

Seminar 6: Advanced SPIN

Non-deterministic Algorithms, Model Extraction

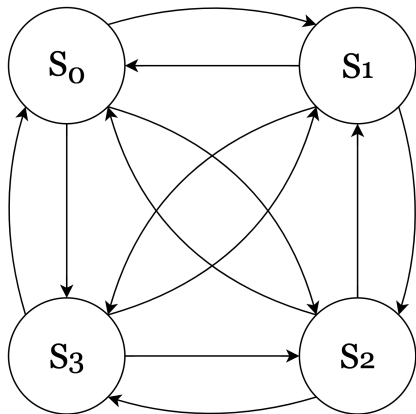
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TSP

Travelling Salesman Problem



	0	1	2	3
0	-	7	9	2
1	4	-	3	7
2	6	7	-	8
3	2	3	8	-

Promela

Ruys & Holzmann (2004): *Advanced SPIN Tutorial*

- Single process looking for a path
- Variable cost to hold the path cost so far.
- From a state we jump **non-deterministically** to another state **not yet visited**.

Promela

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- Single process looking for a path
- Variable cost to hold the path cost so far.
- From a state we jump **non-deterministically** to another state **not yet visited**.

```
bit visited[4];
int cost;

active proctype TSP()
{
S0:  atomic {
      if
      :: !visited[3] -> cost = cost+2; goto S3;
      :: !visited[1] -> cost = cost+7; goto S1;
      :: !visited[2] -> cost = cost+9; goto S2;
      fi;
    }
S1:  atomic {
      visited[1] = true;
      if
      :: !visited[2] -> cost = cost+3; goto S2;
      :: !visited[3] -> cost = cost+7; goto S3;
      :: else        -> cost = cost+4; goto end;
      fi;
    }
    // ...
end: skip;
}
```

Find a solution

[Ruys & Brinksma - TACAS 1998]

- We can use SPIN model checking to find the **lower bound** for the variable cost.
- We will verify *iteratively*:
 - ① $\Diamond(\text{cost} \geq 1000)$
 - The counterexample will be a path shorter than 1000.
 - Ex. a path with cost 20.
 - ② $\Diamond(\text{cost} \geq 20)$
 - Ex. a path with cost 14
 - ③ $\Diamond(\text{cost} \geq 14)$
 - Satisfied

Find a solution

[Ruys & Brinksma - TACAS 1998]

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Algorithm Find Min Cost

```
1:  $min :=$  guess of maximum cost
2:  $error :=$  true
3: while  $error$  do
4:   Verify  $\mathcal{M} \models \Diamond(\text{cost} \geq min)$ 
5:   if  $error$  then
6:      $min :=$  cost
7:   end if
8: end while
```

Optimization

- Model Checkers are already being used for serious optimization problems.
- Although the original idea works, it is **inefficient**
 - The state space already contains the optimal solution.
 - Iteratively checking $\diamond(\text{cost} \geq \text{min})$ is not needed.
- With *SPIN*'s **on-the-fly** model checking we won't explore the whole state space
 - We can save the best path found in the past for future checks

- We can implement C code inside our Promela model!
 - ① `c_expr`: executes a C expression and can return a value to the model.
 - ② `c_code`: executes C code as an atomic statement
 - ③ `c_state`: can be used to track memory, holding state information

C code (2)

Ruys & Holzmann (2004): *Advanced SPIN Tutorial*

- In the declaration of the model we can add:
c_state "int min_cost" "Hidden" "1000"
- at the **end** label we can add:

```
c_code {  
    if(now.cost < min_cost) {  
        min_cost = now.cost;  
    }  
}
```

C code (3)

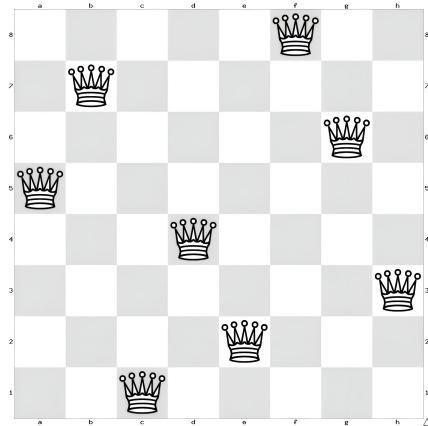
Ruys & Holzmann (2004): *Advanced SPIN Tutorial*

- At the beginning of each state ***Si***:

```
Si: atomic {  
    visited[i] = true;  
    if  
    :: c_expr { now.cost > min_cost } -> goto end;  
    :: else -> skip;  
    fi;  
  
    if  
    :: !visited[1] -> cost = ... ; goto S1;  
    :: ...  
    :: else -> cost = ... ; goto end;  
    fi;  
}
```

8-Queens

8-Queens Problem



Promela

Ben-Ari (2008): *Principles of the SPIN Model Checker*

- ① **Non-deterministically** choose a row for each Queen
- ② Check if the placement is valid
- ③ If it isn't, the run gets **stuck**
 - All the traces that get to the **end** are valid solutions
- ④ The solution will be the counterexample of:
`ltl sol {<> !(Queens@end)};`

