



# Sensing Tree Automata as a Model of Syntactic Dependencies

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MOL

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# The Talk in One Minute

## The research program

- ▶ a tight upper bound to the complexity of natural language dependencies?

## In this talk

- ▶ Sensing tree automata as a uniform upper bound
- ▶ MG dependency trees

## Spoilers

- ▶ A (linguistically) natural perspective!
- ▶ Empirically attested restrictions on movement
- ▶ Head-argument relations
- ▶ C-command and licensing conditions

# Outline

**1** Preliminaries

**2** Merge and Move via STA

**3** Licensing Conditions

**4** Conclusion & Open Questions

# Computational Theories of Language

## The subregular program

Can we provide tight complexity characterizations for natural language?

- ▶ Particularly successful in phonology  
(Heinz et al. 2011; Chandlee 2014; Jardine 2016; McMullin 2016; Graf 2017; Graf and Mayer 2018)
- ▶ Some results for syntax
  - ▶ regular tree languages  
(Michaelis 2004; Kobele et al. 2007; Graf 2012)
  - ▶ subregular operations? (Graf 2012, 2018)
  - ▶ subregular dependencies? (Vu 2018; Vu et al. 2019)
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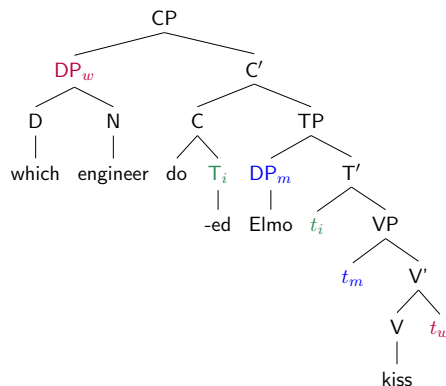
**Can we gain a unified perspective for syntax?**

# Syntax?

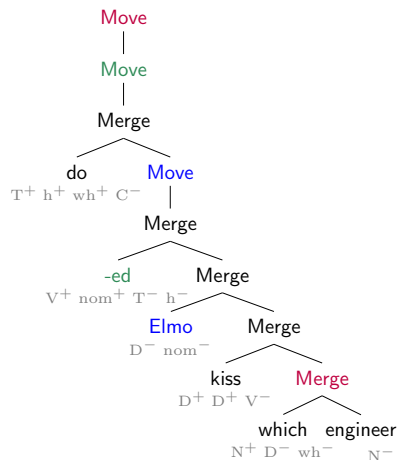
## We need a formal model of syntactic structures.

- ▶ Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- ▶ Operations:
  - ▶ **Merge**  
category feature  $N^{-}$ ,  $D^{-}$ , ...  
selector feature  $N^{+}$ ,  $D^{+}$ , ...
  - ▶ **Move**  
licensee feature  $wh^{-}$ ,  $nom^{-}$ , ...  
licensor feature  $wh^{+}$ ,  $nom^{+}$ , ...
- ▶ Adopt Chomsky-Borer hypothesis:  
Grammar is just a finite list of feature-annotated lexical items
- ▶ The set of derivation trees is a regular tree language.  
(Michaelis 2004; Kobele et al. 2007; Graf 2012)

# MG Syntax: Derivation Trees



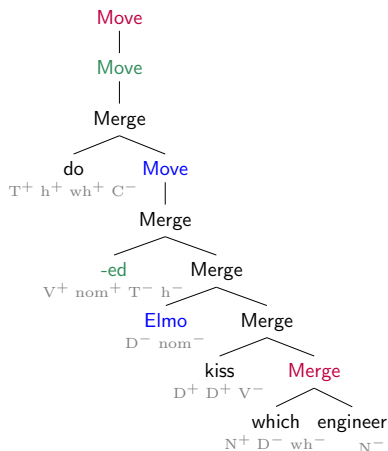
Phrase Structure Tree



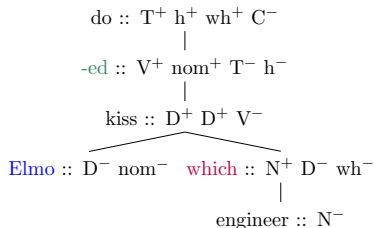
Derivation Tree



# MG Syntax: Dependency Trees



**Derivation Tree**



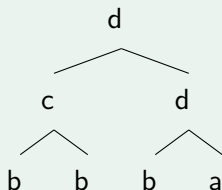
**Dependency Tree**

# Sensing Tree Automata (STA)

## Sensing Tree Automaton (Martens 2006)

Deterministic top-down tree automaton with finite look-ahead of 1.

Example: a *c-commanded* by *c*



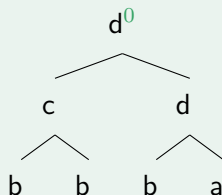
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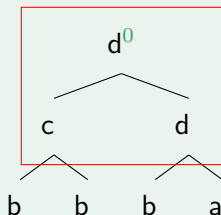
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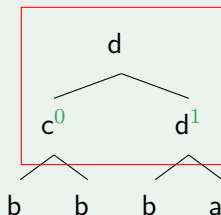
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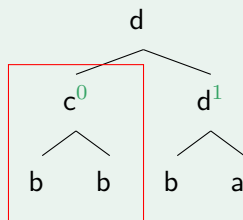
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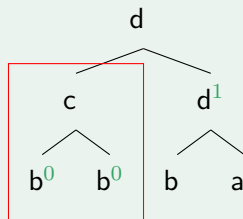
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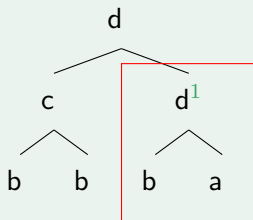
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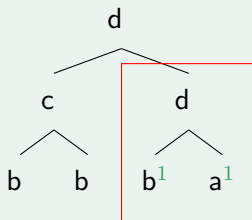


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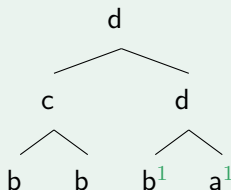
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# Interim Summary

**We are looking for a complexity upper bound for syntax...**

- ▶ MG dependency trees (MDEP)
- ▶ STA

## Upcoming

- ▶  $\text{MDEP}[\textit{merge}] \subsetneq \text{STA}$
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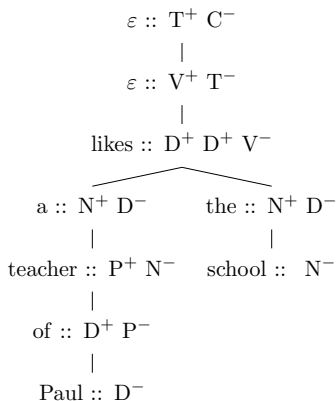
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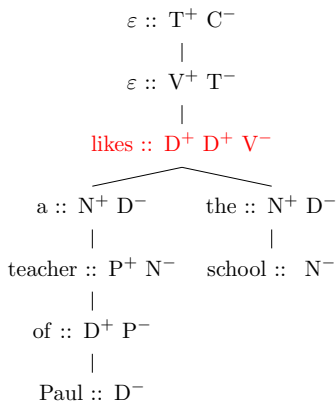
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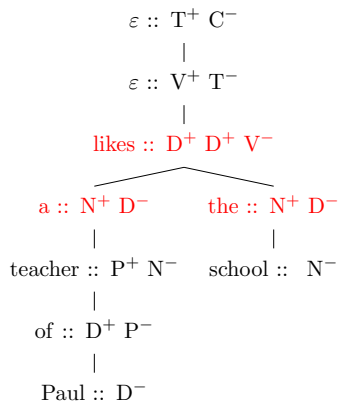
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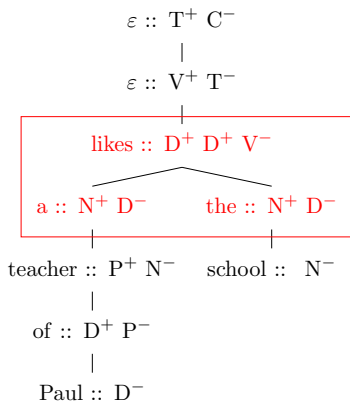
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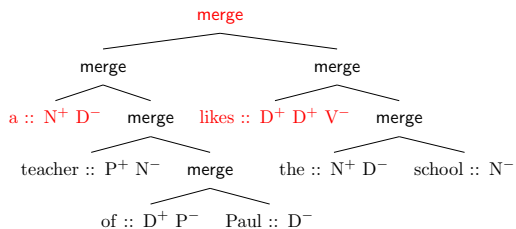
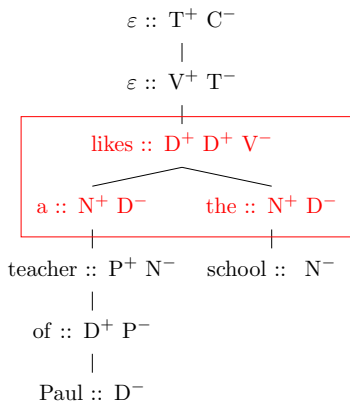


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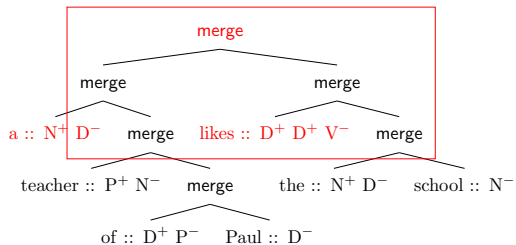
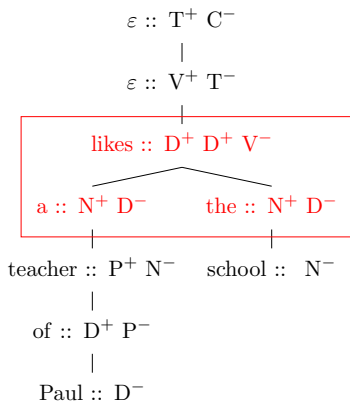




