

Machine Learning for Networks: Clustering and Anomaly Detection

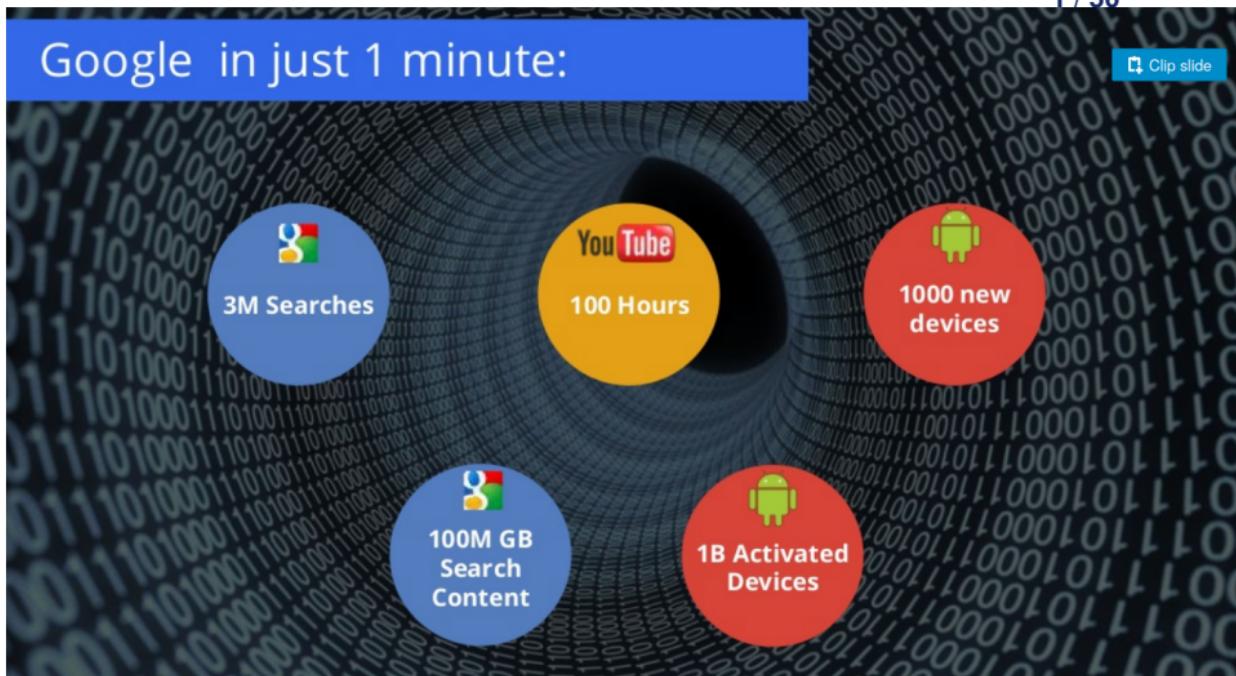
Andrea Araldo

January 31, 2022



The challenge of Big Data

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From D. Marcus (Google, Waze) [presentation](#)

Supervised Learning is impossible:

- Users do not label their actions
- We cannot label data manually

Section 1

Clustering

Unsupervised Learning: Clustering

- K-means clustering

Unsupervised Learning: Dimensionality reduction (next class)

Anomaly detection

- k-means anomaly detection
- Isolation Forests
- Neural Networks: Autoencoders

What is Clustering?

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- Clustering means grouping M observations into clusters (partitions).
- There are no labels \mathbf{y}
 - We group observations, $\mathbf{x}^{(i)}$, by their similarity
 - *unsupervised learning*
- **Exploratory** technique to discover interesting relationships in data.

Clustering Application: Marketing

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- Customer segmentation based on brand loyalty and price sensitivity scores.

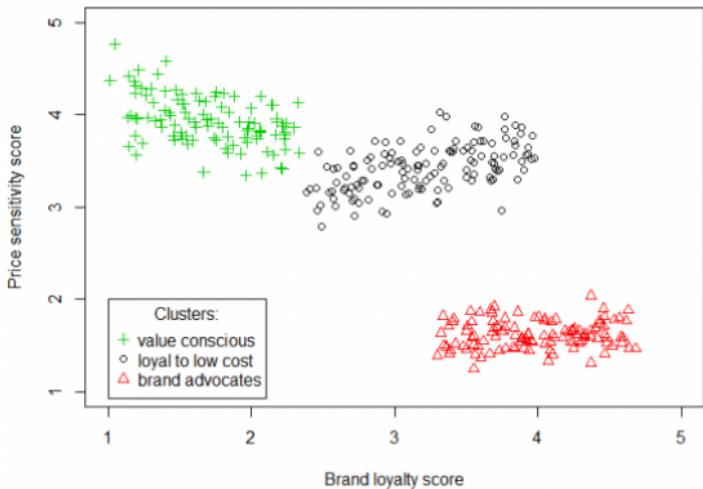
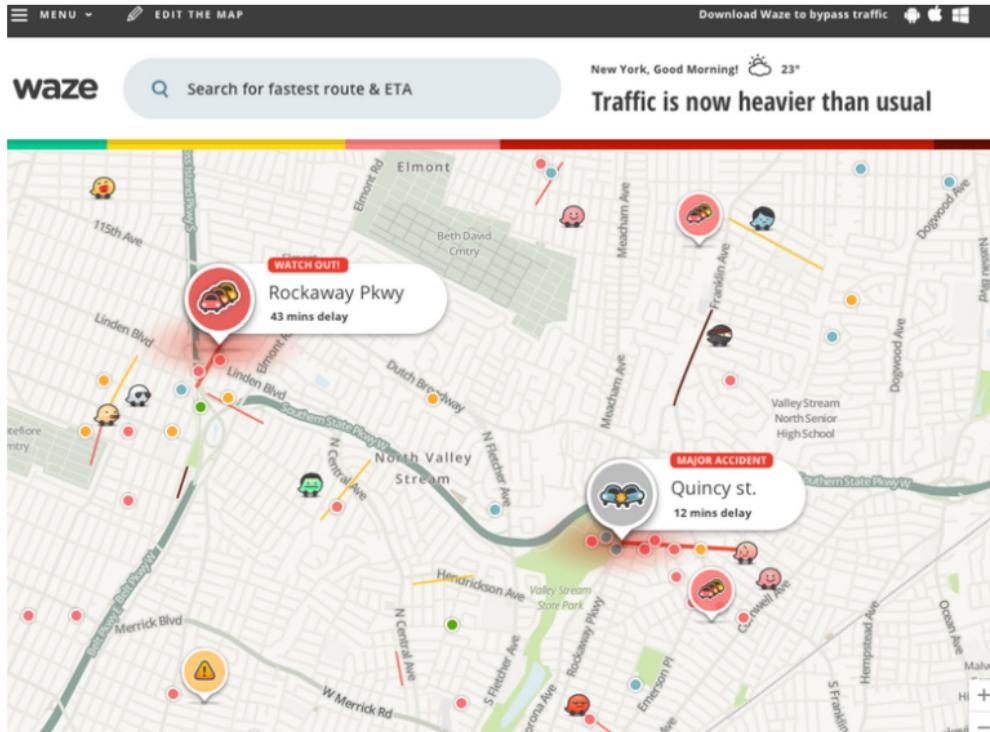


Fig. from <http://www.select-statistics.co.uk/>

Discover events in Waze

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K-means Clustering

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- K : Number of clusters.
Hyper-parameter.
- Cluster **centroid**: mean of observations assigned to cluster C_k :

$$\bar{\mathbf{x}}_k \triangleq \frac{1}{|C_k|} \sum_{\mathbf{x} \in C_k} \mathbf{x}$$

- **Within-cluster variation** of C_k
(§10.3.1 of [JWHT13])

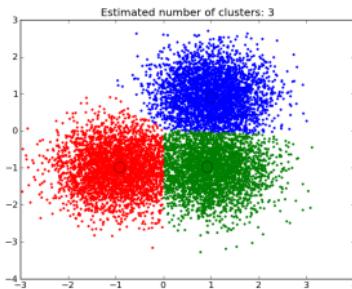
$$W(C_k) \triangleq \frac{1}{|C_k|} \sum_{\mathbf{x} \in C_k} d(\mathbf{x}, \bar{\mathbf{x}}_k)^2$$

- also called **inertia** [Cha].
- $d(.,.)$ is usually Euclidean distance
 - Scale!

