

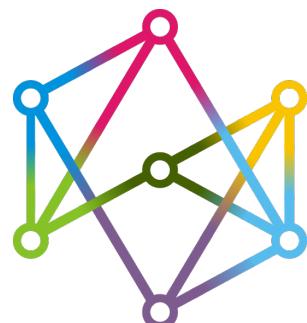
Towards Scalable and Safe Online Decision Making Under Uncertainty in Partially Observable Environments

Vadim Indelman



TECHNION

Israel Institute
of Technology



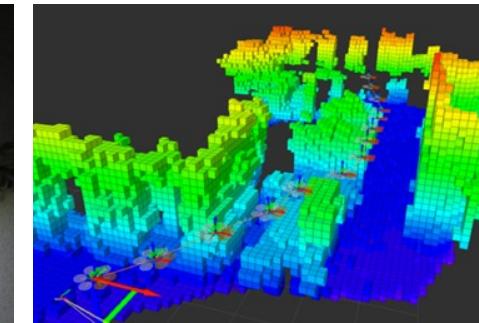
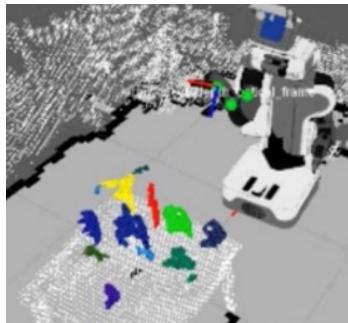
Stanford SISL Seminar

ANPL
Autonomous Navigation and
Perception Lab

July 7, 2025

Advanced Autonomy

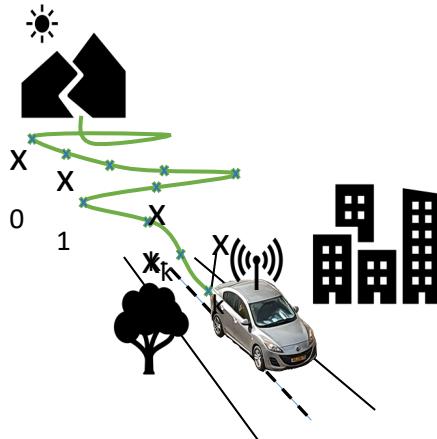
Involves autonomous navigation, active SLAM, informative gathering, active sensing, etc.



Advanced Autonomy

Perception and Inference

Where am I? What is the surrounding environment?



Decision-Making Under Uncertainty

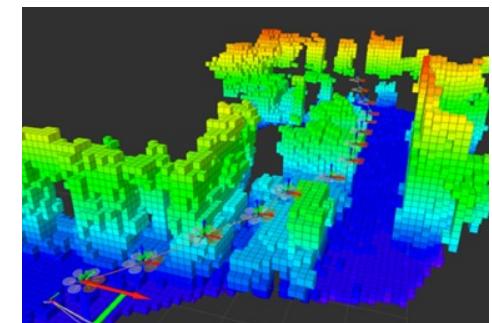
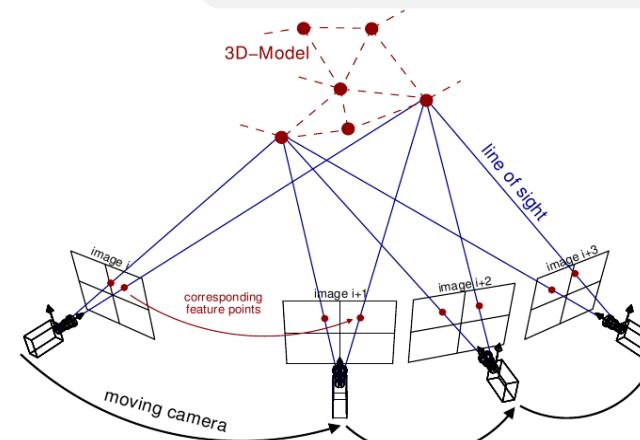
What should I be doing next?

Determine best action(s) to accomplish a task, account for different sources of uncertainty

Perception and Inference



Decision-Making Under Uncertainty

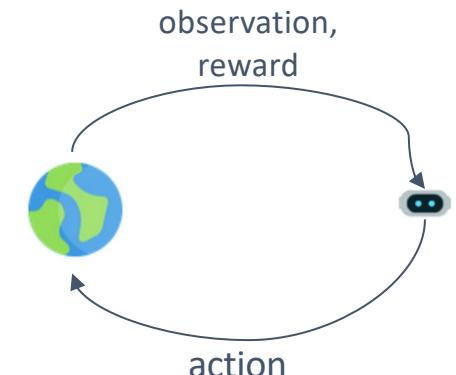


Partially Observable Markov Decision Process (POMDP)

- POMDP tuple:

$$\langle \mathcal{X}, \mathcal{Z}, \mathcal{A}, T, O, \rho, b_k \rangle$$

— state, observation, and action spaces
— transition and observation models
— Belief-dependent reward function
— Belief at planning time instant k



- Value function

$$V^\pi(b_k) = \mathbb{E}_{z_{k+1:k+L}} \left[\sum_{l=k}^{k+L} \rho(b_l, \pi_l(b_l)) \right]$$

Belief-dependent reward function

Challenge

Probabilistic Inference

Maintain a distribution over the state given data

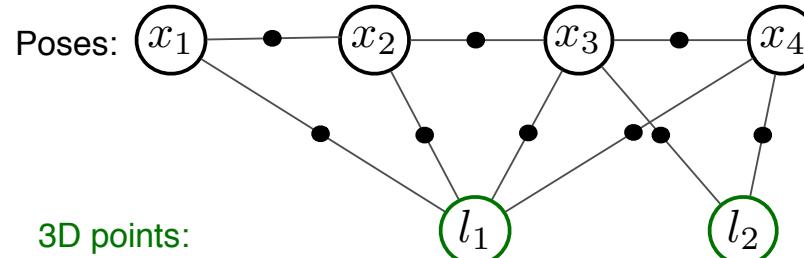
$$b_k \triangleq b[X_k] = \mathbb{P}(X_k \mid \underbrace{\text{state}}_{a_0:k-1}, \underbrace{\text{actions}}_{z_1:k})$$

Decision-making under uncertainty

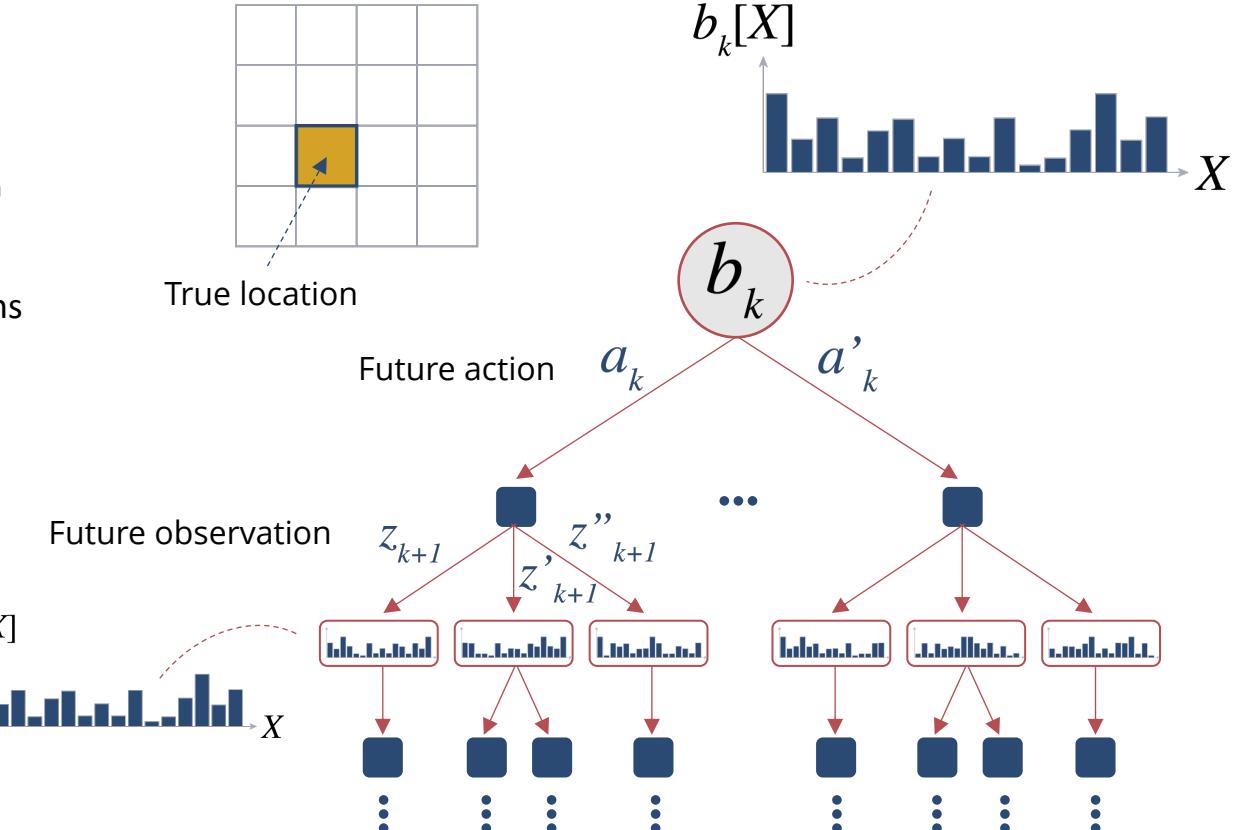
Involves reasoning about the entire observation and action spaces along planning horizon

Computationally intractable

More so, in high dimensional settings



Example - grid world



How can we act autonomously online and efficiently complete tasks in a safe and reliable fashion??

Agenda

Experience Reuse in POMDP Planning

POMDP Planning with Hybrid Beliefs

Simplification of POMDP with Formal Guarantees

Multi-agent POMDP Planning with Inconsistent Beliefs

Agenda

Experience Reuse in POMDP Planning

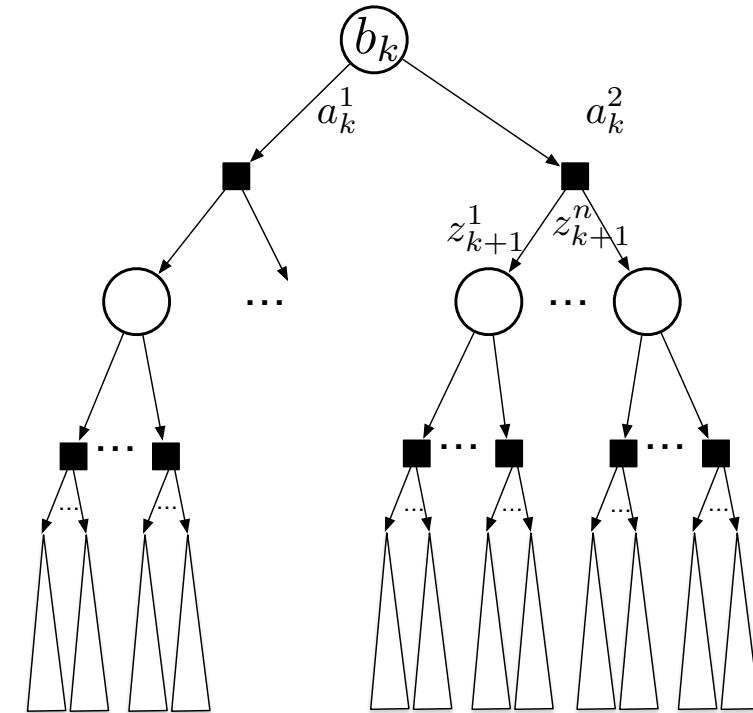
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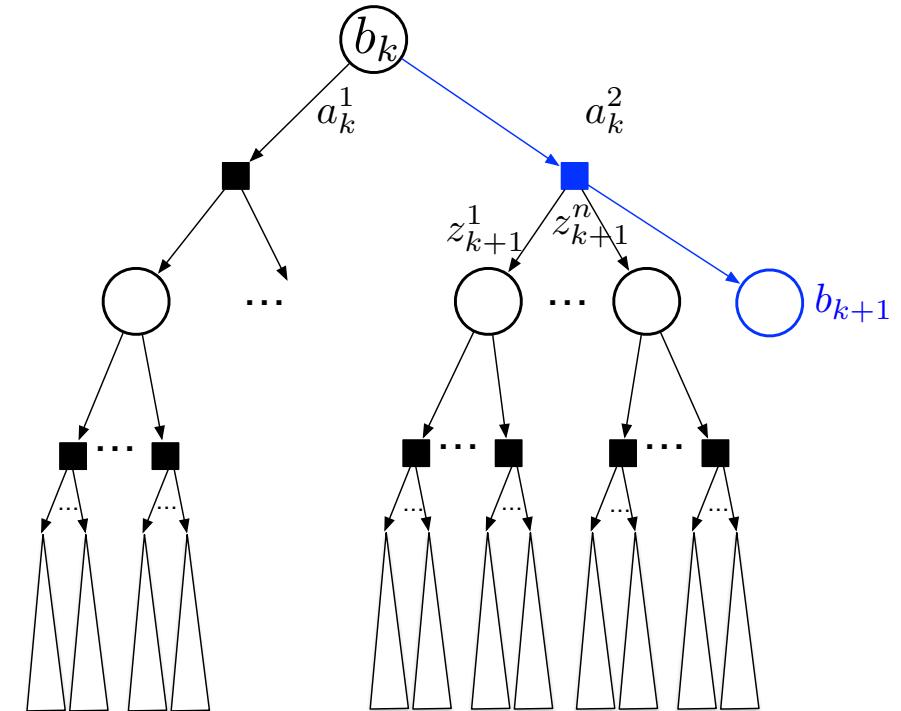
Experience Reuse in POMDP Planning

- Consider POMDPs with continuous state, action, and observation spaces



Experience Reuse in POMDP Planning

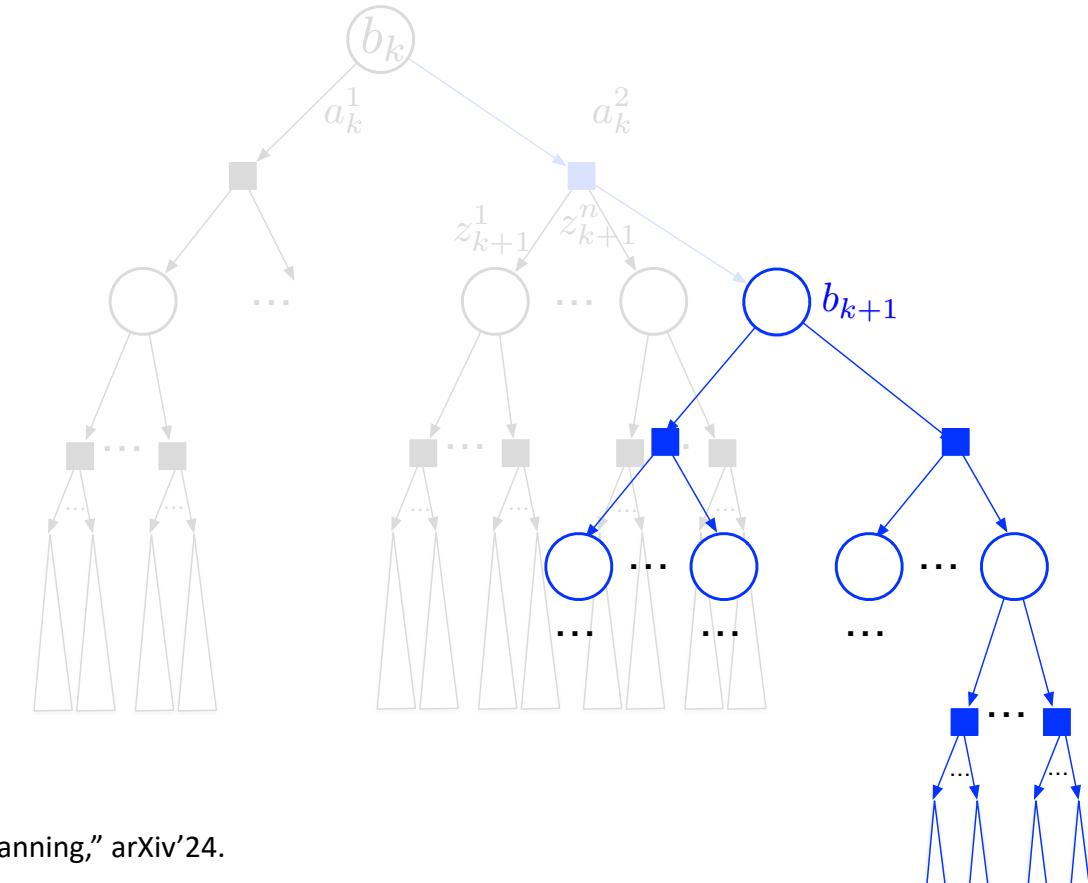
- Consider POMDPs with continuous state, action, and observation spaces
- The probability of sampling the same belief/observation twice is zero



