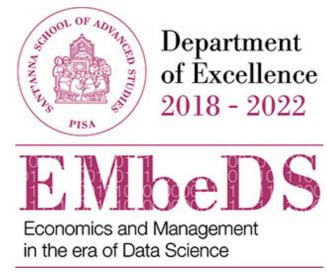
AUTOMATED & DISTRIBUTED STATISTICAL ANALYSIS of ECONOMIC ABMs

Andrea Vandin



Institute of Economics



Joint work with

Daniele Giachini, Francesco Lamperti, Francesca Chiaromonte

LEM Working Paper available at:

www.lem.sssup.it/WPLem/2020-31.html

Tool and models available at:

https://bit.ly/MultiVeStATool

CEF 2021, Session F1: Agent-Based Models (II), 17/06/2021

OUTLINE

1. Motivation, vision, and proposal

- 1. Automated analysis with statistical guarantees for ABMs
- 2. The MultiVeStA Statistical Model Checker

2. Transient Analysis of a large-scale financial macro ABM

- 1. Estimation of expected outcome and Confidence Interval
- 2. Counterfactual analysis for different model configurations

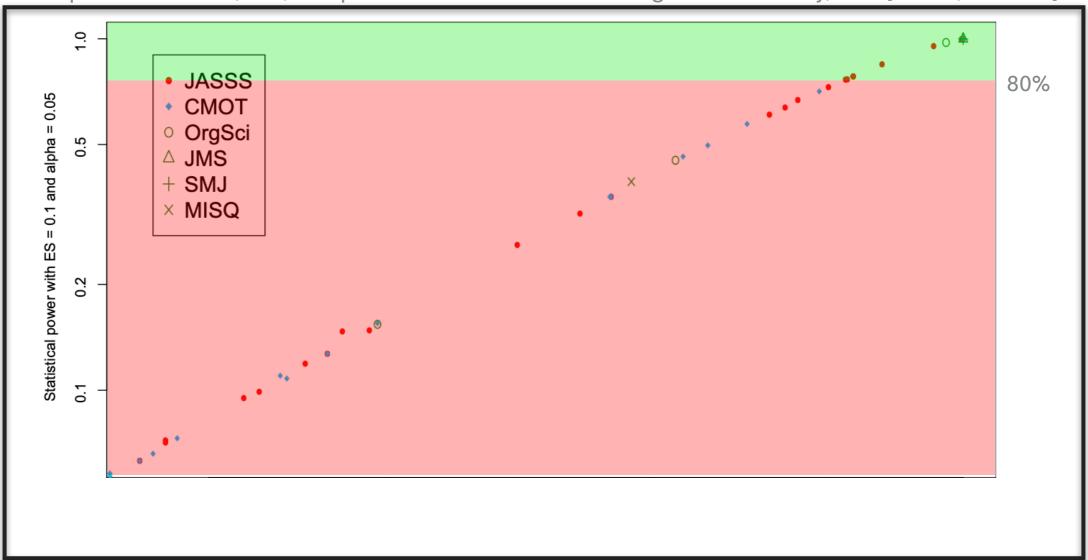
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4. Conclusions & Future works

'Quality' of Statistical Analysis on 55 ABM from Management & Organisational Research





- The importance of designing well simulation-based analysis.
 - Power analysis on 'are the expected outcomes of different configurations of parameters the same'?
- Power is 1 P(Type II error)
 - Roughly, P(test='outcomes are different' | outcomes are different)
 - "The value that seems to be more commonly accepted is 80%"
- "We need to encourage researchers to be more precise in the determination of the number of runs"

Similar studies can be found also in other communities

A systematic review of statistical power in software engineering experiments

Tore Dybå a,b,*, Vigdis By Kampenes a, Dag I.K. Sjøberg a

^a Simula Research Laboratory, P.O. Box 134, NO-1325 Lysaker, Norway
^b SINTEF ICT, NO-7465 Trondheim, Norway

Received 11 May 2005; revised 24 August 2005; accepted 31 August 2005 Available online 3 November 2005

Abstract

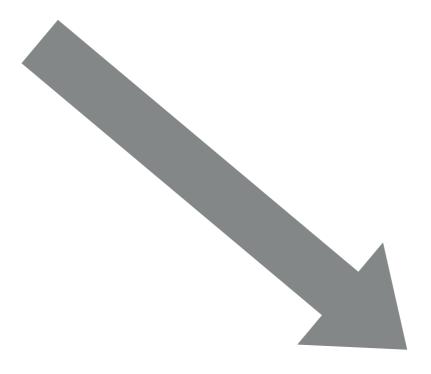
Statistical power is an inherent part of empirical studies that employ significance testing and is essential for the planning of studies, for the interpretation of study results, and for the validity of study conclusions. This paper reports a quantitative assessment of the statistical power of empirical software engineering research based on the 103 papers on controlled experiments (of a total of 5,453 papers) published in nine major software engineering journals and three conference proceedings in the decade 1993–2002. The results show that the statistical power of software engineering experiments falls substantially below accepted norms as well as the levels found in the related discipline of information systems research. Given this study's findings, additional attention must be directed to the adequacy of sample sizes and research designs to ensure acceptable levels of statistical power. Furthermore, the current reporting of significance tests should be enhanced by also reporting effect sizes and confidence intervals.

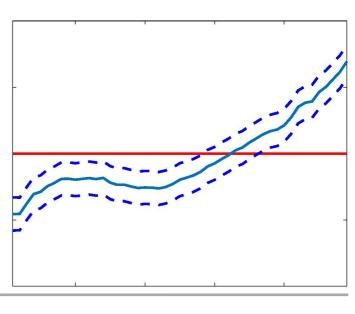
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Our Proposed Approach to Simulation-Based Analysis



newstalkzb.co.nz/news/education/modern-lego-sets-more-complex-less-inspiring/





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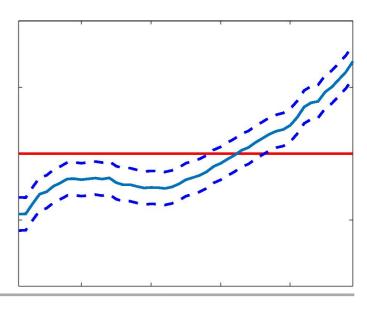


https://www.alamy.com/

Handcrafted

- Mainly manual process
 - > Time-consuming
 - ▶ Problems with replicability
 - ▶ Error-prone
 - Modify model, interpret CSV
- Ad-hoc implementations
 - ▶ Reliability? Efficiency?





