Table 1: Comparison of TMLE and one-step ATT estimators under weak overlap across mediator types.

|        |                  | Univariat           | e Binary            | Univariate Continuous |                     |                              |                        |                        |                        | Bivariate Continuous         |                        |                        |                        |
|--------|------------------|---------------------|---------------------|-----------------------|---------------------|------------------------------|------------------------|------------------------|------------------------|------------------------------|------------------------|------------------------|------------------------|
|        |                  | $\psi_1(\hat{Q}^*)$ | $\psi_1^+(\hat{Q})$ | $\psi_1(\hat{Q}^*)$   | $\psi_1^+(\hat{Q})$ | $\psi_{2a}(\hat{Q}^{\star})$ | $\psi^+_{2a}(\hat{Q})$ | $\psi_{2b}(\hat{Q}^*)$ | $\psi^+_{2b}(\hat{Q})$ | $\psi_{2a}(\hat{Q}^{\star})$ | $\psi^+_{2a}(\hat{Q})$ | $\psi_{2b}(\hat{Q}^*)$ | $\psi^+_{2b}(\hat{Q})$ |
| n=500  | Bias             | -0.001              | -0.01               | 0.006                 | 0.031               | 0.004                        | 0.045                  | 0.01                   | 0.021                  | -0.012                       | 0.305                  | -0.023                 | -0.074                 |
|        | $^{\mathrm{SD}}$ | 0.103               | 0.613               | 0.161                 | 1.147               | 0.415                        | 3.644                  | 0.398                  | 1.748                  | 0.5                          | 5.278                  | 0.456                  | 2.021                  |
|        | MSE              | 0.011               | 0.376               | 0.026                 | 1.316               | 0.172                        | 13.264                 | 0.158                  | 3.054                  | 0.25                         | 27.92                  | 0.208                  | 4.087                  |
|        | CI coverage      | 87.4%               | 93.7%               | 97.6%                 | 95.5%               | 97.2%                        | 96.6%                  | 97.2%                  | 96.6%                  | 98.9%                        | 96.7%                  | 97.2%                  | 97.2%                  |
|        | CI width         | 0.391               | 1.002               | 1.834                 | 1.808               | 5.331                        | 6.614                  | 3.142                  | 4.133                  | 11.005                       | 13.085                 | 3.223                  | 4.539                  |
| n=1000 | Bias             | 0.004               | 0.011               | 0.002                 | -0.02               | -0.002                       | 0.108                  | -0.002                 | 0.02                   | 0.008                        | -0.004                 | 0.007                  | 0.03                   |
|        | $^{\mathrm{SD}}$ | 0.074               | 0.288               | 0.116                 | 0.609               | 0.319                        | 2.026                  | 0.311                  | 0.98                   | 0.363                        | 2.637                  | 0.322                  | 0.962                  |
|        | MSE              | 0.006               | 0.083               | 0.013                 | 0.37                | 0.102                        | 4.113                  | 0.097                  | 0.959                  | 0.131                        | 6.946                  | 0.104                  | 0.926                  |
|        | CI coverage      | 88.2%               | 94.5%               | 97.8%                 | 95.6%               | 97.8%                        | 97%                    | 98%                    | 97.1%                  | 99.1%                        | 97%                    | 96.6%                  | 95.3%                  |
|        | CI width         | 0.299               | 0.555               | 1.055                 | 1.042               | 3.444                        | 3.975                  | 2.072                  | 2.476                  | 5.411                        | 6.096                  | 2.058                  | 2.443                  |
| n=2000 | Bias             | 0.002               | -0.001              | 0.002                 | 0.013               | 0.007                        | -0.003                 | 0.013                  | 0.022                  | 0.01                         | 0.022                  | 0.013                  | 0.042                  |
|        | $^{\mathrm{SD}}$ | 0.051               | 0.17                | 0.08                  | 0.343               | 0.24                         | 1.035                  | 0.244                  | 0.64                   | 0.304                        | 1.463                  | 0.282                  | 0.678                  |
|        | MSE              | 0.003               | 0.029               | 0.006                 | 0.118               | 0.058                        | 1.07                   | 0.06                   | 0.41                   | 0.093                        | 2.138                  | 0.08                   | 0.461                  |
|        | CI coverage      | 91.2%               | 96.8%               | 97.8%                 | 95%                 | 96.9%                        | 96.4%                  | 98%                    | 96.5%                  | 99.8%                        | 97.6%                  | 97.9%                  | 96.2%                  |
|        | CI width         | 0.213               | 0.382               | 0.748                 | 0.739               | 2.267                        | 2.468                  | 1.611                  | 1.815                  | 3.644                        | 3.961                  | 1.604                  | 1.825                  |