

Introduction to C++: MyVector and ODE_Solver

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Overview

1. Background: libraries and toolkits
2. Why object orientation / C++
3. Introduction to the C++ language: MyVector
4. More advanced topics: ODE_Solver

Tools for Building Simulators

- Standard programming tools:
 - programming languages (FORTRAN 77/90, C/C++, Java,...)
 - editors, debuggers and software analysis
 - version control systems
- Computer algebra programs
 - Maple, Mathematica, MathCad, Reduce, Axiom, ..
- Numerics:
 - Matlab, Mathematica, Maple, Scilab, Octave,
- Numerical libraries and toolkits:
 - a vast number available
- Visualisation
- Benchmark tests

Libraries and Repositories

- GAMS - guide to available mathematics software
 - <http://gams.nist.gov/>
 - catalogue and database of packages and libraries with tens of thousands of routines
 - the majority is numerical routines written in FORTRAN
- NETLIB - repository of free numerical software
 - <http://www.netlib.org/>
 - more than 160 libraries (BLAS, LAPACK, MPI, Atlas, ..)
- Numerical Recipes
 - <http://www.nr.com/>
 - book series (FORTRAN 77/90, C/C++,...)
 - algorithms and their (efficient) implementation
 - about 350 routines

Fundamental libraries: BLAS

BLAS - Basic Linear Algebra Subprograms:

- collection of portable, robust and efficient modules for elementary vector and matrix operations
- basis for many other routines, e.g., LAPACK (next slide)
- implemented in FORTRAN, but also used from C/C++/Java
- plug-and-play for numerical subroutines
- three levels:
 - Level 1: vector and vector-vector operations
 - Level 2: matrix-vector operations
 - Level 3: matrix-matrix operations
- see also ATLAS - Automatically Tuned Linear Algebra Software

Fundamental libraries: LAPACK

LAPACK - Linear Algebra PACKage

- popular collection of FORTRAN 77 subroutines for numerical linear algebra
 - linear systems, matrix decomposition, singular-value decomposition, ..
- dense and banded matrices (but not general sparse ones)
- fine-tuned for both single processors and supercomputers (memory access, block operations, etc)
- relies heavily on BLAS routines
- other variants
 - LAPACK90, JLAPACK, CLAPACK, LAPACK++
 - ScaLAPACK

Examples of toolkits

Diffpack:

- developed at SINTEF / Ifi, UiO
- object-oriented problem solving environment for PDEs

deal.II: A Finite Element Differential Equations Analysis Library

- developed at University of Heidelberg
- primarily targeted at adaptive finite elements and error estimation
- data structures and algorithms in C++

Clawpack - conservation law package

- developed by R.J. LeVeque, Univ. Washington
- finite volume routines for solving conservation laws
- written in FORTRAN

The choice of language

Traditional simulator software uses procedural programming

- subroutines
- data structures = variables, arrays
- data transferred between subroutines

typically coded in FORTRAN (or C).

New paradigm in late 1990s, object oriented languages (C++, Java, ..)

- data and operations on data grouped together in logical objects
- inheritance, hierarchies, polymorphism

The choice of language cont'd

Why stick to tradition?

- A lot of legacy codes!
- Very high efficiency
- A lot of procedural numerical libraries (Nag, Lapack, Eispack,..) available

Why not?

- large codes with too many visible details
- little correspondence between mathematical abstraction and computer code
- redesign and reimplementations tend to be expensive

My advice: use libraries whenever possible to avoid reinventing the wheel

Object-oriented numerics

Why is it suited for simulator codes (involving heavy number crunching)?

- High level of abstraction/modularity possible
 - hide irrelevant data/information
 - hide implementation details
 - stronger correspondence between math and code
- Extensive type-checking
- Localization
- Increased flexibility, code reuse, ...

Object-oriented numerics cont'd

However, one should be a bit careful to avoid

- low code efficiency
- the wrapper class explosion
- obfuscation of simple codes
- good designs with nothing inside

OO is a strong tool that should be utilized with great care!

It is the same as with fertilizer; without it, your crop grows slowly, but too much of it destroys your soil. It should be administered with great care

Introduction to OON in C++

As an example consider the implementation of a mathematical vector.

Surely, this must be available somewhere?

Oh yes! Vector classes are typically provided in (OO) numerical libraries and there will seldom be a need for writing new vector classes yourself. But this example can be used to give a hands-on feeling with many concepts:

- see how (numerical) C++ classes are programmed
- exemplify many different aspects of the C++ language
- exemplify efficiency considerations

Advice: get a good book on C++!

A mathematical vector

- What is a vector?

A well defined mathematical quantity consisting of a set of elements (v_1, \dots, v_n) and a set of legal operations.