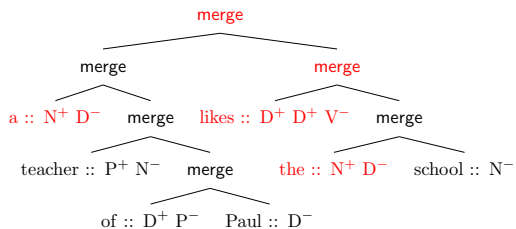
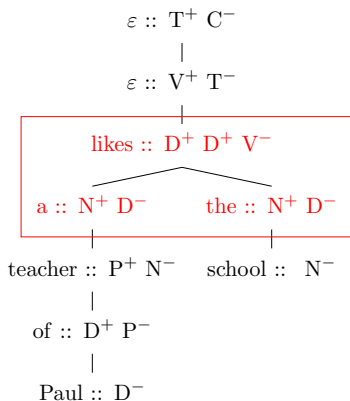
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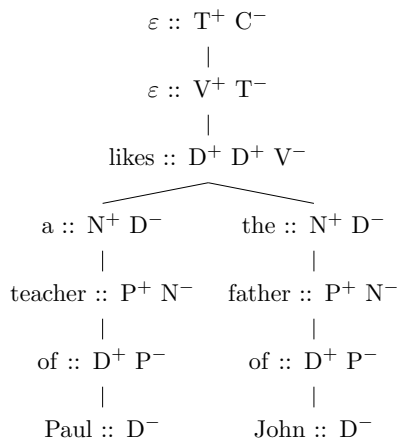
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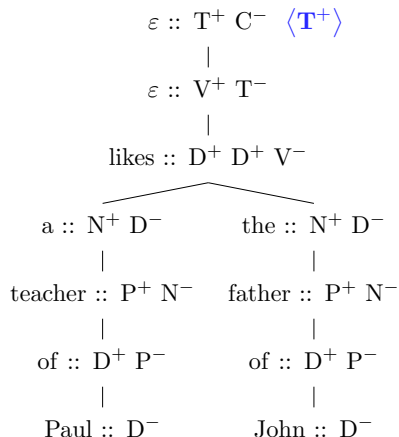
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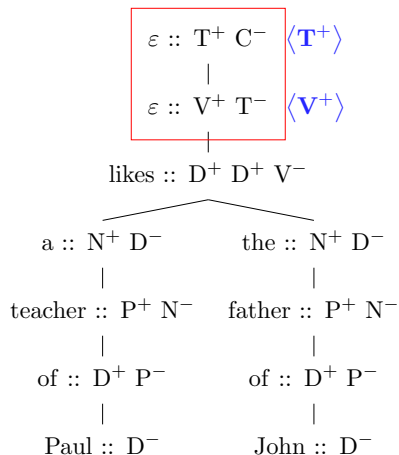
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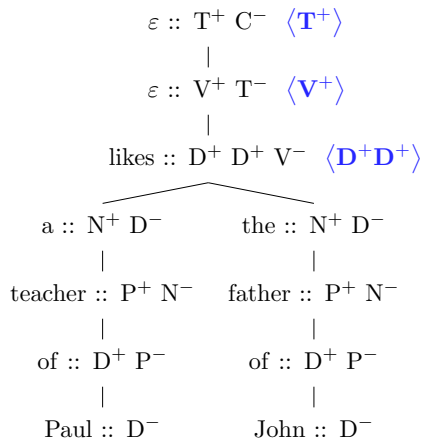
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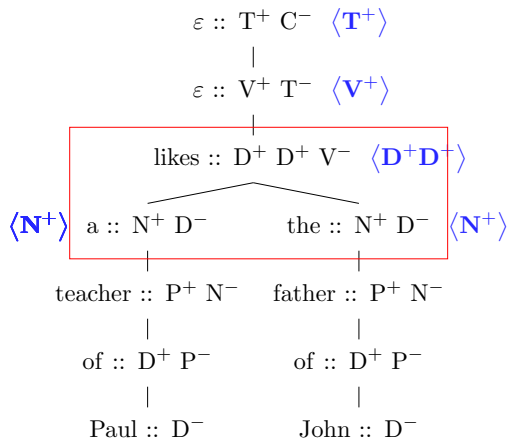
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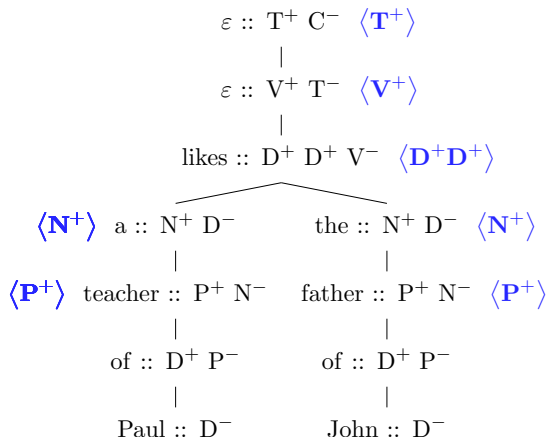


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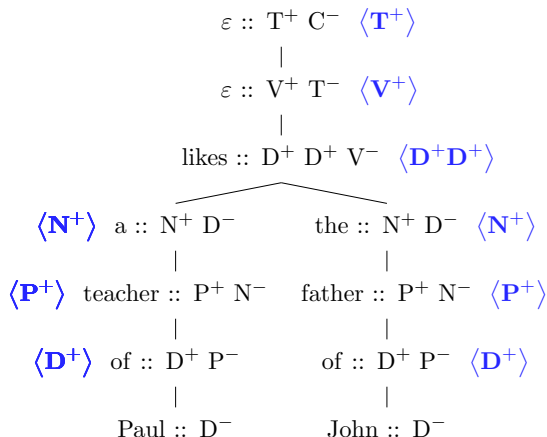




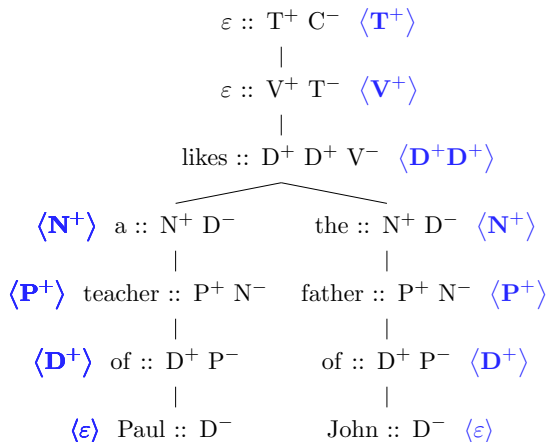
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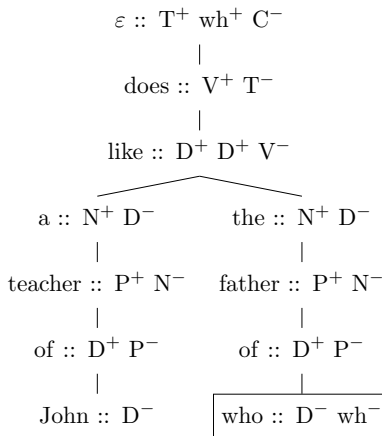
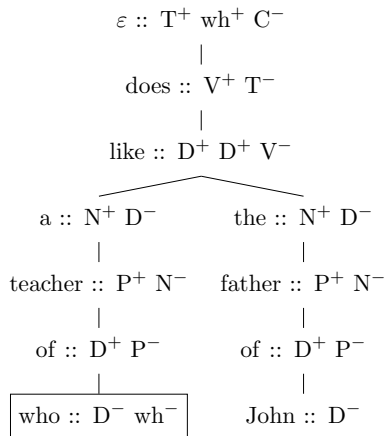
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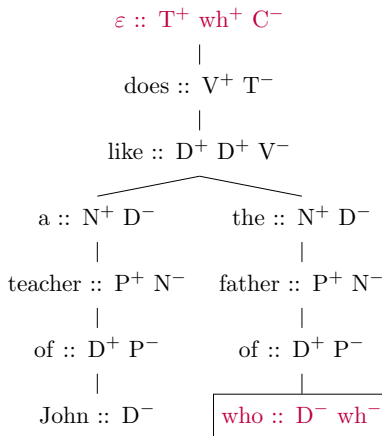
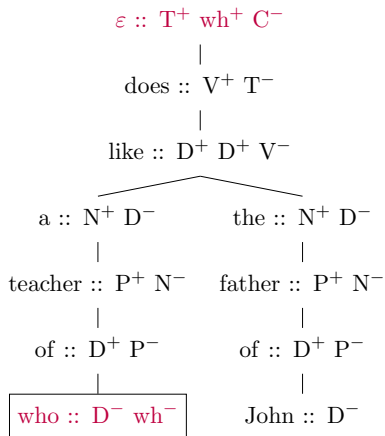
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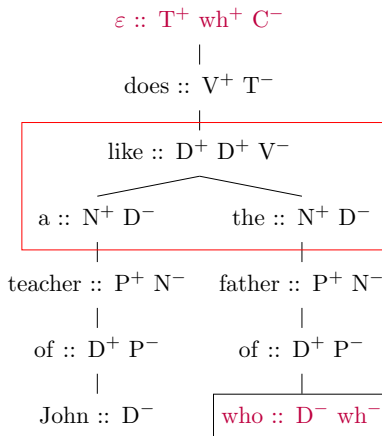
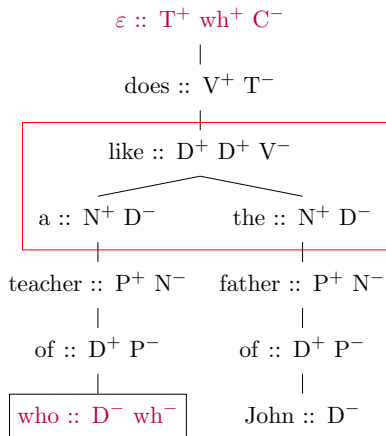
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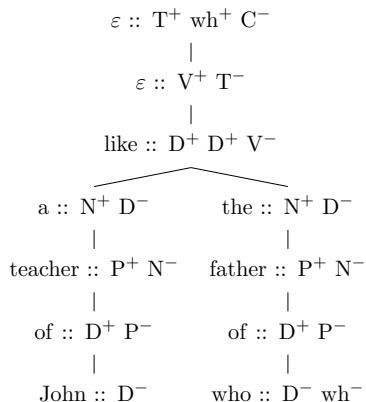