- Goal: minimize total inertia

$$\min W = \sum_{k=1}^K W(C_k)$$

- \Rightarrow Assign \mathbf{x} to C_k with minimum $d(\mathbf{x}, \bar{\mathbf{x}}_k)$



Source: www.scikit-learn.org

K-means Clustering: Illustration

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Minimize total inertia:

$$\min \sum_{k=1}^K \frac{1}{|C_k|} \sum_{\mathbf{x} \in C_k} d(\mathbf{x}, \bar{\mathbf{x}}_k)^2$$

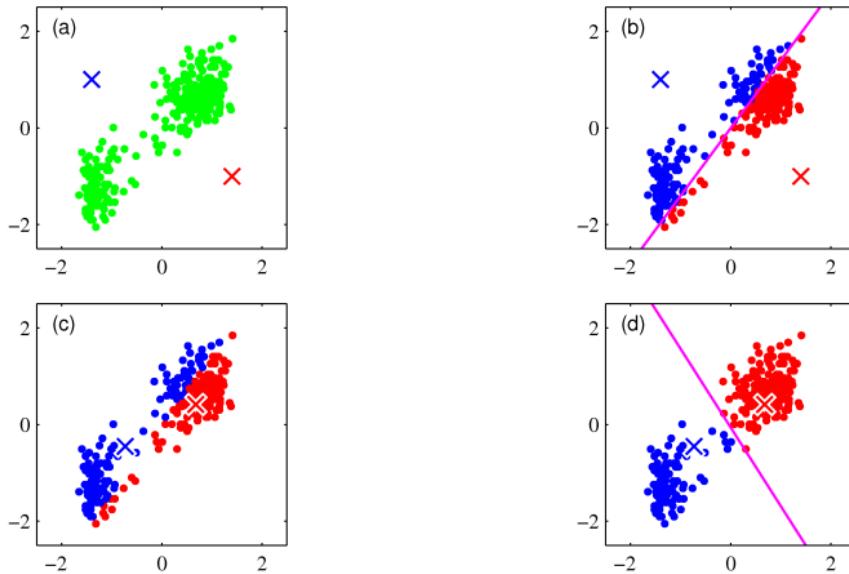


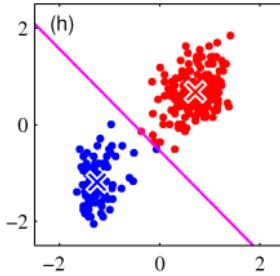
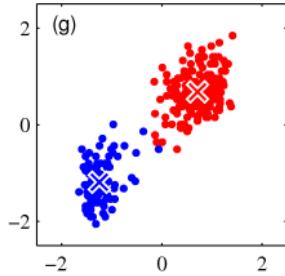
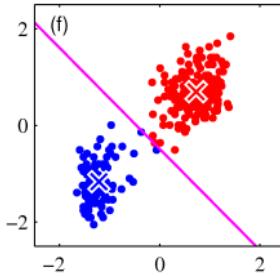
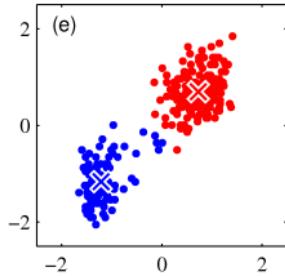
Fig.: Cristopher M. Bishop, *Pattern Recognition and Machine Learning*

K-means Clustering: Illustration

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Minimize total inertia:

$$\min \sum_{k=1}^K \frac{1}{|C_k|} \sum_{\mathbf{x} \in C_k} d(\mathbf{x}, \bar{\mathbf{x}}_k)^2$$

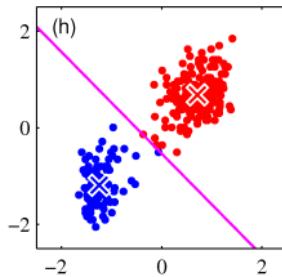
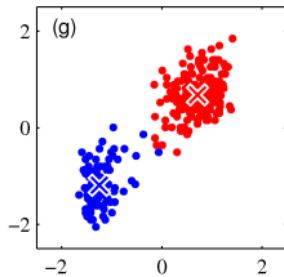
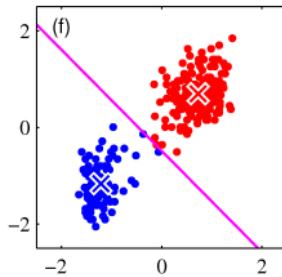
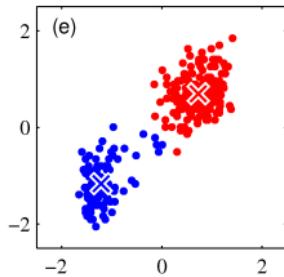


K-means Clustering: Illustration

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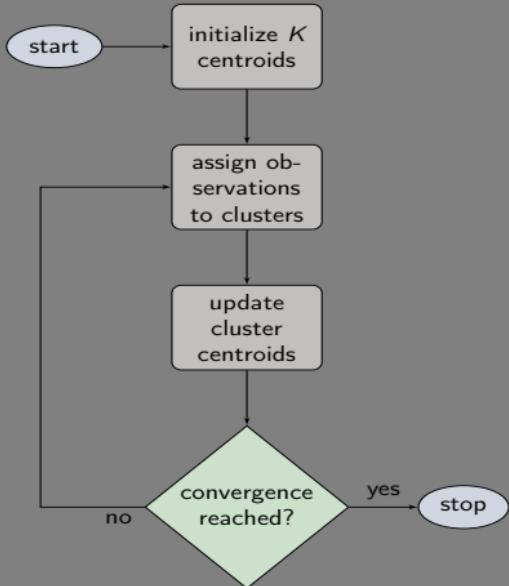
Minimize total inertia:

$$\min \sum_{k=1}^K \frac{1}{|C_k|} \sum_{\mathbf{x} \in C_k} d(\mathbf{x}, \bar{\mathbf{x}}_k)^2$$



If you change initial centroids \Rightarrow final clusters change

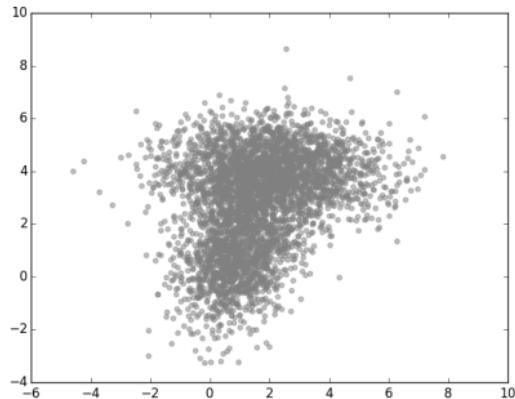
- Repeat random initial centroids at least 20 times, and choose the clustering with the lowest W.



- Thm: at each Assign and Update, the total W decreases until *convergence*.
- Smallest possible W at convergence?
- The W at convergence depends on the initial centroids chosen. So?
- Repeat the algorithm with different random initial centroids at least 20 times , and choose the clustering with the lowest W.

From [ZZPBA17]

Which K would you choose?

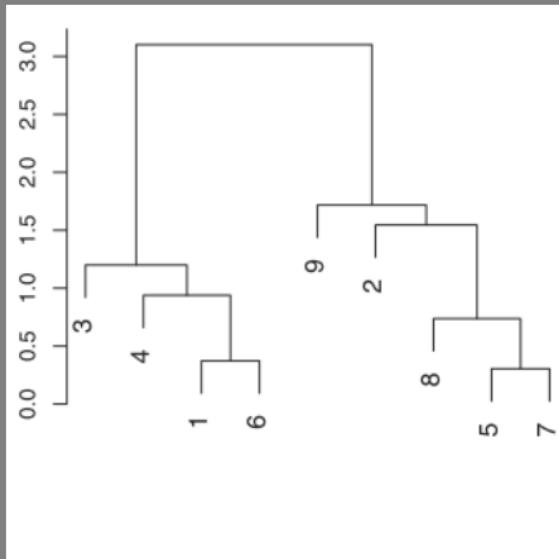


Other clustering techniques choose K for you.

- Hierarchical Clustering
- DBScan
- ...

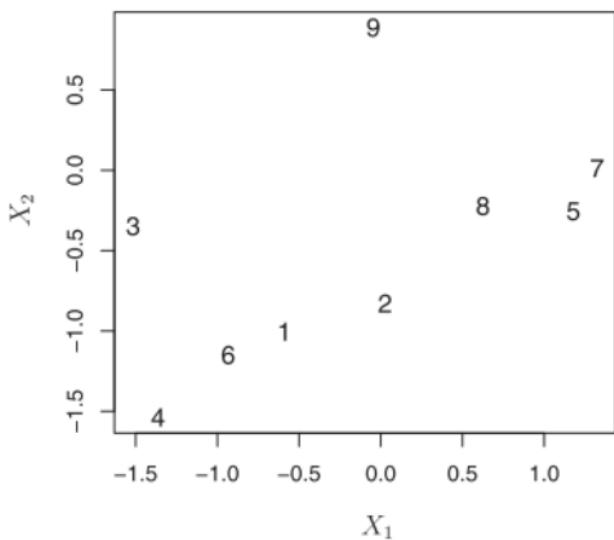
Hierarchical Clustering: Dendrogram

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Source: https://www.csie.ntu.edu.tw/~cjlin/libsvm/

- Distance between 5 and 7? And between $\{5,7,8,2\}$ and $\{9\}$?



- Are 2 and 9 “close”? Distance between 2 and 9? Distance between $\{5,7,8\}$ and $\{9\}$?