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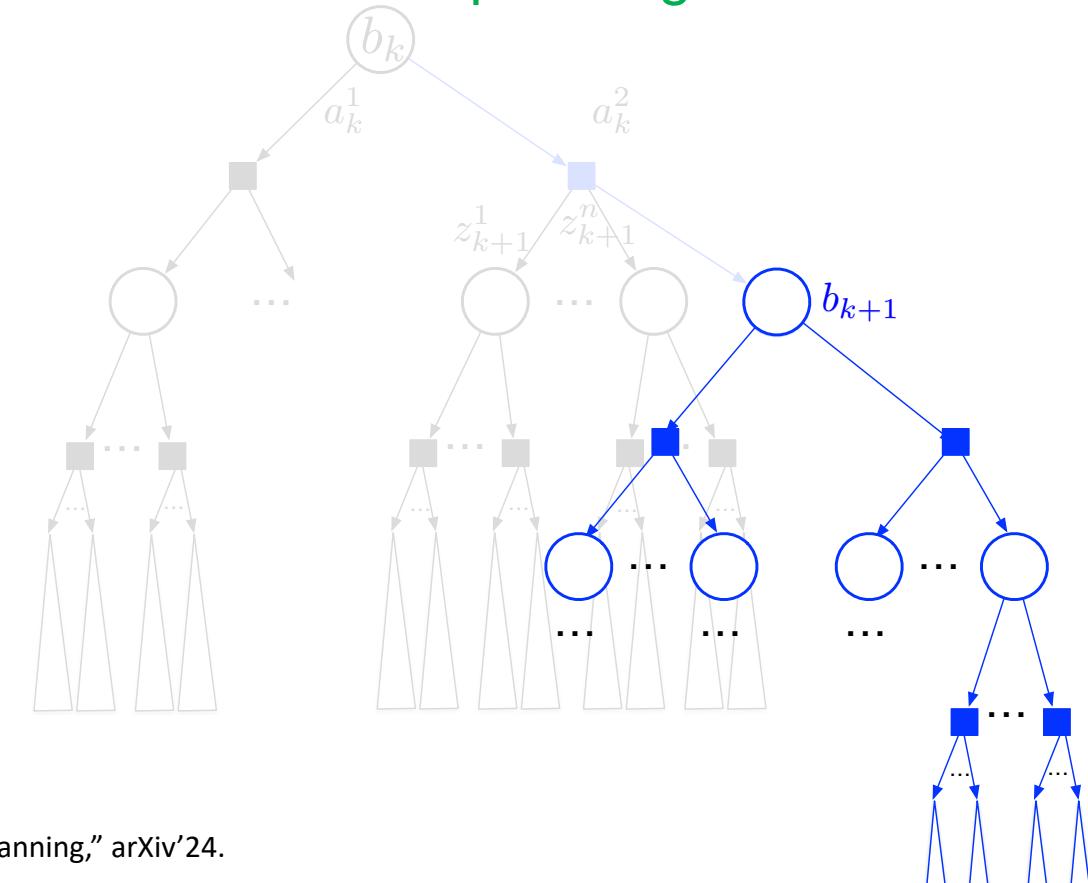
Online SOTA POMDP solvers typically perform calculations from **scratch at each planning session**



Experience Reuse in POMDP Planning

- Consider POMDPs with continuous state, action, and observation spaces
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- Previously sampled beliefs can still provide useful info in the current planning session

Online SOTA POMDP solvers typically perform calculations from **scratch at each planning session**



Experience Reuse in POMDP Planning

- Consider POMDPs with continuous state, action, and observation spaces
- The probability of sampling the same belief/observation twice is zero
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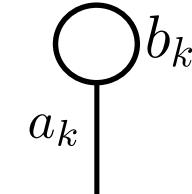
Key idea: Reuse previous trajectories/calculations to get an efficient estimation of

$$Q^\pi(b, a) = \mathbb{E}_\pi \left[\sum_{i=k}^{k+L-1} \gamma^{i-k} r(b_i, \pi_i(b_i), b_{i+1}) \mid b_k = b, a_k = a \right] \triangleq \mathbb{E}_\pi[G \mid b_k = b, a_k = a]$$

- Instead of calculating each planning session from scratch (state of the art)

Experience Reuse in POMDP Planning

- Consider a planning session at time instant k

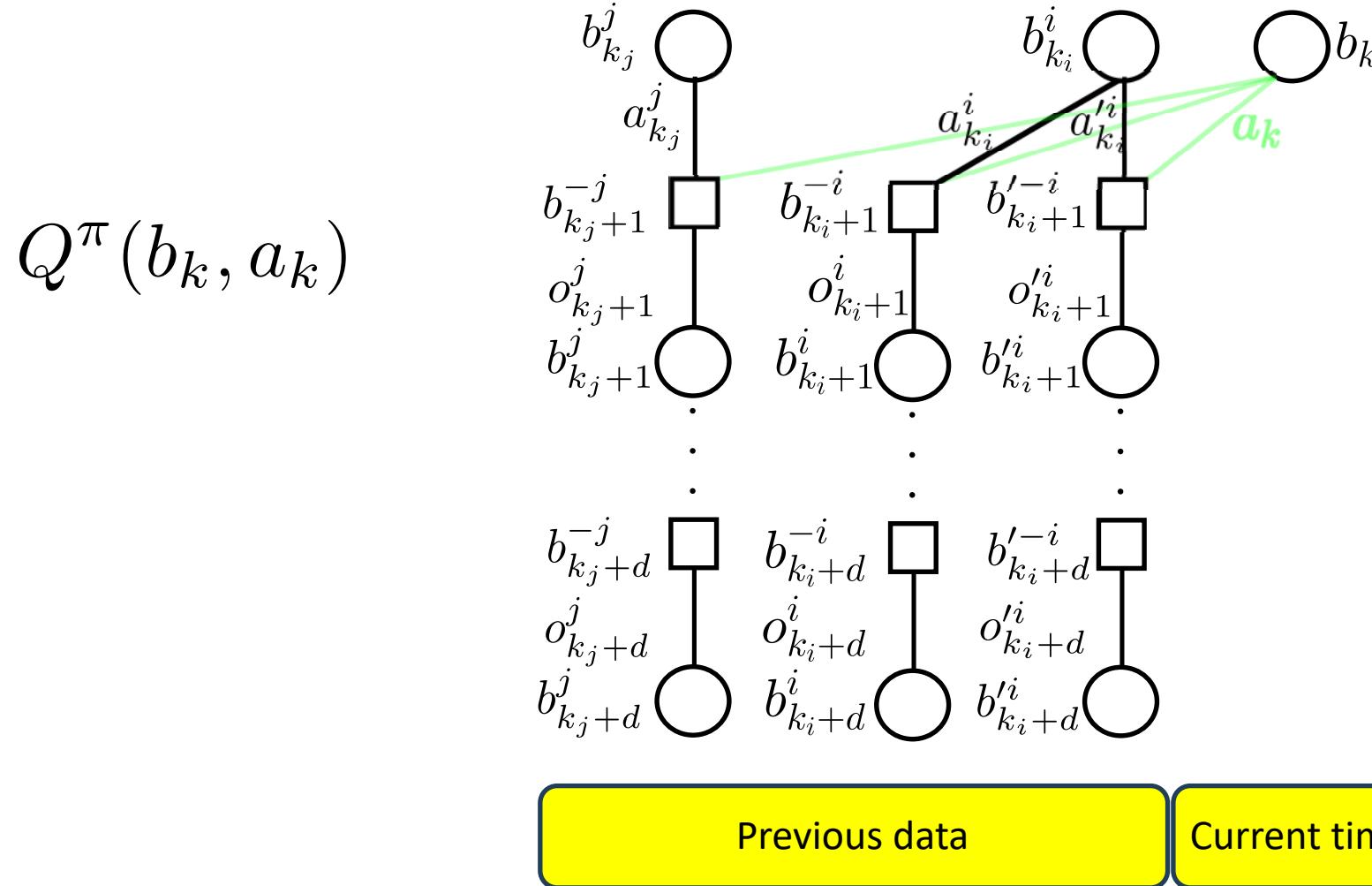


$$Q^\pi(b_k, a_k)$$

Current time

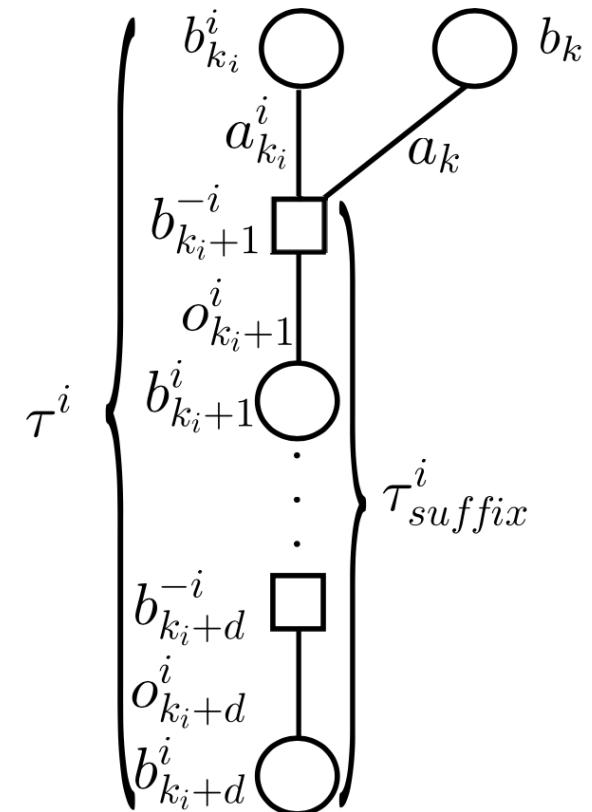
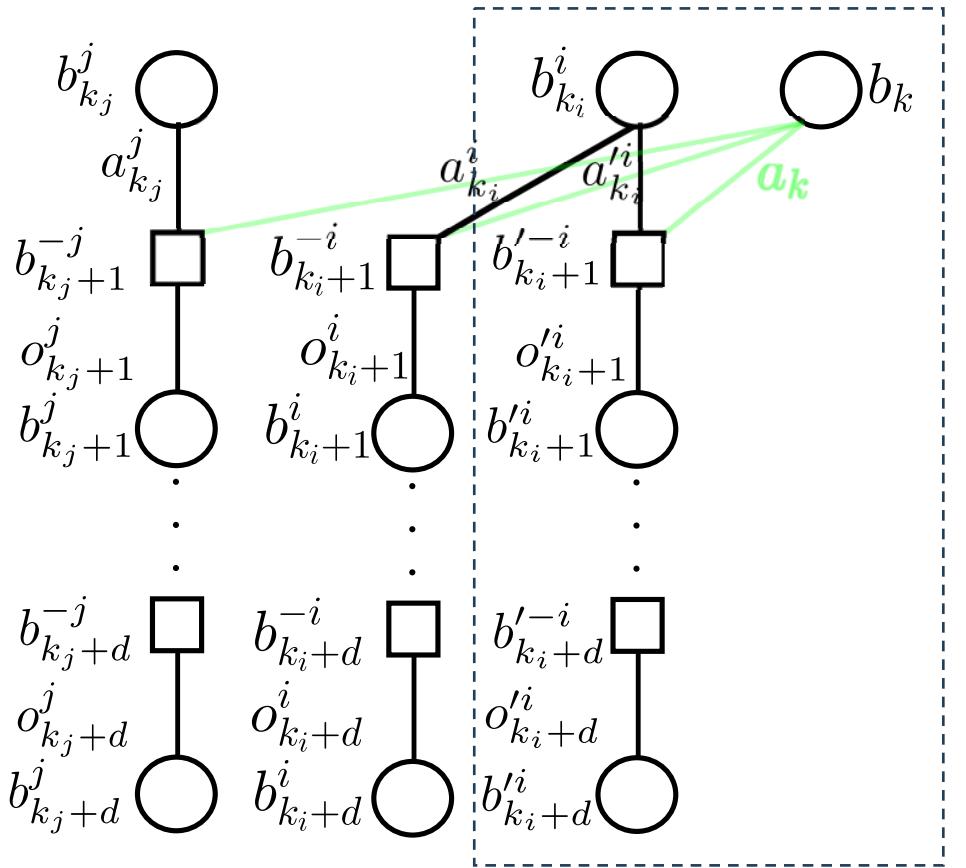
Experience Reuse in POMDP Planning

- Consider a planning session at time instant k



Experience Reuse in POMDP Planning

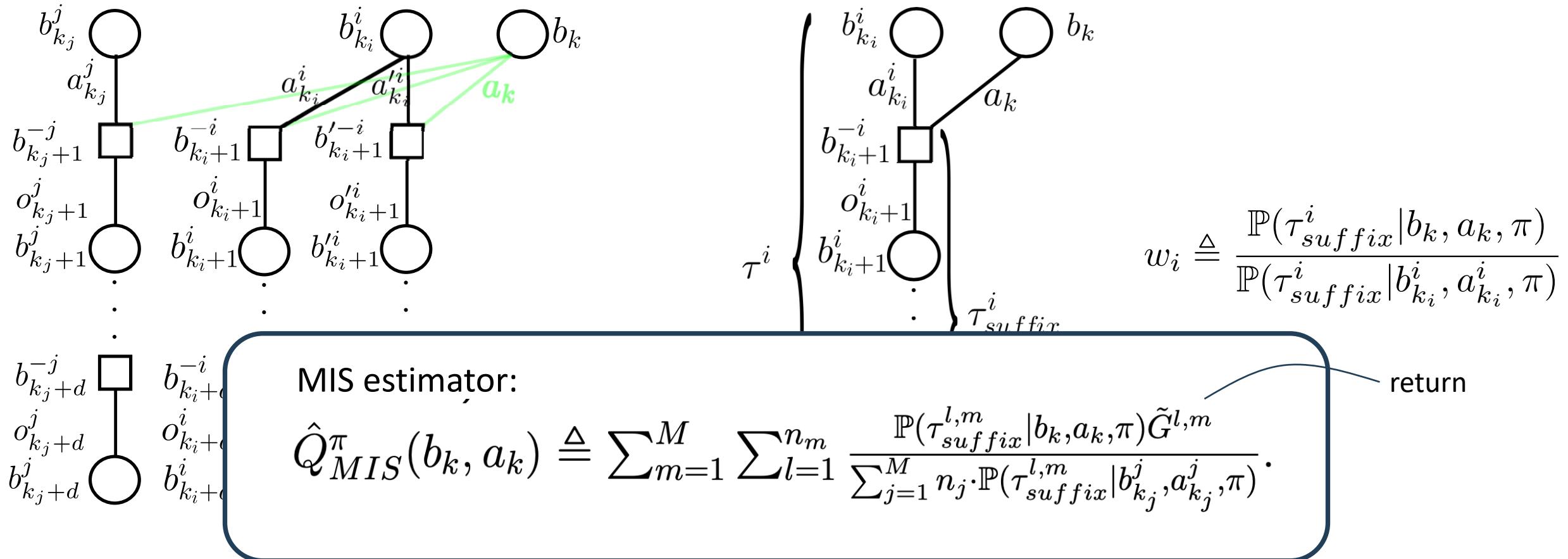
- **Key idea:** multiple importance sampling (MIS) estimator



$$w_i \triangleq \frac{\mathbb{P}(\tau_{suffix}^i | b_k, a_k, \pi)}{\mathbb{P}(\tau_{suffix}^i | b_{k_i}^i, a_{k_i}^i, \pi)}$$

Experience Reuse in POMDP Planning

- **Key idea:** multiple importance sampling (MIS) estimator



Experience-Based Value Function Estimation

MIS estimator:

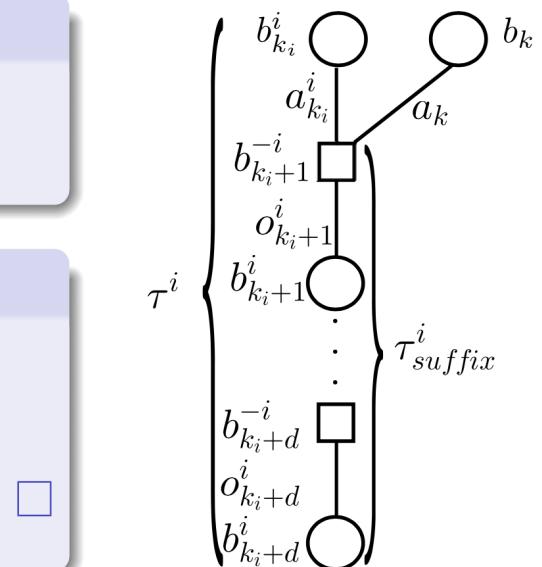
$$\hat{Q}_{MIS}^{\pi}(b_k, a_k) \triangleq \sum_{m=1}^M \sum_{l=1}^{n_m} \frac{\mathbb{P}(\tau_{suffix}^{l,m} | b_k, a_k, \pi) \tilde{G}^{l,m}}{\sum_{j=1}^M n_j \cdot \mathbb{P}(\tau_{suffix}^{l,m} | b_{k_j}^j, a_{k_j}^j, \pi)}.$$

Theorem 1

$$\frac{\mathbb{P}(\tau_{suffix}^i | b_k, a_k, \pi)}{\mathbb{P}(\tau_{suffix}^i | b_{k_i}^i, a_{k_i}^i, \pi)} = \frac{\mathbb{P}(b_{k_i+1}^{-i} | b_k, a_k)}{\mathbb{P}(b_{k_i+1}^{-i} | b_{k_i}^i, a_{k_i}^i)}$$

Proof.