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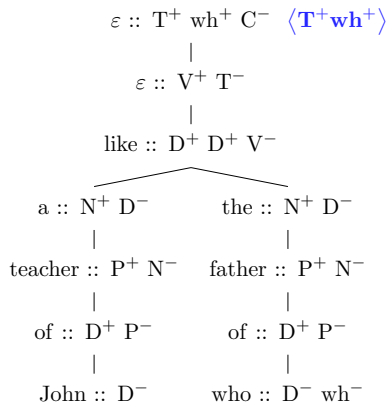
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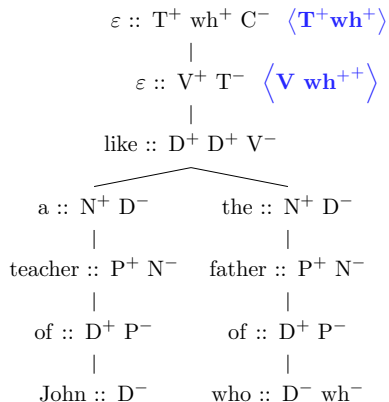
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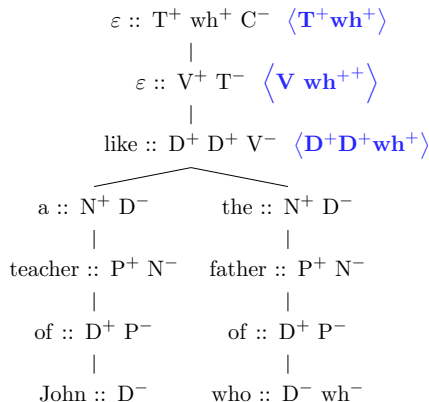
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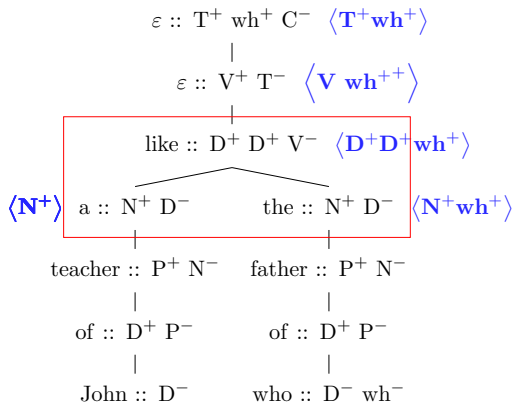
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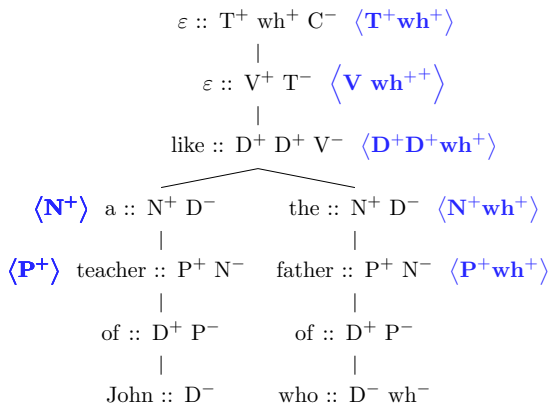
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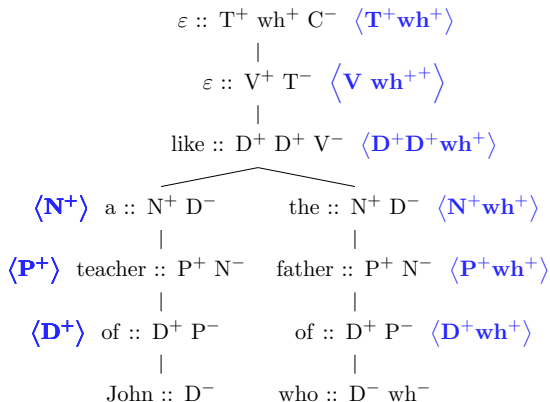
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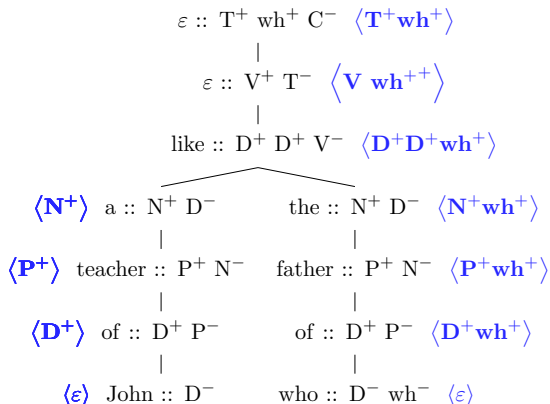
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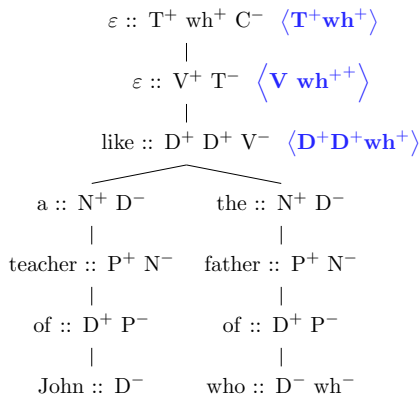
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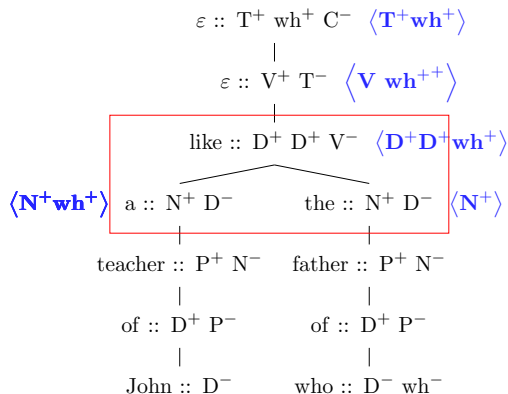
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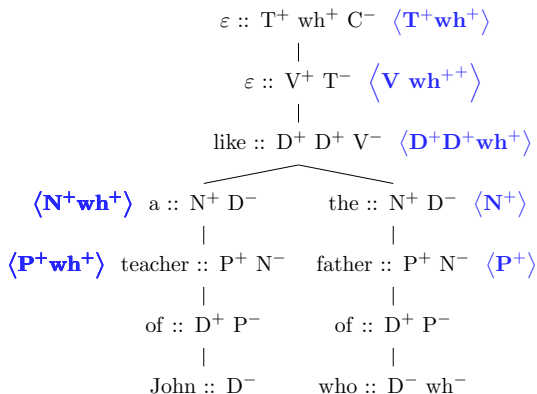
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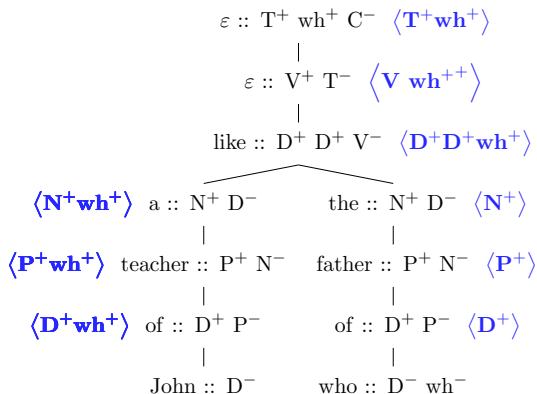
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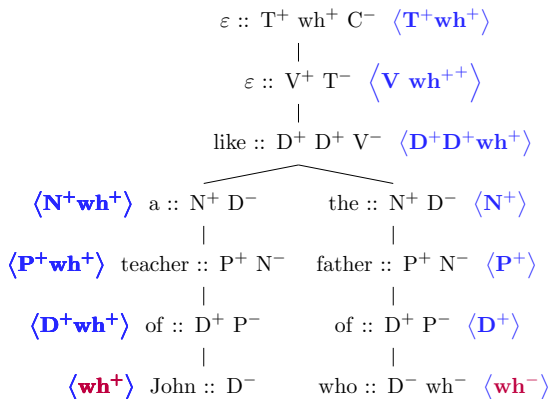
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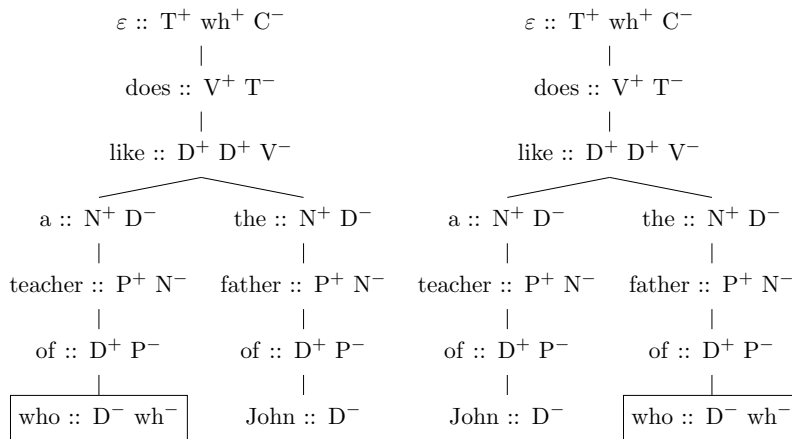


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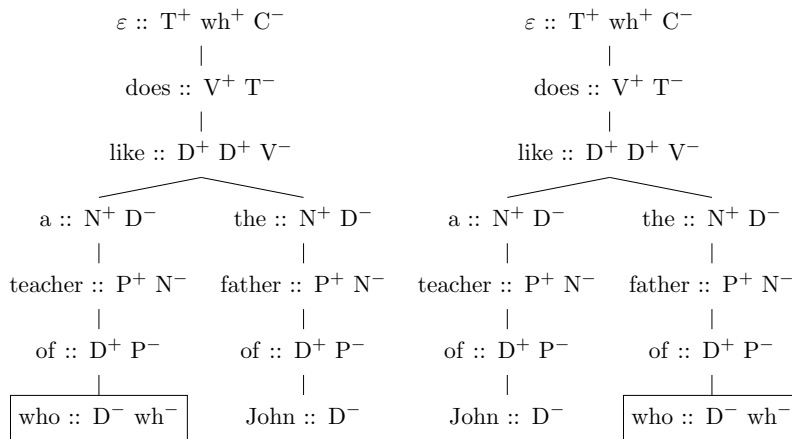
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## The Specifier Island Constraint (SpIC)

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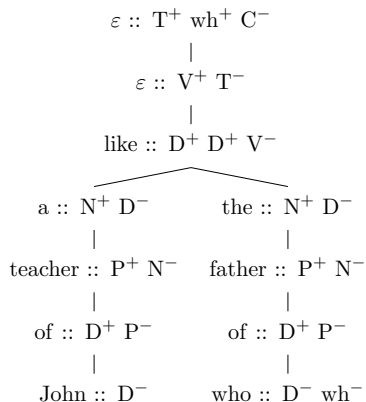


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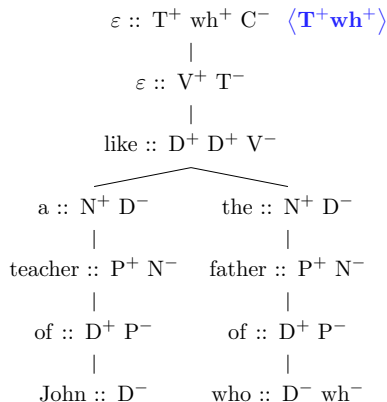
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The **SpIC** guarantees **STA** recognition.