Hierarchical Clustering: Linkage

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- **Single linkage:**

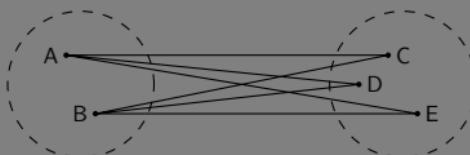
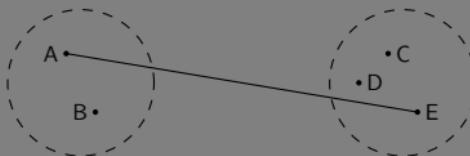
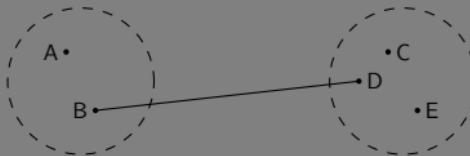
minimum distance or nearest neighbor (2 closest border points)

- **Complete linkage:**

maximum distance or farthest neighbor (2 farthest border points)

- **Average linkage:**

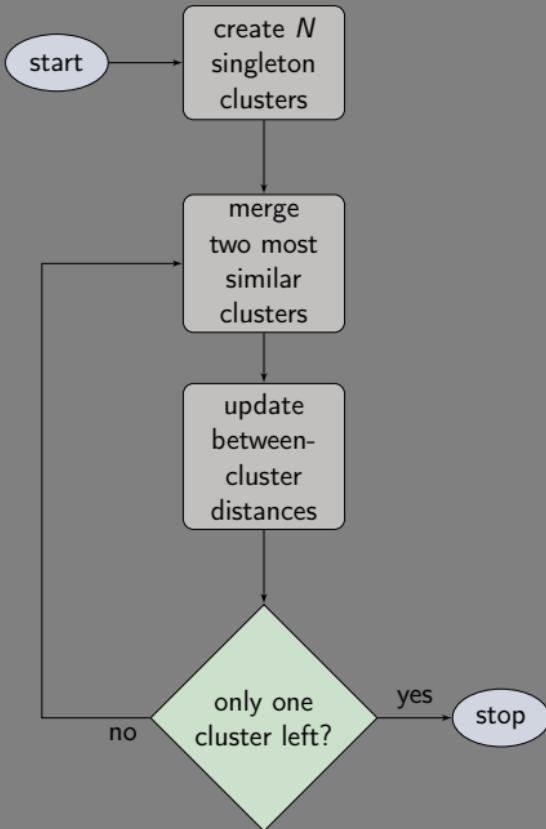
average distance (all to all)



From [ZZPBA17]

Building a dendrogram

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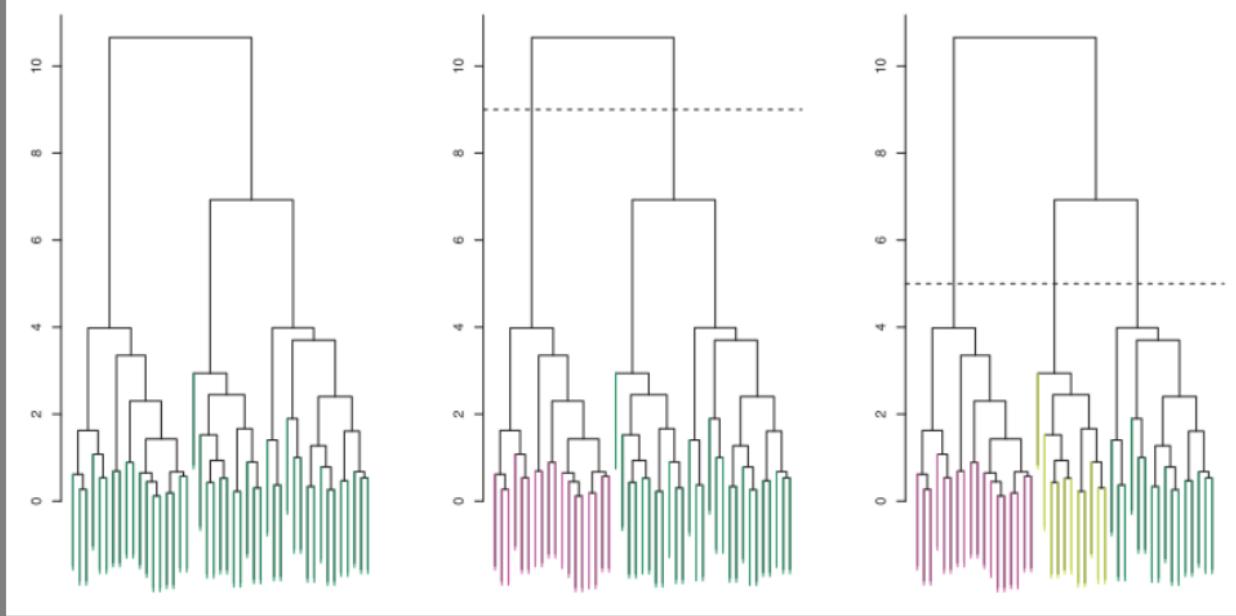


From [ZZPBA17]

Choosing the clusters

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We decide a Cut



Source: James et Al., Introduction to Statistical Learning

Same cluster with K-means, K=2?

Advantages

- No apriori number of clusters required
- Simple algorithms
- Self-organized structural view of data

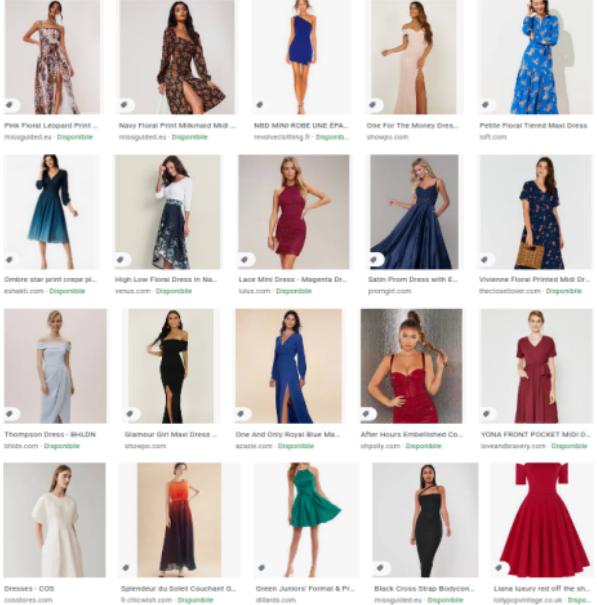
Disadvantages

- Dendrogram often difficult to visualize
- Bad performance when inherent clusters are not hierarchical by nature
 - Ex.: incidents in the road

Similarity Measures

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- How similar are two observations?
 - Color
 - Price
 - Size
 - Brand
 - Fabric
 - ...



Similarity Measures: Distance

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Comparing two vectors, \mathbf{z}_k and \mathbf{z}_j , with r variables

- With *Numerical data*:
 - Euclidean distance

$$d(\mathbf{z}_k, \mathbf{z}_j) = \sqrt{\sum_{i=1}^r (z_{ki} - z_{ji})^2}$$

- Manhattan distance

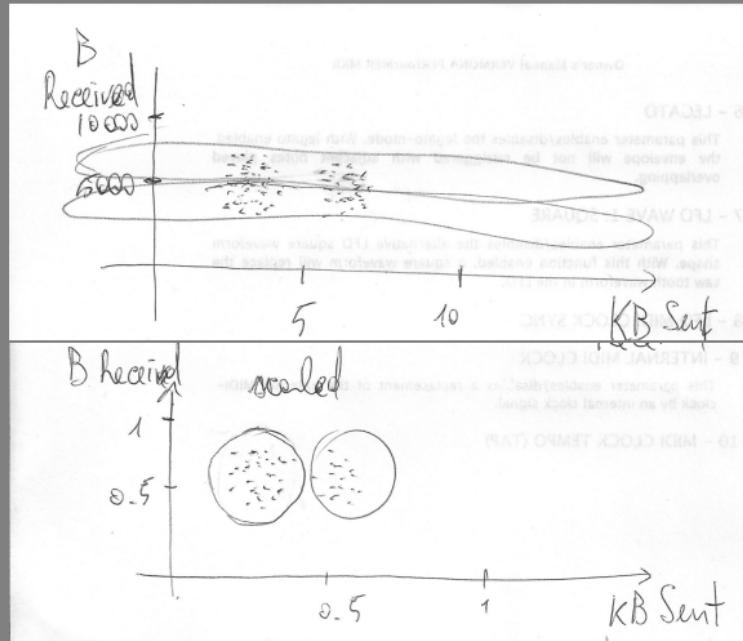
$$d(\mathbf{z}_k, \mathbf{z}_j) = \sum_{i=1}^r |z_{ki} - z_{ji}|$$

- Minkowski distance

$$d(\mathbf{z}_k, \mathbf{z}_j) = \left[\sum_{i=1}^r |z_{ki} - z_{ji}|^m \right]^{1/m}$$

- Observe that:
 - Different groupings
 - Subjective and domain-dependent
 - Dependent on the variable type (discrete, continuous, binary).

Scaling



Without scaling, cluster would be just driven by features with large values.

