NO		NULL	
sonar_perc_correct	float	NO		NULL	
sonar_perc_wrong	float	NO		NULL	
sonar_perc_outOfWater	float	NO		NULL	
sonar_perc_error	float	NO		NULL	
sonar_perc_uncertain	float	NO		NULL	
safety_factor_00	float	NO		NULL	
stressed_pylon_00	int	NO		NULL	
safety_factor_01	float	NO		NULL	
stressed_pylon_01	int	NO		NULL	
safety_factor_10	float	NO		NULL	
stressed_pylon_10	int	NO		NULL	
safety_factor_11	float	NO		NULL	
stressed_pylon_11	int	NO		NULL	
water_speed	float	NO		NULL	
water_flow_rate	float	NO		NULL	
timestamp	timestamp	NO		CURRENT_TIMESTAMP	on update CURRENT_TIMESTAMP

- In these tables are stored the information about the safety factor in the whole four traffic combinations, so 00, 01, 10 and 11. For the web view this four columns are used to show the critical factor related to what the user has selected on the checkbox. These four columns are also used in the historical page, to show the trend of the safety factor in time
- The columns “*water speed*” and “*water flow rate*” are requested from the customer because can be useful to the engineers know those values
- To be able to represent this kind of information about the situation of the pylons we have to do a more general situation for each traffic combination; below is explained it.

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### 10.2.2 Tables of “Worst Case”

worst\_case\_00 / worst\_case\_01 / worst\_case\_10 / worst\_case\_11

Field	Type	Null	Key	Default	Extra
ID	int(10)	NO	PRI	NULL	auto_increment
pylon_number	int	NO		NULL	
N	float	NO		NULL	
Tx	float	NO		NULL	
Ty	float	NO		NULL	
Mx	float	NO		NULL	
My	float	NO		NULL	
M	float	NO		NULL	
cs	float	NO		NULL	
comb_number	float	NO		NULL	
timestamp	timestamp	NO		CURRENT_TIMESTAMP	on update CURRENT_TIMESTAMP

In these four tables are stored the information about the worst case for each pylon for each kind of combination.

This means that in the table “*worst\_case\_00*” there are the information about all the six pylons, one pylon per row.

In each row there is stored the information on the forces acting on that pylon in its worst case between the whole combination of kind 00 (there is only one combo for type 00 and 01, but the idea and the algorithm are the same).

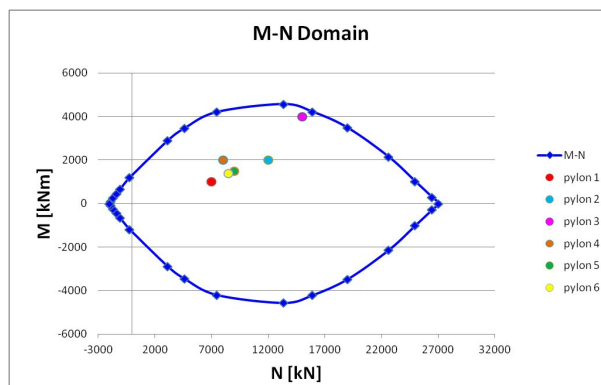
Then are stored the c.s. (safety factor) and the combo number that generate that c.s.

These tables have to be used into the view part, in this simple way: each row of a table represents the information about the worst situation of each pylon in this specific combination and the columns “*N*” and “*M*” are the coordinates of the specific pylon into the ***M-N Domain*** (see chapt. 9.1), so the view part can use these data to represent all the six pylons into the M-N Domain graph for the specific combination of *T-D* user selection.

In the same way the view changes the showed safety factor value based on the selection of T-D checkbox, the view should change the M-N Domain graph based on this selection and read coordinates from the correct table of worst case.

In each table of worst case should be stored only the last useful data about pylons situation so the respective dao object used by the view module, has to do only a select \* from the correct table and then the view module has just to show in the graph the pylons (example in fig. 27).

The following picture is an example of what the user should see on the current state view page relative at the M-N domain and pylons situation.



(fig. 27)

To draw the M-N domain has to be use the value into the M-N table into the database.

For the M-N domain information see the previous chapt. 9.1 on the M-N Domain.