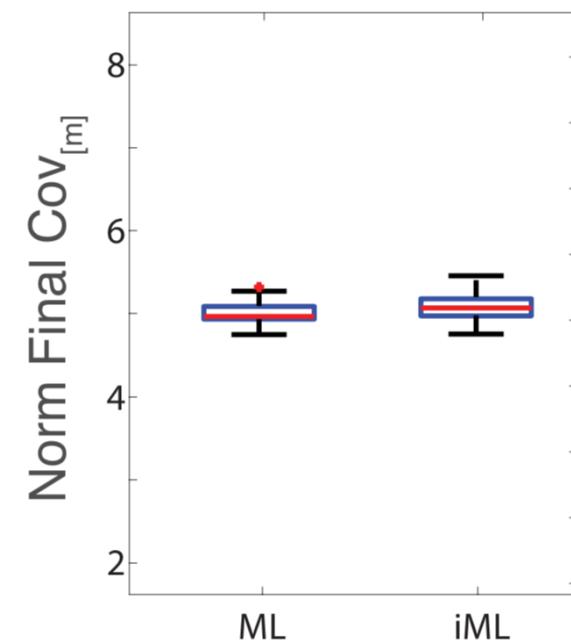
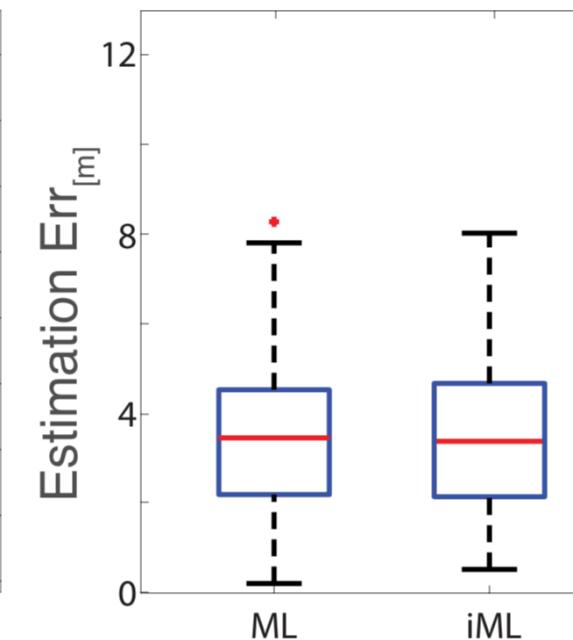
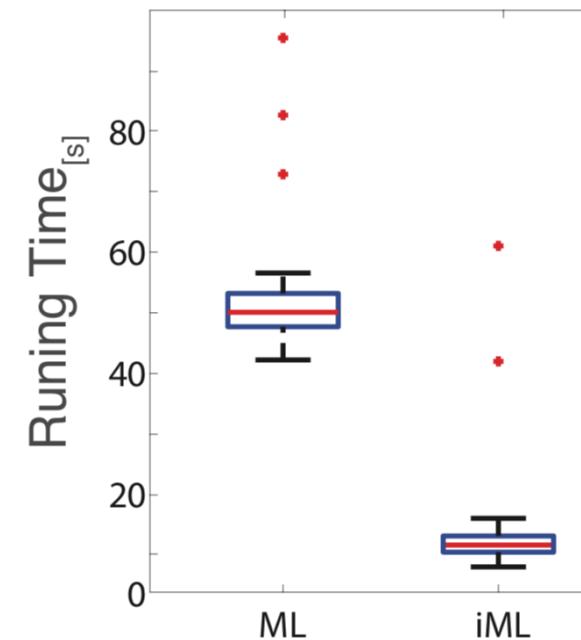
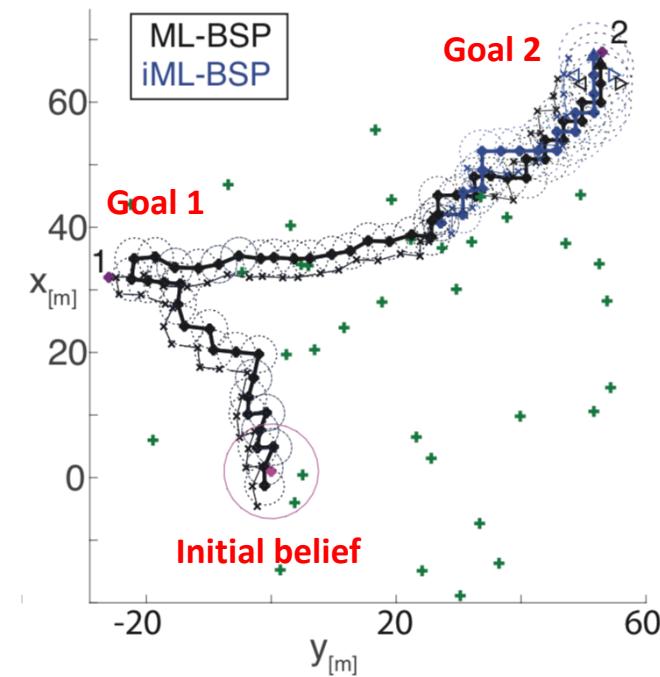
$$\begin{aligned} \frac{\mathbb{P}(\tau_{suffix}^i | b_k, a_k, \pi)}{\mathbb{P}(\tau_{suffix}^i | b_{k_i}^i, a_{k_i}^i, \pi)} &= \frac{\mathbb{P}(b_{k_i+1}^{-i}, o_{k_i+1}^i, \dots, b_{k_i+L}^i | b_k, a_k, \pi)}{\mathbb{P}(b_{k_i+1}^{-i}, o_{k_i+1}^i, \dots, b_{k_i+L}^i | b_{k_i}^i, a_{k_i}^i, \pi)} = \\ &\frac{\mathbb{P}(b_{k_i+1}^{-i} | b_k, a_k)}{\mathbb{P}(b_{k_i+1}^{-i} | b_{k_i}^i, a_{k_i}^i)} \cdot \frac{\cancel{\mathbb{P}(o_{k_i+1}^i, \dots, b_{k_i+L}^i | b_{k_i+1}^{-i}, \pi)}}{\cancel{\mathbb{P}(o_{k_i+1}^i, \dots, b_{k_i+L}^i | b_{k_i+1}^{-i}, \pi)}} = \frac{\mathbb{P}(b_{k_i+1}^{-i} | b_k, a_k)}{\mathbb{P}(b_{k_i+1}^{-i} | b_{k_i}^i, a_{k_i}^i)} \end{aligned}$$



Incremental Belief Space Planning

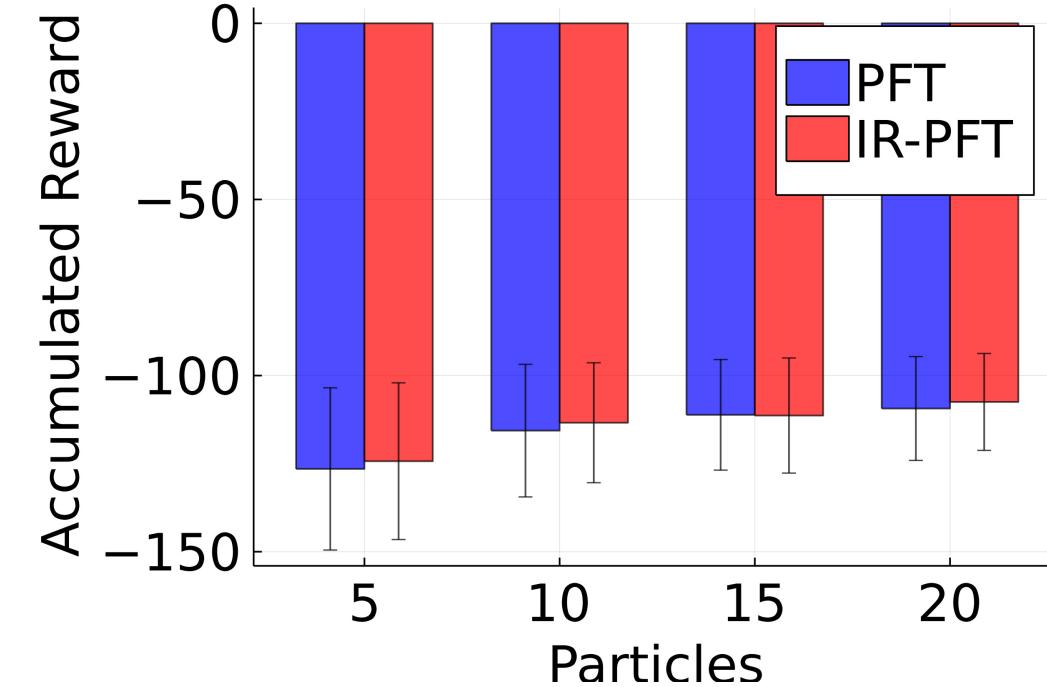
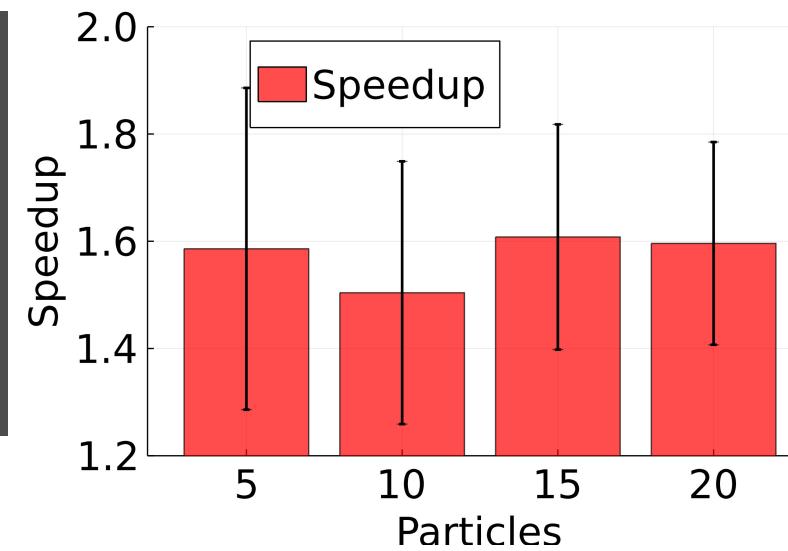
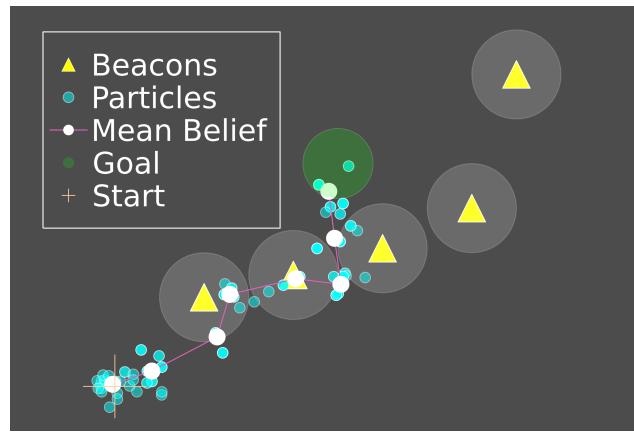
Basic simulation – autonomous navigation in unknown environments:

ML-BSP: BSP with ML observations
(one sample per look ahead step)



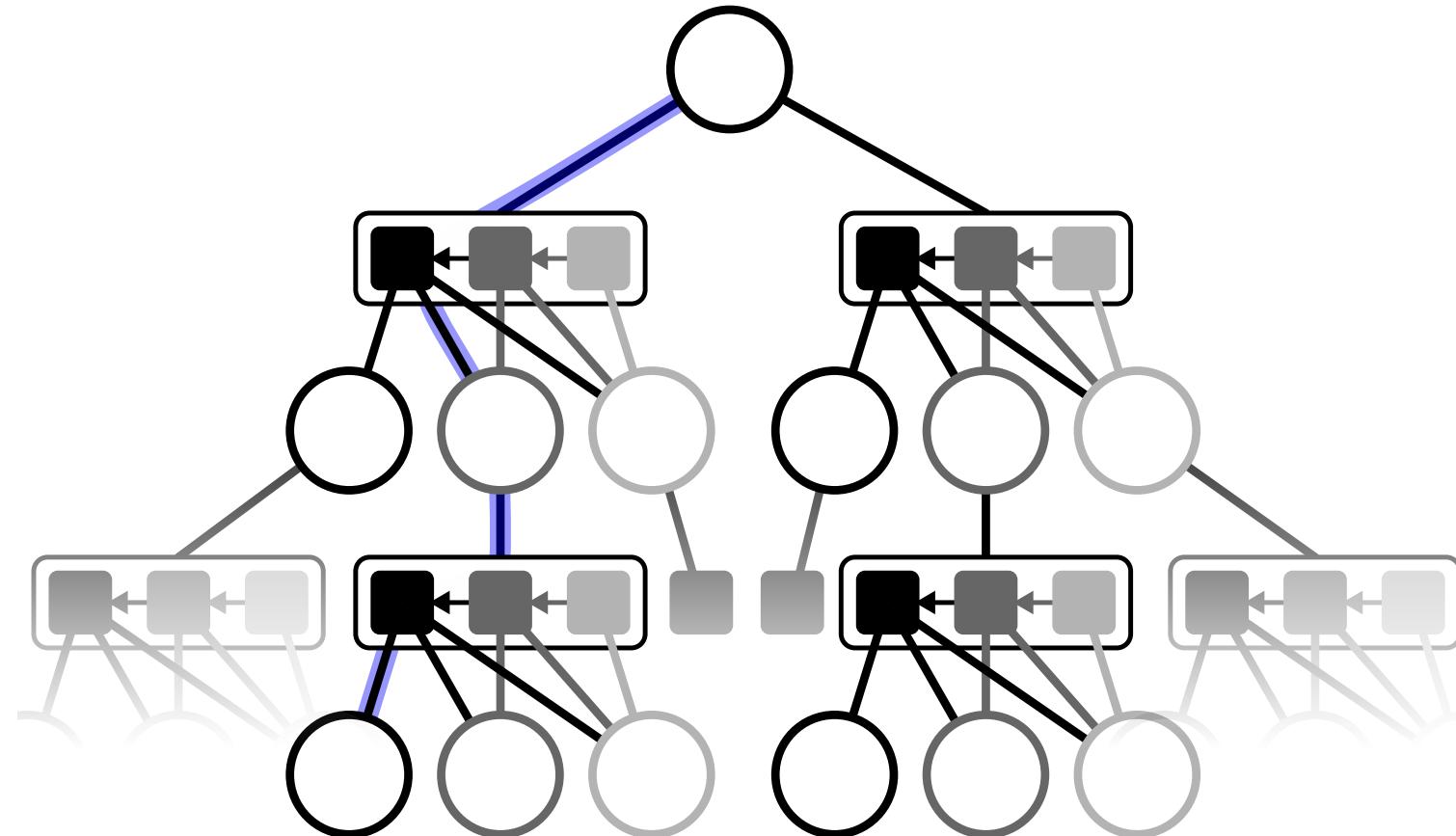
Incremental Reuse Particle Filter Tree (IR-PFT)

- Extend PFT-DPW¹, incorporating trajectories from previous planning sessions for fast estimation of $Q(b_k, a_k)$



¹Z. Sunberg and M. Kochenderfer. "Online algorithms for POMDPs with continuous state, action, and observation spaces." ICAPS, 2018.