Limits of within-cluster variation

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Good clustering should:

- Minimize **within-cluster** variation (W)
- ... but also maximize the separation between clusters
- \Rightarrow Inertia W is not enough

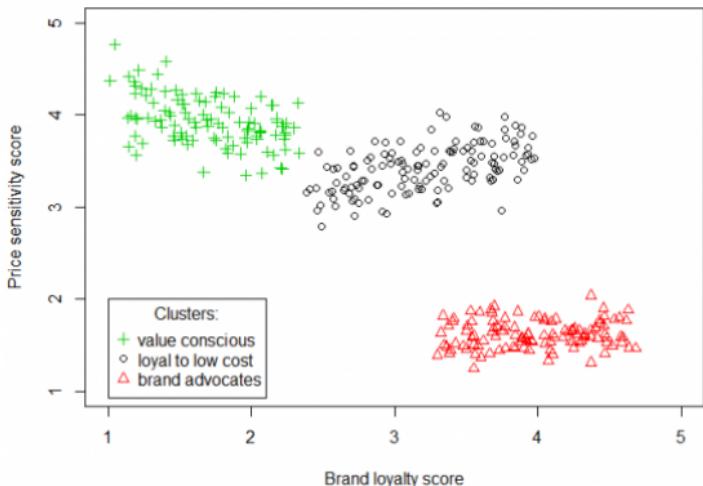


Fig. from <http://www.select-statistics.co.uk/>

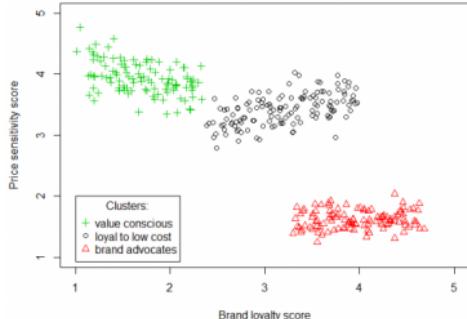
Silhouette:

- Silhouette of sample \mathbf{x} :

$$s(\mathbf{x}) \triangleq \frac{b(\mathbf{x}) - a(\mathbf{x})}{\max(a(\mathbf{x}), b(\mathbf{x}))}$$

- $a(\mathbf{x})$ = average distance between \mathbf{x} and *all* other elements of its cluster (intra-cluster distance)
- $b(\mathbf{x})$ = average distance between \mathbf{x} and *all* elements of the second nearest cluster.
- Measures how well an observation fits a cluster
- $-1 < s(\mathbf{x}) < 1$
- We want $a(\mathbf{x})$ to be small and $b(\mathbf{x})$ to be large:

$$a(\mathbf{x}) \ll b(\mathbf{x}) \implies s(\mathbf{x}) \rightarrow 1$$



Source: <http://www.select-statistics.co.uk/>

Silhouette: visualization

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See:

- silhouette score:
Avg silhouette across all samples
- Cluster size

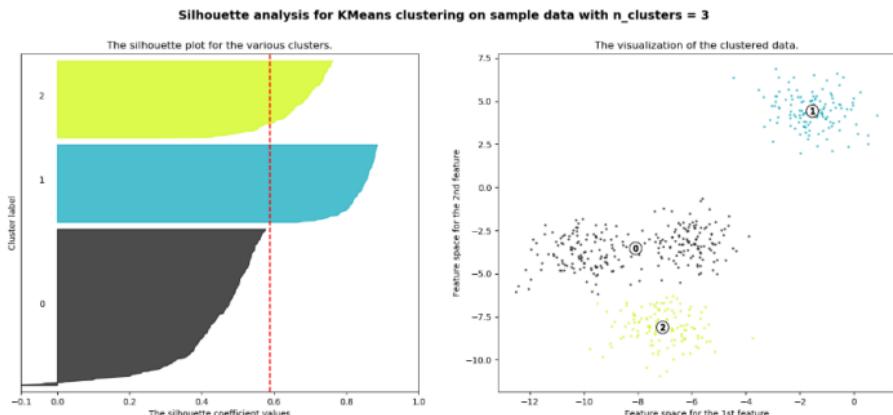
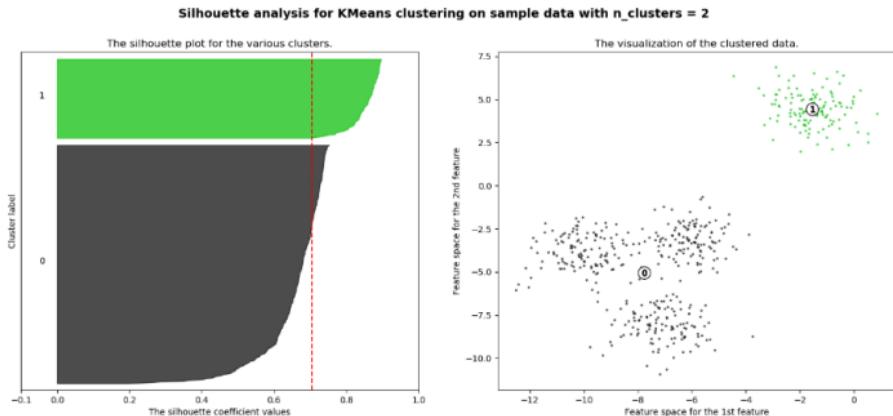


Fig. from [Scikit-learn doc.](#)

Choose the number K of clusters

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Check the silhouette score

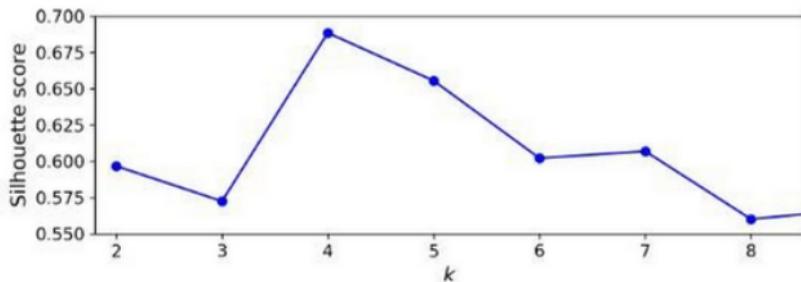


Figure 9-9. Selecting the number of clusters k using the silhouette score

Take $k = 4$ in the example.

Fig. From [Ger19]

Limits of K-means clustering

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It can only find “spherical clusters”, all with the same size.
Otherwise you need to resort to other approaches (like DBSCAN)

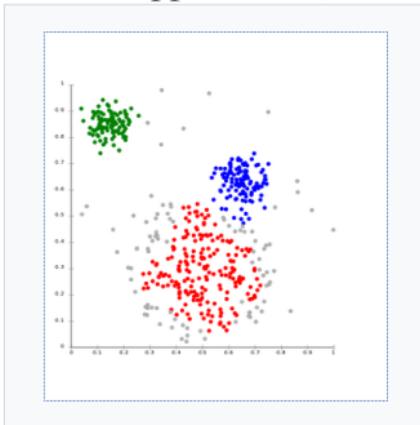
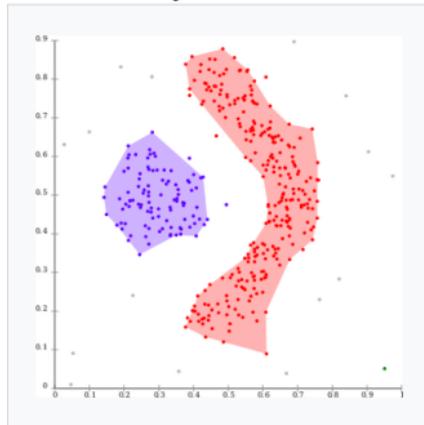


Fig. from [Wikipedia](#), User:Chire.

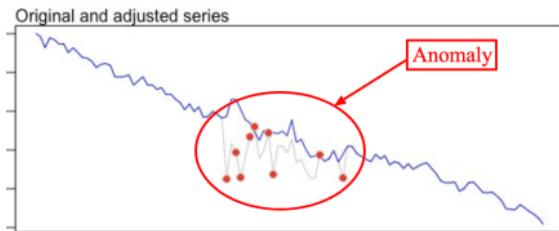
Section 2

Anomaly detection

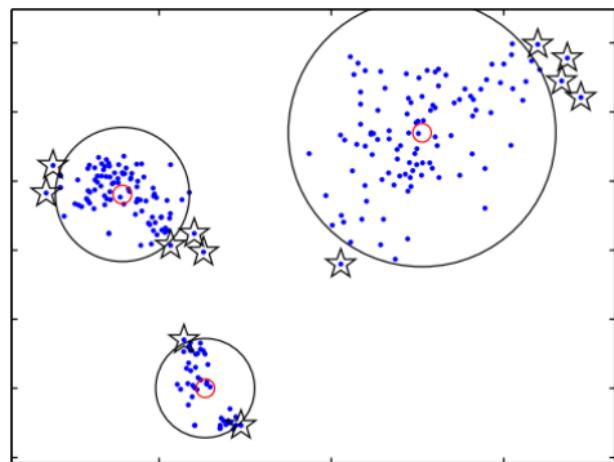
Anomaly: A sample that is not “normal” = outlier.

Causes:

- Intrusion or Fraud
- Sensor measurement errors
- Fault or Damage
- Unpredictable event (accident)



Credits to [Tiunov](#)



From [KH08]

Supervised methods:

- Training set with samples labeled as “normal”, “anomaly type 1”, , “anomaly type 2”

What if a new anomaly occurs, never seen before?