Our Proposed Approach to Simulation-Based Analysis



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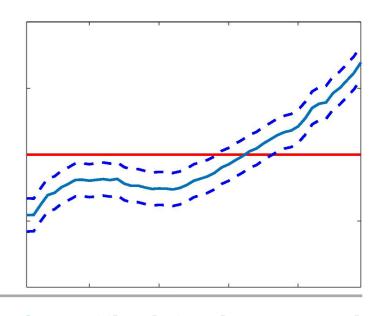
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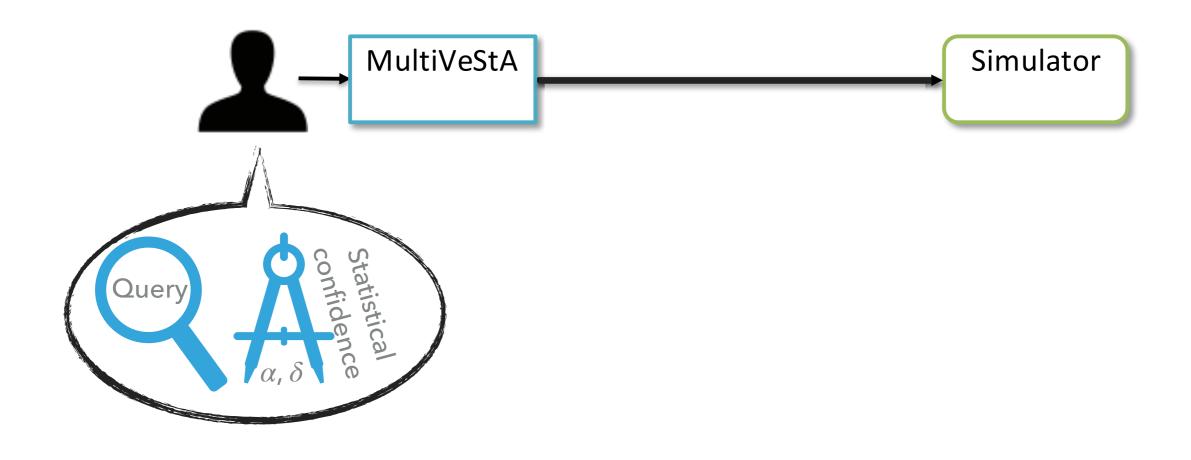


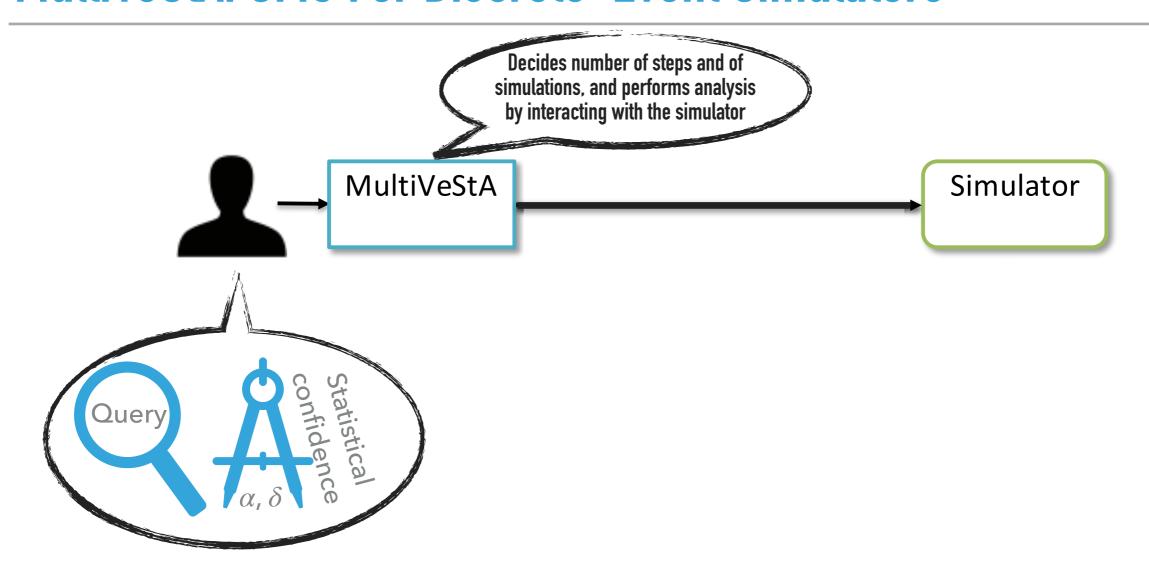
Statistical Model Checking

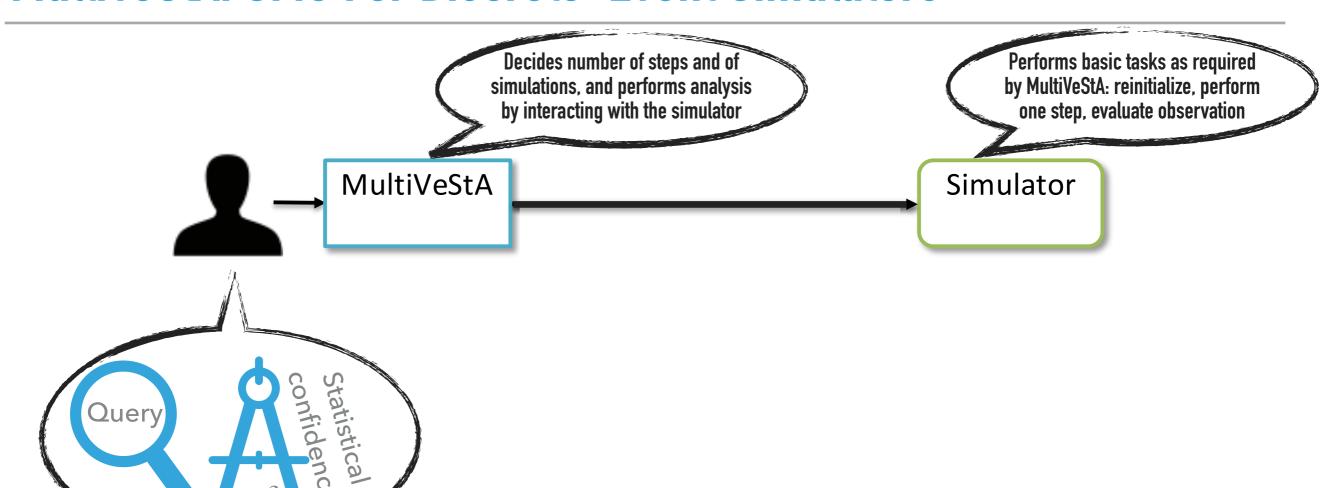
- Automatic
 - ▶ Time-saving and Reproducible
 - ▶ Promotes use of *standard* analysis
- Reference implementation
 - ▶ Reliable and Efficient