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### 10.3 Table of Parameters

GEOMETRY OF THE STACK N.30			
$D_{pylon}$	1.5	m	Diameter of the pylon
$C_{span}$	9.5	m	Distance between two line of pylon
$h_{beam}$	17.5	m	Height of the lower beam
$bottom\_ref$	10	m	Height of the reference of the bottom of the river
$h1$	7.3	m	Distance between the pulvino and the inferior beam
$h2$	7.5	m	Distance between the inferior beam and the bottom_ref
$(h1)/2$	3.65	m	Mean value of h1
$k$	0	m	Sinking of the bases over the ground
$d$	8.5	m	Width of the chassis
$R_{pylon}$	0	m	Internal radius
$numb\_id\_bar$	12	--	Number of identical bars
$D_{bar}$	0,024	m	Bars diameter
$C_{cb}$	0,042	m	Barycentric concrete cover
$Steel\_class$	FeB44K	--	Steel class
$Concrete\_class$	C25/30	--	Concrete class
WIND THRUST			
$\alpha$	6	°	Planimetric anticlockwise inclination of the bridge form the north
$C_{Dwi}$	2	-	“Drag planking” coefficient
$\rho_{air}$	1.2	Kg/m <sup>3</sup>	Air density
$A_{stack}$	168	m <sup>2</sup>	Planking area exposed to the wind pressure
$A_{traf}$	177	m <sup>2</sup>	Surface of traffic exposed to the wind pressure
$\beta_1$	1	-	Coefficient of reduction for A1 and A2 traffic scenarios
$\beta_2$	0.5	-	Coefficient of reduction for A3 traffic scenario
$r$	2.25	m	Thrust center due to longitudinal asymmetry, only of $S_{Vplank}$
$e_{plank}$	1.91	m	“arm” for bending moment of $S_{Vplank}$
$e_{traf}$	3.41	m	“arm” for bending moment of $S_{Vtraf}$
HYDRODYNAMIC THRUST			
$C_{D0wa}$	2.4	-	“Drag planking” coefficient (D=0)
$C_{D1wa}$	2	-	“Drag planking” coefficient (D=1)
$\rho_{water}$	1000	Kg/m <sup>3</sup>	Water density
$\beta_A$	0.5	-	Area reduction for D=1
$a$	-0.0014	-	Coefficient for the relation $V_{water}([IDRO1])$
$b$	0.0341	-	Coefficient for the relation $V_{water}([IDRO1])$
$c$	0.052	-	Coefficient for the relation $V_{water}([IDRO1])$

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<b>h<sub>water1</sub></b>	17	m	Height limit of the river for parameters a1,b1,c1
<b>a1</b>	46	-	Coefficient for Q(h) when [IDRO1] < h <sub>water1</sub>
<b>b1</b>	-902	-	Coefficient for Q(h) when [IDRO1] < h <sub>water1</sub>
<b>c1</b>	4658	-	Coefficient for Q(h) when [IDRO1] < h <sub>water1</sub>
<b>h<sub>water2</sub></b>	22	m	Height limit of the river for parameters a2,b2,c2
<b>a2</b>	60	-	Coefficient for Q(h) when [IDRO1] < h <sub>water2</sub>
<b>b2</b>	-1350	-	Coefficient for Q(h) when [IDRO1] < h <sub>water2</sub>
<b>c2</b>	8000	-	Coefficient for Q(h) when [IDRO1] < h <sub>water2</sub>
<b>h<sub>max</sub></b>	25.3	m	Max height level of river and limit for use parameter a3,b3,c3
<b>a3</b>	96		Coefficient for Q(h) when h <sub>water2</sub> < [IDRO1] < h <sub>max</sub>
<b>b3</b>	-2800		Coefficient for Q(h) when h <sub>water2</sub> < [IDRO1] < h <sub>max</sub>
<b>c3</b>	22500		Coefficient for Q(h) when h <sub>water2</sub> < [IDRO1] < h <sub>max</sub>
<b>WEIGHT OF THE STACK</b>			
<b>Pp</b>	10710	kN	Plank weight on the stack
<b>Ppu</b>	1680	kN	Weight of single pulvino
<b>Ptp</b>	1601	kN	Weight of the trunk of pylon
<b>Pb</b>	1007	kN	Weight of the single beam
<b>Ppy</b>	44	kN/m	Weight per meter of pylon
<b>Mt</b>	9720	kNm	Moment generated by asymmetry
<b>MOBILE WEIGHTS</b>			
<b>N(A1)</b>	4024	kN	Axial load for load combination A1
<b>Mxx(A1)</b>	4368	kNm	Bending moment for load combination A1
<b>Myy(A1)</b>	3908	kNm	Bending moment for load combination A1
<b>N(A2)</b>	3116	kN	Axial load for load combination A2
<b>Mxx(A2)</b>	8077	kNm	Bending moment for load combination A2
<b>Myy(A2)</b>	3015	kNm	Bending moment for load combination A2
<b>N(A3)</b>	1979	kN	Axial load for load combination A3
<b>Mxx(A3)</b>	2121	kNm	Bending moment for load combination A3
<b>Myy(A3)</b>	25756	kNm	Bending moment for load combination A3
<b>Vehicle braking</b>			
<b>F<sub>r</sub></b>	206	kN	Value of the force due to the vehicle braking
<b>n</b>	3.3	m	“arm” for the vehicle braking moment