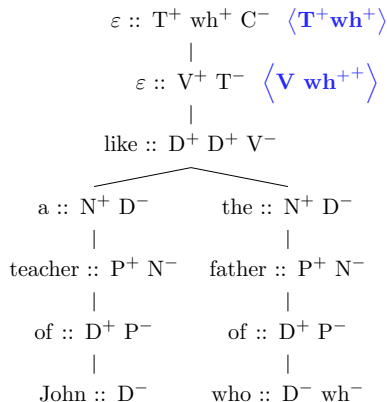
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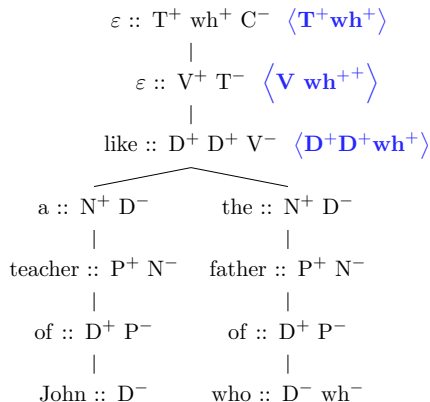
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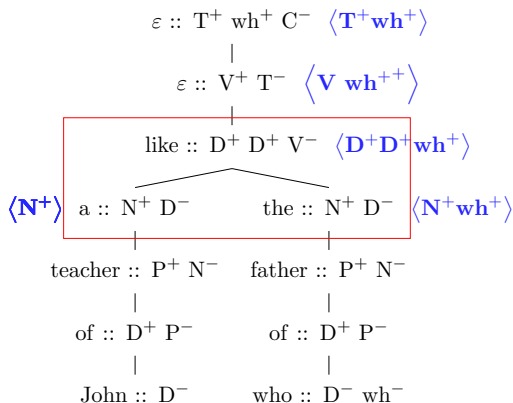
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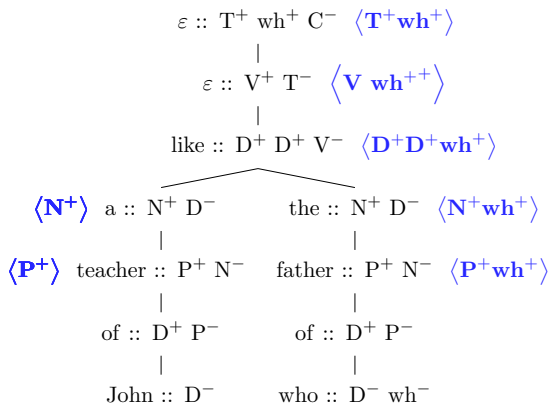
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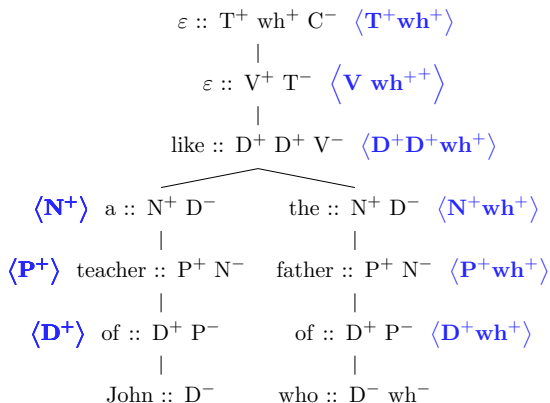
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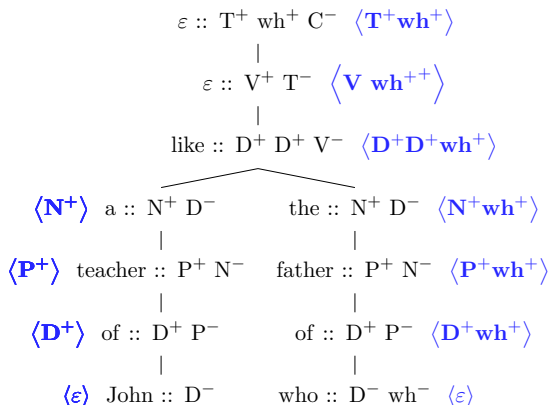
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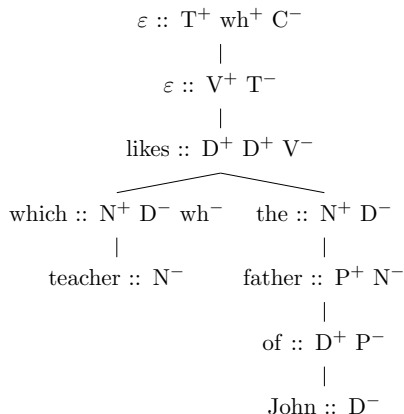
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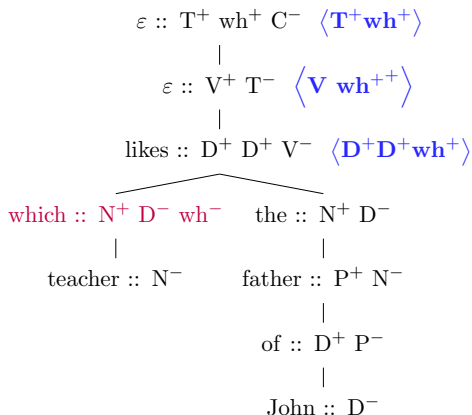
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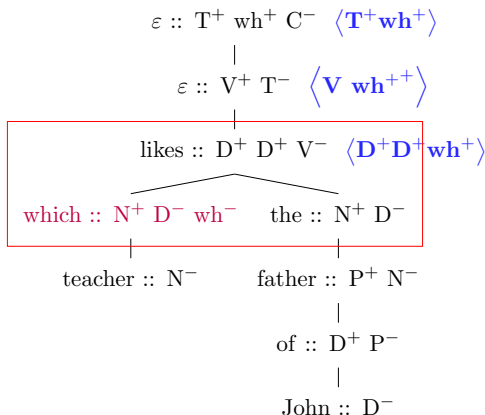
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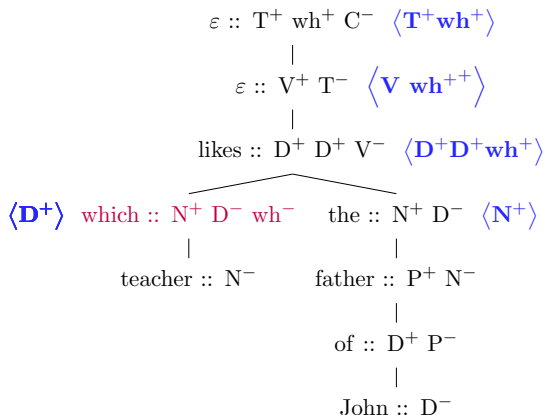
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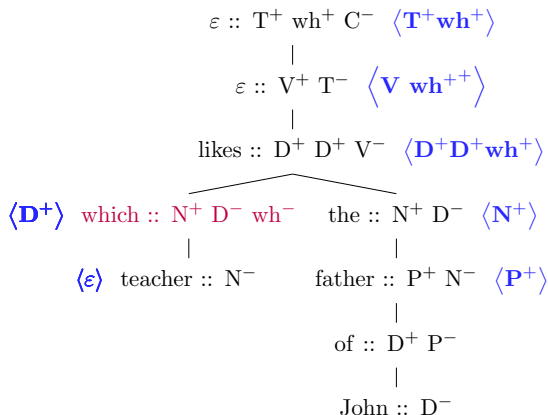
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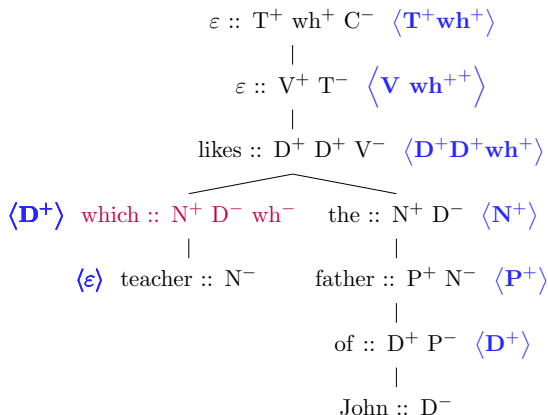
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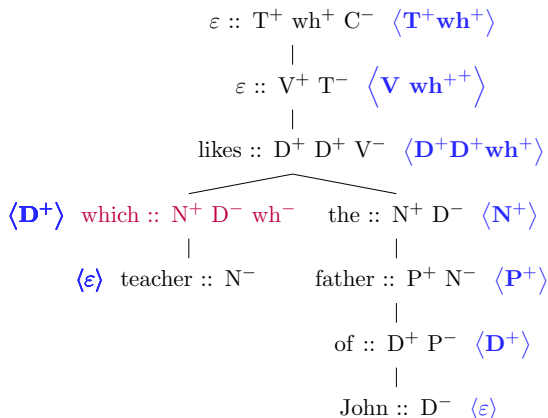
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# Interim Summary [2]

We are looking for a complexity upper bound for syntax...

## The road so far

- ▶  $\text{MDEP}[\text{merge}] \subsetneq \text{STA}$
- ▶  $\text{MDEP}[\text{merge}, \text{move}] \not\subseteq \text{STA}$
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## Syntax is not just about Merge and Move...

### NPI licensing

- 1a) \*Every student said that the train **ever** arrives on time.
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- 2a) \*John said that **Mary** likes **himself**.
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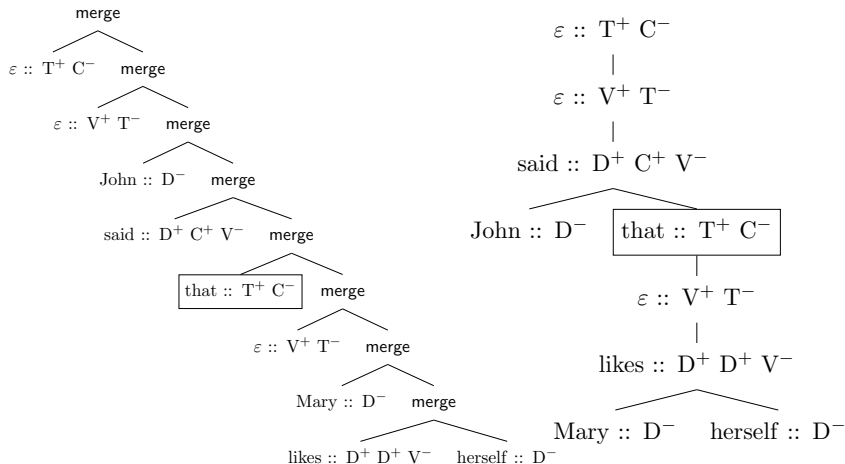
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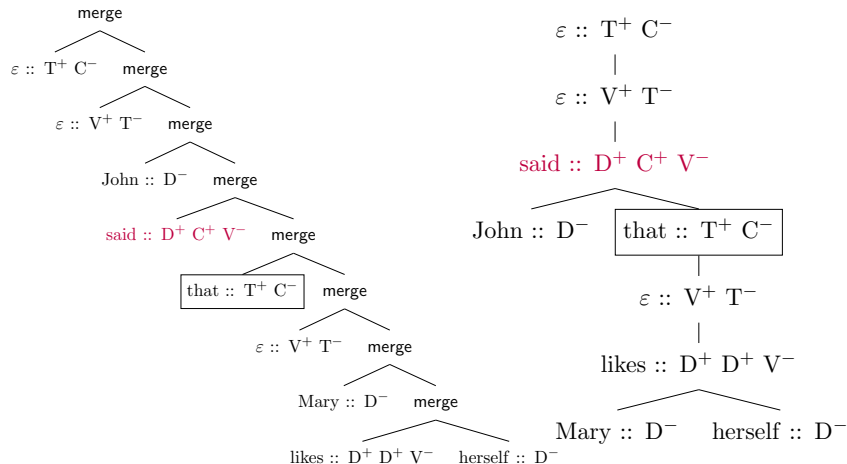
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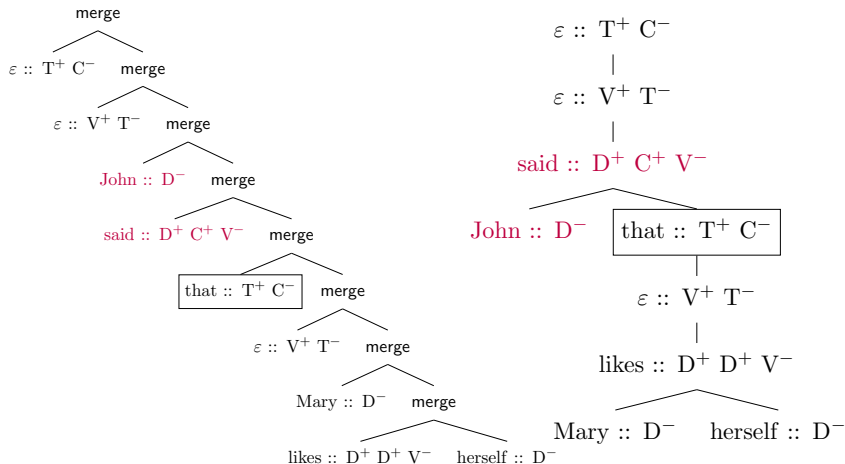
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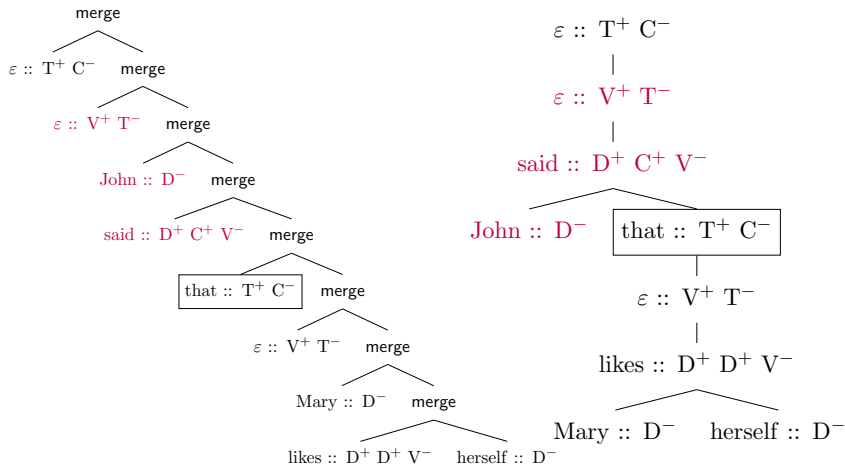
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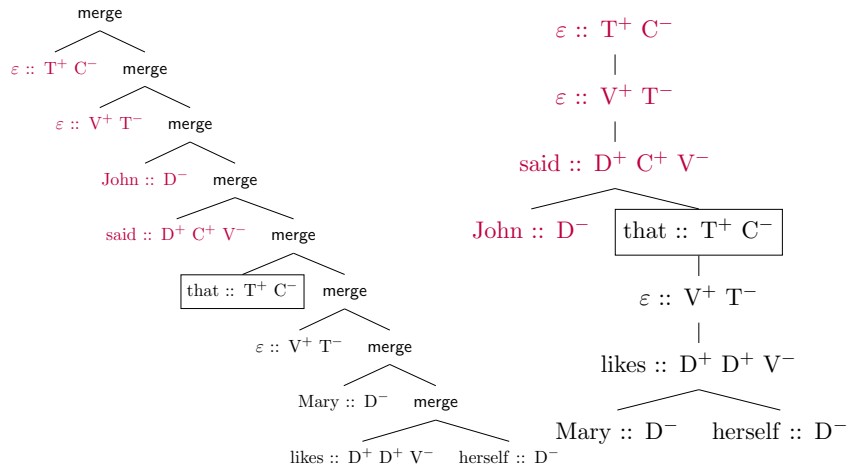
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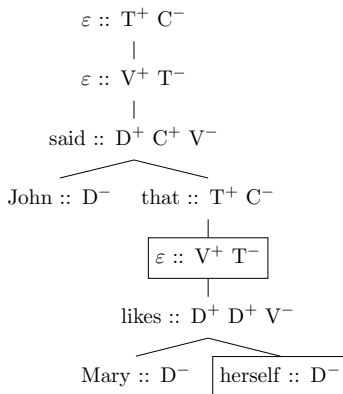
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# Enforcing Principle A with an STA