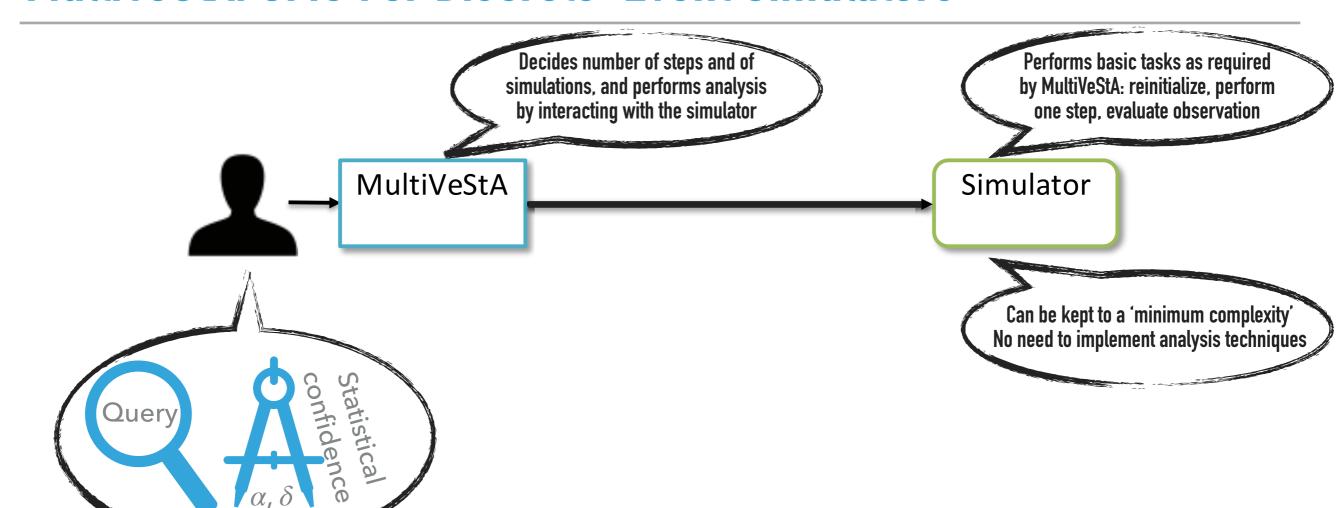


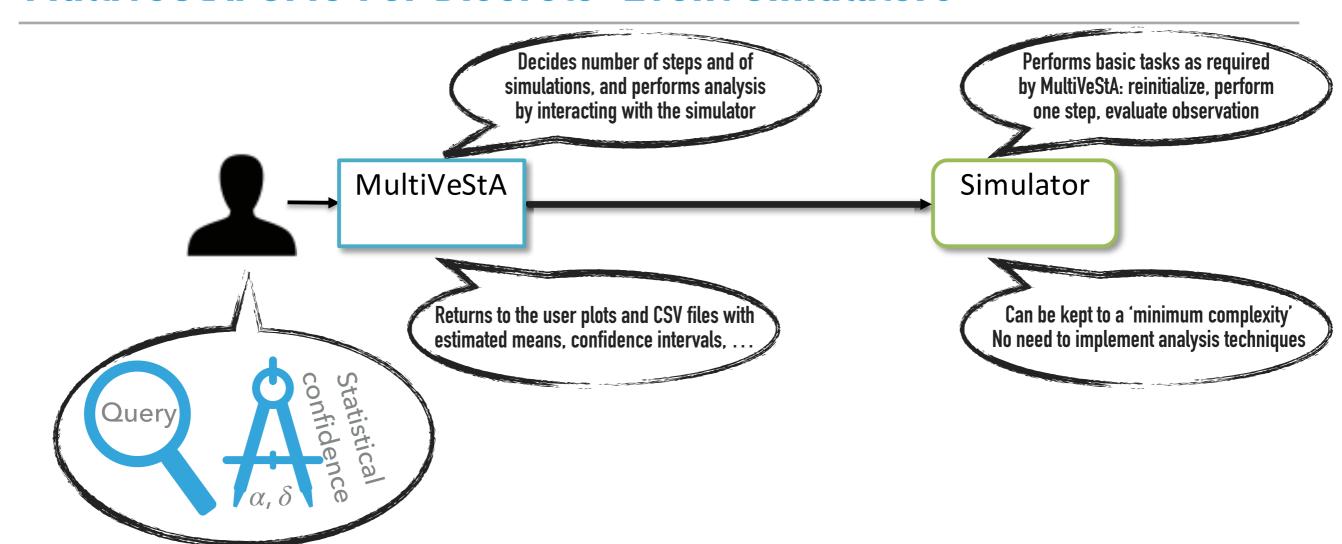


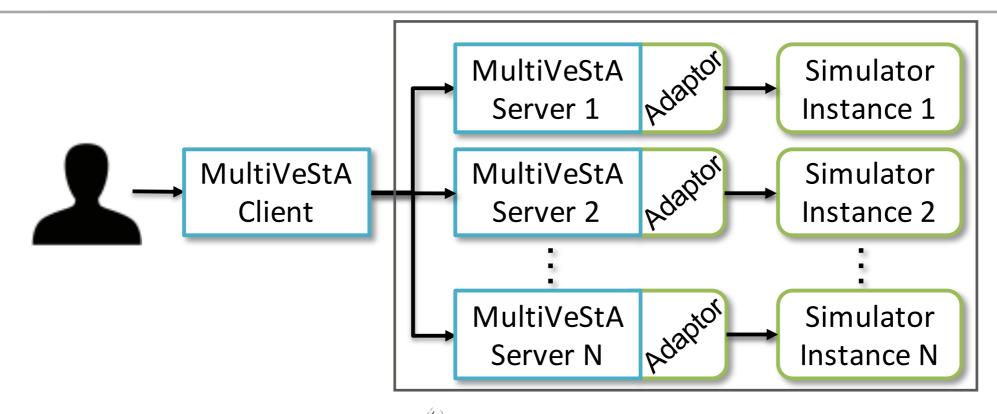


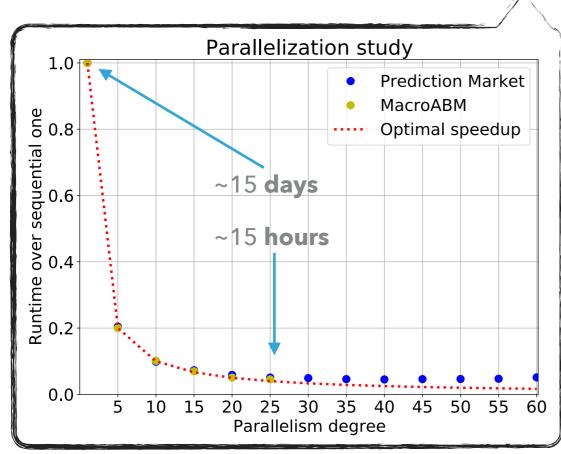


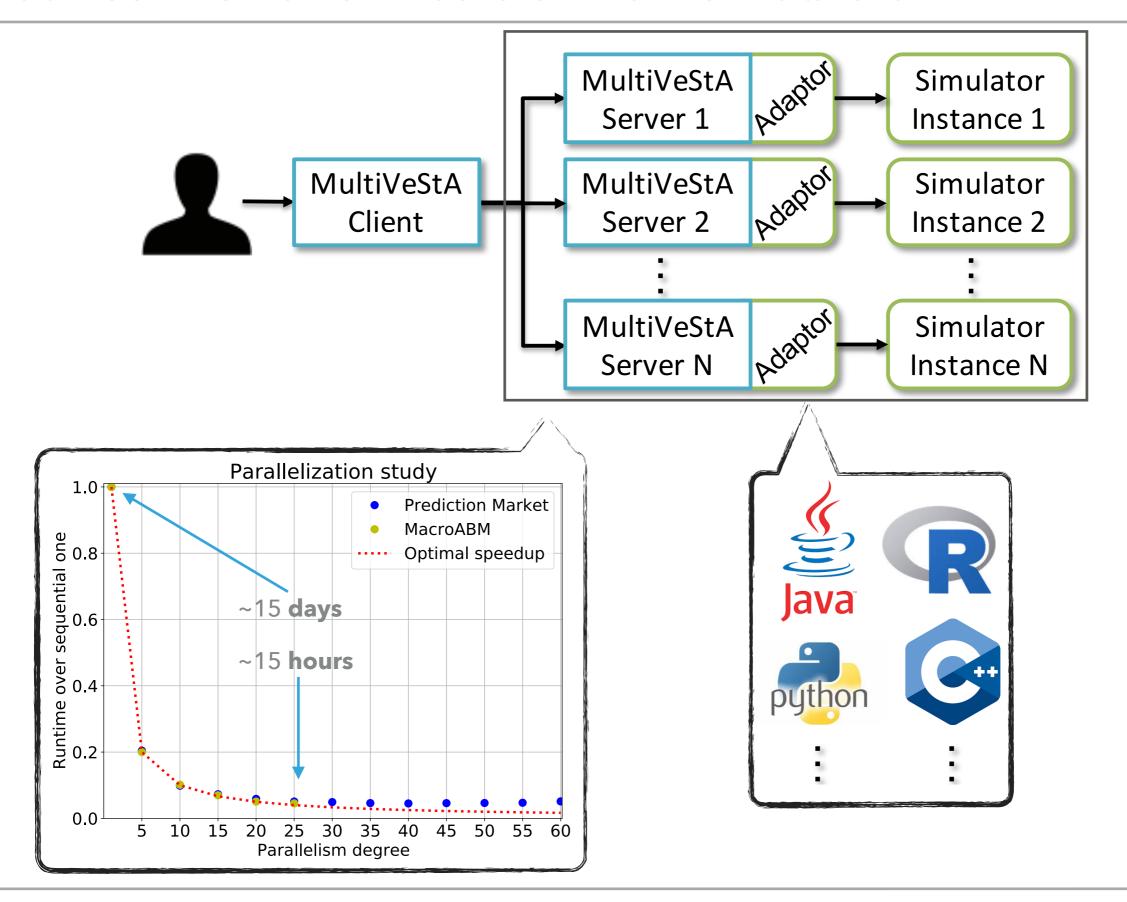












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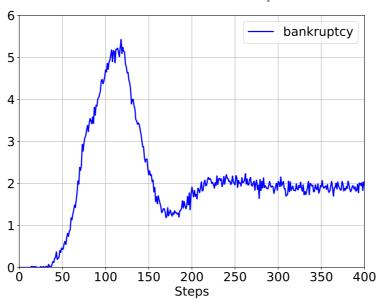
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Large-scale macro financial ABM from Caiani et al, JEDC, 2016[Caiani et al2016]

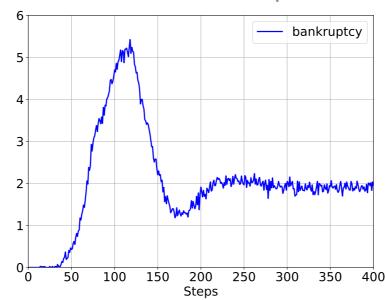
- An economy with households, consumption/capital firms, commercial banks, government, central bank
- Thousands of agents
- Implemented in JMAB: Java framework for macro stock-flow consistent ABM models.
 - Side product: any model implemented in JMAB is now natively integrated with MultiVeStA



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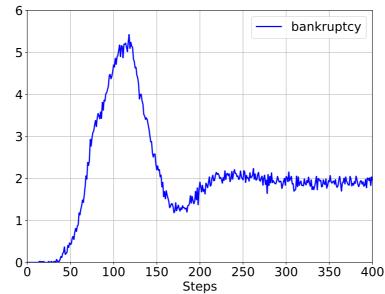
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y ₁ y ₂ ... y ₄₀₀