Promela

Ben-Ari (2008): *Principles of the SPIN Model Checker*

- 1 **Non-deterministically** choose a row for each Queen
- 2 Check if the placement is valid
- 3 If it isn't, the run gets **stuck**
 - All the traces that get to the **end** are valid solutions
- 4 The solution will be the counterexample of:
`ltl sol {<> !(Queens@end)};`

```
byte result[8]; // queens placement
bool a[8];      // row
bool b[15];     // diagonal of type \
bool c[15];     // diagonal of type /

active proctype Queens()
{
    byte col = 1;
    byte i = 0;
    byte row;
    do
        :: Choose(row);
           !a[row-1];
           !b[row+col-2];
           !c[row-col+7];
           a[row-1] = true;
           b[row+col-2] = true;
           c[row-col+7] = true;
           result[col-1] = row;
           if
               :: (col >= 8) -> break;
               :: else -> col++;
           fi;
        od;
    end: skip;
}
```

Generate a **random** number

Ben-Ari (2008): *Principles of the SPIN Model Checker*

- *SPIN* does not support Real numbers
- When model checking, we will check **every possible choice**
 - We only need randomness when during **simulations**
- We can use **non-determinism** to decide whether to increment or not the number
 - Within **bounds**.

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- We can use **non-determinism** to decide whether to increment or not the number
 - Within **bounds**.

```
inline Choose(row)
{
    row = 1; // min
    do      // max
    :: (row < 8) -> row++;
    :: break;
od;
}
```

Model Extraction

Motivation

Holzmann (2001): *From Code to Models*

Classical approach: write model manually given (prelim.) system design

- Difficult for evolving systems: model may not match anymore
- Writing model manually is complex (similar to programming)
- Cannot detect errors introduced in implementation
- Unclear rules to derive abstraction from concrete systems
- Low expressiveness of modelling languages \implies can be huge

Idea

Holzmann (2001): *From Code to Models*

Idea: derive model from concrete implementation

- How much semantic details to keep?
- How to keep model size manageable?
- Finite model from program?
- How to keep verification context while implementation evolves?

Observation: a C program's control structure is finite

Also, it can be mechanically transferred to Promela

Data is the main problem (say, 64-bit long)

Verification Context

Holzmann (2001): *From Code to Models*

Verification Context = Test Drivers + Native Code + Instrumented Code

Test Drivers: user-written Promela, implements environment

Native Code: C code that is not extracted, merely embedded into Promela
(c_code, ...)

Instrumented Code: C code extracted to Promela

Extraction is guided by optional *replacement rules/filters*.

Only thread operations *need* filter rules (“this call creates a new process”).

Handshaking Example

Holzmann (2001): *From Code to Models*

```
extern const int p0; enum msg_type { Msg, Ack, TimeOut };

void handshake(void) {
    send(p0, Msg);
    set_timer(16000); /* msec */
    int resp = wait_recv();
    switch (resp) {
    case Ack:      reset_timer(); break;
    case TimeOut: /* handle */ break;
    default: reset_timer(); error("meh"); break;
    }
}
```

Timer

Holzmann (2001): *From Code to Models*

Timer process can be modelled in Promela

Problem: Integer variable \implies huge state space

Observation: we only care about nonzero (timer ticking) vs zero (timeout)!

Improved Timer

Holzmann (2001): *From Code to Models*

```
chan timer = [0] of { mtype, chan, int };

mtype = { Msg, Ack, Other, Set, Reset, TimeOut };

active proctype timer_p()
{ chan who = 0;
  do
    :: timer?Set(who,_)
    :: timer?Reset(who,_)
    :: who != 0 -> who!TimeOut
  od
}
```


Handshake (raw extraction)

Holzmann (2001): *From Code to Models*

```
active proctype handshake() { int resp;  
    c_code { send(now.p0,Msg); };  
    c_code { set_timer(16000); };  
    c_code { Phandshake->resp=wait_recv(); };  
    do  
        :: c_expr{ Ack == Phandshake->resp };  
            c_code { reset_timer(); };  
            break; goto C_0  
    [...]  
    od;  
}
```

Replacement Rules Table

Holzmann (2001): *From Code to Models*

<code>set_timer(16000)</code>	<code>timer!Set(q0,16000)</code>
<code>reset_timer()</code>	<code>timer!Reset(q0,0)</code>
<code>send(p0,Msg)</code>	<code>p0!Msg</code>
<code>resp=wait_recv()</code>	<code>q0?resp</code>
<code>error(. . .)</code>	<code>assert(false)</code>

Handshake (using rules)

Holzmann (2001): *From Code to Models*

```
active proctype handshake() {  
    int resp;  
    p0!Msg;  
    timer!Set(q0,16000);  
    q0?resp;  
    do  
        :: c_expr {Ack == Phandshake->resp};  
            timer!Reset(q0,0);  
            break; goto C_0  
    [...]  
    od;  
}
```

Previous paper, as primer: FeaVer model extractor

Modex is a similar tool

Packages test harness in a single .prx file

Composed of sections and commands such as

```
%P
```

```
<Promela code>
```

```
%%
```

```
%X <C function name to extract>
```

Fin.