

1.1)

The machine recognizes any binary string of minimum length 2.

At least two `1` must be input.

Therefore, strings that are not recognized in the alphabet $\{0,1\}^*$ are:

(three dots means repetition of last symbol)

0...

0...1

0...10...

1.2)

\+ means the literal plus symbol, not the “repeat at least once”

As a regex:

$(-|\epsilon)[0-9]+(.[0-9]+)((\backslash+|-)[0-9]+(.[0-9]+)i)$

As “dragon-convention” (the book):

letter $\rightarrow i$

digit $\rightarrow [0-9]$

prefix $\rightarrow (-|\epsilon)$

real $\rightarrow \text{digit}+(\. \text{digit}+)$

midoperator $\rightarrow (\backslash+|-)$

imaginary $\rightarrow \text{real}[i]$

complex_number $\rightarrow (-)?\text{real}(\text{midoperator imaginary})?$

1.3)

A regular language can be accepted by DFAs.

DFA have a finite amount of states and no memory.

Lets assume our DFA has n states, $n \geq 0$.

Regular expressions have properties of Dyck Language: an opening bracket (or parenthesis) must have exactly one matching closing bracket.

Assuming our input is larger than the number of states in our DFA, this means that there exists a state which is reached twice.

Since $(^n$ (opening parenthesis n times) followed by $)^n$ is a valid regular expression, this must mean that the DFA has a loop on opening parenthesis.

However, if we input $(^{n+k}$ (opening parenthesis $n+k$, $k \geq 1$ times), this will still be recognized by the DFA, but since it has no memory, it does not detect that there is an invalid number of parenthesis.

Thus, if a DFA for regular languages existed, it must accept invalid parenthesis matches, which is a contraction. Thus, regular expressions are not regular languages.