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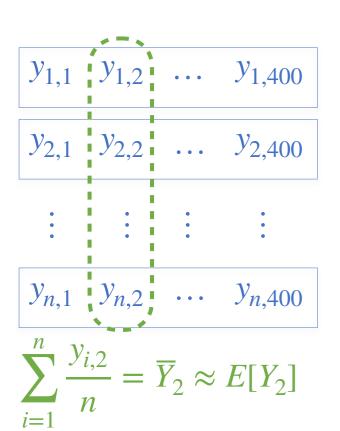


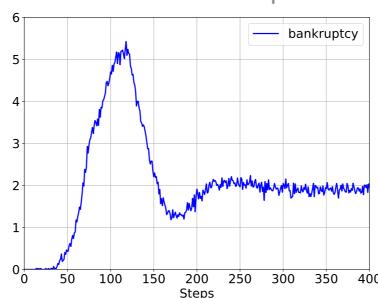
$$y_{2,1}$$
 $y_{2,2}$... $y_{2,400}$

$$y_{n,1}$$
 $y_{n,2}$ \dots $y_{n,400}$

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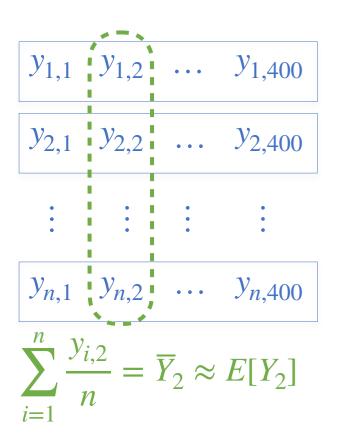
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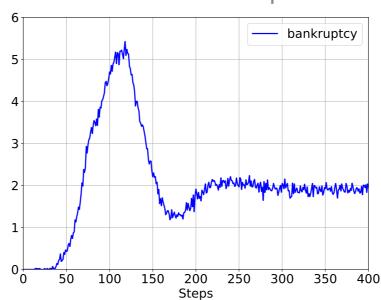


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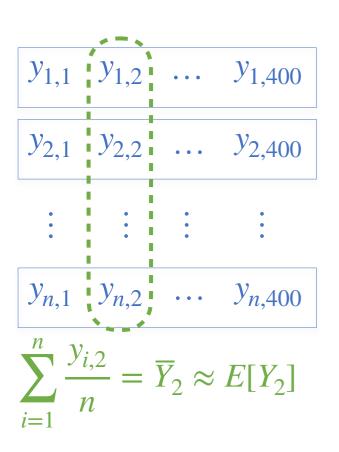
Evolution of bankruptcies



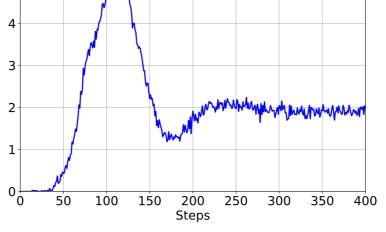
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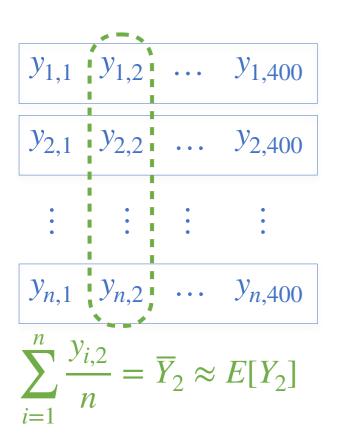




What is the correct value of n? Typical answer: 100

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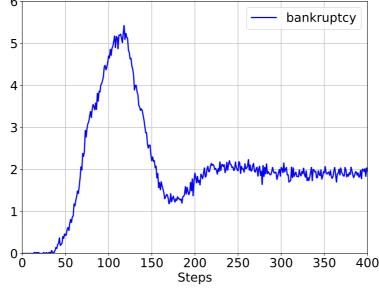
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What is the correct value of n?