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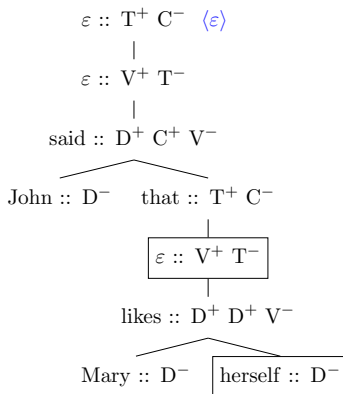




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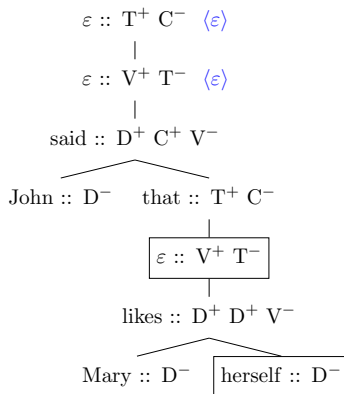
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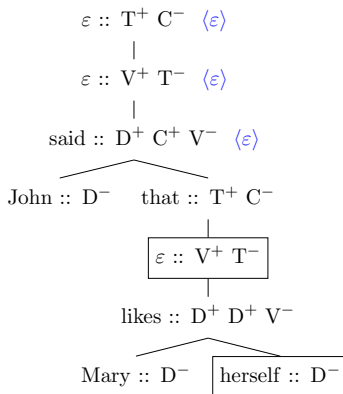
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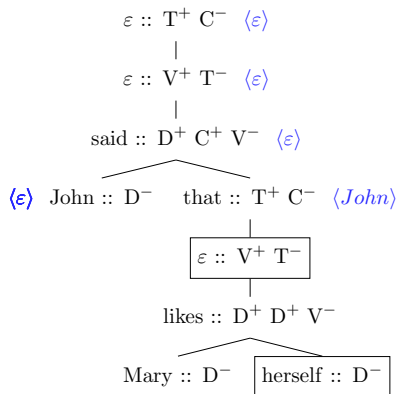
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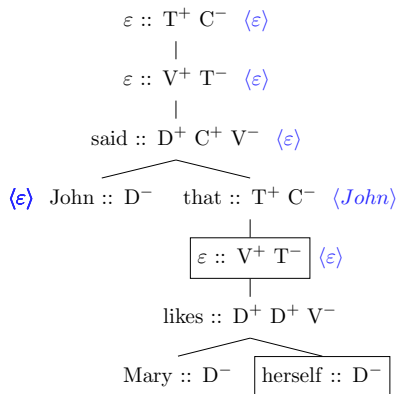
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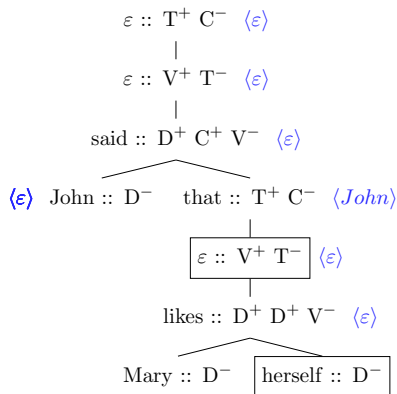
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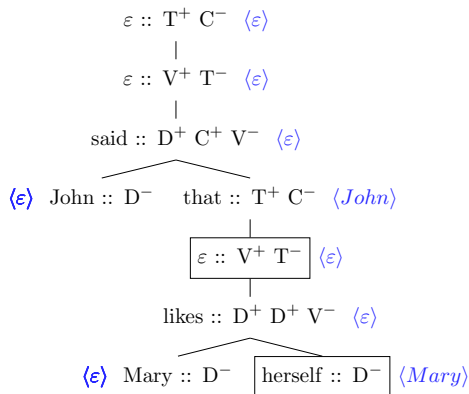
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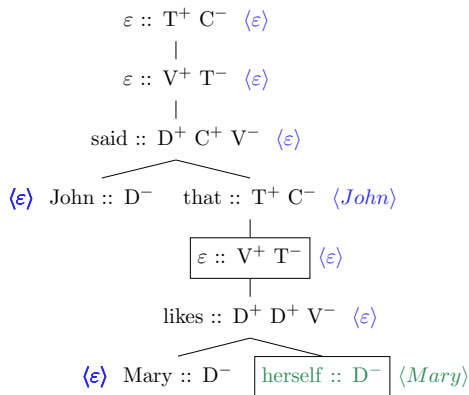
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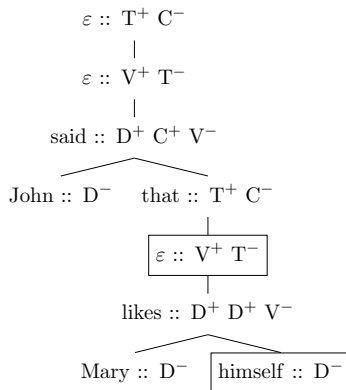




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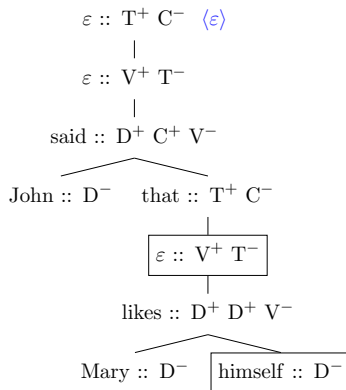
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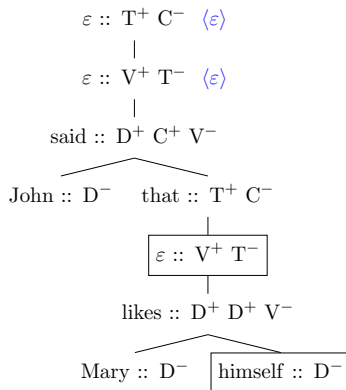
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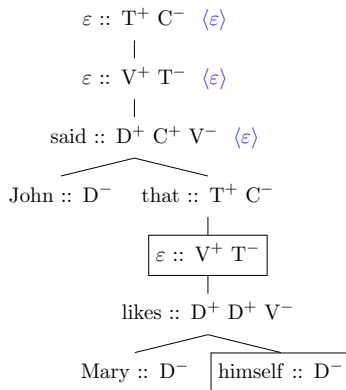
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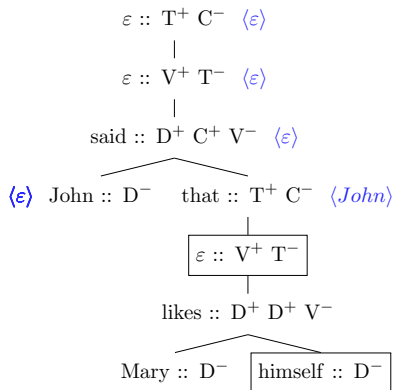
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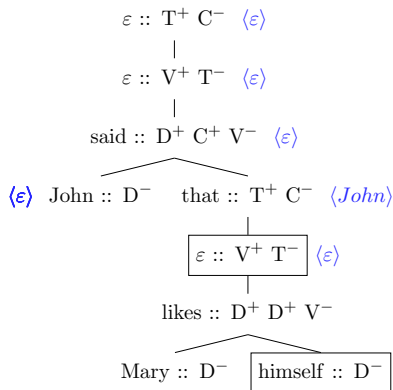
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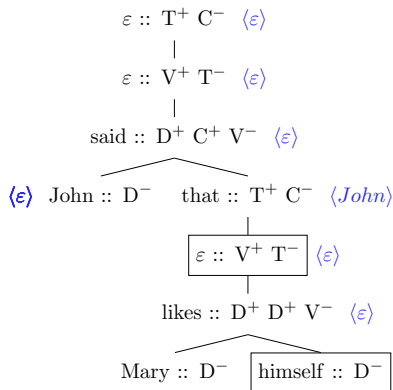
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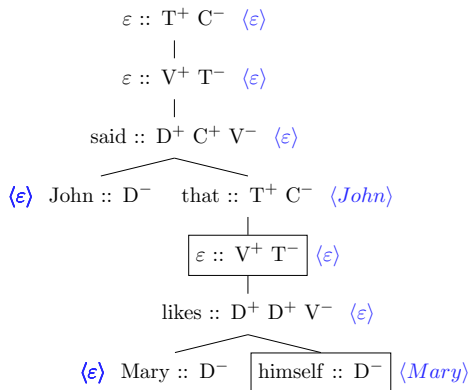
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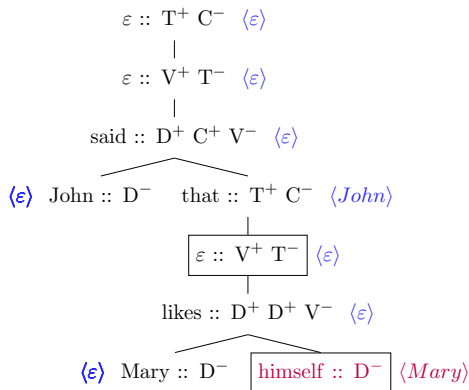




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# Conclusion

## STA as an upper bound for syntax

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- ▶ STA and C-Command Conditions

## Merge, Move, Licensing enforced by the same machinery!

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*⟨Thank you!⟩*

## Acknowledgments I



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# References I

- Chandlee, Jane. 2014. *Strictly local phonological processes*. Doctoral Dissertation, University of Delaware. URL <http://udspace.udel.edu/handle/19716/13374>.
- Graf, Thomas. 2012. Locality and the complexity of Minimalist derivation tree languages. In *Formal Grammar 2010/2011*, ed. Philippe de Groot and Mark-Jan Nederhof, volume 7395 of *Lecture Notes in Computer Science*, 208–227. Heidelberg: Springer. URL [http://dx.doi.org/10.1007/978-3-642-32024-8\\_14](http://dx.doi.org/10.1007/978-3-642-32024-8_14).
- Graf, Thomas. 2017. The power of locality domains in phonology. *Phonology* 34:385–405. URL <https://dx.doi.org/10.1017/S0952675717000197>.
- Graf, Thomas. 2018. Why movement comes for free once you have adjunction. In *Proceedings of CLS 53*, ed. Daniel Edmiston, Marina Ermolaeva, Emre Håkğüder, Jackie Lai, Kathryn Montemurro, Brandon Rhodes, Amara Sankhagowit, and Miachel Tabatowski, 117–136.
- Graf, Thomas, and Connor Mayer. 2018. Sanskrit n-retroflexion is input-output tier-based strictly local. In *Proceedings of SIGMORPHON 2018*, 151–160.
- Graf, Thomas, and Nazila Shafiei. 2019. C-command dependencies as TSL string constraints. In *Proceedings of the Society for Computation in Linguistics (SCiL) 2019*, ed. Gaja Jarosz, Max Nelson, Brendan O'Connor, and Joe Pater, 205–215.
- Heinz, Jeffrey, Chetan Rawal, and Herbert G. Tanner. 2011. Tier-based strictly local constraints in phonology. In *Proceedings of the 49th Annual Meeting of the Association for Computational Linguistics*, 58–64. URL <http://www.aclweb.org/anthology/P11-2011>.