Action-Gradient Monte Carlo Tree Search for Non-Parametric Continuous (PO)MDPs



Agenda

Experience Reuse in POMDP Planning

POMDP Planning with Hybrid Beliefs

Simplification of POMDP with Formal Guarantees

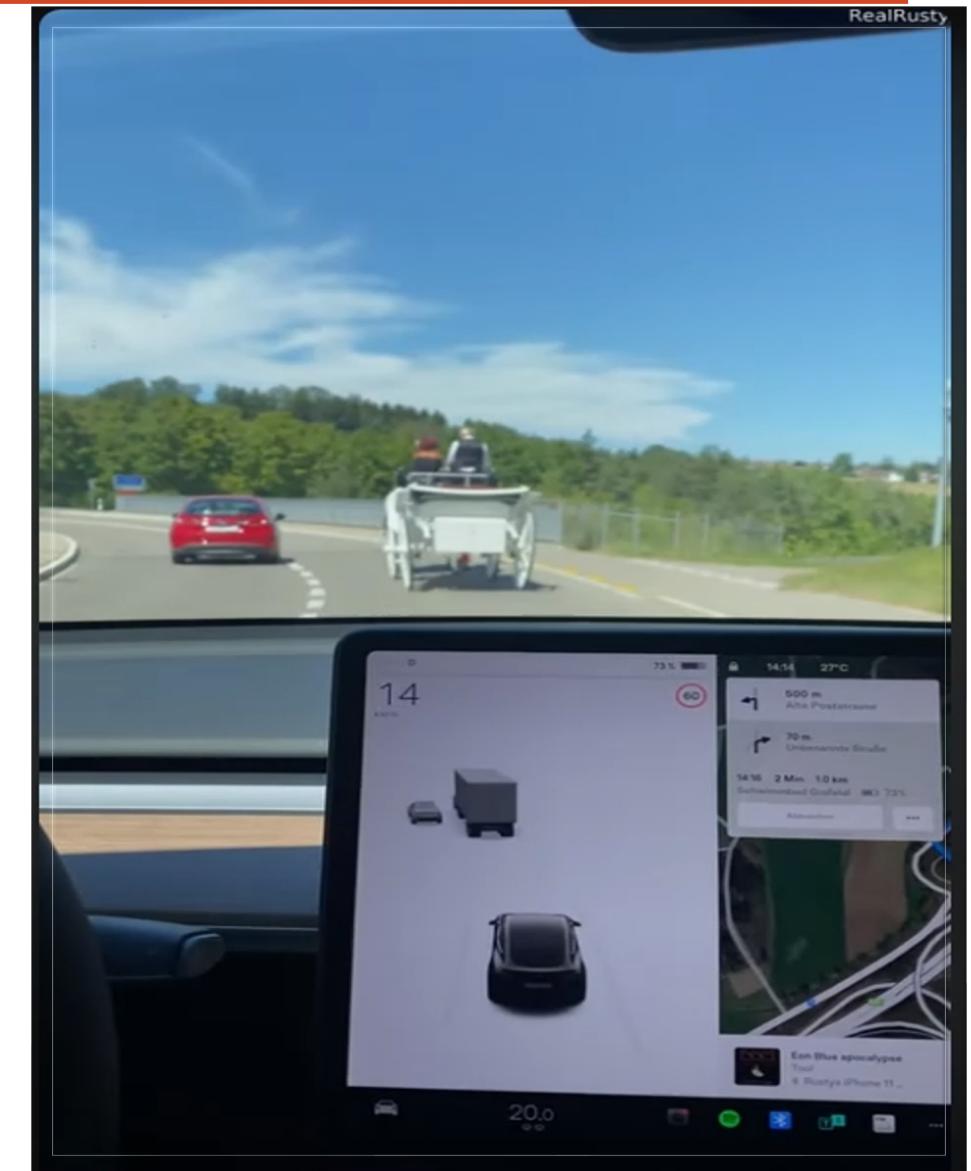
Multi-agent POMDP Planning with Inconsistent Beliefs

Semantic Risk Awareness

Ambiguous Environments

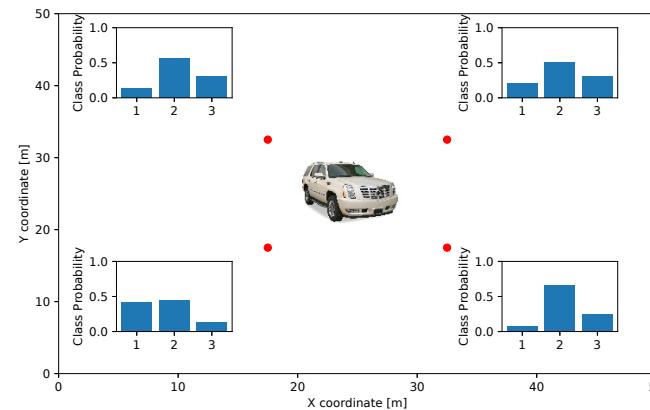
Semantic Perception & SLAM

- Usually, semantics and geometry are considered **separately**
- Cannot use coupled observation models or priors
- Can lead to absurd & **unsafe** performance



Coupled Models

- View-dependent semantic observation model:



$$\mathbb{P}(z^s \mid c, \mathcal{X}^{rel})$$

Semantic observation
(from a classifier)

Object class

Agent's viewpoint
relative to object

- Class and poses can be coupled via learned prior probabilities
- Reward/constraint can depend on both classes and poses

Y. Feldman and V. Indelman, "Bayesian Viewpoint-Dependent Robust Classification under Model and Localization Uncertainty," ICRA'18.

V. Tchuiiev, Y. Feldman, and V. Indelman, "Data Association Aware Semantic Mapping and Localization via a Viewpoint Dependent Classifier Model," IROS'19.

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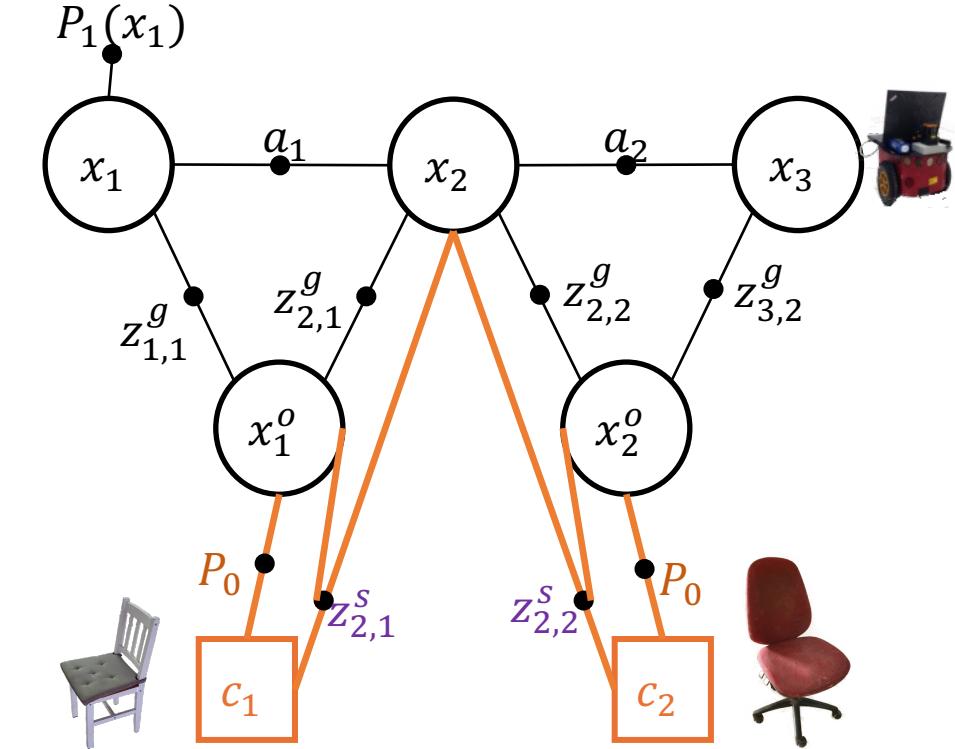
Hybrid Belief

- **Hybrid Belief** at time instant k:

$$b[X_k, C] = \mathbb{P}(X_k, C \mid \mathcal{H}_k)$$

Robot's and objects' poses Objects' classes History (actions, geometric & semantic observations)

- Classes and agent poses are dependent
- Classes of different objects are dependent
- As opposed to:
 - Per-frame classification
 - Modeling semantic observations as viewpoint **independent**



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POMDP Planning with Hybrid Semantic-Geometric Beliefs

- Value function

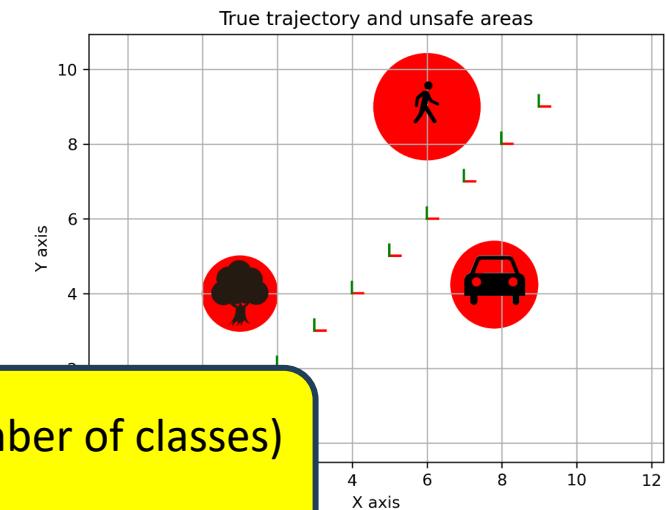
$$V^\pi(b_k) = \mathbb{E}_{z_{k+1:k+L}} \left[\sum_{l=k}^{k+L-1} \rho(b_l, \pi_l(b_l), b_{l+1}) \right]$$

- **Semantic Risk Awareness**

$$\mathbb{P}_{safe} \triangleq \mathbb{P}(\{\wedge_{t=k+1}^L x_t \notin \mathcal{X}_{unsafe}(C, X^o)\} \mid b_k[x_k, C, X^o], \pi)$$

Objects' classes Objects' poses

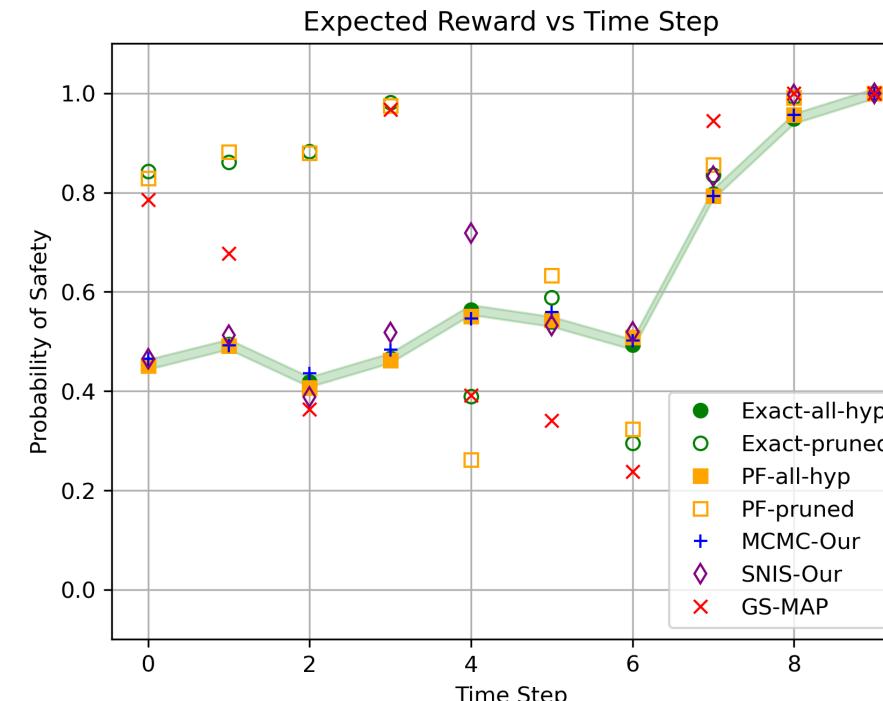
The number of classification hypotheses is M^N (N: number of objects, M: number of classes)
 How to sample w/o pruning hypotheses? How to estimate \mathbb{P}_{safe} ?



POMDP Planning with Hybrid Semantic-Geometric Beliefs

Experiments - Estimation of \mathbb{P}_{safe} with different methods

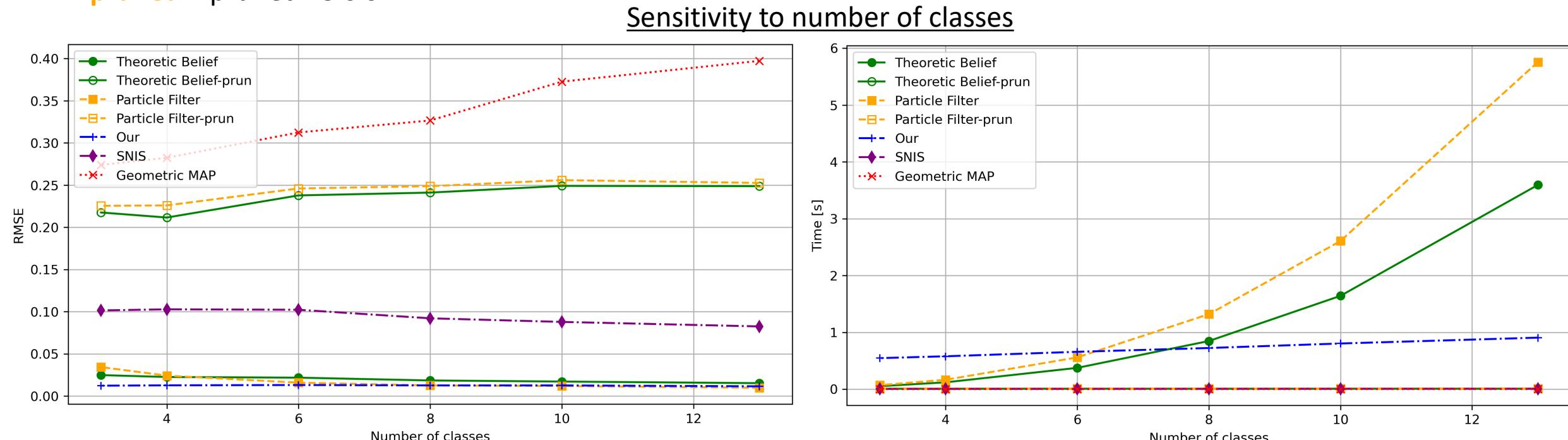
- **Exact-all-hyp** – belief computed exactly
 - **Exact-pruned** – pruned version
 - **PF-all-hyp** – Particle filter
 - **PF-pruned** – pruned version
- Our methods
- **MCMC-Our** – MCMC samples
 - **SNIS-Our** – self-normalized importance sampling
 - **GS-MAP** – separate semantic and geometric