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Evolution of bankruptcies — bankrup



Our answer:

The question itself is ill-posed

Each property and time step might require a different n

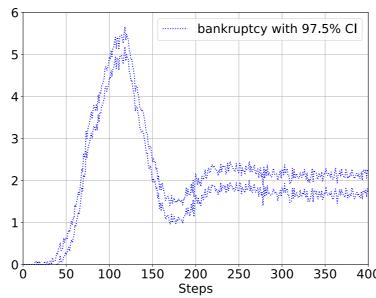
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Evolution of bankruptcies

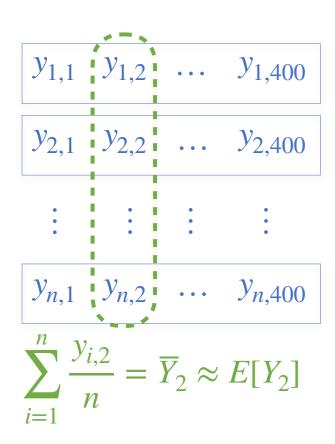


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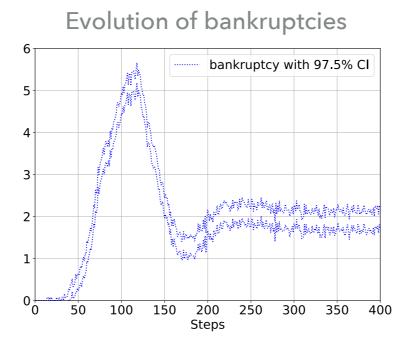
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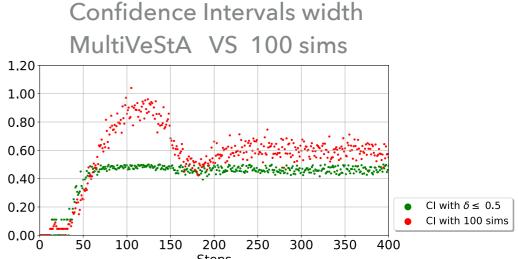
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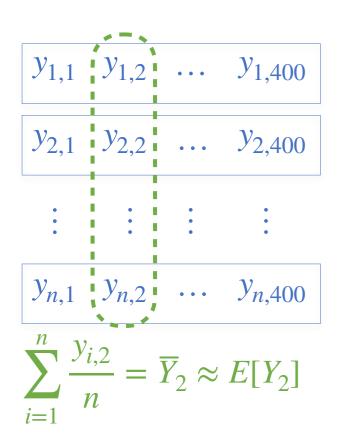


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What is the correct value of n? The question itself is ill-posed Each property and time step might require a different n

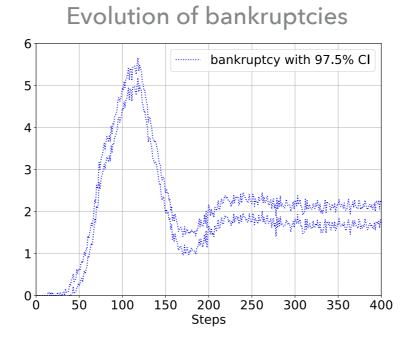
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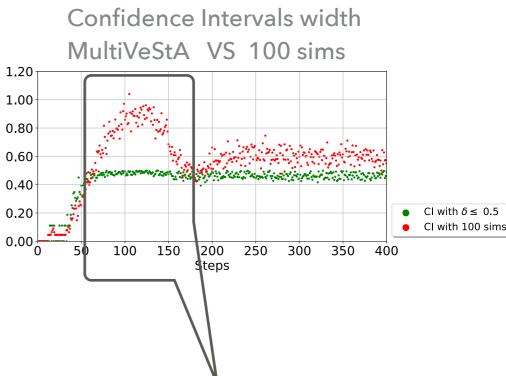
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What is the correct value of n?

Typical answer: 100





More simulations required here We save a lot of time halting the latest simulations to 150 steps

Our answer:

The question itself is ill-posed Each property and time step might require a different n

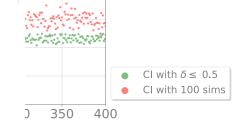
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y_{2,1} y_{2,2} ... y_{2,40} IS THIS IMPORTANT?

$$y_{n,1}$$
 $y_{n,2}$ \cdots $y_{n,400}$

$$\sum_{i=1}^{n} \frac{y_{i,2}}{n} = \overline{Y}_2 \approx E[Y_2]$$

More simulations required here We save a lot of time halting the latest simulations to 150 steps

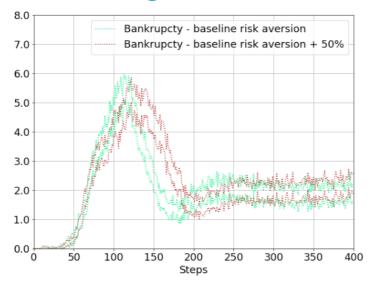
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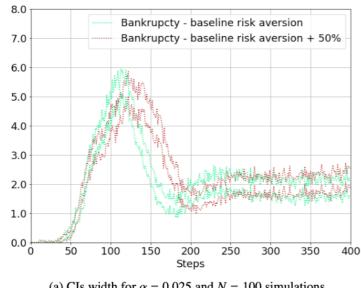
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97.5% CI 100 Simulations

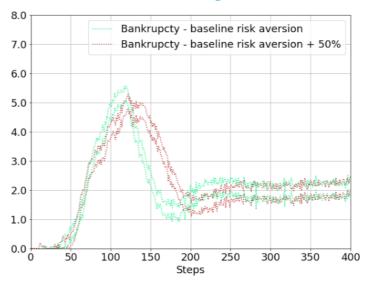


(a) CIs width for $\alpha = 0.025$ and N = 100 simulations

97.5% CI 100 Simulations



(a) CIs width for $\alpha = 0.025$ and N = 100 simulations

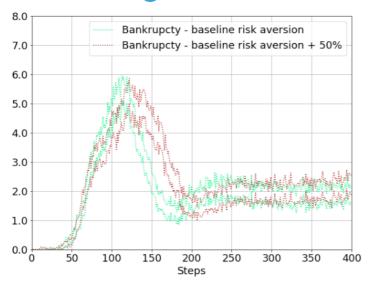


(b) CIs width for $\alpha = 0.025$ and $\delta = 0.5$

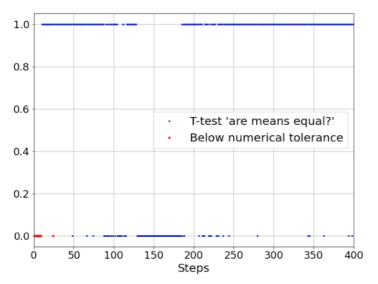
97.5% CI MultiVeStA $|\operatorname{CI}| \leq \delta = 0.5$

