# A Low Power VLSI Implementation of the Izhikevich Neuron Model

A. Samil Demirkol, Serdar Ozoguz

Istanbul Technical University, Department of Electronics and Communications Engineering 34469, Maslak, Istanbul, Turkey E-mail: demirkola@itu.edu.tr, ozoguz@itu.edu.tr

Abstract— We present a low-power VLSI implementation of the Izhikevich neuron model utilizing two first-order log-domain filters as the main building block. One of the filters includes an active diode connection in order to lower current levels to obtain a low-power, large time constant design. Thus, the neuron circuit operates in sub-threshold regime with biological time scale. The possible applications of the presented implementation are simulating large scale VLSI neural networks and building hybrid interface systems. The simulation results demonstrate the success of replicating the firing patterns of real neurons.

## INTRODUCTION

There has been a growing interest in the last decade to realize VLSI implementations of biological neurons relying on the mathematical models, which vary in complexity and accuracy from the simple Integrate and Fire (I&F) model to the complex Hodgkin-Huxley (HH) model [1-10]. A possible application area of these implementations is designing neuromorphic systems including thousands of neurons coupled with each other on a single silicon wafer [11-16]. The aim of such systems is to observe neurocomputational properties of real neural systems and it is hoped to design silicon brains in the future. The challenge in designing such systems is to obtain a low power compact VLSI neuron circuit which can exhibit rich dynamics of the biological neurons. For this purpose, the choice of the I&F model, which is easy to implement electronically, would be inappropriate because of its poor dynamics, while the choice of HH model would lead to very complicated electronic circuit, despite offering rich dynamical behavior.

New low power and compact neuron designs operating at biological timescale have been proposed recently in [17, 18]. However, in these works, either the spike shapes are poor as in [17] or restricted dynamical behavior is obtained as in [18]. Nevertheless, there exists quite a popular model introduced by Izhikevich [19] which is not only computationally efficient providing easier electronic design but also can produce rich dynamical behavior. An excellent review of this model can be found in [20]. There are two simultaneous log-domain VLSI implementations of Izhikevich model [21, 22]. However, the circuit in [21] consumes much power and occupies much chip area for a large scale network design. Similarly, in [22], the circuit consumes considerable power for a 90nm design and the spike shapes are not fair considering different phases of an

action potential such as depolarization and repolarization phases. In this work, we show that it is possible to realize power and area efficient log-domain Izhikevich VLSI neuron, while the circuit also mimics the dynamical behavior of the real neurons successfully. In section II, the mathematical model will be introduced and in section III, the circuit implementation will be presented. Simulation results will be given in section IV and the paper concludes with section V.

## THE IZHIKEVICH MODEL

The Izhikevich model is first introduced in [19] and a detailed phase plane analysis with different set of parameters can be found in [20]. The main form of Izhikevich model is as given below:

$$\dot{u} = a\{b(v - v_r) - u\} \tag{2}$$

$$if \ v \ge v_{neak}, v \leftarrow c, u \leftarrow u + d \tag{3}$$

where v is the membrane potential, u is the recovery current,  $v_r$ is the resting membrane potential,  $v_t$  is the instantaneous threshold potential,  $I_{in}$  is the external input current, k is a scaling coefficient,  $v_{peak}$  is the spike cutoff value, c is the reset value of variable v and d is the increment amount of variable uat reset time. A possible selection of parameters that leads to typical neuron behavior may be, k = 1.5,  $v_r = -60$ ,  $v_t = -40$ , a = 1, b = 4,  $v_{peak} = 35$ , c = -50 and d = 100. For these parameter values, regular spiking is observed with an approximate period of 1.8 s where v takes value between (-60,+35) and u changes between (60,160). It should be noted that the parameters k, a and b are dimensionless and the rest of parameters has the same dimension with two variables.

