

# Introduction to NuSMV

Di Marco, Okwieka



# Getting Started

# Set up NuSMV

NuSMV has binary releases for Linux (libc6), Mac OS X and Windows

They work out of the box, just extract the archive!

Run `./bin/NuSMV -int <model (.smv)>`

# Set up NuSMV

We also provide a Docker container for Linux based on Alpine.

Call `./build-docker` to build the image, `./nusmv` to open the container shell.

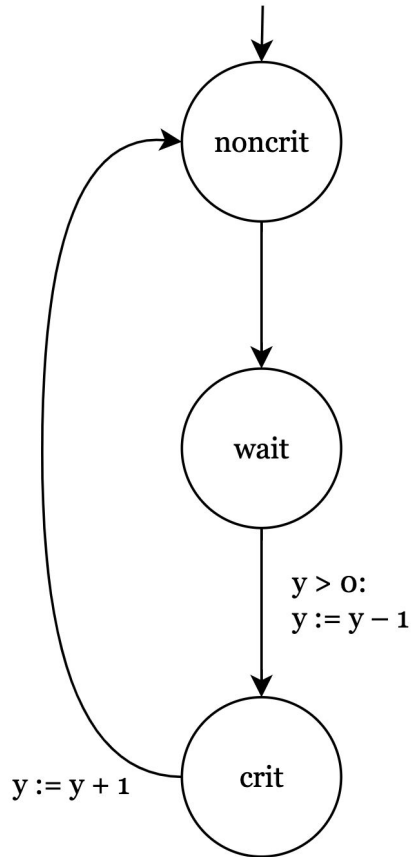
NuSMV Model files (.smv) in `./models` are bind-mounted to `/models` in container.

# Run NuSMV

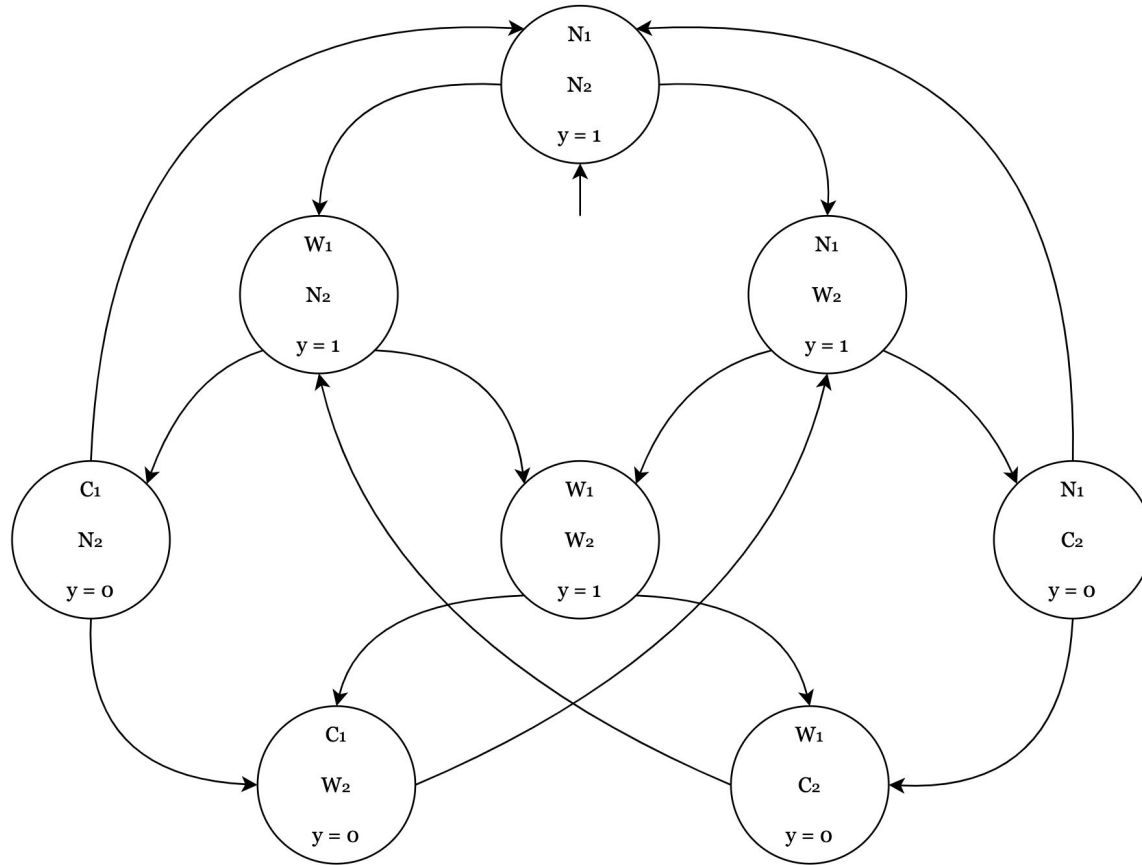
1. Start: `NuSMV -int <file>`
2. Build the model and BDDs: `go`