Supervised methods:

- Training set with samples labeled as “normal”, “anomaly type 1”, , “anomaly type 2”

What if a new anomaly occurs, never seen before?

Unsupervised methods:

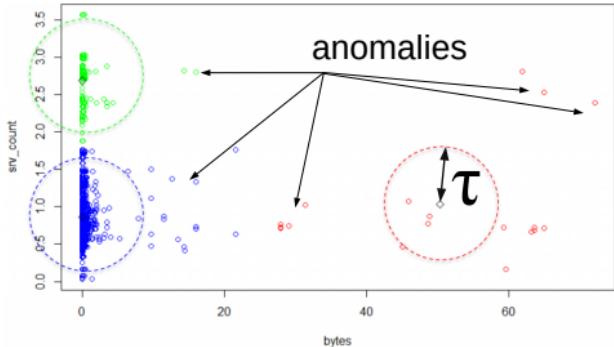
- Clustering
- Isolation Forests
- Neural Networks
 - Auto-Encoders
 - Self-organizing map

Anomaly detection with K-means clustering

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- Find K clusters
- **Anomaly score** $s(\mathbf{x}^{(i)})$: distance to the closest centroid
 - Don't confuse it with the silhouette score.
- If $s(\mathbf{x}^{(i)}) > \tau \implies \mathbf{x}^{(i)}$ is an anomaly

To know more: [\[HKF04\]](#)



Anomaly detection with K-means clustering

29 / 50

- Find K clusters
- **Anomaly score** $s(\mathbf{x}^{(i)})$: distance to the closest centroid
 - Don't confuse it with the silhouette score.
- If $s(\mathbf{x}^{(i)}) > \tau \implies \mathbf{x}^{(i)}$ is an anomaly

To know more: [HKF04]

Variation:

Clusters with few samples are also considered anomalies.

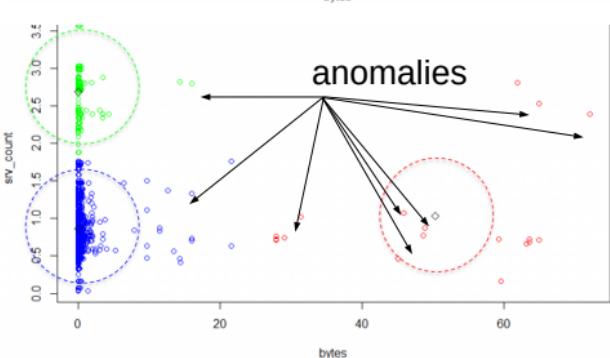
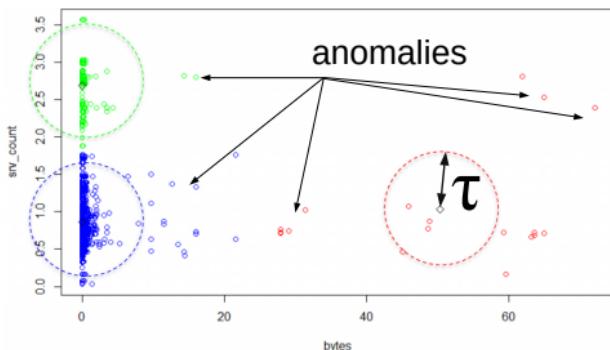
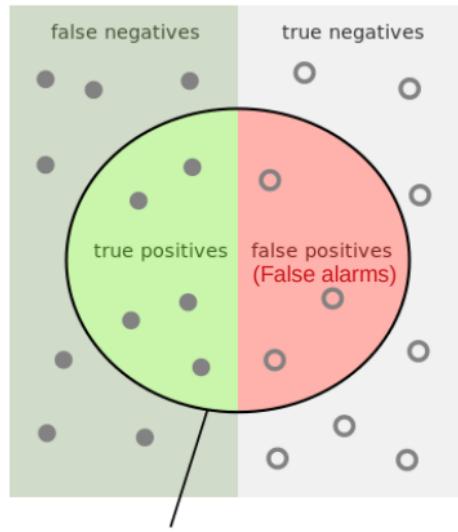


Fig. from Keppel and Schmalz.

Precision and Recall

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True anomalies



Alarms

Among the alarms,
how many are the
true anomalies?

$$\text{Precision} = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

Among the
anomalies,
how many we found?

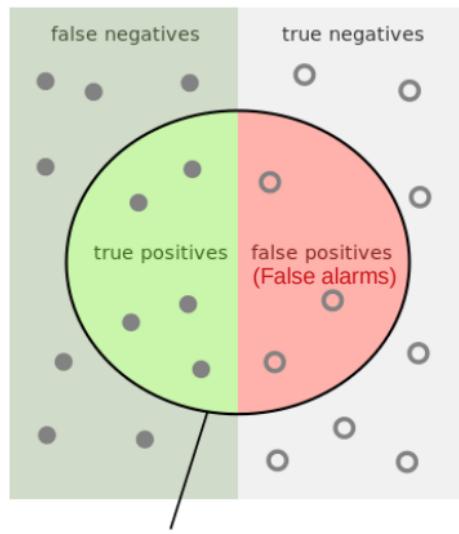
$$\text{Recall} = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$

Figs. from [Wikipedia](#) and [Walber \(Wikipedia\)](#), modified.

Precision and Recall

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True anomalies

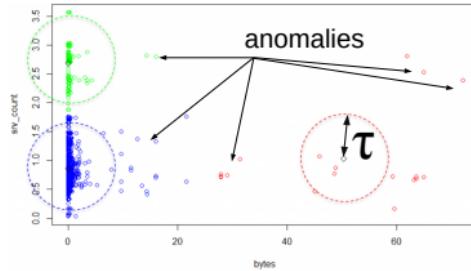


Among the alarms,
how many are the
true anomalies?

$$\text{Precision} = \frac{\text{True Positives}}{\text{True Positives} + \text{False Positives}}$$

Among the
anomalies, how
many we found?

$$\text{Recall} = \frac{\text{True Positives}}{\text{True Positives} + \text{False Negatives}}$$

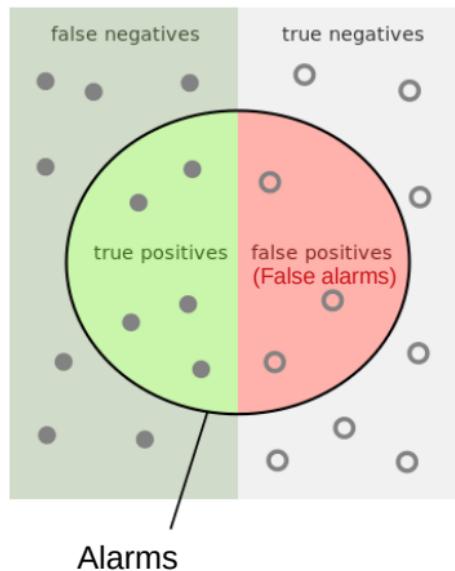


$\tau \nearrow \Rightarrow$ precision \nearrow , recall \searrow
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Precision and Recall

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True anomalies

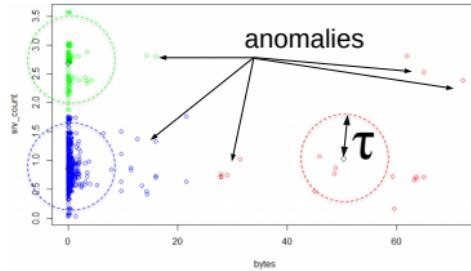


Among the alarms,
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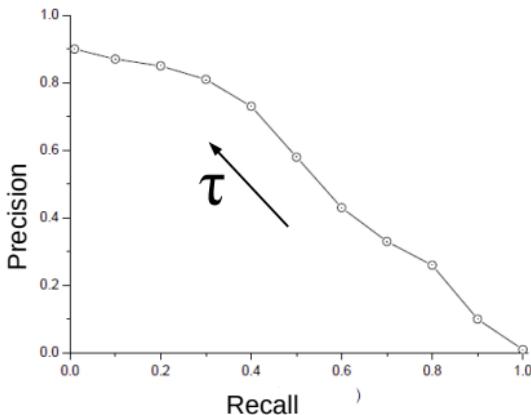
$$\text{Precision} = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

Among the
anomalies, how
many we found?

$$\text{Recall} = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$



$\tau \nearrow \Rightarrow \text{precision} \nearrow, \text{recall} \searrow$
 $\tau \searrow \Rightarrow \text{precision} \searrow, \text{recall} \nearrow$



Figs. from [Wikipedia](#) and [Walber \(Wikipedia\)](#), modified.