97.5% CI 100 Simulations

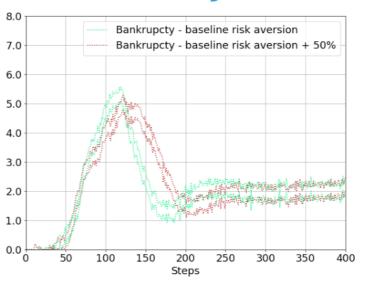
Welch's t-test with significance α =2.5% [Welch1947]



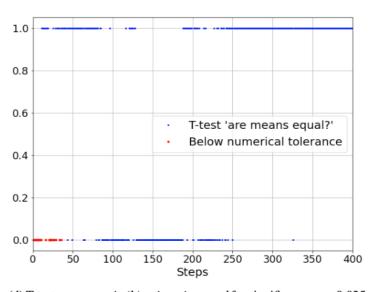
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(c) T-test are means in (a) point-wise equal for significance $\alpha = 0.025$



(b) CIs width for $\alpha = 0.025$ and $\delta = 0.5$



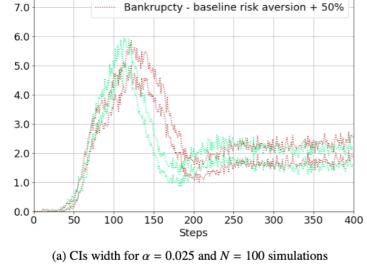
(d) T-test are means in (b) point-wise equal for significance $\alpha = 0.025$

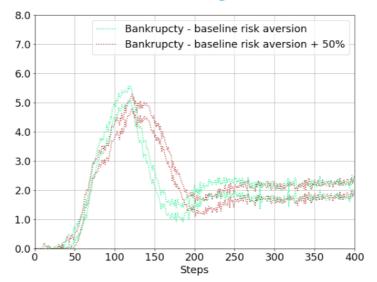
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Bankrupcty - baseline risk aversion

97.5% CI 100 Simulations

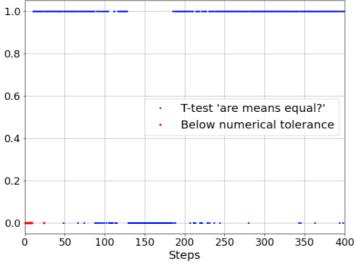


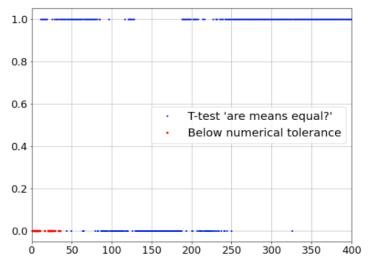


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97.5% CI MultiVeStA $|CI| \le \delta = 0.5$

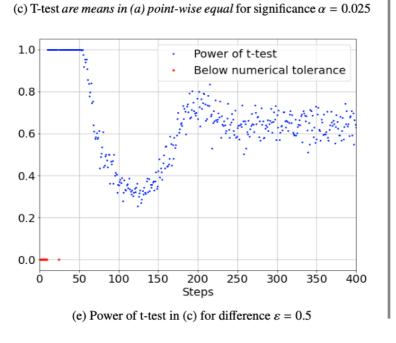
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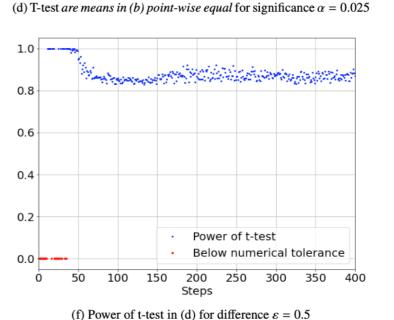




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Power of the test P(Test=0 | Real=0) 1 - P(Type II error) [Chow2002]





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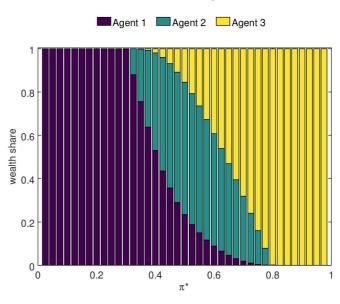
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Simple repeated betting market from [Kets et al2014]

- 1 event realises at every step with a fixed probability π^*
- * 3 Fractional Kelly bettors with a belief on π^* and place bets accordingly

Agents wealth at steady state



14

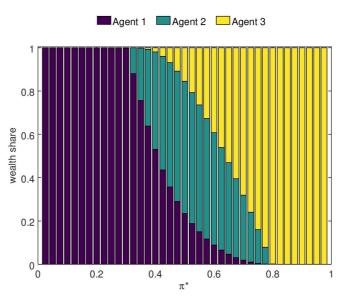
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$$y_{2,1}$$
 $y_{2,2}$... $y_{2,m}$

$$y_{n,1}$$
 $y_{n,2}$... $y_{n,m}$



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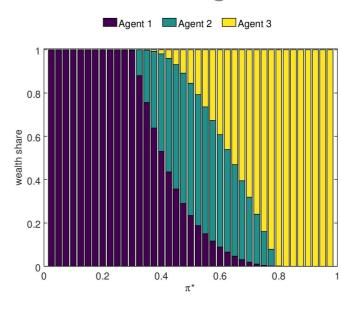
14

Warmup w steps

$$y_{1,1}$$
 $y_{1,2}$ \dots $y_{1,m}$

$$y_{2,1}$$
 $y_{2,2}$... $y_{2,m}$

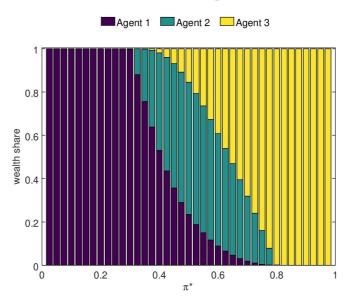
$$y_{n,1}$$
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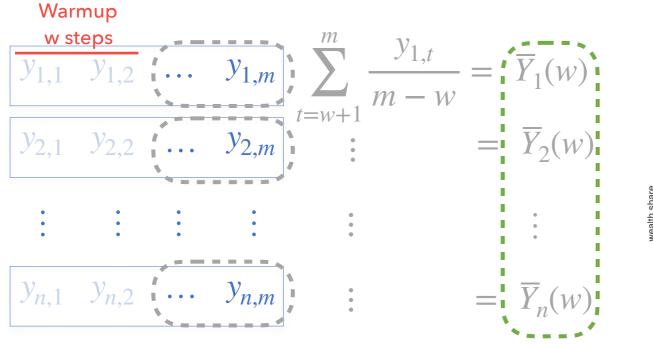
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Warmup

