

General Regulations.

- Please hand in your solutions in groups of up to two people.
- Your solutions to theoretical exercises can be either handwritten notes (scanned), or typeset using \LaTeX . In case you hand in handwritten notes, please make sure that they are legible and not too blurred or low resolution.
- For the practical exercises, always provide the (commented) code as well as the output, and don't forget to explain/interpret the latter. Please hand in both the notebook (`.ipynb`), as well as an exported PDF.
- Submit all your files in the Übungsgruppenverwaltung, only once for your group.

1 Restricted Hartree-Fock

In the restricted, closed shell setting, two spin orbitals ϕ with spin up and down are paired and share the same spatial orbital φ (this only works for systems with even numbers of electrons), for instance

$$\phi_1(x) = \varphi_1(r)\alpha(w) \quad \text{and} \quad \phi_2(x) = \varphi_1(r)\beta(w).$$

Write down the energy in the restricted Hartree-Fock approximation. The sums should only go up to $N/2$, where N is the number of electrons. Remember that some integrals vanish due to spin. (8 pts)

2 Diagonalization of the overlap matrix

In the LCAO ansatz (linear combination of atomic orbitals), the molecular orbitals are given by

$$\phi_i = \sum_{\alpha} C_{\alpha i} \chi_{\alpha}.$$

The overlap matrix S of the atomic orbitals χ is defined as

$$S_{\alpha\beta} = \langle \chi_{\alpha} | \chi_{\beta} \rangle.$$

Show that C diagonalizes S , i.e., prove that $C^{\dagger} S C = \mathbb{I}$. (6 pts)

3 Understanding PySCF logging

Perform a restricted Hartree-Fock calculation PySCF with verbosity set to 9. Use the molecule HF (hydrogen fluoride) with the 6-31G* basis. Comment on every line of the output and explain what it means. You can group repeating blocks and only comment once. (6 pts)