For a proper log-domain implementation of the model equations in (1-3), the state variables should be given in terms of currents with positive values. Hence, model equations are altered in order to shift the equilibrium point such that the instantaneous values of variables u and v become always positive. For this purpose, the variable v is shifted up by an amount of  $v_{offset}$  while the variable u is shifted up by  $b(v_{\text{offset}} + v_r)$ . Additionally, for low-power operation, the magnitudes of the variables are scaled such that the currents are in the pA range. After proper shifting and magnitude scaling, the new set of equation is obtained as follows:

$$\tau \dot{I}_v = k I_v (I_v - I_a) 10^{12} + (I_{DC} + I_{in} - I_u) \tag{4}$$

$$\tau \dot{I}_u = a(bI_v - I_u) \tag{5}$$

if 
$$I_v \ge I_{peak}, I_v \leftarrow I_c, I_u \leftarrow I_u + I_{incr}$$
 (6)

where  $I_{DC}$  stands for the current required for DC level shifting of variables  $I_v$  and  $I_u$ ,  $I_a$  is the shifted threshold value,  $I_{peak}$  is the spike cutoff value,  $I_c$  is the reset value of  $I_v$  and finally  $I_{incr}$  is the amount of increment of  $I_u$  at reset time. Note that all the terms, except the time constant  $\tau$  and dimensionless parameters k, a and b, are currents in the pA range.

## III. CIRCUIT IMPLEMENTATION

As the main building block of the neuron circuit realizing the model equations in (4-6), we consider the first-order log-domain filter in Fig. 1. In this circuit, all the transistors operate in subthreshold region with an i- $\nu$  relationship given by:

$$I_{DS} = I_s \frac{w}{L} \exp(\alpha V_{GS}) \tag{7}$$

where  $\alpha$  is a parameter with an approximate value of 33. Using translinear principle, one can easily show that the state equation of this circuit is,

$$C\dot{I}_{out} = -I_{out}(\alpha I_d) + I_{in}(\alpha I_b)(r_2 r_4/r_1 r_3)$$
 (8)

where  $r_1$ - $r_4$  are the aspect ratios of  $M_1$ - $M_4$  respectively. In order to obtain an expression similar to that in (8), we rearranged (4-5) and obtained the following system equations to be used to realize the final neuron circuit.

$$C_v \dot{I}_v = -I_v (I_a - I_v) 10^{12} k C_v / \tau + (I_{DC} + I_{in} - I_u) C_v / \tau \quad (9)$$

$$C_u \dot{I}_u = -I_u (aC_u/\tau) + I_v (abC_u/\tau) \tag{10}$$

These two state equations can readily be realized using a pair of the log-domain filter structure in Fig. 1. The circuit thus obtained with additional circuitry for reset dynamics is shown in Fig. 2. The values of the parameters are chosen as k = 1.5, a = 1, and b = 4. For a low area design, the values of the capacitors are set to  $C_u = C_v = 500 \,\mathrm{fF}$ , the time constant is chosen  $\tau \cong 25$ . Thus, the values of the DC currents are  $I_{d-u} = 250 \text{fA}$ ,  $I_{b-u} = 1 \text{pA}$ ,  $I_{d-v} = 7.5 \text{pA}$  and  $I_{b-v} = 250 \text{fA}$ ,  $I_{DC} = 90 \text{pA}$ . With these values, the peak value of variable  $I_v$ become  $I_{peak} = 90 \text{pA}$ . The transistors  $M_5$ - $M_8$  realize the differential equation in (10) related to  $I_u$ , while  $M_{11}$ - $M_{14}$  and  $M_{16}$  realize the state equation in (9) related to  $I_{\nu}$ . The transistors  $M_{10}$  and  $M_{15}$  serve as a switch to reset the current  $I_{\nu}$ to  $I_c$  and  $I_u$  to  $I_u+I_{incr}$ . The values of the currents  $I_c$  and  $I_{inc}$  are made adjustable through the voltages  $V_c$  via  $M_{15}$  and  $V_d$  via M<sub>9</sub>, respectively. Transistors M<sub>17</sub>-M<sub>19</sub> compose multiple output current mirror generating replicas of the current  $I_{\nu}$ , and the comparator along with the NOT gates produce the voltages  $V_{reset}$  and  $V_{reset}$ . The diode connection of  $M_{13}$  is supplied by a buffer which is indeed a simple differential pair with a 35pA bias current.

The crucial point of this design is the shifted source voltages and the active diode connection which enables transistors to handle low current levels at a few ten of hertz frequency, resulting in a circuit with very low power consumption.