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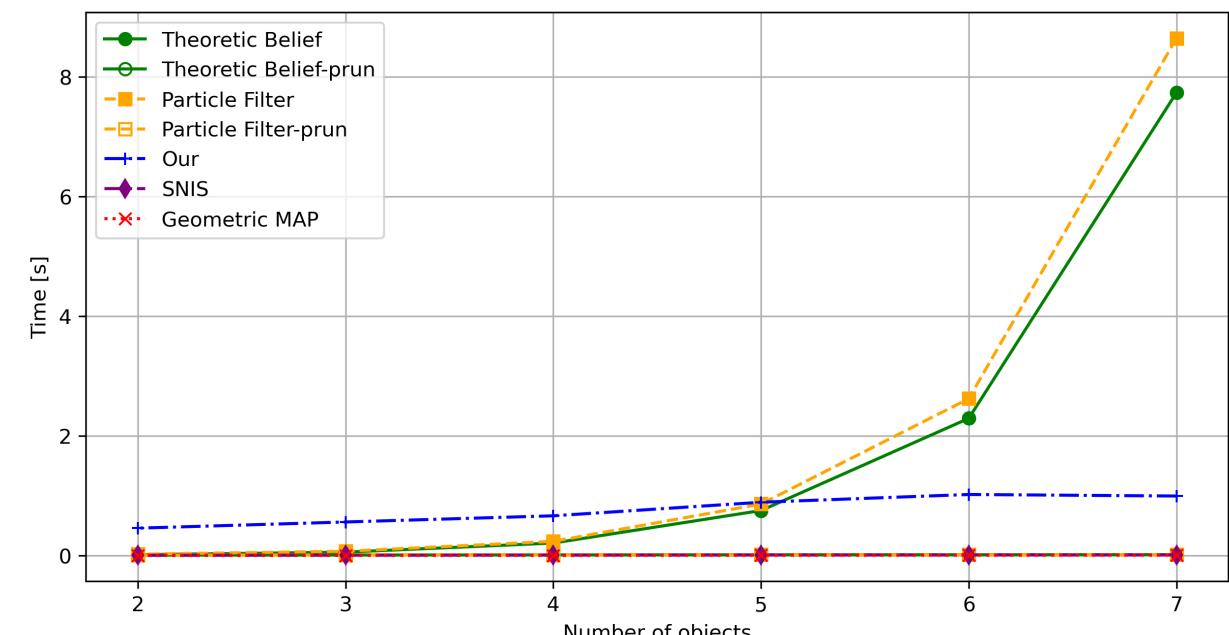
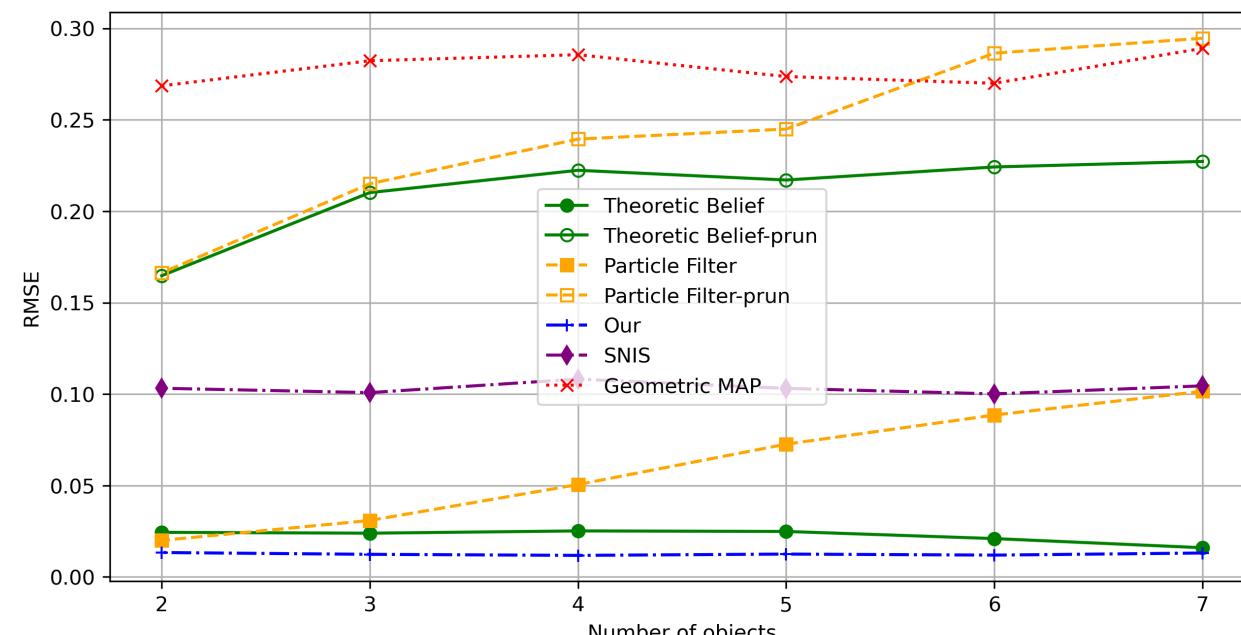


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Sensitivity to number of objects



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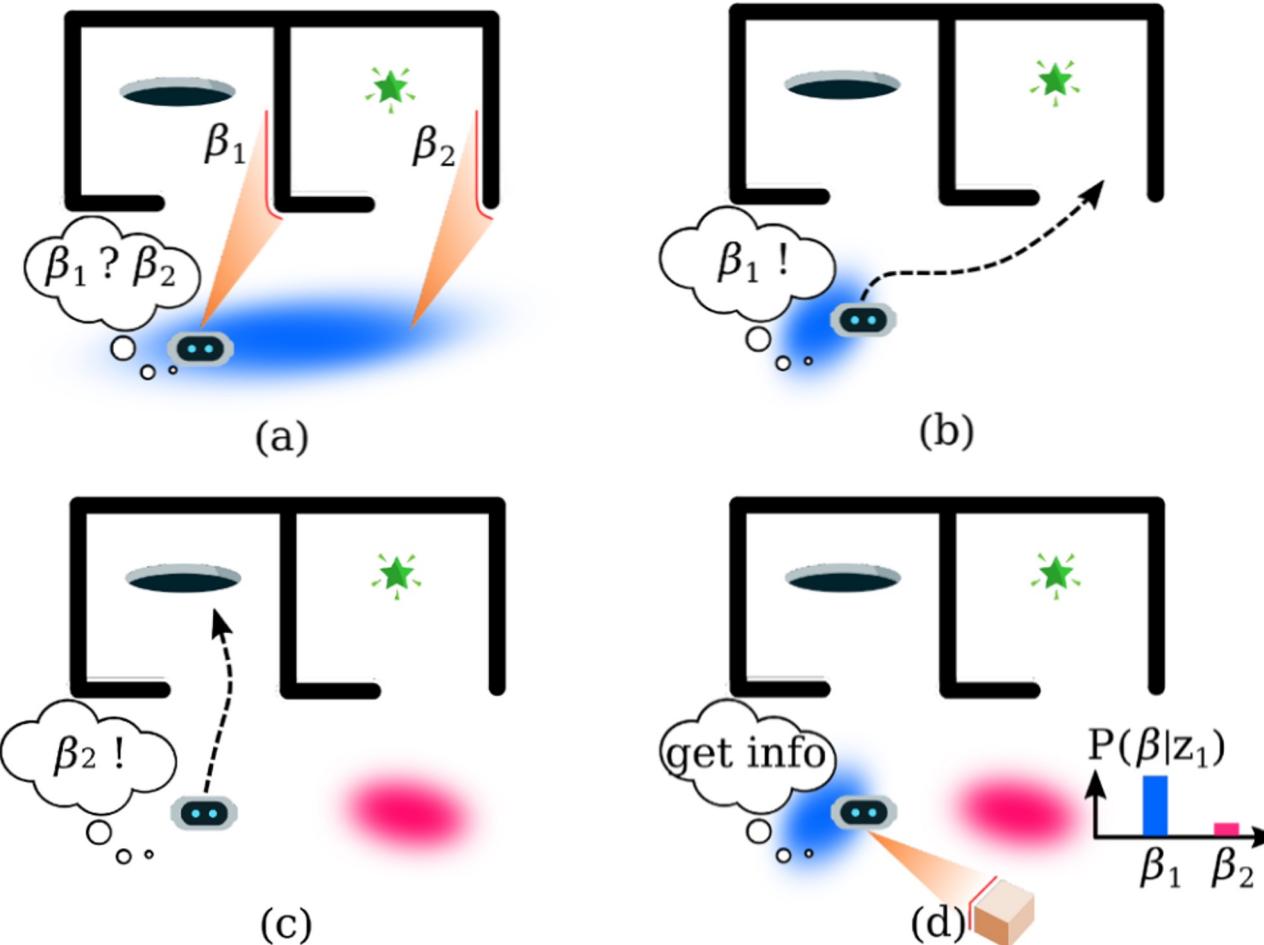
Ambiguous Environments

Ambiguous Scenarios

- Have to reason about data association hypotheses within inference and planning

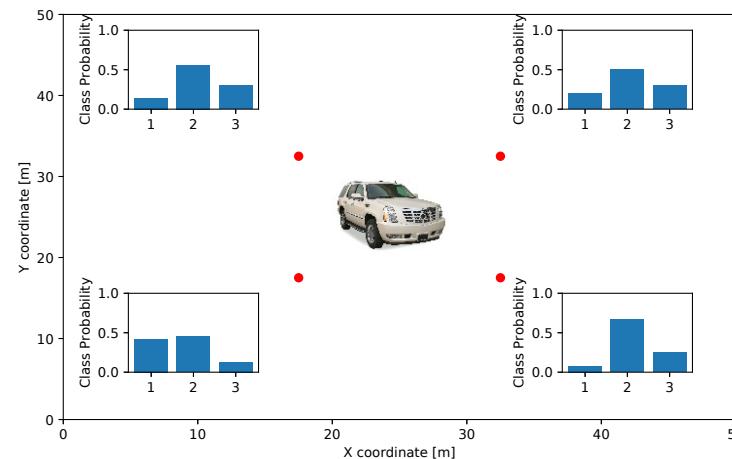
An observation:
(e.g. LIDAR)

How should the agent act?

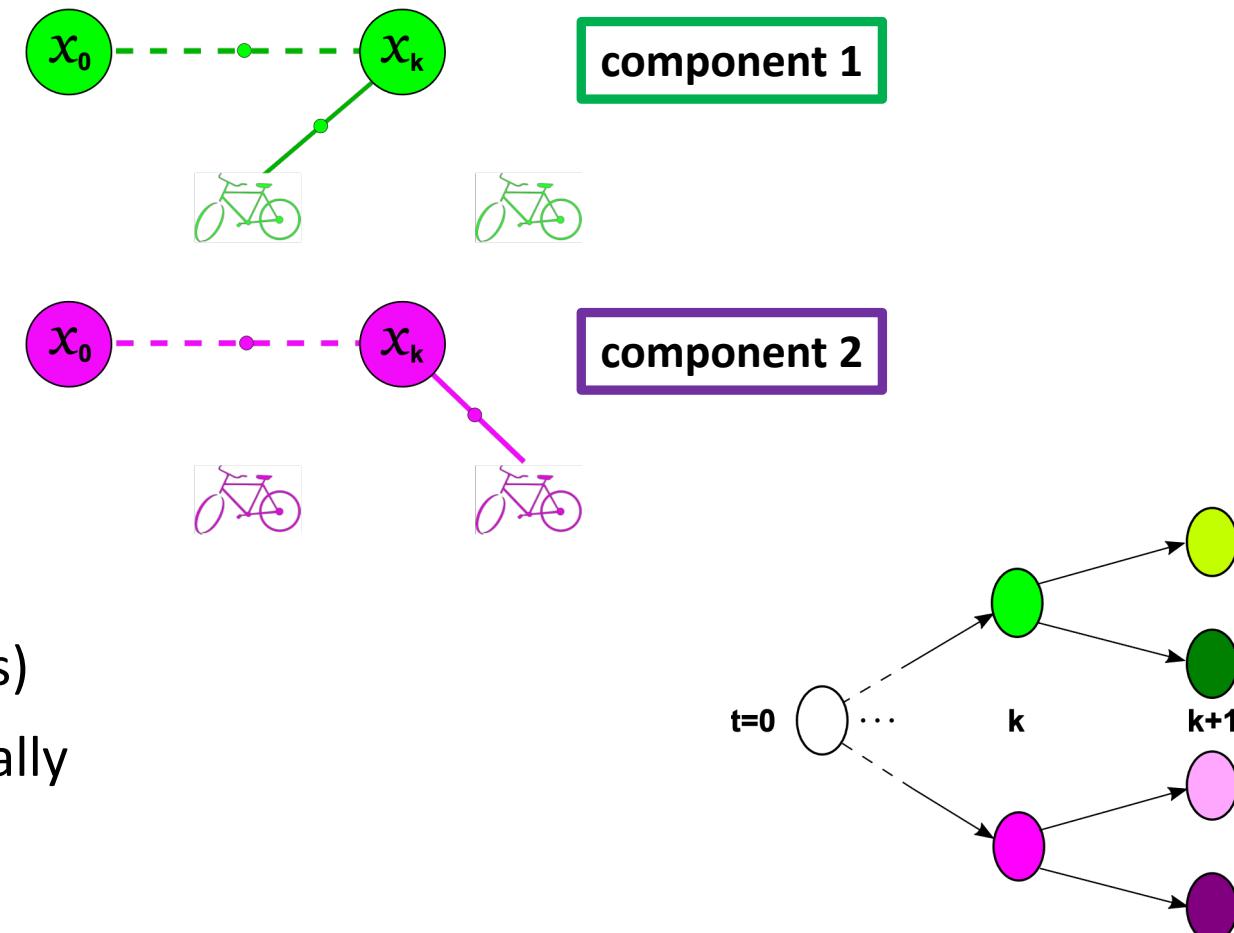


Autonomous Semantic Perception & Ambiguous Environments

Viewpoint dependent semantic models



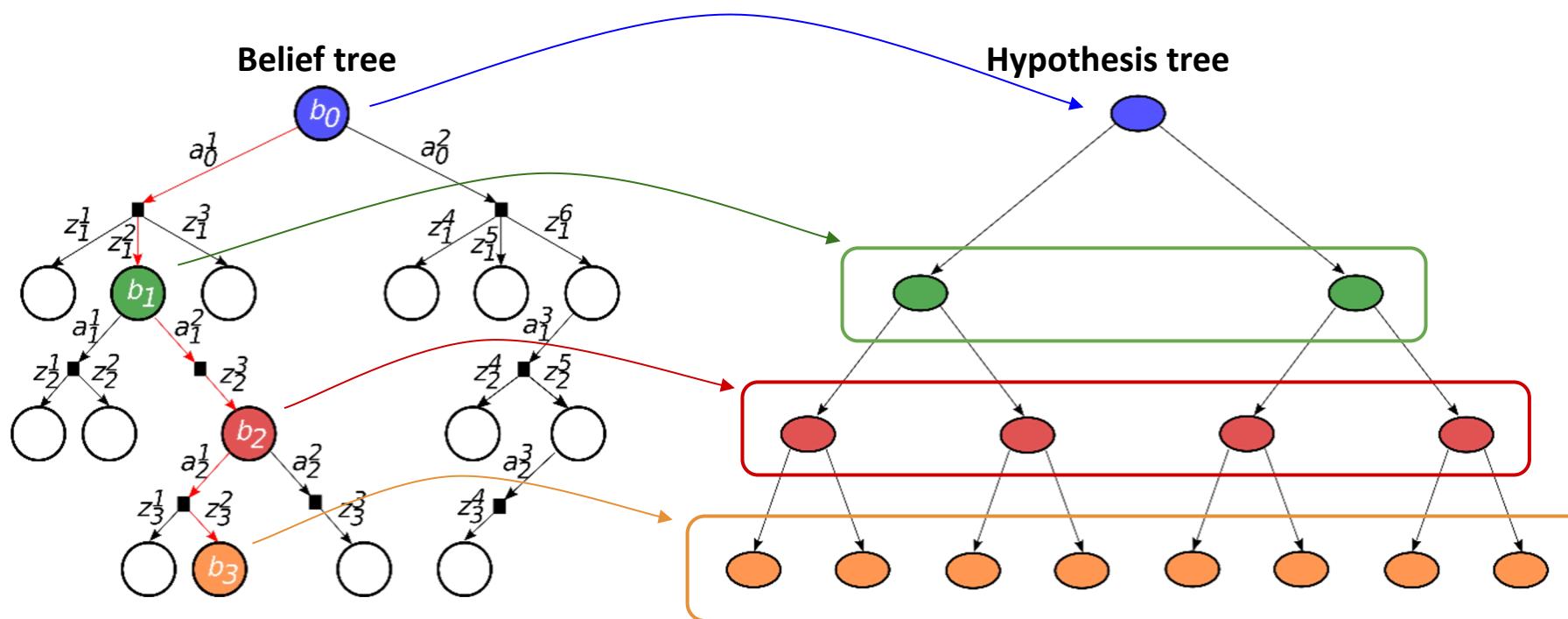
Data association hypotheses



- Hybrid beliefs (over continuous and discrete RVs)
- The number of hypotheses can grow exponentially
- Impact on **safe** decision making?

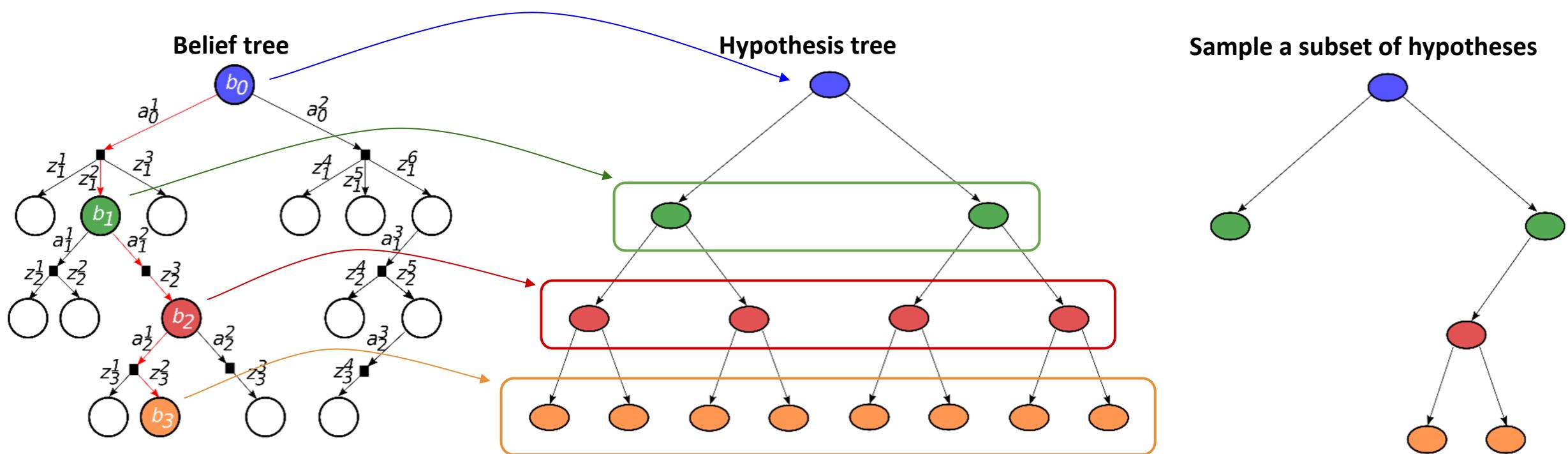
Continuous-Discrete State Spaces - the Challenge

- The number of hypotheses may grow **exponentially** with the planning horizon!