# Modeling

# A Simple Mutual Exclusion Model

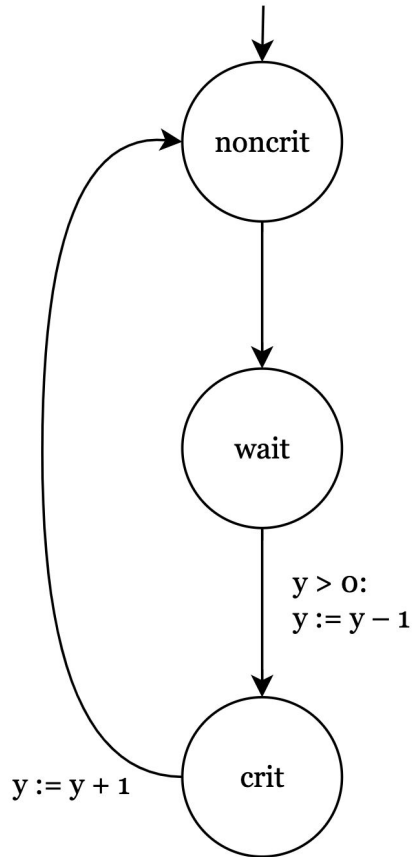


# A Simple Mutual Exclusion Model



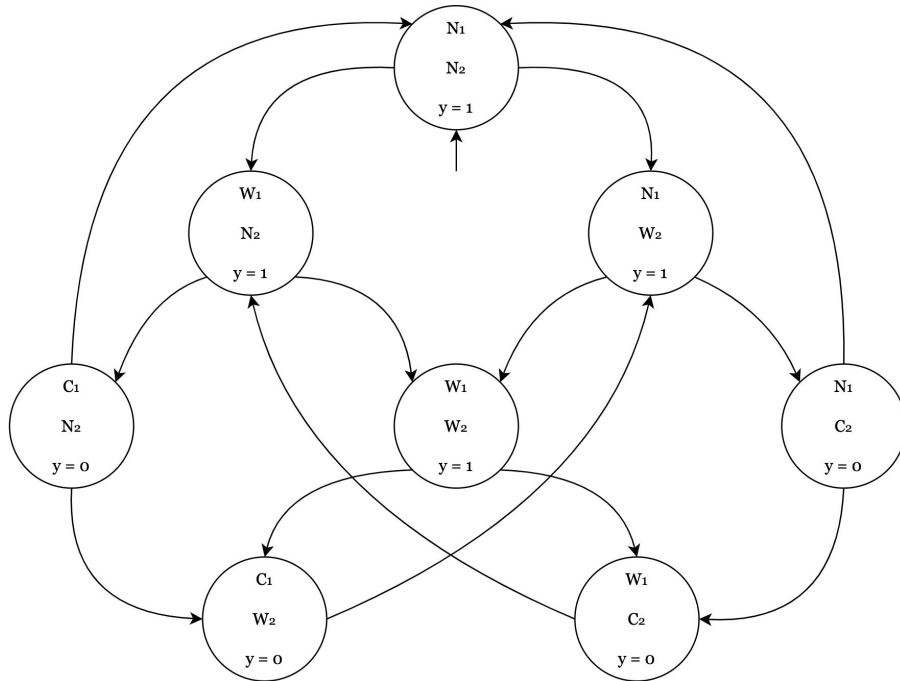


# A Simple Mutual Exclusion Model



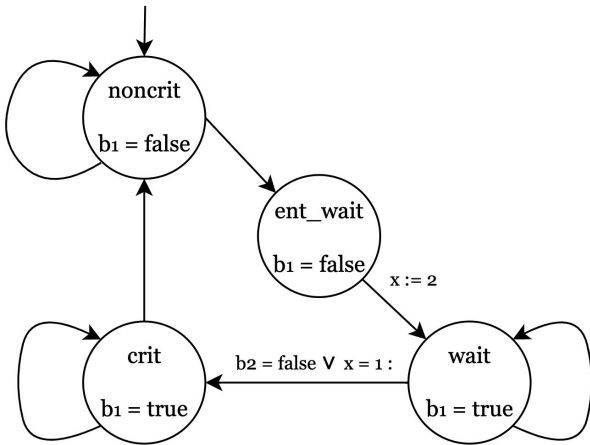
```
MODULE pg(y)
VAR
  state : { noncrit, wait, crit };
ASSIGN
  init(state) := noncrit;
  next(state) := case
    (state = noncrit)           : wait;
    (state = wait) & (y>0)      : crit;
    (state = crit)             : noncrit;
    TRUE                        : state;
  esac;
  next(y) := case
    (state = wait) & (y>0)      : y - 1;
    (state = crit) & (y<2)      : y + 1;
    TRUE                        : y;
  esac;
```

# A Simple Mutual Exclusion Model

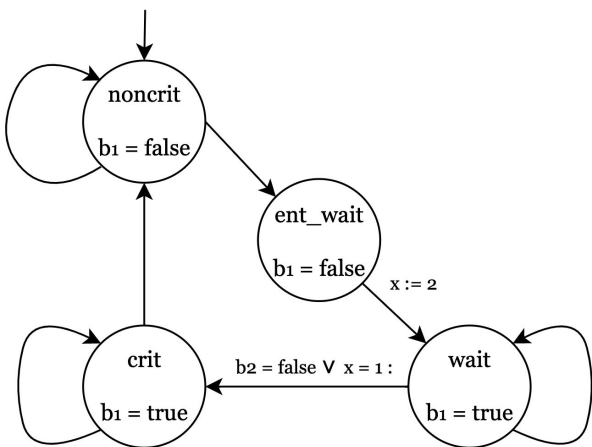


```
MODULE main
VAR
    y : 0 .. 2;
    pg1 : process pg(y);
    pg2 : process pg(y);
ASSIGN
    init(y) := 1;
```

# Peterson's Algorithm



# Peterson's Algorithm



```

MODULE peterson(id, x, other_b)
VAR
    state : { noncrit, entering_wait, wait, crit };
ASSIGN
    init(state) := noncrit;
    next(state) := case
        (state = noncrit)           : { noncrit,
                                         entering_wait };
        (state = entering_wait)     : wait;
        (state = wait)
            & ((id = x) | !(other_b)) : { wait, crit };
        (state = crit)              : { crit, noncrit };