To be clear, a usual way of comparison done for current-mode

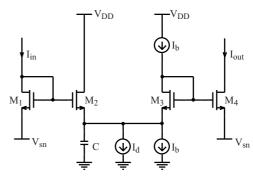


Figure 1. Log domain integrator.

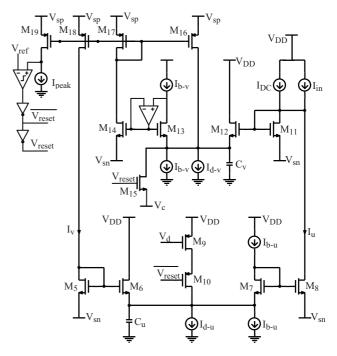


Figure 2. The proposed neuron circuit.

circuits [23, 24] is made between classical (CM), source shifted (SSCM) and active diode connected (ACM) current mirrors that are shown in Fig. 3. DC worst case analysis results of the current mirrors are shown in Fig. 4. The x axis is input current swept from 1fA to 100pA and y axis is the output current. It is obvious that source shifting definitely improves DC behavior and active diode connection also makes an improvement. Note from Fig. 2 that all the transistors have shifted sources and all the currents are above 1pA except  $I_{b-y} = 250$ fA. It is seen from Fig. 4 that standard

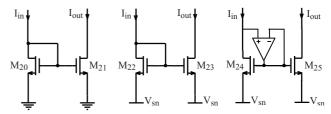


Figure 3. Current mirror toplogies (a) classical; (b) source shifted and (c) active diode connected.

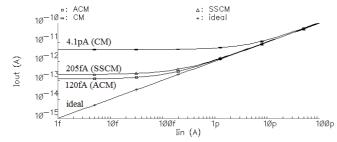


Figure 4. DC response of CM, SSCM and ACM.

CM topology is not an option in our design because of its poor DC performance at current levels below 1pA. Therefore, either SSCM or ACM should be used to obtain proper DC behavior. On the other hand, AC worst case analysis results are given in Fig. 5. Since CM topology is eliminated due to its very large DC gain error, we have only compared SSCM and ACM topologies. The AC bandwidth improvement of ACM with respect to SSCM, while the DC input current is 250fA, can be clearly seen from the simulation results given in Fig. 5. From Fig. 4 and 5, it can be concluded that source shifting is an appropriate solution for a minimum level of 1pA current for an acceptable AC and DC behavior, where only  $I_{h,v}$  is an exception of this condition in Fig. 2. Active diode connection is also enough for a minimum level of 250fA current for proper AC and DC behavior. Therefore, transistor M13 in Fig. 2 has such a connection in order to supply this very low  $I_{h-v}$ current. In fact, an alternative topology exist in [23, 24] utilizing a high-gain opamp. However, this topology is inconvenient for our design because of the high biasing currents of the opamp resulting in high power consumption.

## IV. SIMULATION RESULTS

The circuit in Fig. 2 is simulated using AMS 0.35 $\mu$ m process parameters using Spectre in Cadence design tool. Supply voltage is  $V_{DD}=1.65V$  and source shifting amount is 400mV. Reference voltage of the comparator is set to  $V_{ref}=V_{DD}/2$ . All the transistors have  $W/L=1\mu/1\mu$  except for  $M_{16}$ , the positive feedback transistor, with a ratio  $W/L=1\mu/2.5\mu$ . The tuning range of  $V_c$  and  $V_d$  are (480,505) mV and (350,500) mV respectively. It should be noted that, in (8),  $I_b$  and the aspect ratios of transistors composing the translinear loop appear as a product term for the log-domain filter block. Therefore, the deviations of transistors' aspect ratios can be tolerated by adjusting  $I_{b-\nu}$  and  $I_{b-\nu}$  currents in Fig. 2.