Precision-Recall Curve

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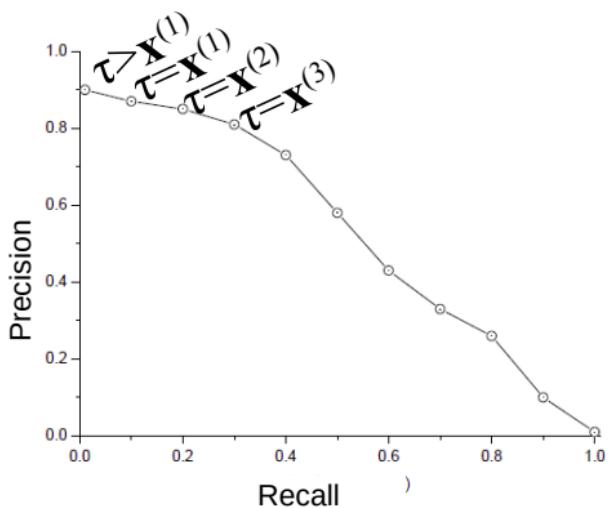
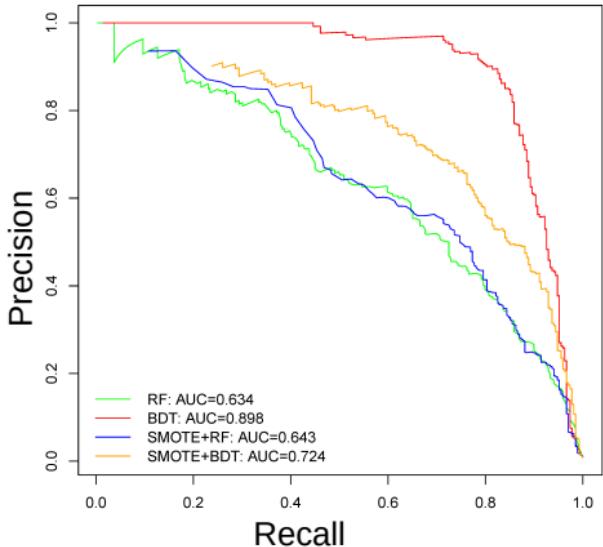


Fig. from [Wikipedia](#).

To build the curve with K -means clust.:

- K-means clustering
- Compute anomaly score $s(\mathbf{x}^{(i)})$
(nothing to do with silhouette!)
- Order $\mathbf{x}^{(i)}$ from the highest to the lowest $s(\mathbf{x}^{(i)})$
- Compute Pr. and Re. when anomaly is $\mathbf{x}^{(1)}$
- Compute Pr. and Re. when anomalies are $\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \dots$
- Compute Pr. and Re. when anomalies are $\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \mathbf{x}^{(3)} \dots$
- ...

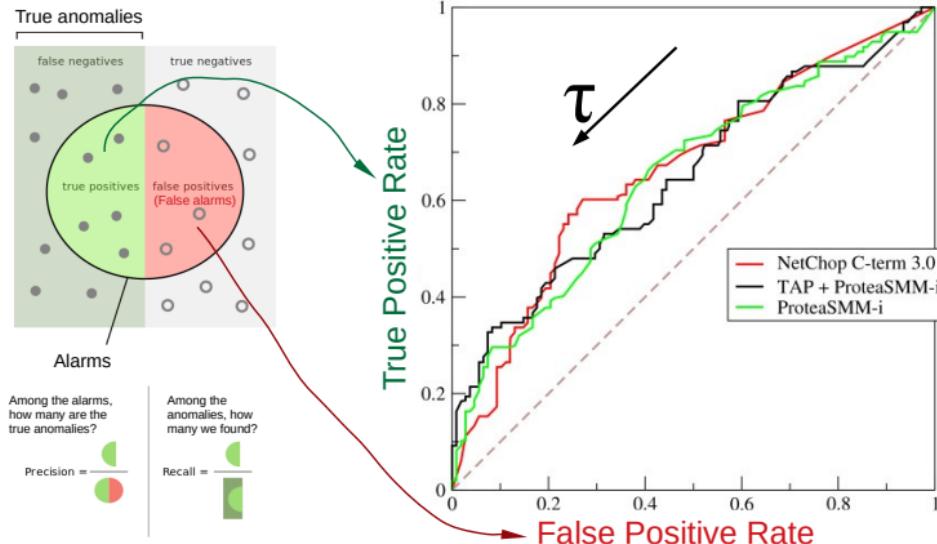


In this figure:

- Each curve represents a different anomaly detection method
- Each point represents an anomaly detector
- **Area Under the Curve (AUC):** quality of a method

Fig. from [LC19].

Receiver-Operating Characteristic (ROC) Curve



Right Fig. from
[Wikipedia](#)

$$\text{True Positive Rate} = \underbrace{TP / (TP + FN)}_{\text{All positives}} = \text{Recall}$$

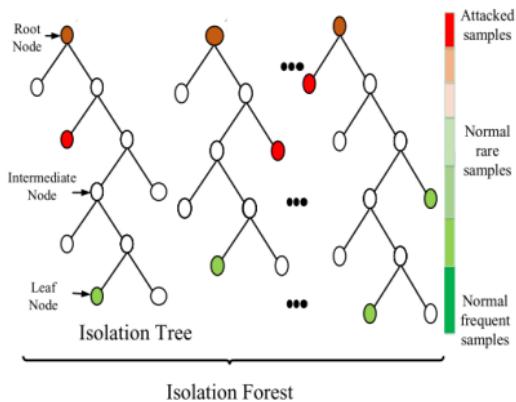
$$\text{False Positive Rate} = \underbrace{FP / (FP + TN)}_{\text{All negatives}}: \text{Probability of False Alarms.}$$

Isolation Forest

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Assumption:

- The samples that isolate immediately are very different from the others
⇒ anomalies



From [ALHK19]

Train an extra-tree

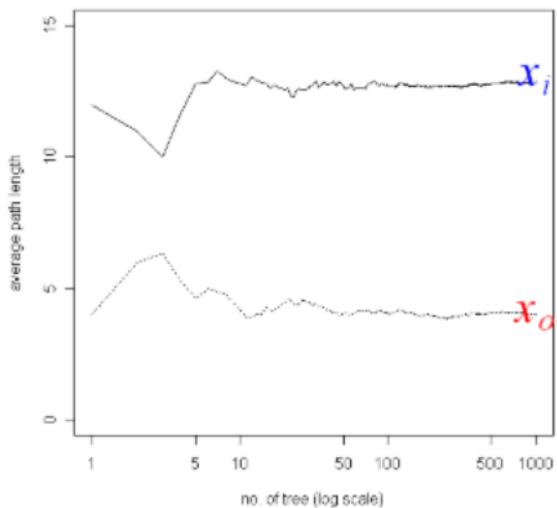
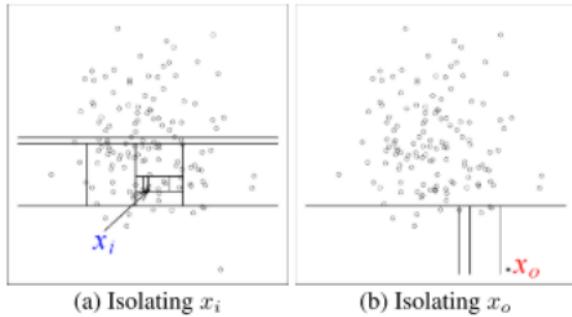
- No need to compute impurity metrics
⇒ No labels needed

Compute sample scores (simplified):

- P : average tree depth
- $h(\mathbf{x}^{(i)})$: path length
Depth of the leaf in which the sample falls, averaged across all trees
- $s(\mathbf{x}^{(i)}) = 2^{-\frac{h(\mathbf{x}^{(i)})}{P}}$

Isolation Forest

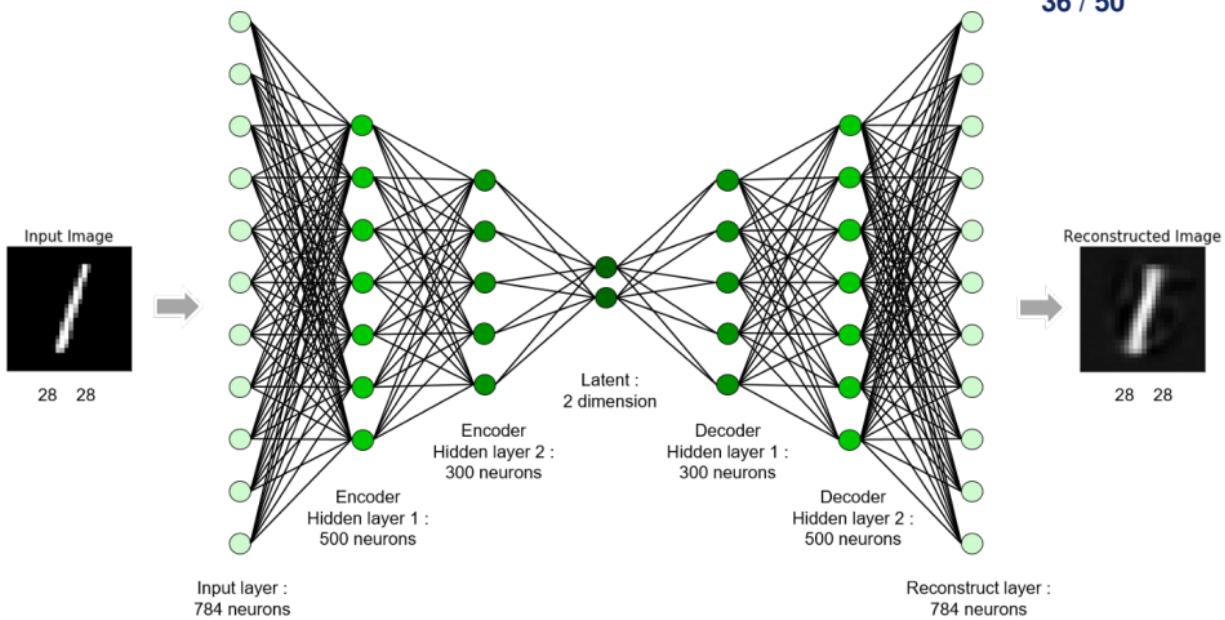
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From [TMZ08]

