

# Plotting, checking, and calibrating Emulators

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[https://github.com/andrewcparnell/intro\\_emulators](https://github.com/andrewcparnell/intro_emulators)

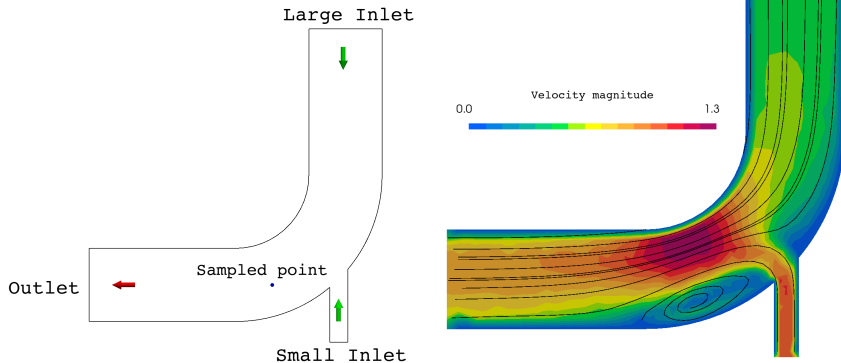
# Introduction

- ▶ We now have a shiny and very fast emulator for our simulator
- ▶ But how do we know whether it works well?
- ▶ In this section we will go through some simple plots that work in both low and high dimensional problems
- ▶ We will then discuss some performance measures that enable us to judge whether the emulator is fitting well or not

It is helpful for this section to revise the use of `ggplot2`; see the [Rafternoon](#) course for a revision class

## Reminder: Navier-Stokes example

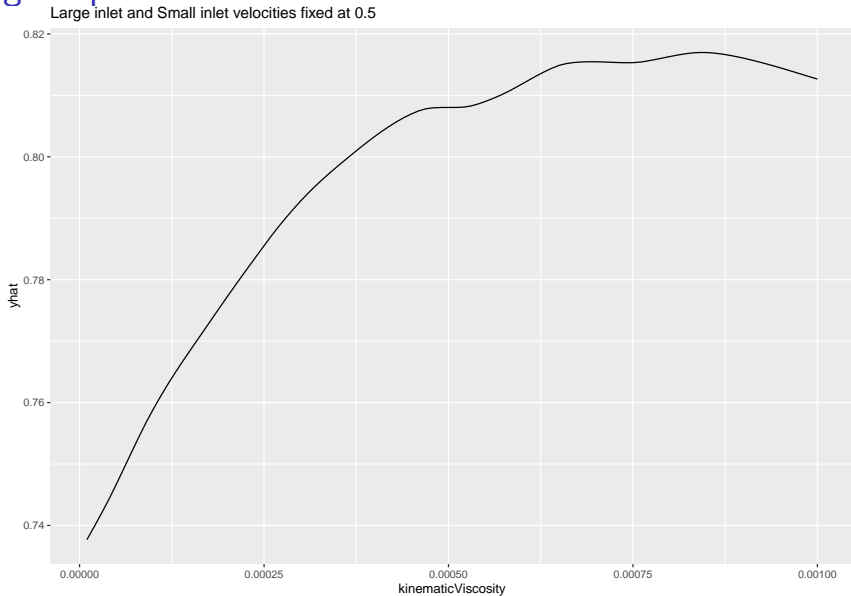
Recall our 2D Navier-Stokes example with 3 inputs and 1 output:



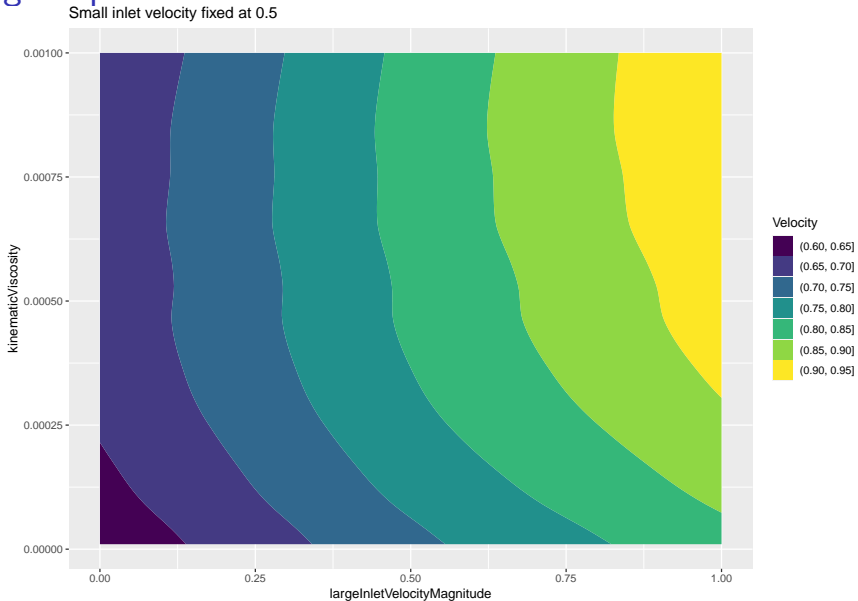
## Plotting the output

- ▶ One way of creating a neat plot is to fix all the variables but one or two
- ▶ We can then produce a plot of the remaining variable(s) changing across its range of values according to the emulator
- ▶ Suppose for example that we were just interested in the variable `kinematicViscosity`, we could fix the others at chosen values (e.g. 0.5) and then predict across the chosen variable
- ▶ We could extend this to look at two dimensions whilst holding the other fixed
- ▶ With further plotting magic we could add slider bars or an animation to look at the effect of changing the input values

# A 1D marginal plot



# A 2D marginal plot

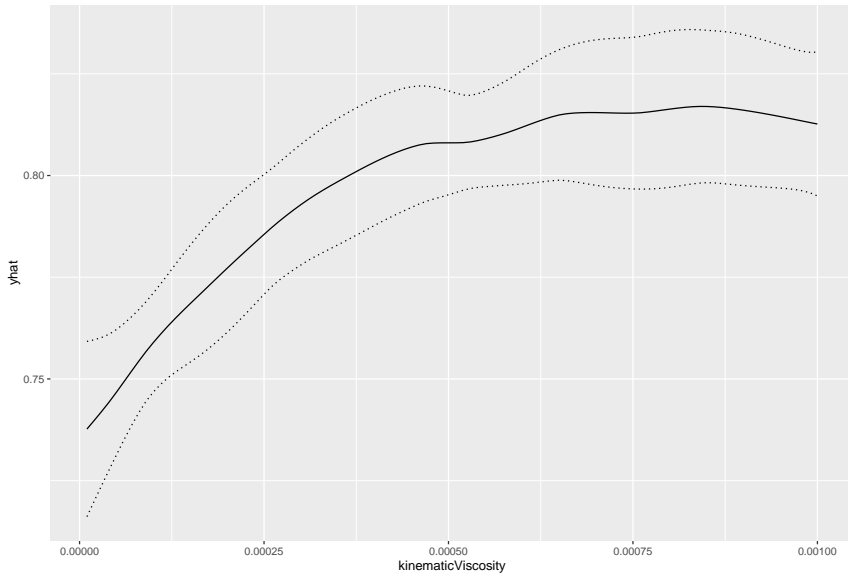


## Further plots

- ▶ These marginal plots give us some idea as to the behaviour of a subset of the variables when others are fixed
- ▶ But the Gaussian Processes also produces an estimate of the error and we can use this too
- ▶ We can plot these alongside the marginal plots to give an idea of places where the emulator is performing poorly

# 1D marginal error plot

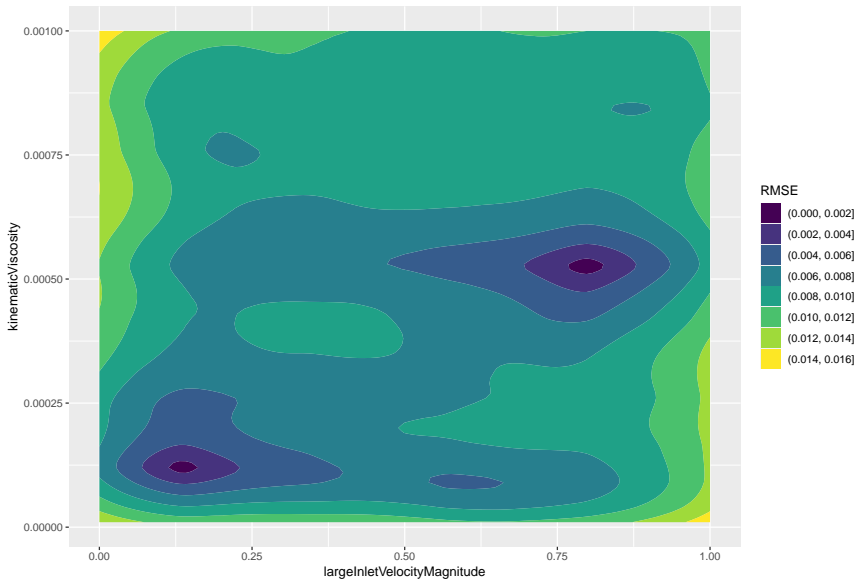
Large inlet and Small inlet velocities fixed at 0.5