    TRUE                             : state;
    esac;
DEFINE
    b := (state = wait) | (state = crit);
  
```

# Peterson's Algorithm

```
MODULE main
VAR
    x    : 1 .. 2;
    pg1  : peterson(1, x, pg2.b);
    pg2  : peterson(2, x, pg1.b);
ASSIGN
    next(x) := case
        (pg1.state = entering_wait) : 2;
        (pg2.state = entering_wait) : 1;
        TRUE                         : x;
    esac;
```

# Simulation

# Simulation

Simulation generates (finite) traces, which are numbered

States of a trace also numbered and labelled

**<Trace Number>.<State Number>**

e.g. **1.42**, **1.43**, **1.44**, ...

Retained in memory during session

Can go to earlier state and branch off new traces

→ Tree shape

# Simulation

Three different modes for choosing the next state

- ❖ **Deterministic**: first in set of possible states
- ❖ **Random**: nondeterministic
- ❖ **Interactive**: user chooses

What if there are too many options in interactive mode?

→ User specifies constraint formula *only for that choice*



# Simulation

Overall process:

1. Pick initial state: `pick_state -r` OR `pick_state -i`  
OR continue from another trace: `goto_state <state label>`
2. Simulate k steps:

`simulate -k <k> -r` OR `-i`

3. Display trace fragment:

`show_traces <trace number>[.from:to]`

Both `pick_state` and `simulate` take the `-c` “constraint” option.