Continuous-Discrete State Spaces - the Challenge

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Impact on **safe** decision making?

Simplification of POMDP with Hybrid Beliefs

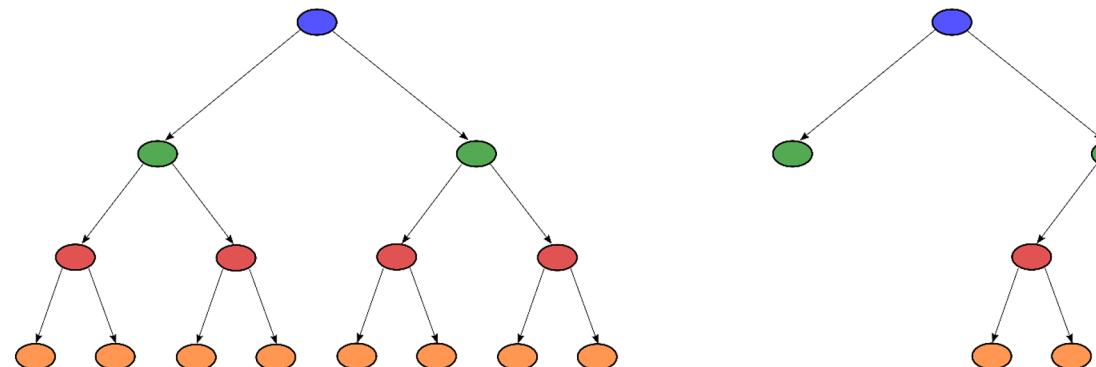
- Deterministic bound to relate the full set of hypotheses to a subset thereof,

Corollary

For any policy π , and selection of hypotheses set $\{\beta_{0:\mathcal{T}}^i\}_{i=0}^{|\mathcal{B}|}$ the following holds,

$$|V^\pi(b_0) - \bar{V}^\pi(\bar{b}_0)| \leq \mathcal{R}_{max} \left[\mathcal{T} \delta_0^\beta + \sum_{k=1}^{\mathcal{T}} \sum_{\tau=1}^k \mathbb{E}_{z_{1:\tau}} [\delta_\tau^\beta] \right].$$

Full tree



Any subset

Importantly, the bound relies on the available hypotheses

Can bound the theoretical value with access only to the simplified tree

Bounds can be evaluated online

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Simplification of Decision-Making Problems

Concept:

- Identify and solve a **simplified (computationally) easier** decision-making problem
- Provide (adaptive) performance guarantees

Specific simplifications include:

- Sparsification of Gaussian beliefs (high dim. state)
- Topological metric for Gaussian beliefs (high dim. state)
- Utilize a subset of samples (nonparametric beliefs)
- Utilize a subset of hypotheses (hybrid beliefs)
- Simplified models and spaces
- Simplification of Risk-Averse POMDP Planning
- Simplification in a multi-agent setting

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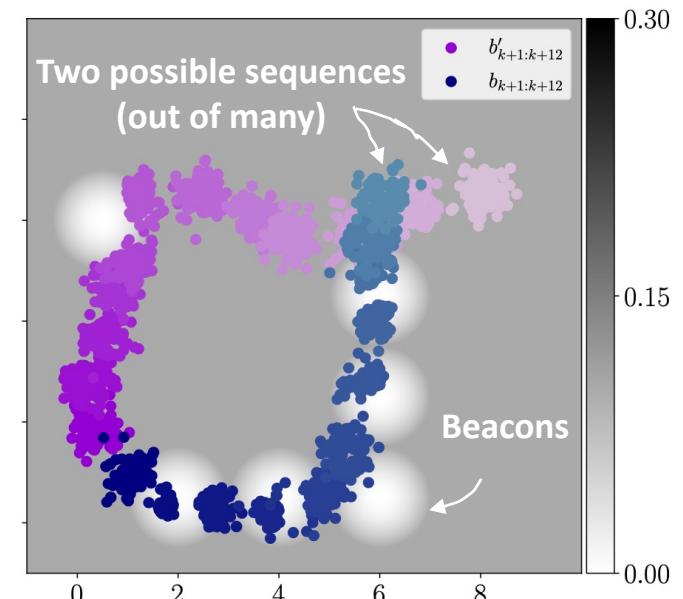
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Simplification of POMDPs with Nonparametric Beliefs

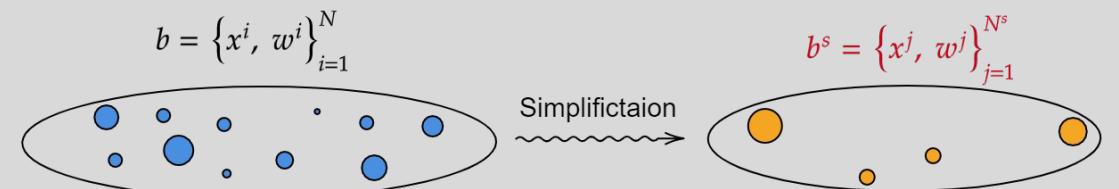
- Value function

$$V_k^\pi(b_k) \equiv J_k(b_k, \pi) = \mathbb{E}\left\{\sum_{l=0}^{L-1} r(b_{k+l}, \pi_{k+l}(b_{k+l})) + r(b_{k+L})\right\}$$



Simplification:

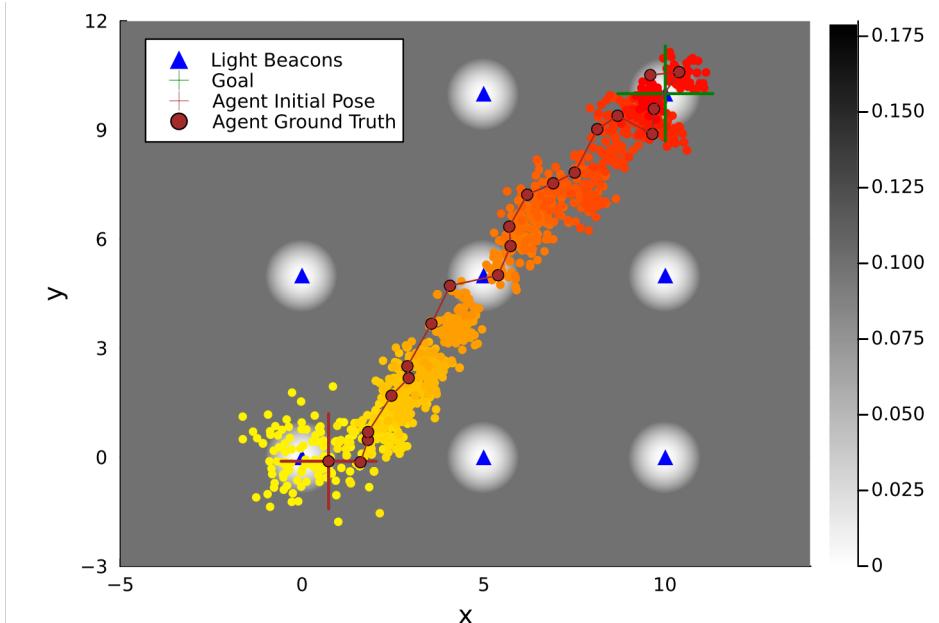
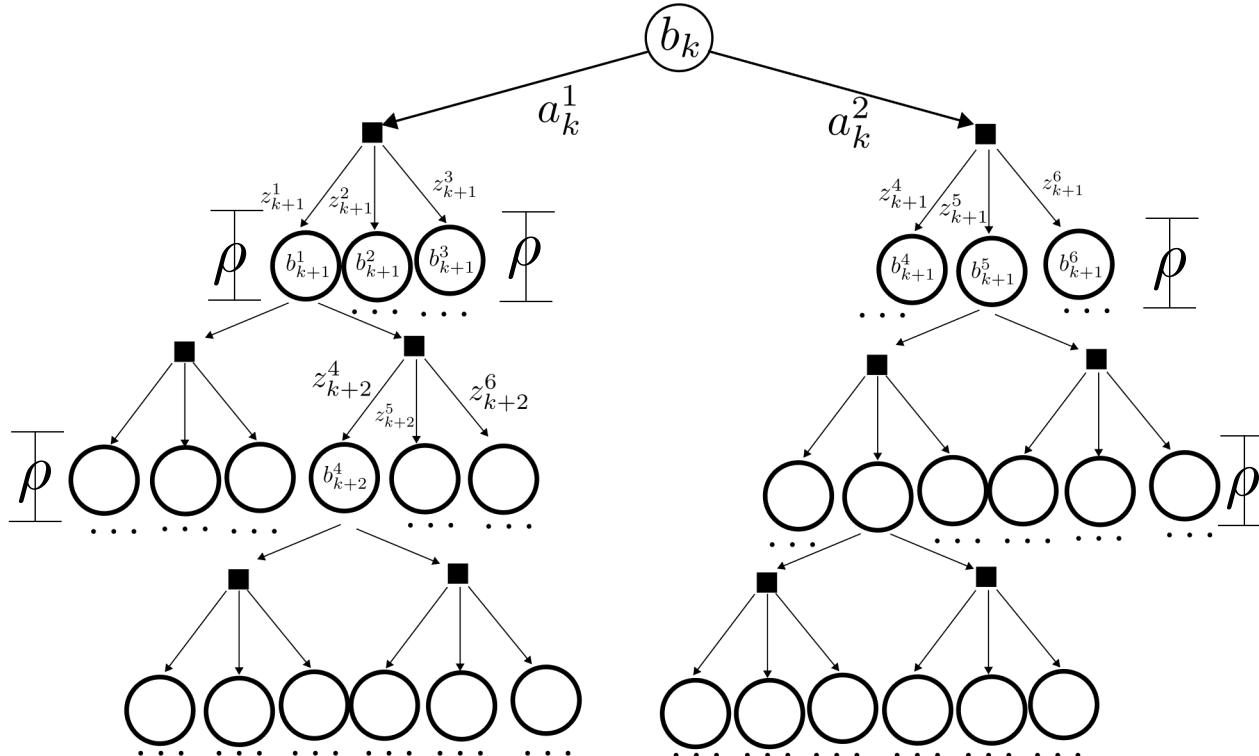
- Utilize a **subset** of samples for planning
- Information-theoretic reward (entropy)
- Analytical (**cheaper**) bounds over the reward



$$lb(b, b^s, a) \leq r(b, a) \leq ub(b, b^s, a)$$

Simplification of POMDPs with Nonparametric Beliefs

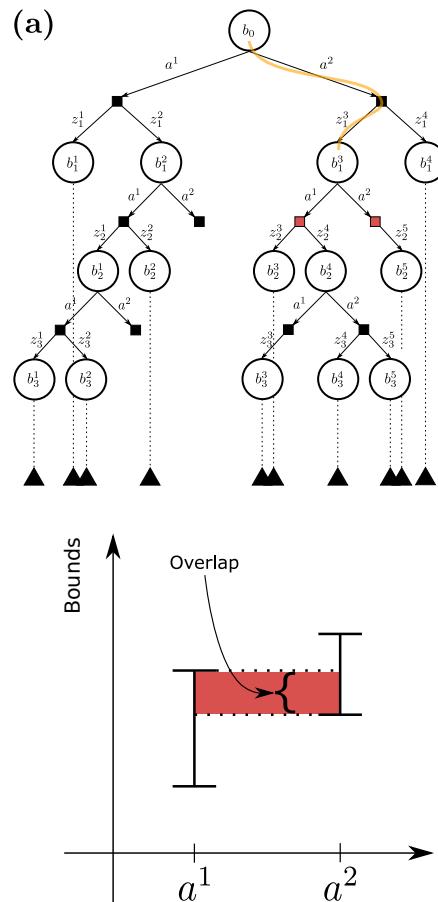
- Adaptive multi-level simplification in a Sparse Sampling setting:



Typical speedup of 20% - 50%,
Same performance!

Simplification of POMDPs with Nonparametric Beliefs

- Adaptive multi-level simplification in an MCTS setting:



Simplification of Decision-Making Problems

Concept:

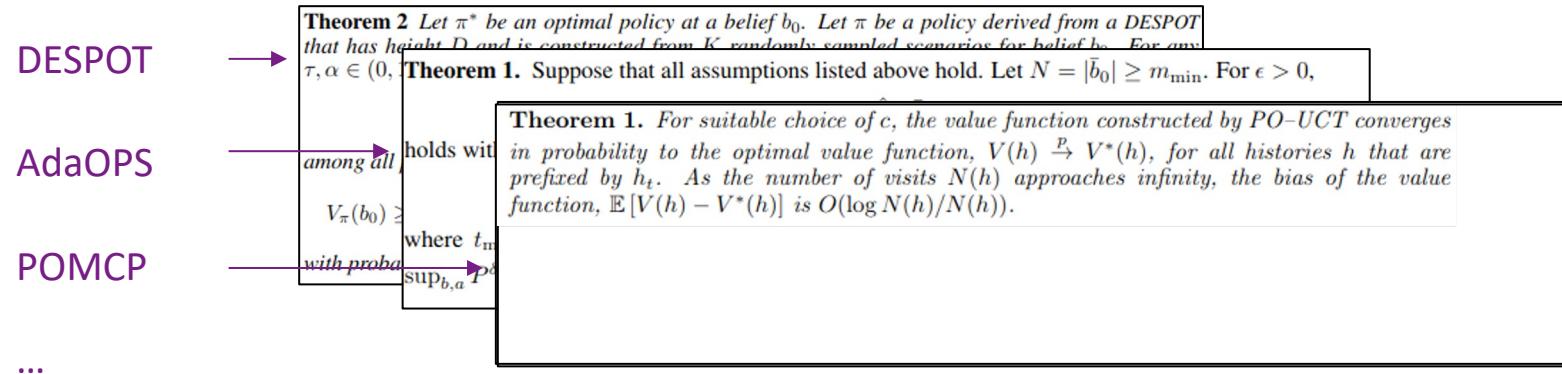
- Identify and solve a **simplified (computationally) easier** decision-making problem
- Provide (adaptive) performance guarantees

Specific simplifications include:

- Sparsification of Gaussian beliefs (high dim. state)
- Topological metric for Gaussian beliefs (high dim. state)
- Utilize a subset of samples (nonparametric beliefs)
- Utilize a subset of hypotheses (hybrid beliefs)
- Simplified models and spaces
- Simplification of Risk-Averse POMDP Planning
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POMDPs with Deterministic Guarantees

SOTA sampling based approaches come with probabilistic theoretical guarantees



Can we get deterministic guarantees?

We show that deterministic guarantees are indeed possible!