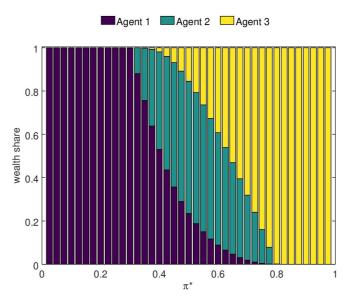


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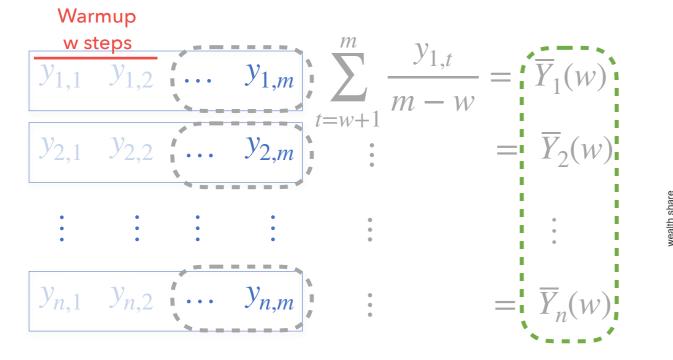


$$\sum_{i=1}^{n} \frac{\overline{Y}_{i}(w)}{n} = \overline{Y}(w) \approx E[Y] = \lim_{t \to \infty} E[Y_{t}]$$

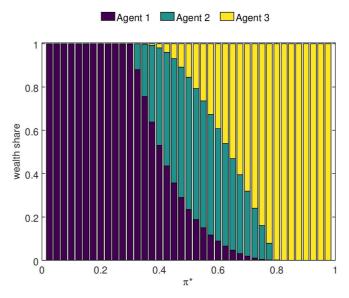


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Agents wealth at steady state

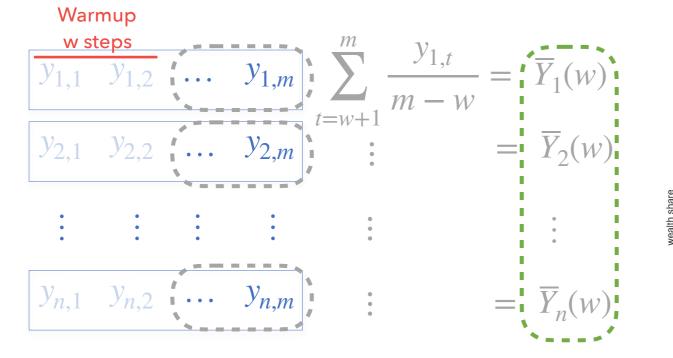


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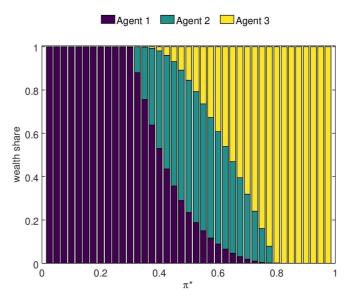
Replication and Deletion (RD) [Law, Kelton 2015]

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Agents wealth at steady state



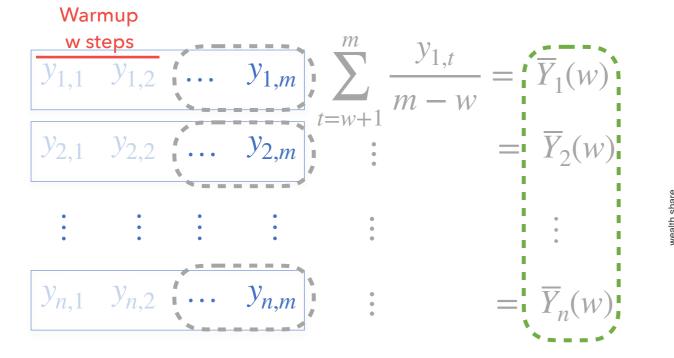
 $\sum_{i=1}^{n} \frac{Y_i(w)}{n} = \overline{Y}(w) \approx E[Y] = \lim_{t \to \infty} E[Y_t]$

Replication and Deletion (RD) [Law, Kelton 2015]

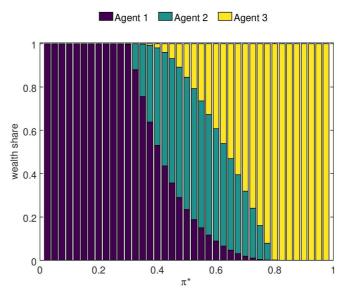
What are the correct values for w, m, n?

Simple repeated betting market from [Kets et al2014]

- 1 event realises at every step with a fixed probability π^* 3 Fractional Kelly bettors with a belief on π^* and place bets accordingly



Agents wealth at steady state



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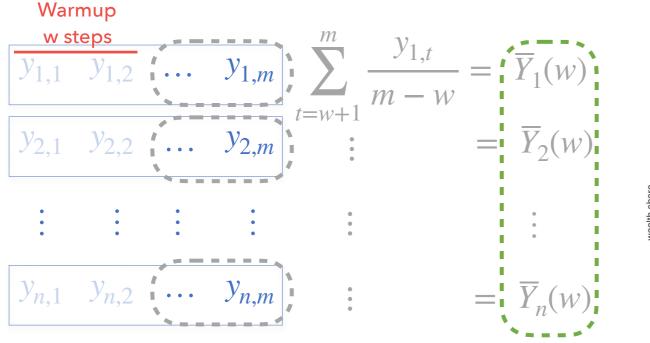
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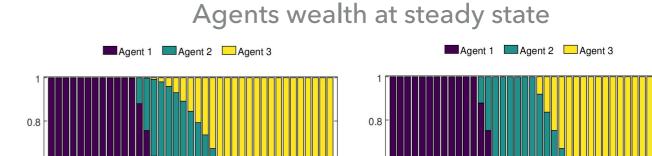
THESE ARE DIFFICULT QUESTIONS **ARE THEY CRUCIAL?**

Simple repeated betting market from [Kets et al2014]

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$$\sum_{i=1}^{n} \frac{\overline{Y}_{i}(w)}{n} = \overline{Y}(w) \approx E[Y] = \lim_{t \to \infty} E[Y_{t}]$$



[Kets et al2014]

Same as analytical solution from [Bottazzi, Giachini 2019]

MultiVeStA

Replication and Deletion (RD) [Law, Kelton 2015]

What are the correct values for w, m, n?

THESE ARE DIFFICULT QUESTIONS **ARE THEY CRUCIAL?**



OUTLINE

1. Motivation, vision, and proposal

- 1. Automated analysis with statistical guarantees for ABMs
- 2. The MultiVeStA Statistical Model Checker

2. Transient Analysis of a large-scale financial macro ABM

- 1. Estimation of expected outcome and Confidence Interval
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4. Conclusions & Future works

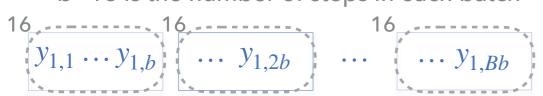
- 1. Do 1 long simulation of length m=B*b
- 2. Divide it in *B batches* of *b* consecutive steps

$$y_{1,1} \cdots y_{1,b}$$
 \cdots $y_{1,2b}$ \cdots $y_{1,Bb}$

16

0. Set m = B*b,

B=128 is the number of batches of simulation 2. Divide it in B batches of b consecutive steps b=16 is the number of steps in each batch