Autoencoder

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From medium.com
Autoencoder:

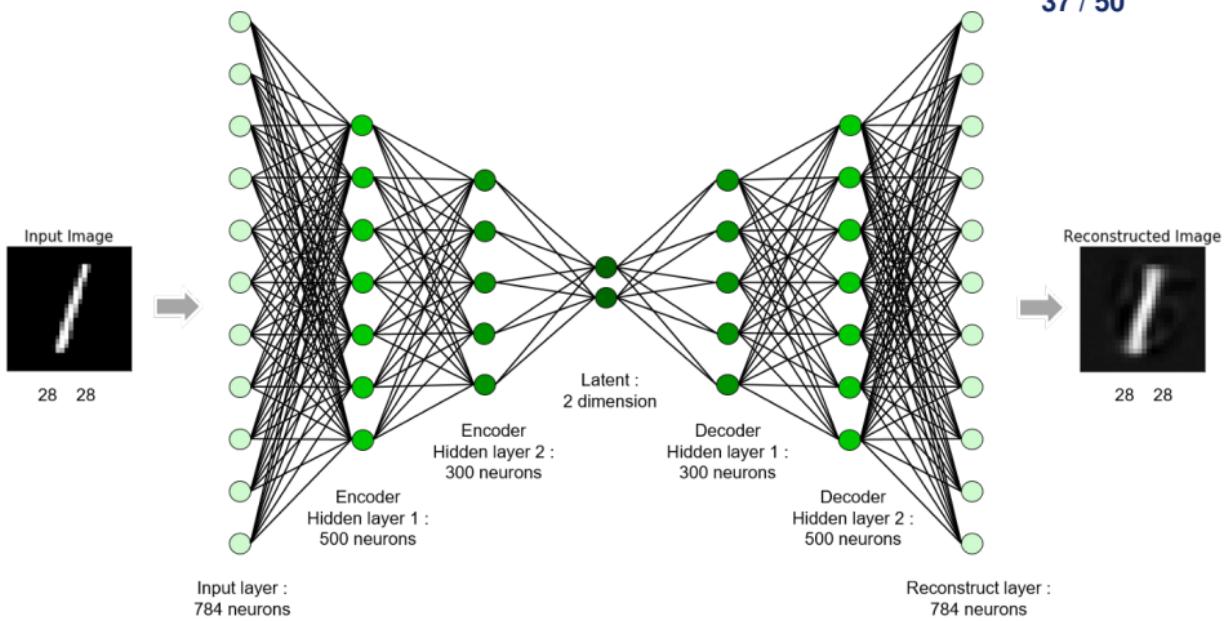
- Symmetric NN: num of outputs = num of features
- Train the NN to produce output \simeq input:

$$J(\theta, \mathbf{x}^{(i)}) = \|\mathbf{x}^{(i)} - h_{\theta}(\mathbf{x}^{(i)})\|^2$$

- Bottleneck: to “compress” the information in fewer neurons

Autoencoder for anomaly detection

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From [medium.com](#)

Assumption:

- Normal samples are the majority
- \implies NN learns to reconstruct normal samples
- \implies and fails to reconstruct anomalous samples
- \implies anomalies are not compressible!

Score = reconstruction error:

$$s(\mathbf{x}^{(i)}) = \|\mathbf{x}^{(i)} - h_{\theta}(\mathbf{x}^{(i)})\|^2$$

Self-Organizing Map (SOM)

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Characteristics:

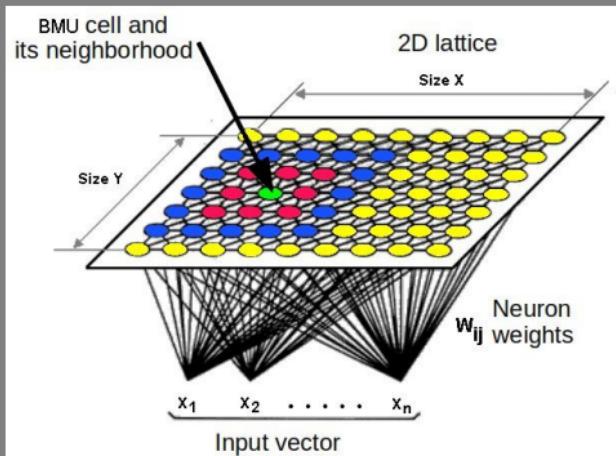
- NN with one layer only
- M neurons, disposed as a square.
- Each feature is connected to all neurons
- θ_q : weight of the q -th neuron.

Output:

- For each $\mathbf{x}^{(i)}$, the best matching unit (neuron) is activated

$$\text{bmu}(\mathbf{x}^{(i)}) = \arg \min_q \|\mathbf{x}^{(i)} - \boldsymbol{\theta}_q\|^2$$

- Dimensionality reduction: we describe all the samples with fewer neurons



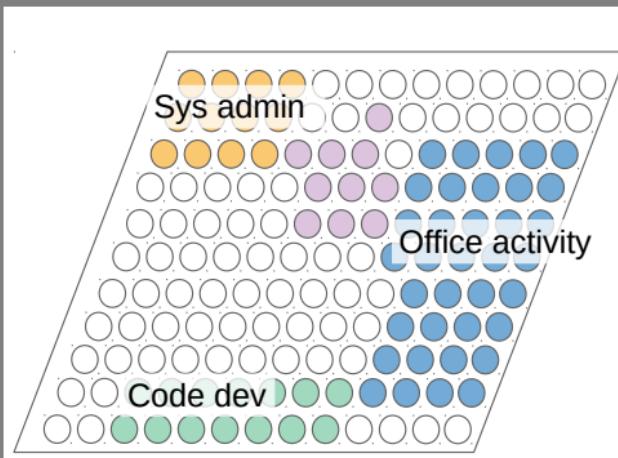
From [BD13]

Training:

- For each $\mathbf{x}^{(i)}$, find the best matching unit (bmu) q
- Modify θ_q in order to get closer to $\mathbf{x}^{(i)}$
- Modify also the weight of the neighbors of q

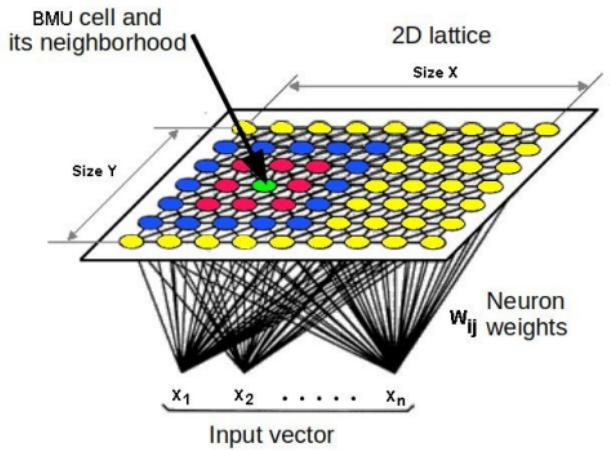
After training, similar $\mathbf{x}^{(i)}$ tend to activate close units

- Each cluster of samples corresponds to a region of the map



Anomaly detection with SOMs

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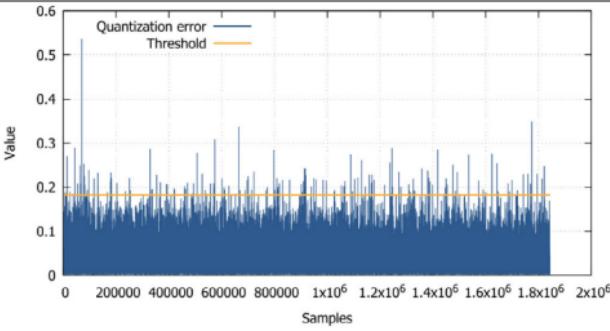
- A SOM compresses the information of a dataset into few neuron weights (similar to auto-encoders).
- A SOM is trained to compress well the majority of samples (normal)
- The error is large with anomalies.