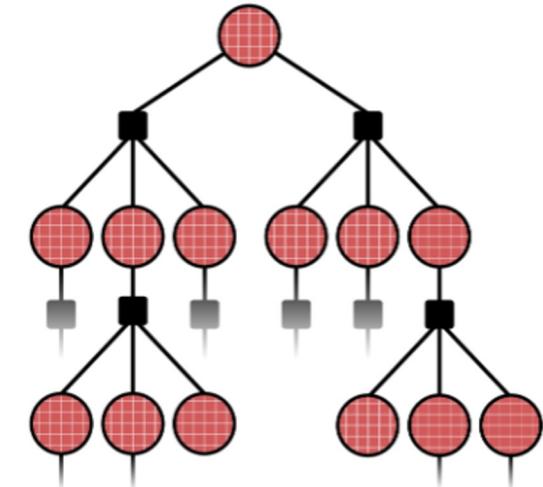
Online POMDP Planning with Anytime Deterministic Guarantees

Concept:

Instead of solving the original POMDP, consider a simplified version of that POMDP.

$$\mathcal{M} \xrightarrow{\text{wavy arrow}} \bar{\mathcal{M}}$$

Derive a mathematical relationship between the solution of the simplified, and the theoretical POMDP.



$$V(b) \xleftarrow{\text{?}} \bar{V}(b)$$

Online POMDP Planning with Anytime Deterministic Guarantees

- Given a POMDP: $\mathcal{M} = \langle \mathcal{X}, \mathcal{Z}, \mathcal{A}, b_0, \mathcal{P}_T, \mathcal{P}_Z, \rho, \gamma \rangle$
- Define a **simplified** POMDP,

$$\bar{\mathcal{M}} = \langle \bar{\mathcal{X}}, \bar{\mathcal{Z}}, \mathcal{A}, \bar{b}_0, \bar{\mathcal{P}}_T, \bar{\mathcal{P}}_Z, \rho, \gamma \rangle$$

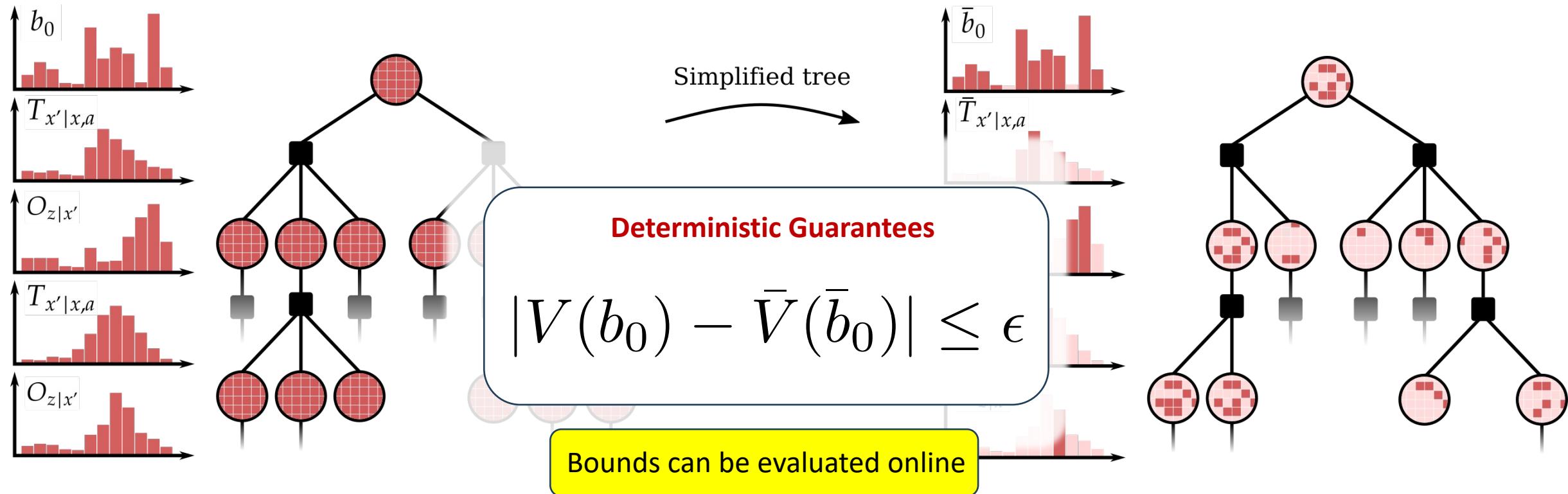
$\bar{\mathcal{X}}(H_t) \subset \mathcal{X}$ $\bar{b}_0(x) \triangleq \begin{cases} b_0(x) & , x \in \bar{\mathcal{X}}_0 \\ 0 & , otherwise \end{cases}$
 $\bar{\mathcal{Z}}(H_t) \subset \mathcal{Z}$ $\bar{\mathbb{P}}(x_{t+1} | x_t, a_t) \triangleq \begin{cases} \mathbb{P}(x_{t+1} | x_t, a_t) & , x_{t+1} \in \bar{\mathcal{X}}(H_{t+1}^-) \\ 0 & , otherwise \end{cases}$
 $\bar{\mathbb{P}}(z_t | x_t) \triangleq \begin{cases} \mathbb{P}(z_t | x_t) & , z_t \in \bar{\mathcal{Z}}(H_t) \\ 0 & , otherwise \end{cases}$

- Simplified value function

$$\bar{V}^\pi(\bar{b}_t) \triangleq r(\bar{b}_t, \pi_t) + \bar{\mathbb{E}}_{z_{t+1:\mathcal{T}}} [\bar{V}^\pi(\bar{b}_{t+1})]$$

Online POMDP Planning with Anytime Deterministic Guarantees

- Deterministic guarantees (assuming discrete spaces)



Online POMDP Planning with Anytime Deterministic Guarantees

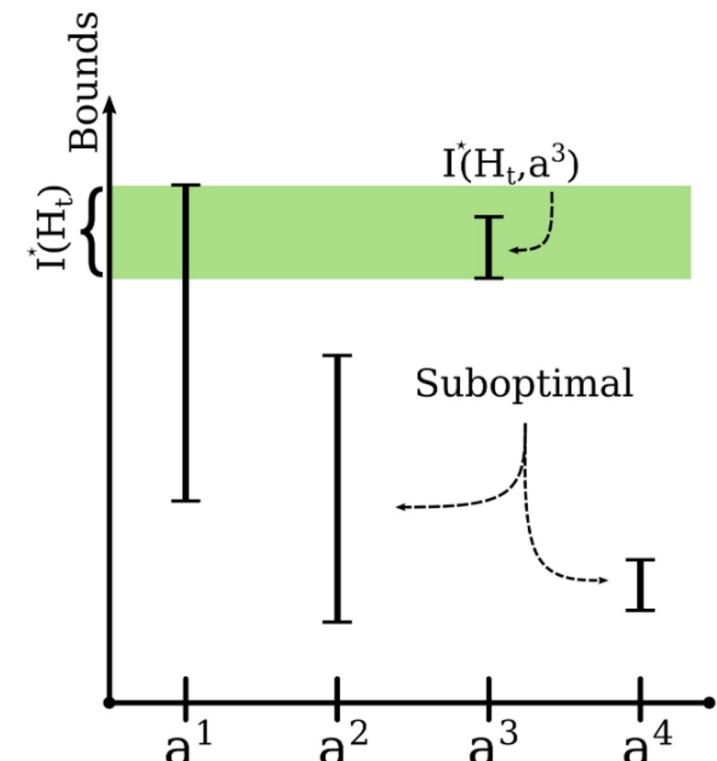
Importantly, the bounds can be calculated during planning.

How can we use them?

- **Pruning of sub-optimal branches**
 - Made possible by the deterministic guarantees
- **Stopping criteria for the planning phase**
 - Made possible by the deterministic guarantees
- **Finding the optimal solution in finite time**
 - Without recovering the theoretical tree

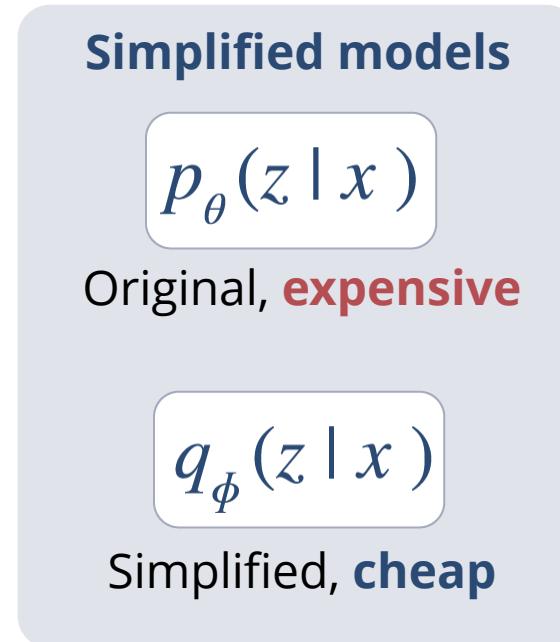
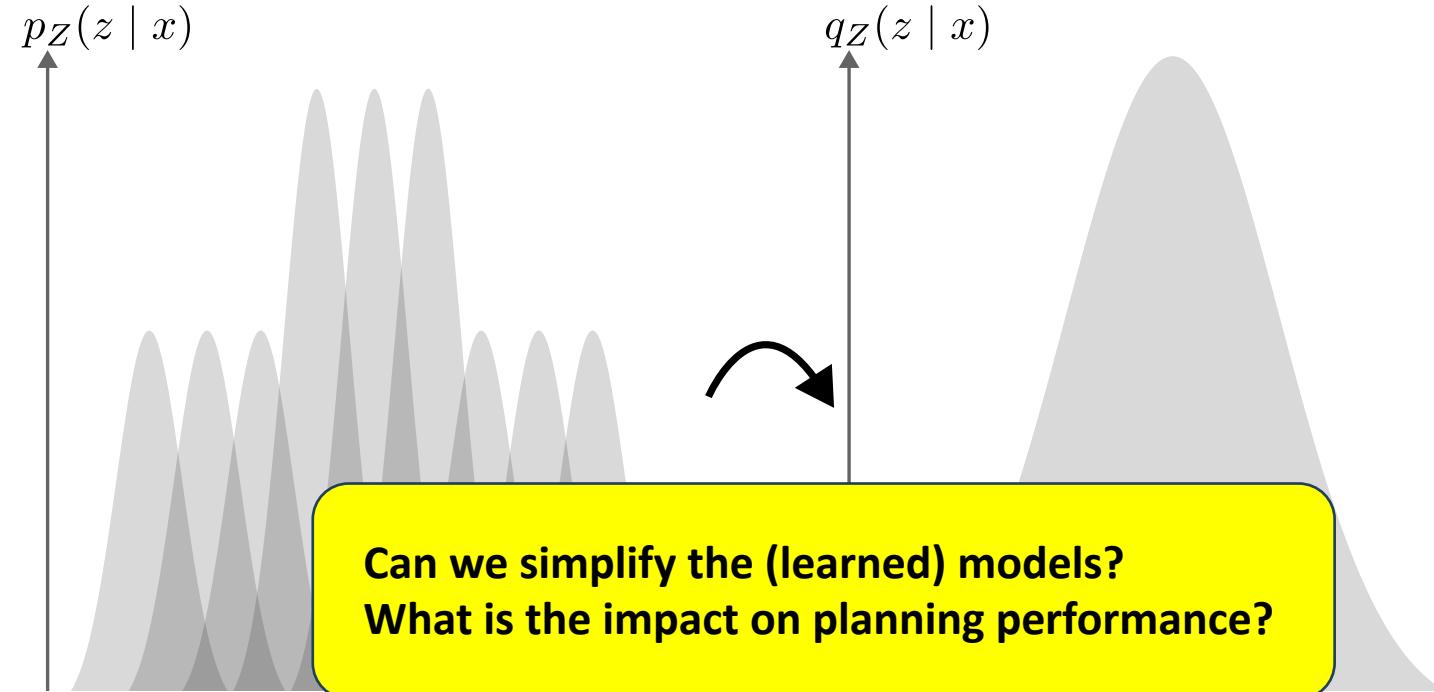
Deterministic Guarantees

$$|V(b_0) - \bar{V}(\bar{b}_0)| \leq \epsilon$$



Simplifying Complex Observation Models with Probabilistic Guarantees

- We replace the (learned) observation model p_Z with a cheaper model q_Z
 - Simpler GMM, Shallower Neural Network, etc.
 - Example:



Simplifying Complex Observation Models with Probabilistic Guarantees

- We replace the (learned) observation model p_Z with a cheaper model q_Z
- Simplified action-value function: $Q_P^{q_Z}$

Corollary 3

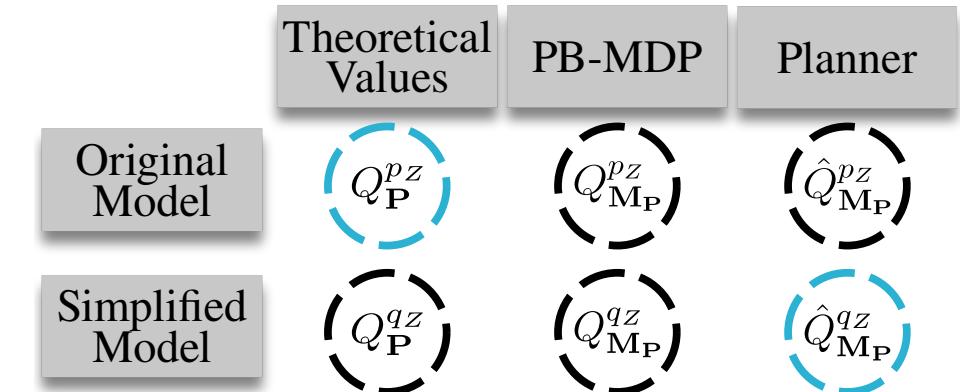
For arbitrary $\varepsilon, \delta > 0$ there exists a number of particles for which

$$\underline{|Q_P^{p_Z}(b_t, a) - \hat{Q}_{M_P}^{q_Z}(\bar{b}_t, a)|} \leq \Phi_{M_P}(\bar{b}_t, a) + \varepsilon$$

with probability of at least $1 - \delta$ for any guaranteed planner

Theoretical Q function
of the POMDP, with
original models

Estimator of the Q function of a
particle-belief POMDP, with
simplified models



- Importance sampling
- Separate calculations to offline/online

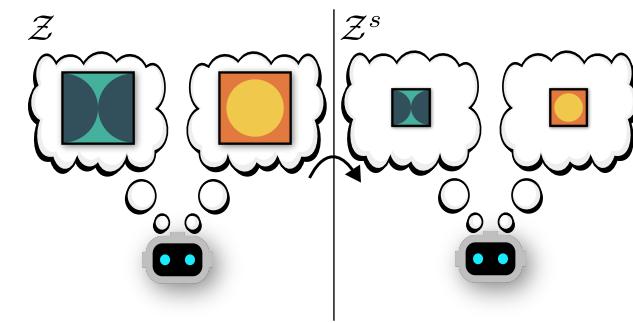
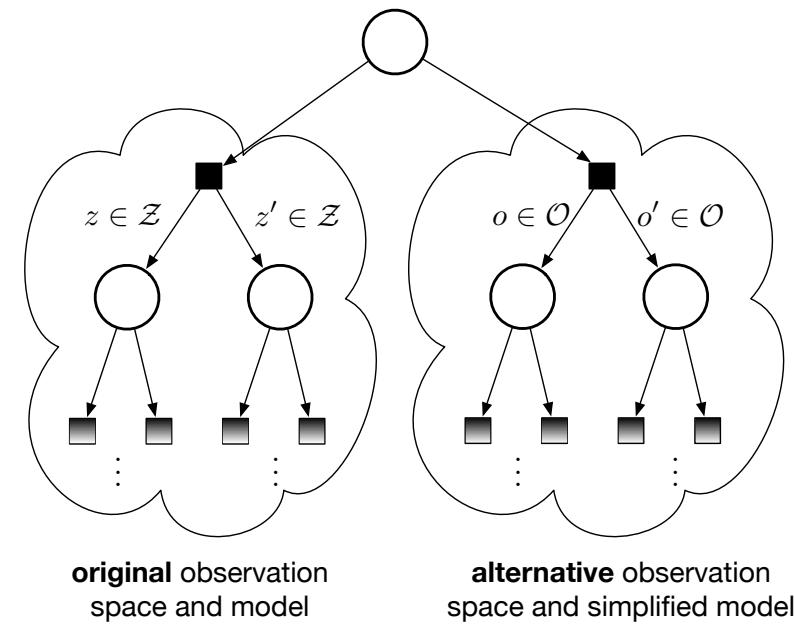
Simplified POMDP Planning with an Alternative Observation Space

- Switch to an alternative observation space and model

Model Definition

POMDP tuple: $\langle \mathcal{X}, \mathcal{A}, \mathcal{Z}, \mathbb{P}_T, \mathbb{P}_Z, b_k, r \rangle \rightarrow \langle \mathcal{X}, \mathcal{A}, \mathcal{O}, \mathbb{P}_T, \mathbb{P}_O, b_k, r \rangle$

- Only at certain levels and branches of the tree



Simplified POMDP Planning with an Alternative Observation Space

- Switch to an alternative observation space and model

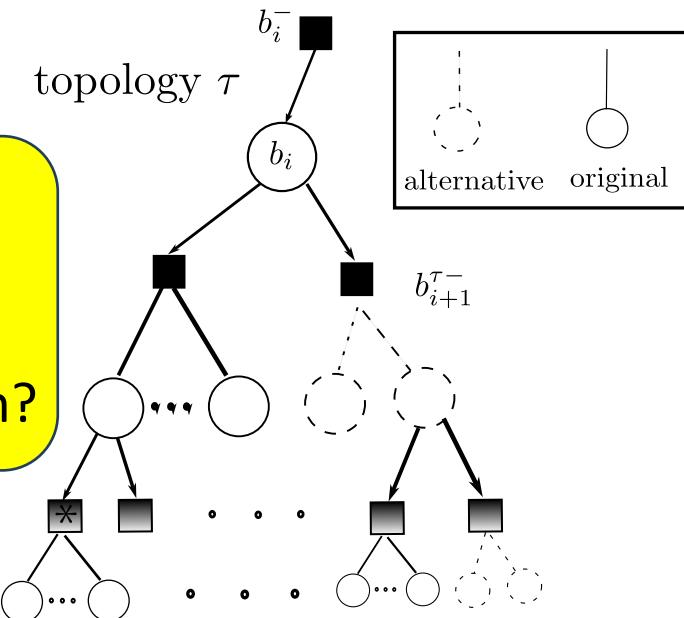
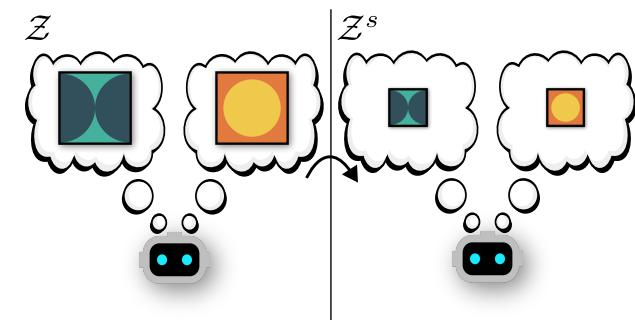
Model Definition

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- Only at certain levels and branches of the tree

Main questions addressed:

- How to decide online where to simplify in belief tree?
- How to provide formal performance guarantees?
- How to adaptively transition between the different levels of simplification?