## 2D marginal error plot

Small inlet velocity fixed at 0.5



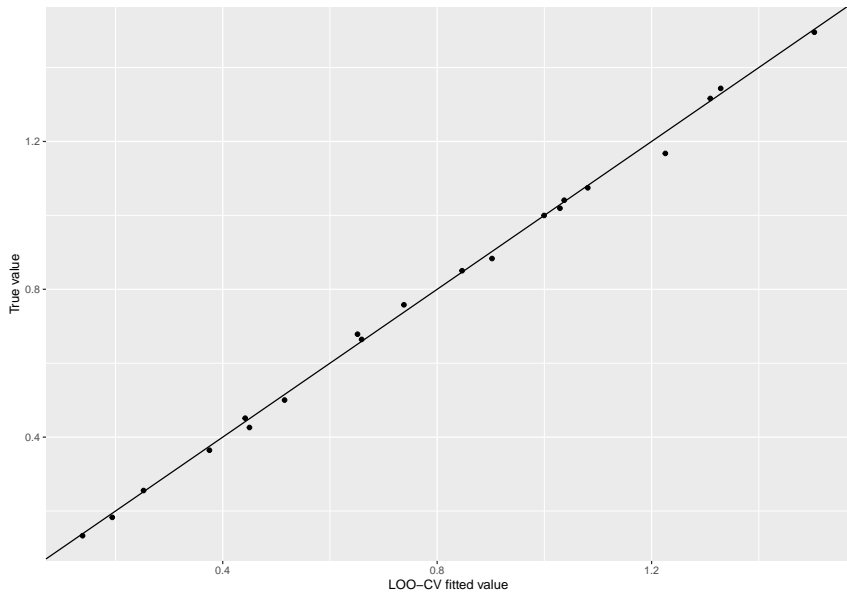
## Cross validation

- ▶ An even better way of judging whether the emulator is working is to use **Cross Validation (CV)**
- ▶ This works by removing some of the data that the model was trained on, re-fitting the emulator, and predicting for the left out observations
- ▶ If the emulator can predict the left out observations well then it is doing a good job
- ▶ We usually plot the predictions from the left out data against the true observations. If they follow an identity relationship then the emulator is working well

## Leave one out CV code

```
loo_fit <- rep(NA, n_runs)
for (i in 1:n_runs) {
  print(i)
  # Fit an emulator with one point missing
  curr_emulator <- GP_fit(
    initial_grid[-i, ],
    df_grid$out[-i]
  )
  # Get the prediction for the missing point
  loo_fit[i] <- predict(
    curr_emulator,
    initial_grid[i, , drop = FALSE]
  )$Y_hat
}
```

## Leave one out CV results



## Calibrating the emulator will real-world observations

- ▶ Sometimes in addition to the emulator values we also have real-world on the process
- ▶ We thus want to check whether the real world data match the emulator and whether there are systematic biases
- ▶ The usual equation people fit is:

$$y(X) = m(X) + \delta(X) + \epsilon$$

- ▶ Where  $X$  are our inputs and  $y$  our output
- ▶  $m$  is the emulator (already fitted)
- ▶  $\delta(x)$  is another GP representing systematic bias
- ▶  $\epsilon$  is a pure noise error term representing observation error
- ▶ You will need to take another module (on Bayesian Modelling) to fit these kind of models!

# Summary

- ▶ We can create marginal 1D and 2D plots to check how well our emulator fits
- ▶ We can also run cross-validation to check out of sample performance
- ▶ Next (and finally): deploying the emulator and making it useful