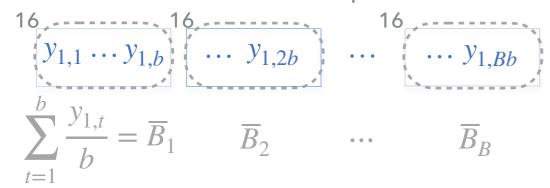


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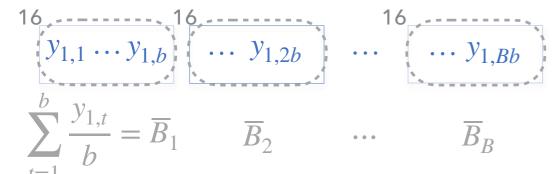
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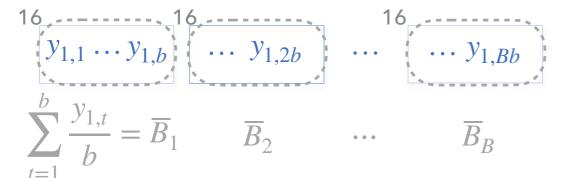
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- 4. Perform statistical tests to check if *m* is large enough Perform a normality test on the computed means Check for low lag-1 autocorrelation on the means

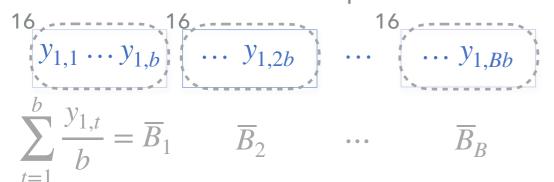
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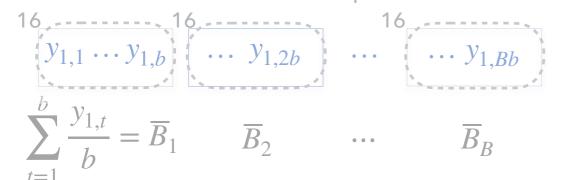
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5.2 If one test fails

Double b squeezing the batches in the first B/2 ones Double m by performing m new simulation steps Go back to step 3

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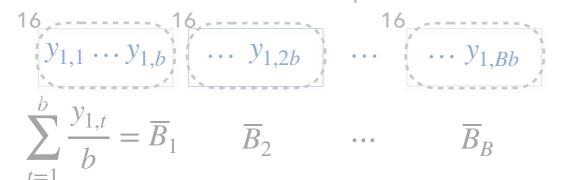
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- 32 32 $y_{1,1} \cdots y_{1,b} \cdots y_{1,\frac{B}{2}b}$ 32 32 $y_{1,\frac{B}{2}b} \cdots y_{1,(\frac{B}{2}+1)b} \cdots y_{1,Bb}$
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Based on the Batch Means (BM) method

- First proposal in [Conway1963], First automatic version in [Law, Carson1979]
- Approach for steady state analysis
 - Alternative to Replication and Deletion based on 1 long simulation

Steady State Analysis by autoBM: our BM-Based Proposal

0. Set m = B*b,

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$$\sum_{t=1}^{b} \frac{y_{1,t}}{b} = \overline{B}_1 \qquad \overline{B}_2 \qquad \overline{B}_B$$

$$\sum_{i=l+1}^{n} \frac{\overline{B}_{j}}{n-l} = \overline{B}(l) \approx E[Y] = \lim_{t \to \infty} E[Y_{t}]$$

- 1. Do 1 long simulation of length m=B*b
- 2. Divide it in *B batches* of *b* consecutive steps
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- 4. Perform statistical tests to check if *m* is large enough Perform a normality test on the computed means Check for low lag-1 autocorrelation on the means
- 5.1 If all tests pass, we conclude that the warmup has endedCompute the grand mean (mean of the means)Compute the width d of the CI of grand meanAdjust d according to the residual correlation in the means
- 5.2 If one test failsDouble b squeezing the batches in the first B/2 onesDouble m by performing m new simulation stepsGo back to step 3

Based on the Batch Means (BM) method

- First proposal in [Conway1963], First automatic version in [Law,Carson1979]
- Approach for steady state analysis
 - Alternative to Replication and Deletion based on 1 long simulation

We also propose a simple novel version of BM for steady-state analysis

Based on [Law, Carson 1979] [Steiger et al 2005] [Tafazzoli et al 2011] [Gilmore et al 2017]

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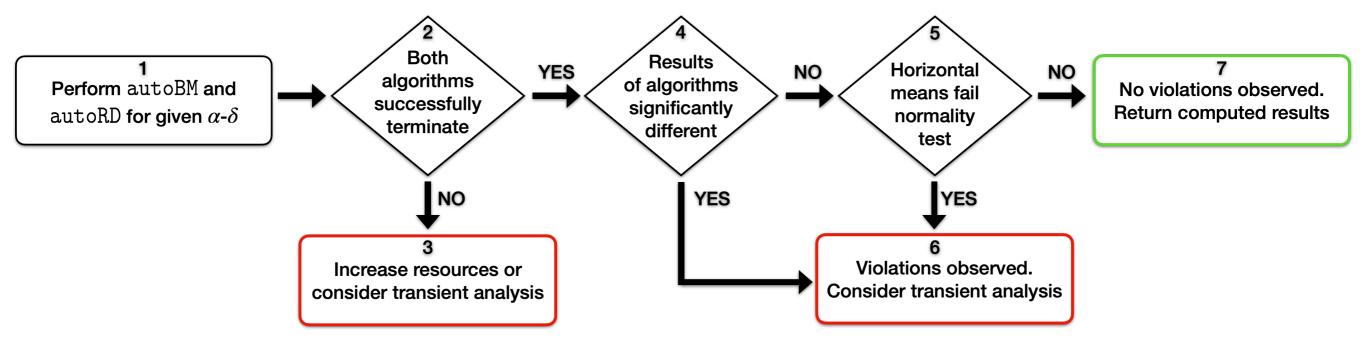
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A Methodology for Ergodicity Diagnostics



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CONCLUSIONS

- Fully automated framework for statistical analysis of ABMs
 - Transient analysis with statistical tests to compare model configurations
 - Warmup estimation, Steady-state analysis by RD and BM
 - Ergodicity diagnostics
- ▶ Tool-supported one-click analysis:
 - Less manual error-prone tasks => more reproducibility & reliability
 - Automatically parallelise simulations: 15 days => 15 hours
 - Support for simulators written in Java, Python, R, C++, JMAB
- Validated on two models from the literature:
 - Large-scale macro financial ABM, Small-scale prediction market model
 - We obtained new insights on the considered models
 - We avoid analysis issues from previous publications
- Our approach is rooted in results from:
 - Communities of Simulation, Computer Science, Operations Research
 - We aim at strengthening the cross-fertilisation with the ABM one

FUTURE WORK

- Add more techniques
 - Detection of multiple stationary points
 - Advanced SMC techniques to
 - Handle rare events, Reduce number of simulations required
 - More!? Model calibration, Sensitivity analysis, ...
- Apply the approach to further models and domains
 - Any JMAB model is now natively supported
 - We wish to natively support further frameworks for ABM modelling
 - Would you like to use MultiVeStA to analyse your models?
 - Just contact us

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THANK YOU FOR YOUR ATTENTION!

QUESTIONS? FEEDBACK?

LEM Working Paper available at: www.lem.sssup.it/WPLem/2020-31.html

Tool and models available at:

https://bit.ly/MultiVeStATool