Simplification of Decision-Making Problems

Concept:

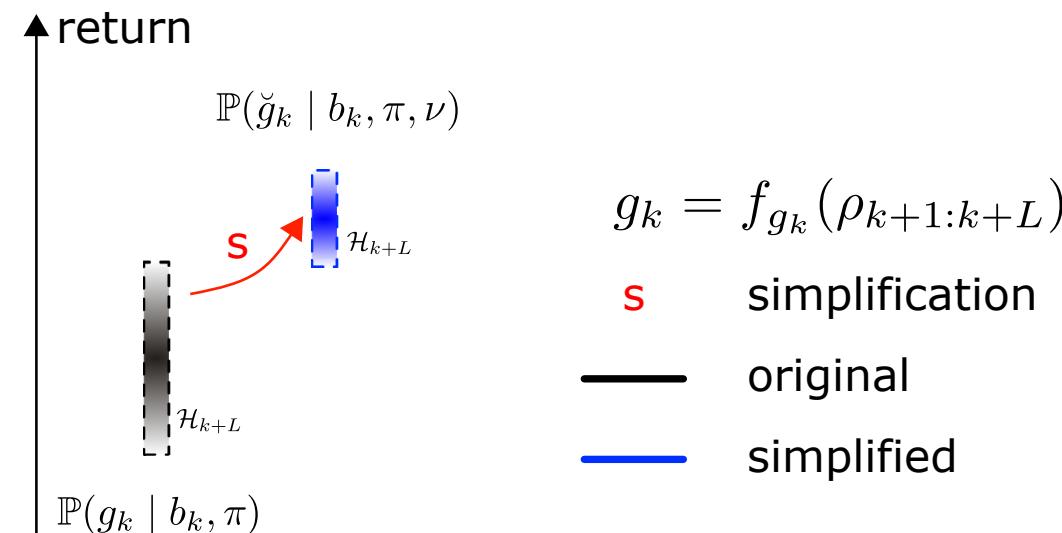
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Specific simplifications include:

- Sparsification of Gaussian beliefs (high dim. state)
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Simplification of Risk Averse POMDP Planning

- Impact of simplification on **distribution** over returns/rewards
- Simplified **risk aware** decision making with belief-dependent rewards



$$V^\pi(b_k) = \varphi \left(\mathbb{P}(\rho_{k+1:k+L} | b_k, \pi_{k:k+L-1}), g_k \right)$$

Probabilistically Constrained Belief Space Planning

$$\max_{\pi_{k+}} \mathbb{E} \left[\sum_{\ell=k}^{k+L-1} \rho_{\ell+1} \middle| b_k, \pi_{k+} \right]$$

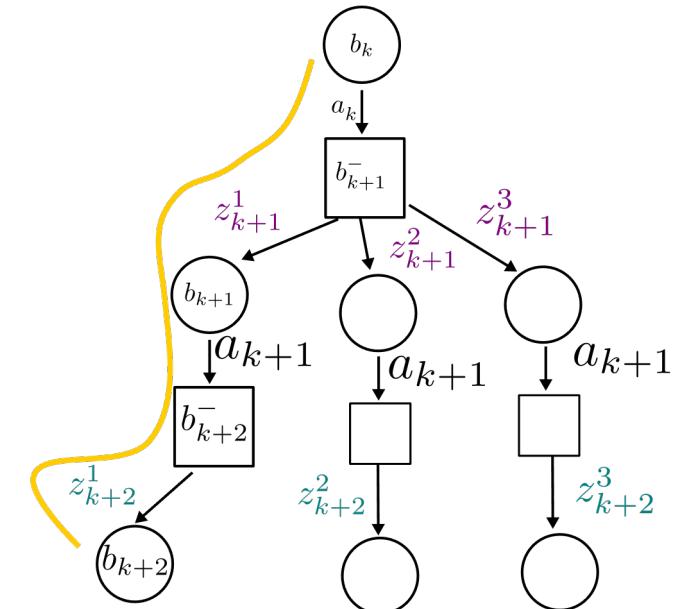
subject to $P(c(b_{k:k+L}; \phi, \delta) = 1 | b_k, \pi_{k+}) \geq 1 - \epsilon$

Information gain¹:

$$c(b_{k:k+L}; \phi, \delta) \triangleq \mathbf{1}_{\left\{ \left(\sum_{\ell=k}^{k+L-1} \phi(b_\ell, b_{\ell+1}) \right) \geq \delta \right\}} (b_{k:k+L})$$

Safety²:

$$c(b_{k:k+L}; \phi, \delta) \triangleq \prod_{\ell=k}^{k+L} \mathbf{1}_{\{b_\ell: \phi(b_\ell) \geq \delta\}} (b_\ell)$$



¹A. Zhitnikov and V. Indelman, "Simplified Continuous High Dimensional Belief Space Planning with Adaptive Probabilistic Belief-dependent Constraints," T-RO'24.

²A. Zhitnikov and V. Indelman, "Anytime Probabilistically Constrained Provably Convergent Online Belief Space Planning," arXiv'24.

Agenda

Experience Reuse in POMDP Planning

POMDP Planning with Hybrid Beliefs

Simplification of POMDP with Formal Guarantees

Multi-agent POMDP Planning with Inconsistent Beliefs

Simplification of Decision-Making Problems

Concept:

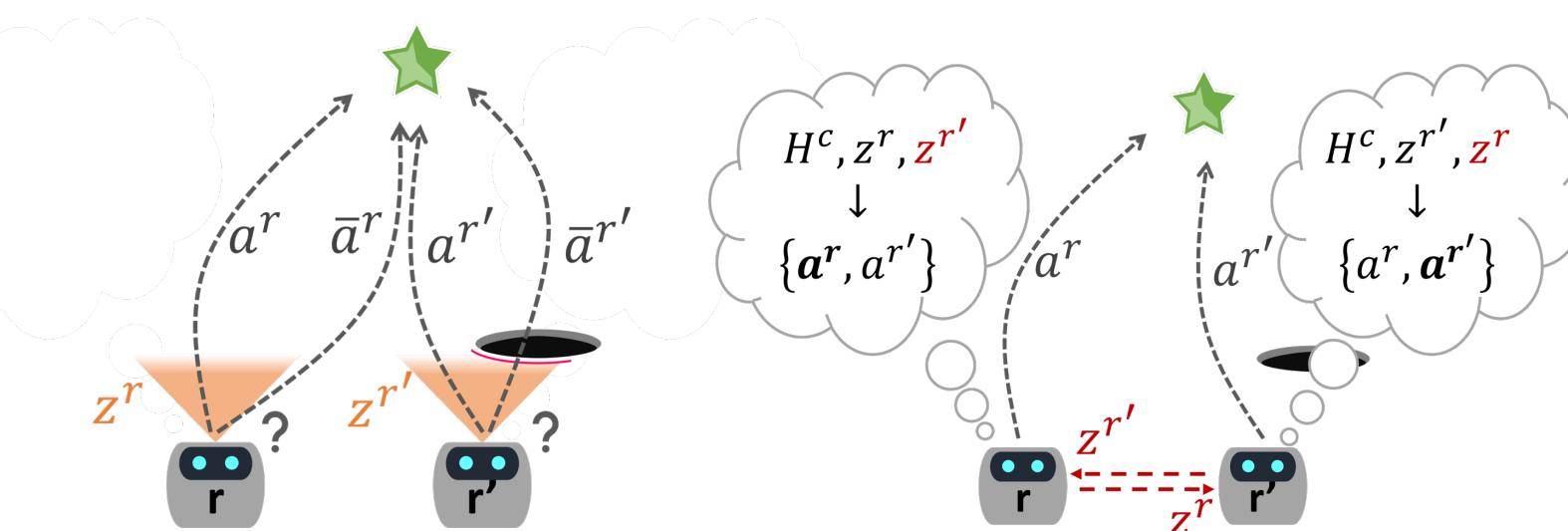
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Multi-Robot Belief Space Planning

- **A common assumption:** Beliefs of different robots are consistent at planning time
- Requires prohibitively frequent data-sharing capabilities!



Multi-Robot Cooperative BSP with Inconsistent Beliefs

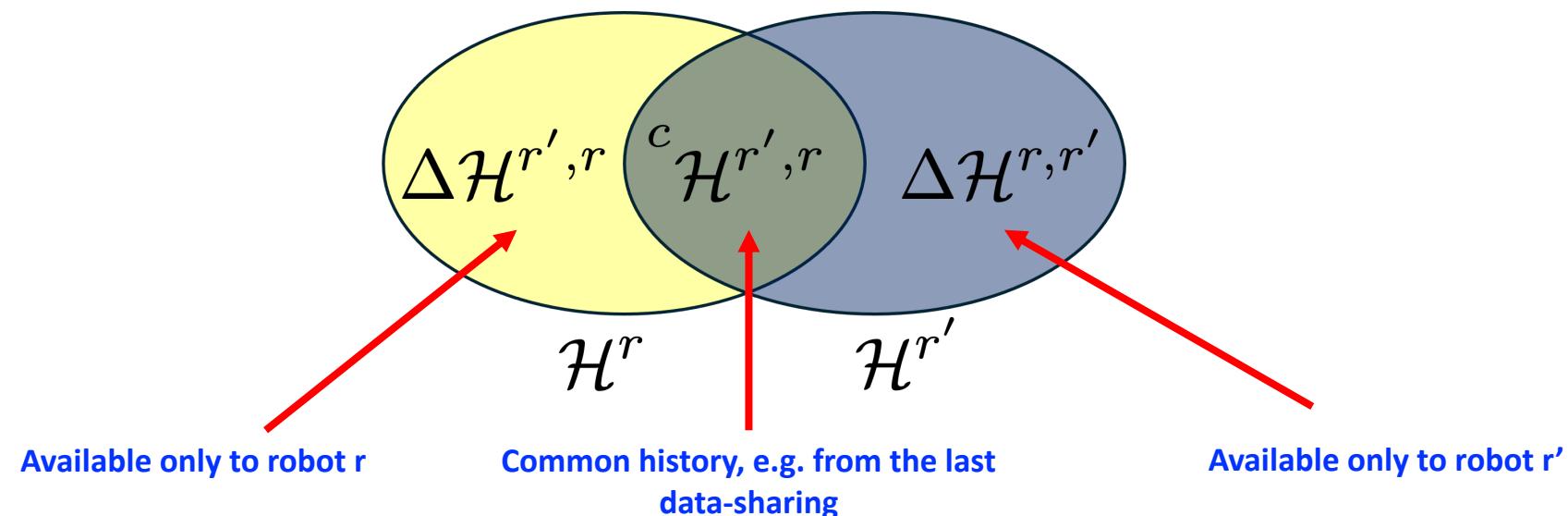
What happens when data-sharing capabilities between the robots are limited?

- Histories & beliefs of the robots may **differ** due to limited data-sharing capabilities

$$b_k^r = \mathbb{P}(x_k \mid \mathcal{H}_k^r)$$

$$b_k^{r'} = \mathbb{P}(x_k \mid \mathcal{H}_k^{r'})$$

$$\mathcal{H}_k^r \neq \mathcal{H}_k^{r'}$$



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- Decentralized POMDP tuple from the perspective of robot r:

$$\langle \mathcal{X}, \mathcal{Z}, \mathcal{A}, T, O, \rho, b_k^r \rangle$$

- Objective function:

$$J(b_k^r, a_{k+}) = \mathbb{E}_{z_{k+1:k+L}} \left[\sum_{l=0}^{L-1} \rho(b_{k+l}^r, a_{k+l}) + \rho(b_{k+L}^r) \right]$$

Multi-Robot Cooperative BSP with Inconsistent Beliefs

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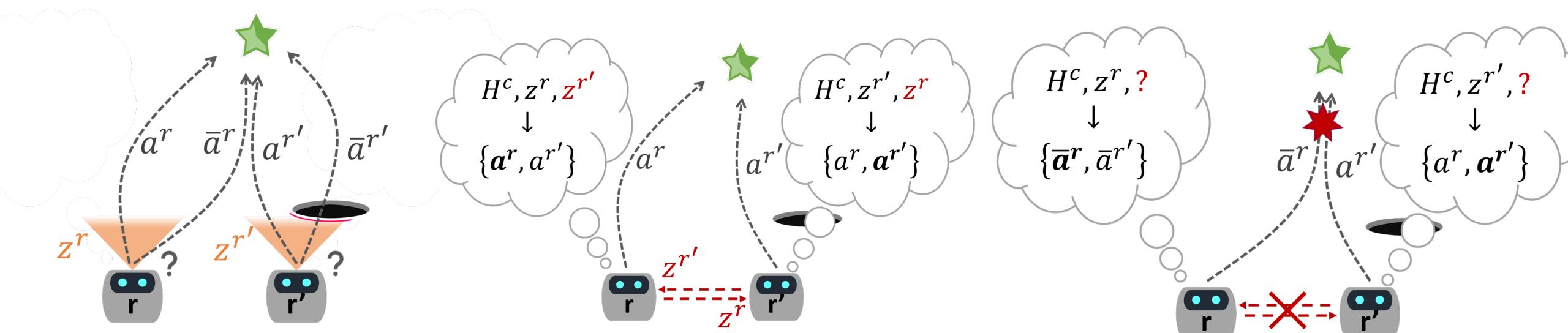
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- Can lead to a lack of coordination and unsafe and sub-optimal actions



T. Kundu, M. Rafaeli, and V. Indelman, "Multi-Robot Communication-Aware Cooperative Belief Space Planning with Inconsistent Beliefs: An Action-Consistent Approach," IROS'24.

T. Kundu, M. Rafaeli, A. Gulyaev, and V. Indelman, "Action-Consistent Decentralized Belief Space Planning with Inconsistent Beliefs and Limited Data Sharing: Framework and Simplification Algorithms with Formal Guarantees," arXiv'25.

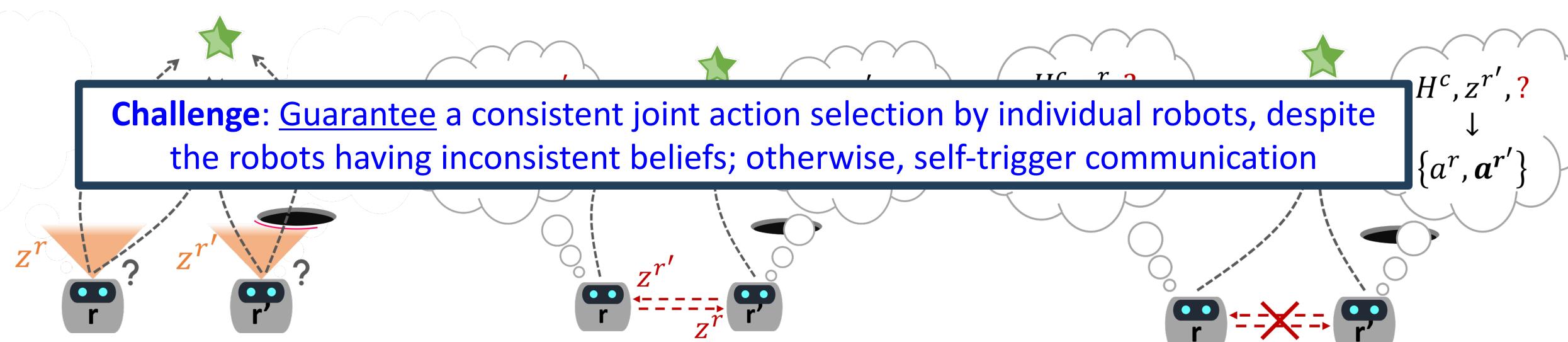
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Experience Reuse in POMDP Planning

POMDP Planning with Hybrid Beliefs

Simplification of POMDP with Formal Guarantees

Multi-agent POMDP Planning with Inconsistent Beliefs

Semantic Risk Awareness

Ambiguous Environments

Thank You