- Do standard arrays in any computer language give good enough support for matrices?

No, for several reasons:

- explicit transfer of length
- explicit transfer of storage format
- no software definition of legal operations
- user implemented consistency checks

My first vector class

A class **MyVector** should do the following:

- Create vectors of length n : `MyVector v(n);`
- Create a vector with zero length: `MyVector v;`
- Redimension a vector to length n : `v.redim(n);`
- Create a vector as a copy of another vector w : `MyVector v(w);`
- Extract an entry: `double e = v(i);`
- Assign a number to an entry: `v(j) = e;`
- Extract the length of the vector: `int n = v.size();`
- Set two vectors equal to each other: `w = v;`
- Take the inner product of two vectors:
`double a = w.inner(v);`
or alternatively `a = inner(w, v);`
- Write a vector to the screen: `v.print(cout);`

We define the proposed syntax through functions in class **MyVector**

The MyVector class: <MyVector.h>

```
class MyVector
{
private:
    double* A;           // vector entries (C-array)
    int     length;      // length of vector
    void     allocate (int n); // allocate memory, length=n
    void     deallocate (); // free memory
public:
    MyVector ();          // MyVector v;
    MyVector (int n);      // MyVector v(n);
    MyVector (const MyVector& w); // MyVector v(w);
    ~MyVector ();         // clean up dynamic memory
}
```

Declaration of the class MyVector: internal stuff and constructors

- private: not accessible from outside MyVector
- public: accessible from outside MyVector

The MyVector class cont'd

```
int redim (int n);           // v.redim(m);  
int size () const { return length ; } // n = v.size ();  
  
void operator= (const MyVector& w); // v = w;  
double operator() (int i ) const; // a = v(i);  
double& operator() (int i );      // v(i) = a;  
  
void print (ostream& o) const;      // v.print(cout);  
double inner (const MyVector& w) const; // a = v.inner(w);  
};
```

Declaration of methods in MyVector

- member functions (print, inner, redim, size)
- operator overloading (= and ())

Constructors

Constructors tell how we declare a variable of type `MyVector` and how this variable is initialized:

```
MyVector v;    // declare a vector of length 0
```

means calling the function

```
MyVector::MyVector ()  
{ A = NULL; length = 0; }
```

Result: empty vector

Constructors II

`MyVector v(n);` *// declare a vector of length n*

means calling the function

```
MyVector::MyVector (int n)
{ allocate(n); }

void MyVector::allocate (int n)
{
    length = n;
    // create n doubles in memory
    A = new double[n];
}
```

Destructor

A `MyVector` object is created (dynamically) at run time, but must also be destroyed when it is no longer in use. The destructor specifies how to destroy the object:

```
MyVector::~~MyVector ()  
{ deallocate (); }  
  
// free dynamic memory:  
void MyVector::deallocate ()  
{  
    delete [] A;  
}
```

The assignment operator

To be able to use assignments of the form

`v = w;` *// v and w are MyVector objects*

we overload the `=` operator:

```
void MyVector::operator= (const MyVector& w) // v = w;
{
    redim (w.size ()); // make v as long as w
    int i;
    for (i = 0; i < length; i++) // C arrays start at 0
        A[i] = w.A[i];
}
```

Redimensioning the length

```
v.redim(n); // make v a vector from 1 to n
```

```
int MyVector::redim (int n)
{
    if (length == n)
        return 0; // no need to allocate anything

    if (A != NULL) {
        // "this" object has already allocated memory
        deallocate();
    }
    allocate(n);
    return 1; // the length was changed
}
```

The copy constructor

We wish to create one vector as a copy of another

```
MyVector v(w); // take a copy of w
```

This can be done as follows

```
MyVector::MyVector (const MyVector& w)
{
    allocate (w.size ()); // length equal w's length
    *this = w;             // call operator=
}
```

Here:

- `this` is a pointer to the current (“this”) object,
- `*this` is the object itself

The const concept

```
const int m=5; // not allowed to alter m
```

```
MyVector::MyVector (const MyVector& w)  
// w cannot be altered inside this function  
// & means passing w by _reference_
```

```
MyVector::MyVector (MyVector& w)  
// w can be altered inside this function, the change  
// is visible from the calling code
```

```
int MyVector::redim (int n)  
// a local _copy_ of n is taken,  
// changing n inside redim  
// is invisible from the calling code
```

```
void MyVector::print (ostream& o) const  
// member function does not alter members of class
```

Subscripting in vector

We use “()” instead of “[]” for generality¹.

```
// a and v are MyVector objects; want to set  
a(j) = v(i+1);  
  
// the meaning of a(j) is defined by  
inline double& MyVector::operator() (int i)  
{  
    return A[i-1];  
    // base index is 1 (not 0 as in C/C++)  
}
```

inline functions: function body is copied to calling code, no overhead of function call!