$$q^* = \text{bmu}(\mathbf{x}^{(i)})$$

Quantization error:

$$s(\mathbf{x}^{(i)}) = ||\mathbf{x}^{(i)} - \Theta_{q^*}||^2$$

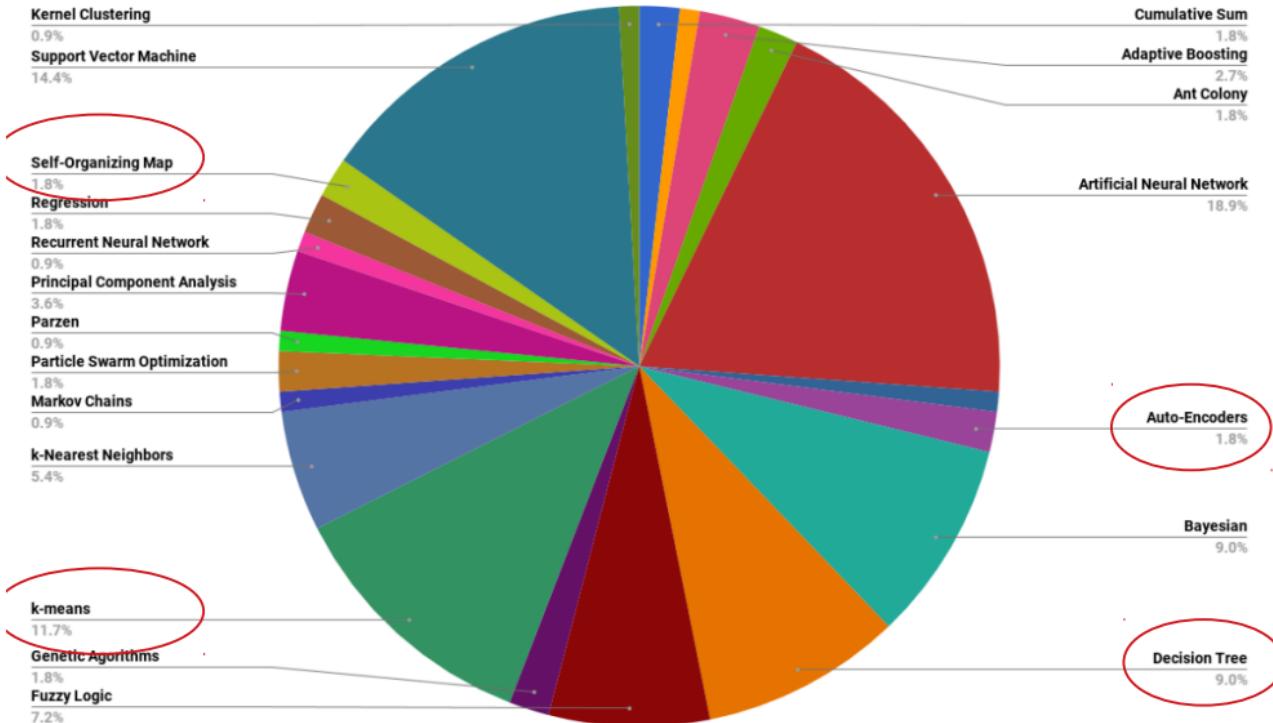
From [BD13]



From [VBMN18]

Different methods

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From [HBB⁺18]

Applications to networks

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Goal	Features	Method	Reference
Discover insider threat	Computer activity from logs	Deep NN, Recurrent NN	[TKH ⁺ 17]
Discover Network Intrusion	IP and TCP connection info	Almost all	A lot
Find malicious sensors	Link delays	SOM	[WWW ⁺ 13]
Find smart energy grid meters reporting wrong measurements	Electric measures	iForests	[ALHK19]
Predictive Maintenance: Predict which turbine is going to fail	Recordings of rotation speeds	SOM	[VBMN18]
Anomalous electric signals	Time series of signals	KMeans	Amid Fish blog

Unsupervised approach:

- Form clusters or forests or train NN on all the dataset \mathcal{D} (normal + anomaly)
- Compute the score $s(\mathbf{x})$, $\forall \mathbf{x} \in \mathcal{D}$
- If $s(\mathbf{x}) > \tau \implies$ anomaly

Semi-supervised approach:

- Form clusters or forests or train NN on only normal samples
- When a new sample \mathbf{x} arrives, compute the score $s(\mathbf{x})$
- If $s(\mathbf{x}) > \tau \implies$ anomaly

Note: You need to have **samples labeled as normal**.

Supervised approach:

- Classify in normal / anomaly
- You can also classify anomaly types

Note: You need to have a training set with **all** samples labeled.

Unsupervised approach:

- Form clusters or forests or train NN on all the dataset \mathcal{D} (normal + anomaly)
- Compute the score $s(\mathbf{x})$, $\forall \mathbf{x} \in \mathcal{D}$
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Semi-supervised approach:

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Supervised approach:

- Classify in normal / anomaly
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Note

The unsupervised and semi-supervised approaches assume **anomalies are a minority** (less than 1%).

Not always true (Denial of Service attack)

- Hyper-parameters to tune:

In K -means clustering:

- K
- The distance function (Euclidean, Manhattan, Minkowski, etc.)

In iForests

- Number of trees

In autoencoders

- The NN architecture

...

In general

- The score threshold τ to recognize anomalies

- We compute Precision, Recall, ROC Curve, etc, based on **ground truth**

To avoid **data leakage**:

- Split the dataset in training/test data
- Choose the hyperparameters only based on training data
- Check the performance on test data

- Anomaly Detection in Telecommunications by Valentina Djordjevic, [Video](#)
- Jan van der Vegt: A walk through the isolation forest | PyData Amsterdam 2019, [Video](#).
- Johnson, R.A. and Wichern, D.W. (2002). Applied Multivariate Statistical Analysis, 5th ed. Prentice Hall [Sections 12.1, 12.2, 12.3 and 12.4](#)
- Isolation Forest: original paper [[TMZ08](#)] (1062 citations)
- Anomaly Detection with Robust Deep Autoencoders [[ZP17](#)]

Unsupervised Learning: Clustering

- K-means clustering

Unsupervised Learning: Dimensionality reduction (next class)

Anomaly detection

- k-means anomaly detection
- Isolation Forests
- Neural Networks: Autoencoders

-  Saeed Ahmed, Youngdoo Lee, Seung Ho Hyun, and Insoo Koo, *Unsupervised Machine Learning-Based Detection of Covert Data Integrity Assault in Smart Grid Networks Utilizing Isolation Forest*, IEEE Transactions on Information Forensics and Security **14** (2019), no. 10, 2765–2777.
-  Juan Carlos Burguillo and Bernabe Dorronsoro, *Using Complex Network Topologies and Self-Organizing Maps for Time Series Prediction*, Advances in Intelligent Systems and Computing (2013).
-  Marie Chavent, *Clustering methods - Lecture Notes*, Université de Bordeaux.
-  Aurelien Geron, *Hands-On Machine Learning with Scikit-Learn, Keras, and TensorFlow*, O'Reilly, 2019.

-  Gaurang Gavai, Kumar Sricharan, Dave Gunning, John Hanley, Mudita Singhal, and Rob Rolleston, *Supervised and unsupervised methods to detect insider threat from enterprise social and online activity data*, Journal of Wireless Mobile Networks, Ubiquitous Computing, and Dependable Applications **6** (2015), no. 4, 47–63.
-  Hanan Hindy, David Brosset, Ethan Bayne, Amar Seeam, Christos Tachtatzis, Robert Atkinson, and Xavier Bellekens, *A Taxonomy and Survey of Intrusion Detection System Design Techniques, Network Threats and Datasets*, no. June.
-  Ville Hautamaki, Ismo Karkkainen, and Pasi Franti, *Outlier Detection Using k-Nearest Neighbour Graph*, IAPR International Conference on Pattern Recognition (ICPR), 2004.
-  Gareth James, Daniela Witten, Trevor Hastie, and Robert Tibshirani, *An introduction to Statistical Learning*, vol. 7, 2013.

-  Pekka Kumpulainen and Kimmo Hätönen, *Local anomaly detection for mobile network monitoring*, Information Sciences **178** (2008), no. 20, 3840–3859.
-  Sunbok Lee and Jae Young Chung, *The machine learning-based dropout early warning system for improving the performance of dropout prediction*, MDPI Applied Sciences **9** (2019), no. 15.
-  Aaron Tuor, Samuel Kaplan, Brian Hutchinson, Nicole Nichols, and Sean Robinson, *Deep learning for unsupervised insider threat detection in structured cybersecurity data streams*, Artificial Intelligence for Cyber-Security, 2017, pp. 224–234.
-  Fei Tony Liu, Kai Ming Ting, and Zhi-Hua Zhou, *Isolation Forest*, EEE International Conference on Data Mining, 2008.

-  Alexander Von Birgelen, Davide Buratti, Jens Mager, and Oliver Niggemann, *Self-Organizing Maps for Anomaly Localization and Predictive Maintenance in Cyber-Physical Production Systems*, Procedia CIRP **72** (2018), 480–485.
-  Wei Wang, Huiran Wang, Beizhan Wang, Yaping Wang, and Jiajun Wang, *Energy-aware and self-adaptive anomaly detection scheme based on network tomography in mobile ad hoc networks*, Information Sciences **220** (2013), 580–602.
-  Chong Zhou and Randy C. Paffenroth, *Anomaly detection with robust deep autoencoders*, ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, 2017.
-  Fang Zhao, Haizheng Zhang, Francisco Pereira, and Moshe Ben-Akiva, *Clustering - Lecture Notes - Multivariate Data Analysis*, 2017.