## References II

- Jardine, Adam. 2016. Computationally, tone is different. *Phonology* URL <http://udel.edu/~ajardine/files/jardinemscomputationallytoneisdifferent.pdf>, to appear.
- Kobele, Gregory M., Christian Retoré, and Sylvain Salvati. 2007. An automata-theoretic approach to Minimalism. In *Model Theoretic Syntax at 10*, ed. James Rogers and Stephan Kepser, 71–80.
- Martens, Wim. 2006. *Static analysis of xml transformation- and schema languages*. Doctoral Dissertation, Hasselt University.
- McMullin, Kevin. 2016. *Tier-based locality in long-distance phonotactics: Learnability and typology*. Doctoral Dissertation, University of British Columbia.
- Michaelis, Jens. 2004. Observations on strict derivational minimalism. *Electronic Notes in Theoretical Computer Science* 53:192–209.
- Shafiei, Nazila, and Thomas Graf. 2019. The subregular complexity of syntactic islands. Ms., Stony Brook University.
- Stabler, Edward P. 1997. Derivational Minimalism. In *Logical aspects of computational linguistics*, ed. Christian Retoré, volume 1328 of *Lecture Notes in Computer Science*, 68–95. Berlin: Springer. URL <https://doi.org/10.1007/BFb0052152>.
- Stabler, Edward P. 2011. Computational perspectives on Minimalism. In *Oxford handbook of linguistic Minimalism*, ed. Cedric Boeckx, 617–643. Oxford: Oxford University Press.

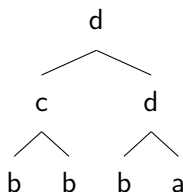


# References III

- Vu, Mai Ha. 2018. Towards a formal description of NPI-licensing patterns. In *Proceedings of the Society for Computation in Linguistics (SCiL) 2018*, volume 1, 154–163. Article 17.
- Vu, Mai Ha, Nazila Shafiei, and Thomas Graf. 2019. Case assignment in TSL syntax: A case study. In *Proceedings of the Society for Computation in Linguistics (SCiL) 2019*, ed. Gaja Jarosz, Max Nelson, Brendan O'Connor, and Joe Pater, 267–276.

# The Spine of a Node

- Example: spine(a)

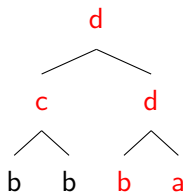


STAs and spine closure (Martens 2006)

A regular tree language  $L$  belongs to the class STA iff  $L$  is spine closed.

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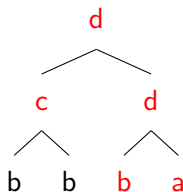


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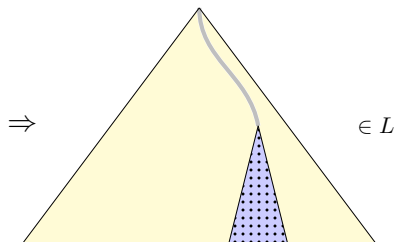
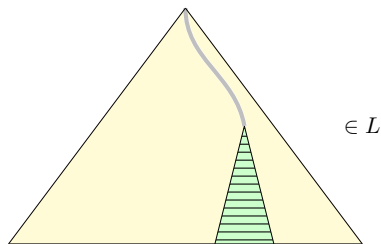
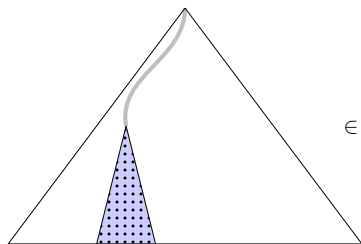
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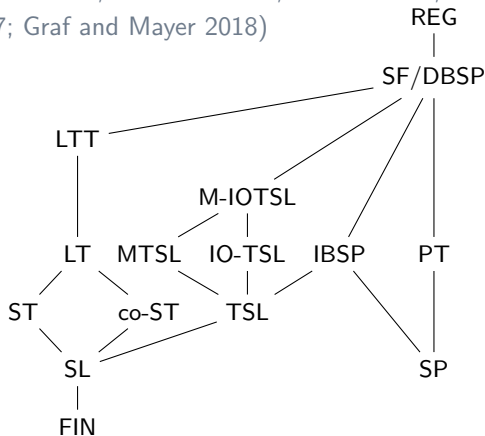
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# Spine Closure



# Subregular Complexity in Phonology

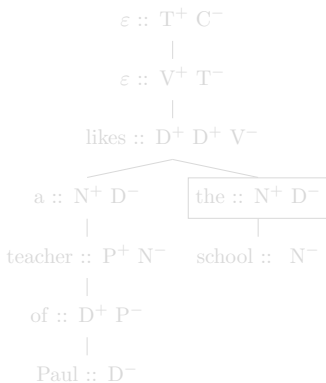
- **Subregular** phonology has proved to be a fruitful enterprise (Heinz et al. 2011; Chandlee 2014; Jardine 2016; McMullin 2016; Graf 2017; Graf and Mayer 2018)



# C-Strings and Spines

Graf and Shafiei (2019)

C-command conditions as subregular **c-string** constraints.



Observation

$\text{spine}(u) \approx \text{c-string}(u)$

Theorem

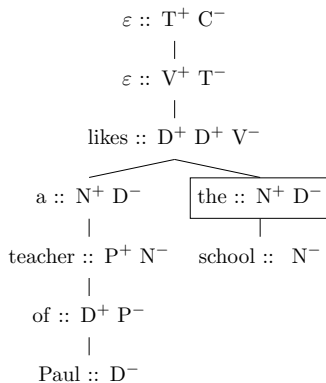
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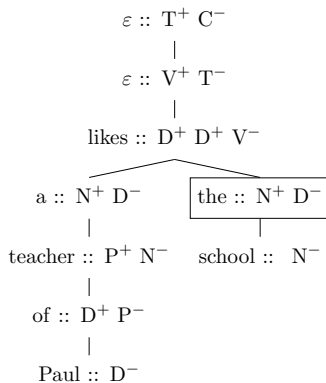
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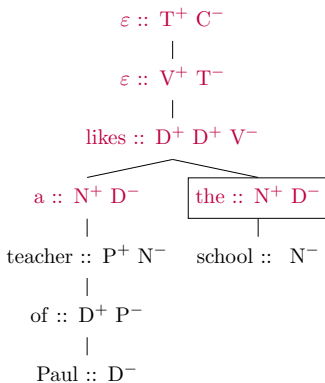
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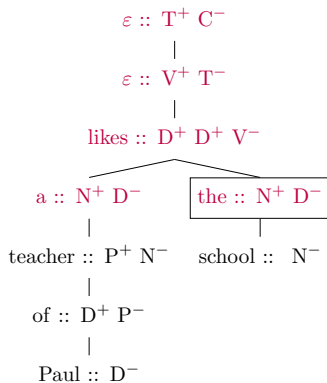
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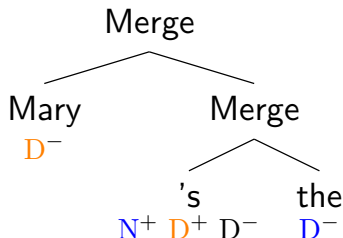
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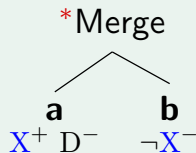
$\text{c-string}(\text{the} :: N^+ D^-) := \varepsilon :: T^+ \text{wh}^+ C^- \uparrow \text{does} :: V^+ T^- \uparrow \text{like} :: D^+ D^+ V^- \uparrow a :: N^+ D^- \text{the} :: N^+ D^-$

## Merge is SL (Graf 2012)

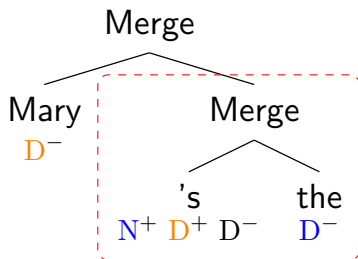


## SL constraints on Merge

- ▶ We lift constraints from **string  $n$ -grams** to **tree  $n$ -grams**
- ▶ We get SL constraints over subtrees.

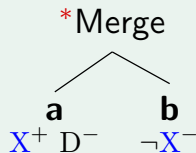


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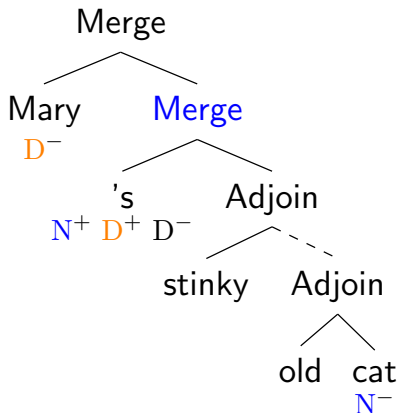
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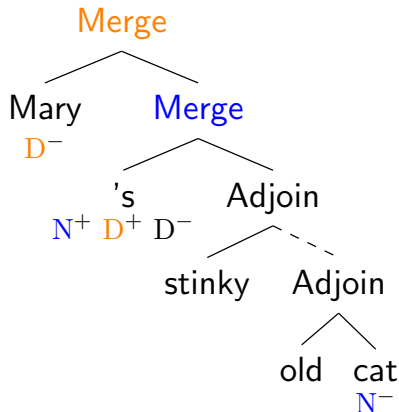
# Non-Local Dependencies in Syntax

Let's stick to core operations:

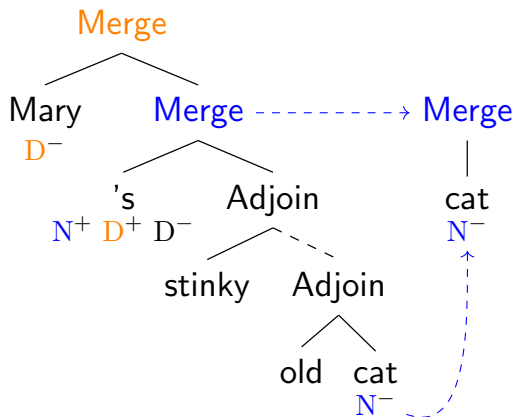
- ▶ Move
  - ▶ **Merge**: Unbounded adjunction
- ??



## TSL over Trees: Projecting Tiers

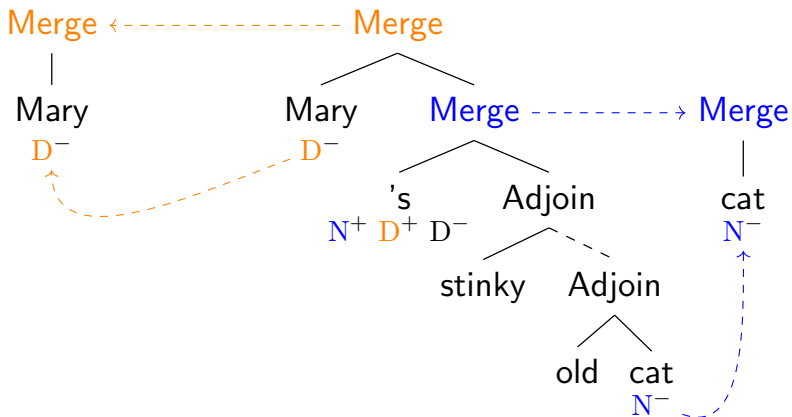


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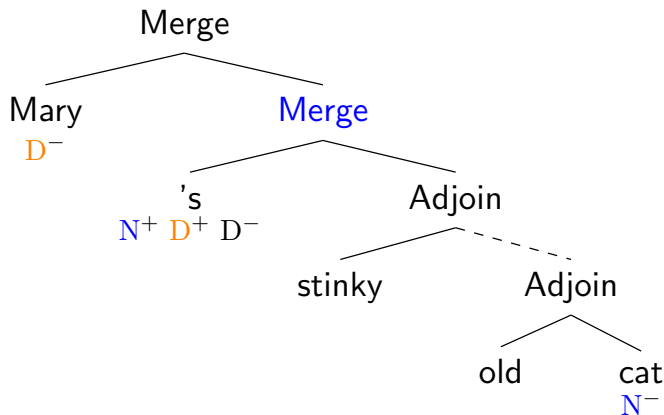