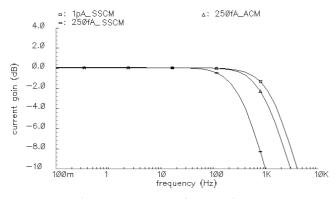


Figure 5. AC response of SSCM and ACM

The estimated chip area is  $1100\mu\text{m}^2$ . At resting state, i.e. zero input state,  $I_v = 3.3\text{pA}$ ,  $I_u = 14.3\text{pA}$  and the current and power consumption of the circuit is 147.2pA and 243pW, respectively. While the circuit is in regular spiking regime with a period of 100ms, the circuit consumes 1.65nW. This is

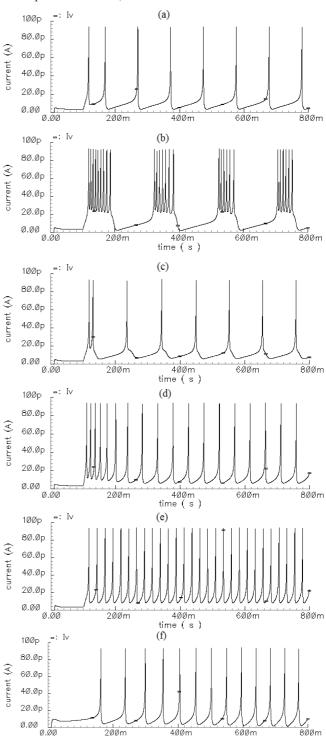


Figure 6. Firing patters. (a) Regular Spiking; (b) Bursting; (c) Intrinsically bursting; (d) Low Threshold Spiking (Spike Frequency Adaption); (e) Fast Spiking; (f) Class II Behavior

a very low value when compared to results in [21] and [22]. Additionally, Monte Carlo simulations are done and the circuit still exhibits successful spiking behavior.

Fig. 6 shows different type of firing patterns reproduced from the circuit. The input is a step current except in Fig. 6f where it is a ramp current. Only  $V_c$  and  $V_d$  are tuned in the circuit to observe Fig. 6a-d and  $I_{b-u}$  and  $I_{d-u}$  are additionally tuned for Fig. 6e. Since b>0 in this design, the neuron circuit behaves as a resonator rather than an integrator. Therefore, we expect to see a *Class II* behavior as depicted in Fig 6f. Here, the neuron starts to fire at a non-zero frequency while excited with a ramp input current.

At this point, we want to note a general mistake done in the literature while interpreting the dynamical properties of firing patterns in *Class II* resonator. In *Class II* behavior, observing long periodic behaviors by supplying very low input currents or resetting the first variable to a low value may mislead to conclude the neuron as an integrator, i.e. shows *Class I* behavior. However, in order to properly justify the *Class* of the behavior, the firing patterns should be studied and obtained following the way explained in [20] by exciting the neuron by a ramp input current and obtaining *f-I* characteristic of the neuron. The study of the dynamical behavior of the proposed neuron model according to this approach leads us to conclude that the proposed circuit is indeed a *Class II* neuron.

The similarity between the firing patterns observed in this work and the numerical results in [19, 20] shows the success of the design.

## V. CONCLUSION

We have implemented Izhikevich neuron model in logdomain and with the aid of additional active diode connection, we have obtained a low power compact VLSI circuit and observed typical firing patterns of a neuron successfully.

Low power and compact design makes the circuit suitable for building human interface electronics systems or large scale neuromorphic systems to simulate complex neural systems such as human brain.

## REFERENCES

- B. Linares-Barranco, E. Sanchez-Sinencio, A. Rodriguez-Vazquez, J. L. Huertas, "A CMOS Implementation of FitzHugh-Nagumo Neuron Model," IEEE Journal of SSC, vol. 26, pp. 956–965, July 1991.
- [2] G. N. Patel, S. P. DeWeerth, "Analogue VLSI Morris Lecar Neuron," Electronic Letters, vol. 33, no. 12, pp. 997-998, June 1997.
- [3] P. Arena, L. Fortuna, M. Frasca, "Extended SC-CNN Implementation of the Hindmarsh-Rose Neuron," IEEE Int. Workshop on CNN and Their App. Proc., pp. 339-344, 2000.
- [4] K. Nakada, T. Asai, H. Hayashi, "A Silicon Resonate-and-Fire Neuron Based on the Volterra System," IEICE NOLTA, pp. 82-85, 2005.
- [5] E. Lazaridis, E. M. Drakasis, M. Barahoma, "Full analogue electronic realisation of the Hodgkin-Huxley neuronal dynamics in weakinversion CMOS," IEEE EMBS, pp. 1200-1203, 2007.
- [6] J. H. B. Wijekoon, P. Dudek, "Integrated Circuit Implementation of a Cortical Neuron," IEEE ISCAS, pp. 1784-1787, 2008.
- [7] F. Folowosele et. al., "A Switched Capacitor Implementation of the Generalized Linear Integrate-And-Fire Neuron," IEEE ISCAS, pp. 2149-2152, 2009.
- [8] G Inidiveri, "A low power adaptive integrate-and-fire neuron circuit," IEEE ISCAS, pp. 820-823, 2003.