---

# Simulation

(CLI Example of Tic-Tac-Toe Model)

# Temporal Logic

# CTL in NuSMV

NuSMV	English
AG $p$	Always Globally $p$
EG $p$	Exists Globally $p$
AF $p$	Always Future $p$
EF $p$	Exists Future $p$
AX $p$	Always Next $p$
EX $p$	Exists Next $p$
A [ $p$ U $q$ ]	Always $p$ Until $q$
E [ $p$ U $q$ ]	Exists $p$ Until $q$

# LTl in NuSMV

NuSMV	English
$G\ p$	Globally $p$
$F\ p$	Future $p$
$X\ p$	Next $p$
$p\ U\ q$	$p$ Until $q$

# Past Temporal Operators

NuSMV	English	Definition	Past version of...
$H\ p$	Historically $p$	$p$ holds always in <u>all</u> past states	Globally (G)
$O\ p$	Once $p$	$p$ holds in <u>at least one</u> state in the past	Future (F)
$Y\ p$	Yesterday $p$	$p$ holds in the previous state	Next (X)
$p\ S\ q$	$p$ Since $q$	$p$ holds up to some states in the past and then $H\ q$ holds.	Until (U)

# Model Checking

# Safety properties

*“it is never the case that both processes are in the critical section at the same time”*

$$\mathbf{G} \neg (crit_1 \wedge crit_2)$$



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# Safety properties

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LTLSPEC  $\mathbf{G} \neg (pg1.state = crit \ \& \ pg2.state = crit)$

```
> read_model -i peterson.smv  
> go  
> process_model
```

# Safety properties

*“it is never the case that both processes are in the critical section at the same time”*

$$\mathbf{G} \neg (crit_1 \wedge crit_2)$$

```
LTLSPEC G !(pg1.state = crit & pg2.state = crit)
```

```
> read_model -i peterson.smv  
> go  
> process_model
```

```
-- specification G !(pg1.state = crit & pg2.state = crit) is  
true
```

# Liveness properties

*“Both processes get into the critical section infinitely often”*

$$\mathbf{GF} \text{ crit}_1 \wedge \mathbf{GF} \text{ crit}_2$$

**LTLSPEC**  $G ( F (\text{pg1.state} = \text{crit})) \ \& \ G ( F (\text{pg2.state} = \text{crit}))$

# Counterexamples

```
-- specification (G (F pg1.state = crit) & G (F pg2.state = crit)) is
false
-- as demonstrated by the following execution sequence
Trace Description: LTL Counterexample
Trace Type: Counterexample
  -- Loop starts here
  -> State: 1.1 <-
    x = 1
    pg1.state = noncrit
    pg2.state = noncrit
    pg1.b = FALSE
    pg2.b = FALSE
  -> State: 1.2 <-
```

# Fairness

FAIRNESS

pg1.state = crit

FAIRNESS

pg2.state = crit

# Fairness

FAIRNESS

pg1.state = crit

FAIRNESS

pg2.state = crit

```
-- specification (G (F pg1.state = crit) & G (F pg2.state = crit)) is  
true
```

# Fairness

JUSTICE

pg1.state = crit

JUSTICE

pg2.state = crit

COMPASSION

( pg1.state = wait, pg1.state = crit )

COMPASSION

( pg2.state = wait, pg2.state = crit )



# Past properties

*“If a process reaches the critical state then it must have requested to enter.”*

$$\mathbf{G}(crit_1 \rightarrow \mathbf{O} wait_1)$$

**LTLSPEC**  $\mathbf{G} (pg1.state=crit \rightarrow \mathbf{O} (pg1.state=wait)) \ \& \ \mathbf{G} (pg2.state=crit \rightarrow \mathbf{O} (pg2.state=wait))$

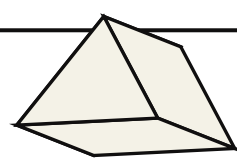
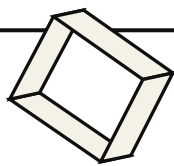
# Past properties

*“If a process reaches the critical state then it must have requested to enter.”*

$$\mathbf{G}(\text{crit}_1 \rightarrow \mathbf{O} \text{ wait}_1)$$

**LTLSPEC**  $\mathbf{G}(\text{pg1.state=crit} \rightarrow \mathbf{O}(\text{pg1.state=wait})) \ \& \ \mathbf{G}(\text{pg2.state=crit} \rightarrow \mathbf{O}(\text{pg2.state=wait}))$

```
-- specification  $\mathbf{G}(\text{pg1.state} = \text{crit} \rightarrow \mathbf{O}(\text{pg1.state} = \text{wait})) \ \&$   
 $\mathbf{G}(\text{pg2.state} = \text{crit} \rightarrow \mathbf{O}(\text{pg2.state} = \text{wait}))$  is true
```



***Fin.***