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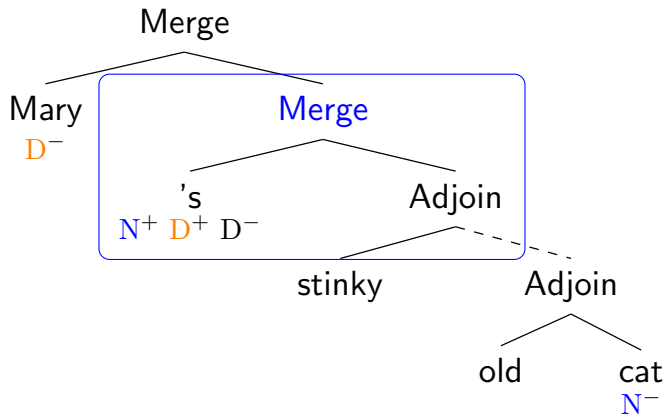


## Merge with Adjunction is TSL



A TSL grammar for Merge

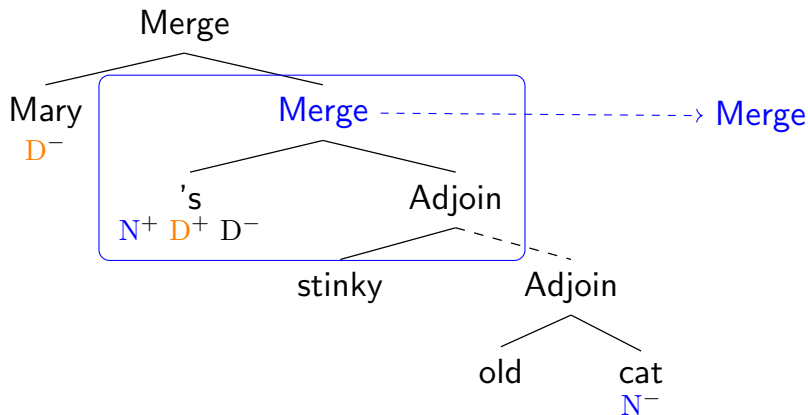
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## A TSL grammar for Merge

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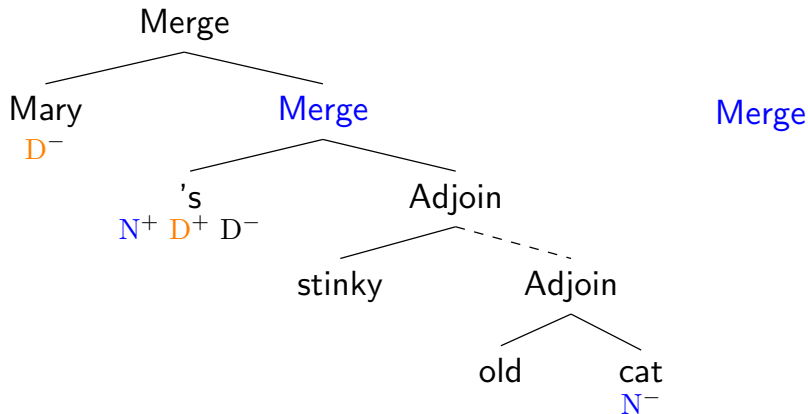
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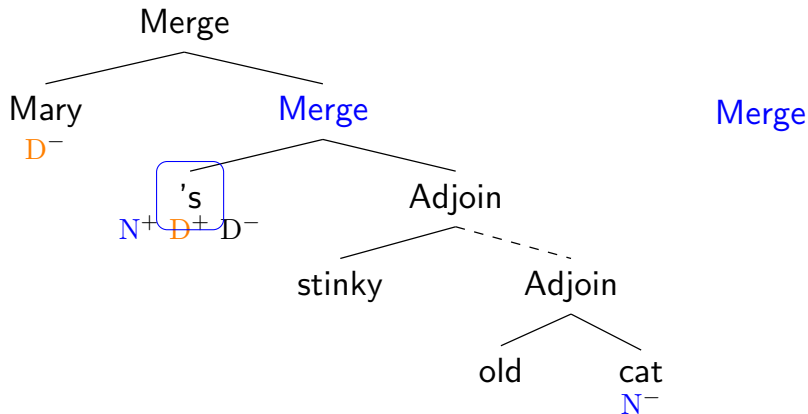
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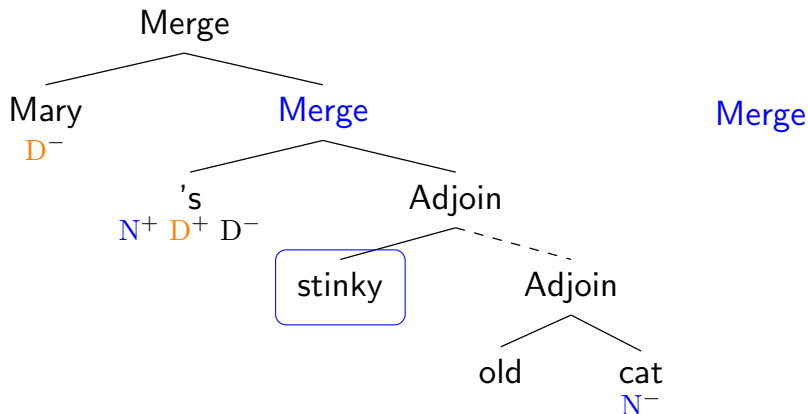
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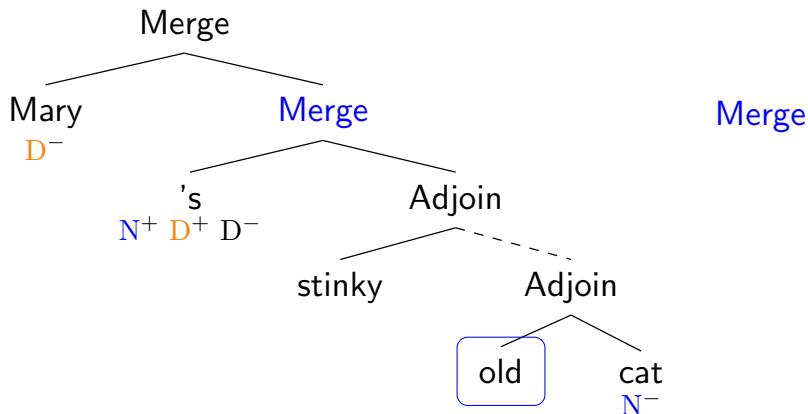
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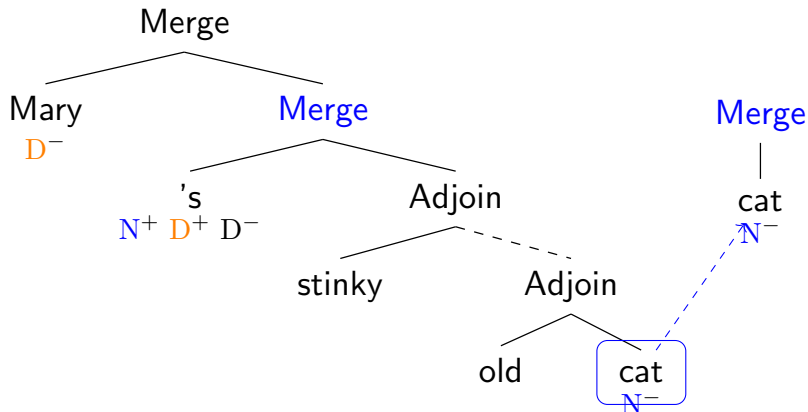


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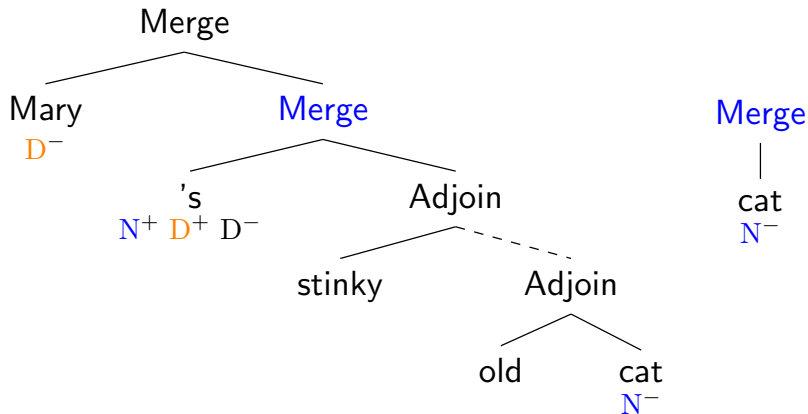
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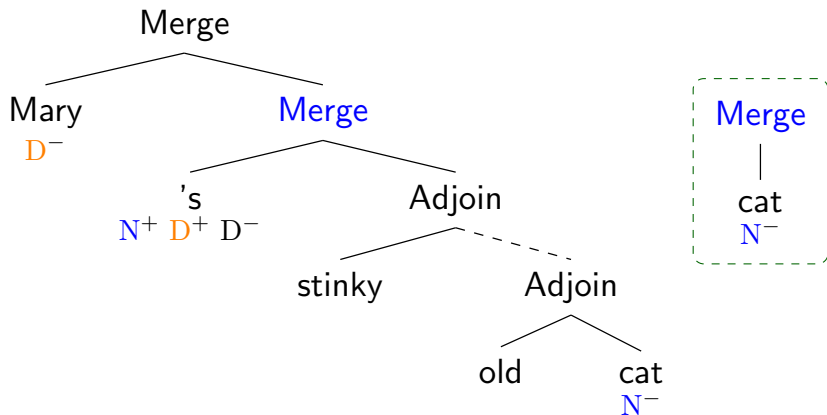
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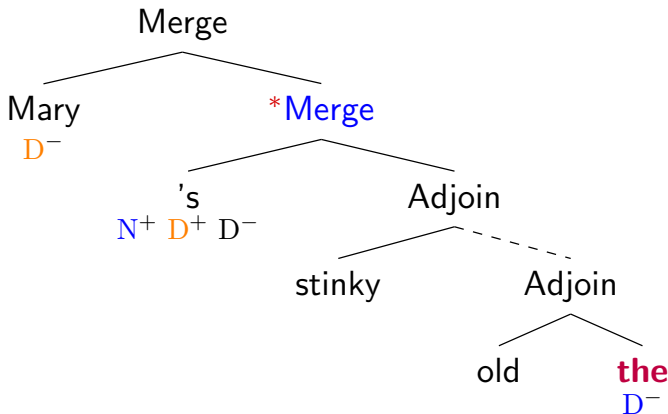
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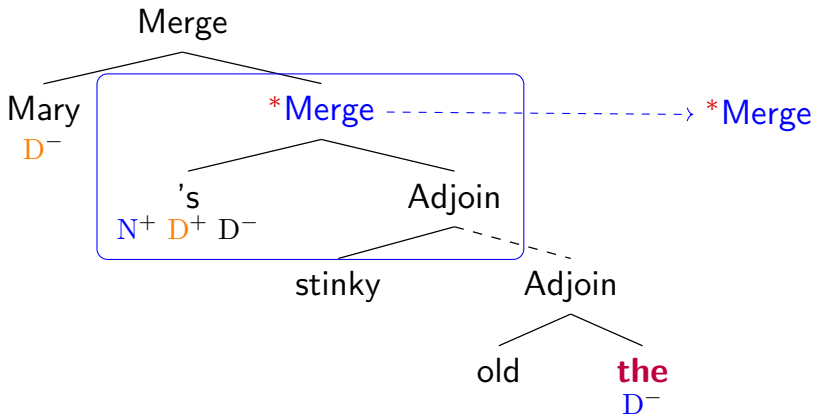
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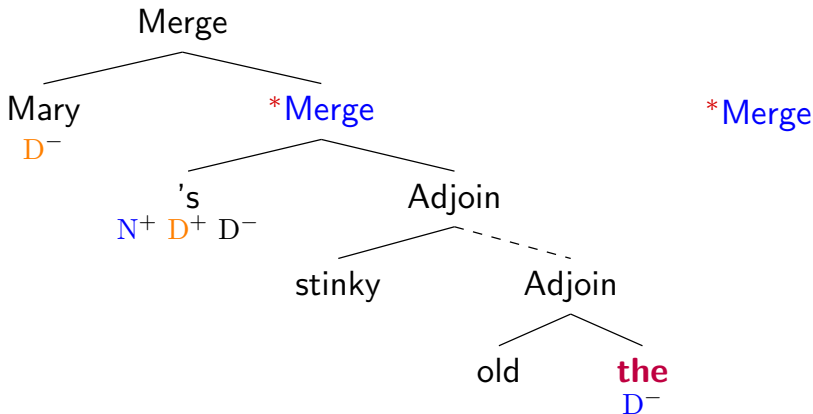
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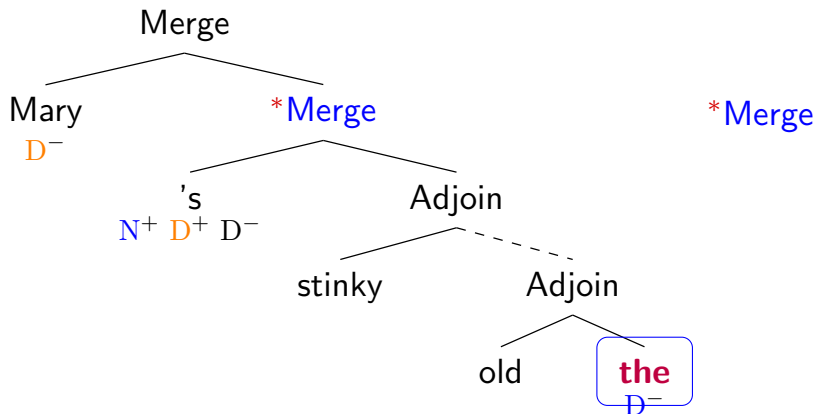
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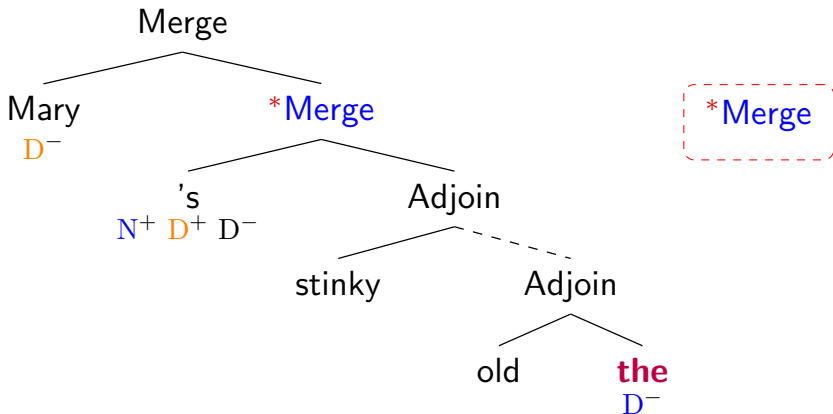
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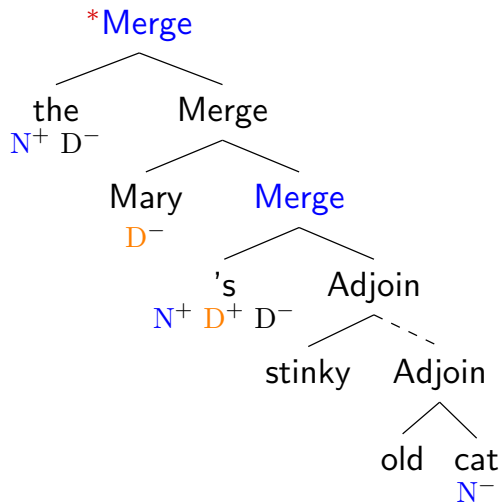