- [9] E. Basham, D. W. Parent, "An Analog Circuit Implementation of a Quadratic Integrate and Fire Neuron," IEEE EMBS, pp. 741-744, 2009.
- [10] S. Millner, A. Grübl, K. Meier, J. Schemmel, M. O. Schwartz, "A VLSI Implementation of the Adaptive Exponential Integrate-and-Fire Neuron Model," NIPS, 2010.
- [11] E. Chicca et. al., "A VLSI Recurrent Network of Integrate-and-Fire Neurons Connected by Plastic Synapses With Long Term Memory," IEEE Transactions on Neural Networks, vol. 14, no. 5, pp. 1297-1307, September 2003.
- [12] J. Tomas, Y. Bornat, S. Saighi, T. Levi, S. Renaud, "Design of modular and mixed neuromimetics ASIC," IEEE ICECS, pp. 946-949, 2006.
- [13] G. Indiveri, E. Chicca, R. Douglas, "A VLSI Array of Low-Power Spiking Neurons and Bistable Synapses With Spike-Timing Dependent plasticity," IEEE Transactions on Neural Networks, vol. 17, no. 1, pp. 211-221, January 2006.
- [14] R. J. Vogelstein, U. Mallik, J. T. Vogelstein, G. Cauwenberghs, "Dynamically Reconfigurable Silicon Array of Spiking Neurons With Conductance-Based Synapses," IEEE Transactions on Neural Networks, vol. 18, no. 1, pp. 253-265, January 2007.
- [15] J. V. Arthur, K. A. Boahen, "Synchrony in Silicon: The Gamma Rhythm," IEEE Transactions on Neural Networks, vol. 18, no. 6, pp. 1815-1825, November 2007.
- [16] J. Schemmel, J. Fieres, K. Meier, "Wafer-Scale Integration of Analog Neural Networks," IEEE IJCNN, pp. 431-438, 2008.
- [17] J.H.B.Wijekoon and P.Dudek, "A CMOS circuit implementation of a spiking neuron with bursting and adaptation on a biological timescale," IEEE BIOCAS, pp.193-196, 2009.
- [18] P. Livi, G. Indiveri, "A current-mode conductance-based silicon neuron for Address-Event neuromorphic systems," IEEE ISCAS, pp. 2898-2901, 2009.
- [19] E. M. Izhikevich, "Simple Model of Spiking Neurons," IEEE Transactions on Neural Networks, vol. 14, no. 6, pp. 1569-1572, November 2003.
- [20] E. M. Izhikevich, Dynamical Systems in Neuroscience: The Geometry of Excitability and Bursting, The MIT press, 2007.
- [21] A. van Schaik, C. Jin, A. McEwan, T. J. Hamilton, "A Log-domain implementation of the Izhikevich neuron model," IEEE ISCAS, pp. 4253-4256, 2010.
- [22] V. Rangan, A. Ghosh, V. Aparin, G. Cauwenberghs, "A Subthreshold a VLSI Implementation of the Izhikevich Simple Neuron Model," IEEE EMBC, 2010.
- [23] B. Linares-Barranco, T. Serrano-Gotarredona, R. Serrano-Serrano-Gotarredona, C. Serrano-Gotarredona, "Current Mode Techniques for Sub-pico-Ampere Circuit Design," Analog Integrated Circuits and Signal Processing, vol. 38, pp. 103-119, 2004.
- [24] L. Zhang, Z. Yu, X. He, "Circuit Design and Verification of On-Chip Femto-Ampere Current Mode Circuit Using 0.18um CMOS Technology," IEEE ICSICT, pp. 1624-1626, 2006.