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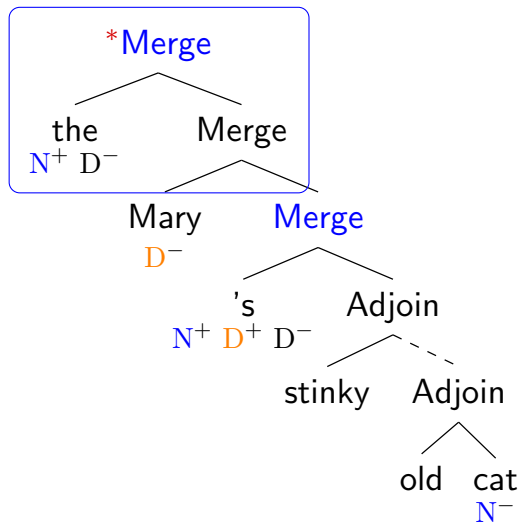
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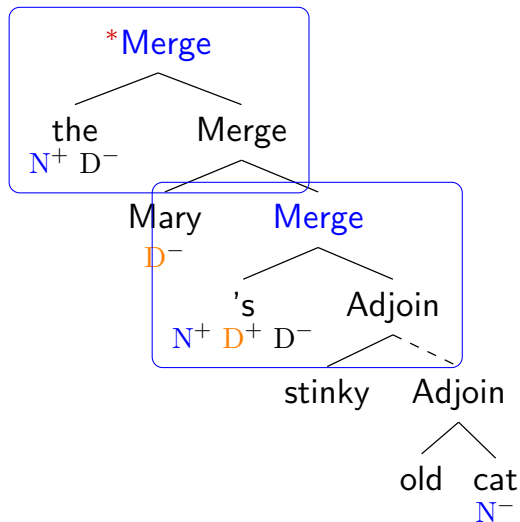
# TSL Merge: Understanding the Constraint



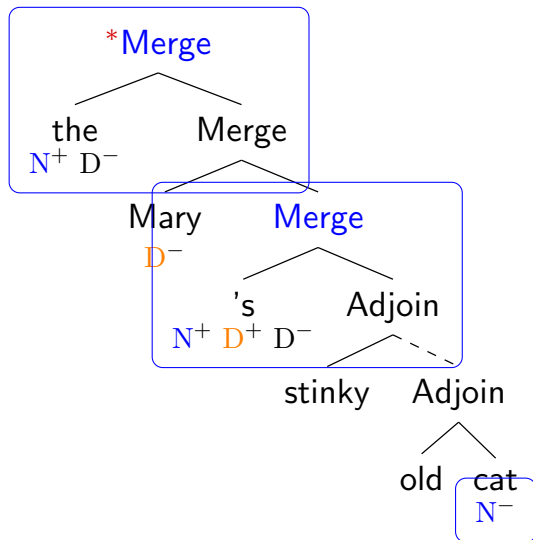
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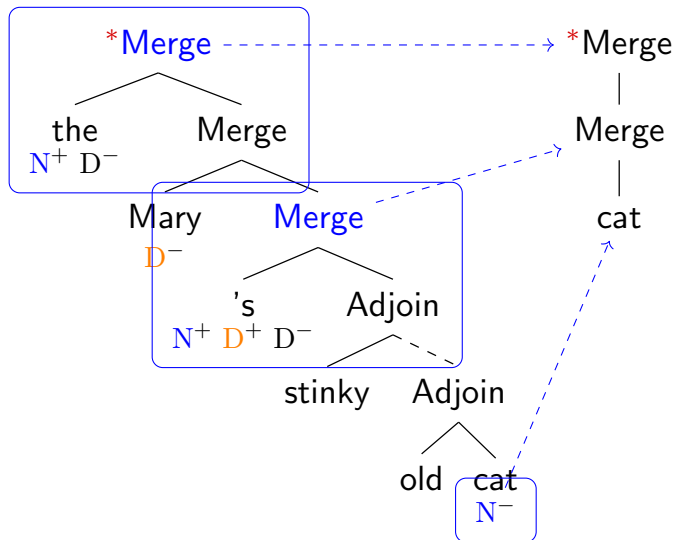
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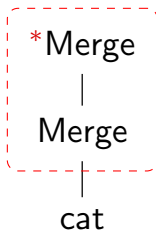
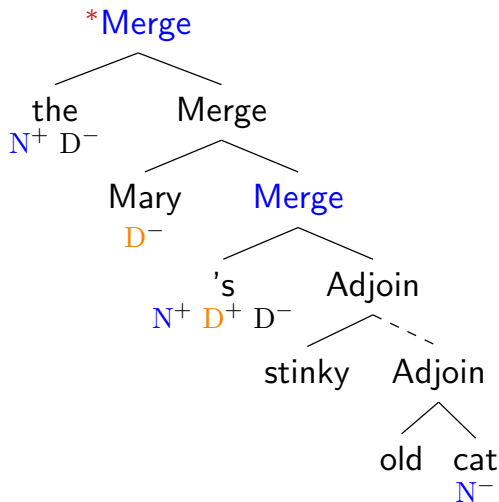
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# Constraints on Move

## What about Move?

Suppose our MG is in **single movement normal form**,

i.e. every phrase moves at most once.

Then movement is regulated by two constraints. (Graf 2012)

### Constraints on Movement

- Move** Every head with a negative Move feature is dominated by a matching Move node.
- SMC** Every Move node is a closest dominating match for exactly one head.

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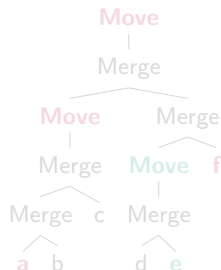
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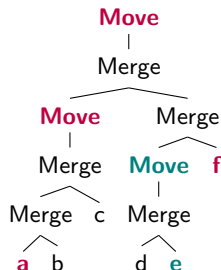
## Tiers for Movement

- ▶ There is no upper bound on the distance between a lexical item and its matching Move node.
- ▶ Consequently, **Move dependencies are not local**.
- ▶ What if every movement type (wh, topic, ...) induces its own tier? Would that make Move dependencies local?



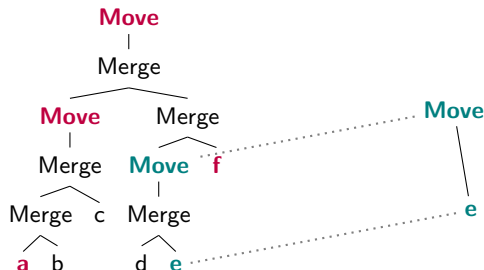
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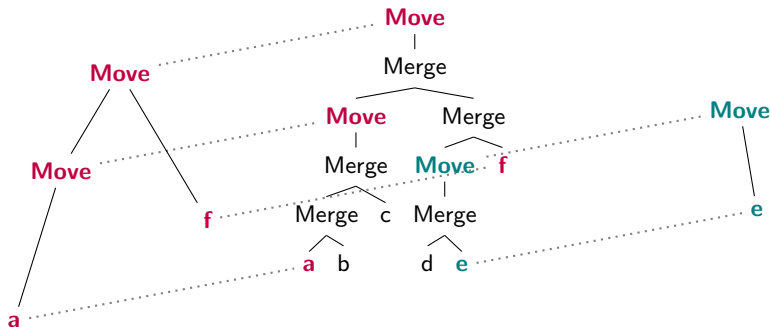
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# Move Constraints over Tiers

|             | Original  | Tier   |
|-------------|---|--|
| <b>Move</b> | Every head with a negative Move feature is dominated by a matching Move node. | Every lexical item has a <b>mother</b> labeled Move.             |
| <b>SMC</b>  | Every Move node is a closest dominating match for exactly one head.           | Exactly one of a Move node's <b>daughters</b> is a lexical item. |

## Tree $n$ -gram Templates