¹ In 2D: `a[i, j]` is a valid expression, but it calls `operator[]()` and evaluates the expression `i, j`.

Inlining

```
for (int i = 1; i <= n; i++)  
    c(i) = a(i)*b(i);  
  
// compiler inlining translates this to:  
for (int i = 1; i <= n; i++)  
    c.A[i-1] = a.A[i-1]*b.A[i-1];  
  
// compiler should optimize this to  
double* ap = &a.A[0];  
double* bp = &b.A[0];  
double* cp = &c.A[0];  
for (int i = 0; i < n; i++)  
    cp[i] = ap[i]*bp[i];           // pure C!
```

Inlining and complete control with the definition of $v(i)$ allow

- safe indexing
- efficiency as in C or Fortran

Add safety checks

```
inline double& MyVector::operator() (int i)
{
    #ifdef SAFETY_CHECKS
    if ( i < 1 || i > length)
        cout << "MyVector::operator(), illegal index, i=" << i ;
    #endif
    return A[i-1];
}
```

Compile with the `-DSAFETY_CHECKS` flag

Printing the vector

```
// MyVector v
cout << v;

inline ostream& operator<< (ostream& o, const MyVector& v)
{ v.print(o); return o; }

void MyVector::print (ostream& o) const
{
    int i;
    for (i = 1; i <= length; i++)
        o << "(" << i << ")=" << (*this)(i) << '\n';
}
```

Inner product¹

```
double a = v.inner(w);
```

```
double MyVector::inner (const MyVector& w) const
{
    int i ; double sum = 0;
    for ( i = 0; i < length; i++)
        sum += A[i]*w.A[i];
    // alternative : sum += (*this)(i)*w(i);
    return sum;
}
```

```
double inner (const MyVector& v, const MyVector w)
{
    return v.inner(w);
}
```

¹ Without safety checks, of course... Add them yourself.

Norm

```
double a = v.norm();
```

```
double MyVector::norm () const
```

```
{
```

```
    int i ; double sum = 0;
```

```
    for ( i = 0; i < length; i++)
```

```
        sum += A[i]*A[i];
```

```
    return sqrt(sum);
```

```
}
```

```
double MyVector::norm() const { return sqrt(inner(this));}
```

Operator overloading

We can redefine the multiplication operator to mean the inner product of two vectors:

```
double a = v*w; // example on attractive syntax
```

```
class MyVector
```

```
{
```

```
    ...
```

```
    double operator* (const MyVector& w) const;
```

```
    ...
```

```
};
```

```
double MyVector::operator* (const MyVector& w) const
```

```
{
```

```
    return inner(w);
```

```
}
```

What about $+$, $-$, ... ?

Why have we not defined the following operations?

$z = v + w;$ $z = va;$
 $z = v - w;$ $z = av;$

```
MyVector MyVector::operator+(const MyVector& w)
{
    int n=this->size();
    if (n != w.size ()) .....

    MyVector x(n);
    for ( int i=1; i<=n; i++)
        x(i) = (* this)(i) + w(i);
    return x;
}
```

How would you implement $z = av$?

What about $+$, $-$, ... ?

What happens here in the `operator+(...)` call?

- allocate `x`
- `x = v + w`
- allocate `tmp`
- `tmp = x`
- `z = tmp`

Hmmm... this is hardly very efficient for large vectors!

What would you do?

Lessons learned

- Low-level C++/C programming involves a lot of intricate details (e.g. pointers, memory handling)
- Rely on ready-made tools (e.g. for arrays)
- Use libraries!
- Object-orientation hides low-level details that dominate in C and F77 programs

Evaluation of MyVector design

Some critical questions at the end:

- Have we made a flexible design?
- Can we reuse the code in other settings?
- What about vectors of integers, complex numbers,?
- What about arrays that are not vectors?

An answer to these questions may be the use of

- Parametrized types
- Layered design, inheritance

Parametrized types

We wish to have a family of vectors

```
MyVector(int)    n(245);
```

```
MyVector(float)  v(19);
```

```
MyVector(double) w(11);
```

```
MyVector(Complex) z(3);
```

In C++ this is achieved by **class templates**, i.e., a template for producing classes:

The MyVector<T> class template

```
template <class T>
class MyVector
{
private:
    T*      A;                // vector entries (C-array)
    :
public:
    :
    MyVector (const MyVector<T>& w);    // MyVector<T> v(w);
    MyVector ();                        // clean up dynamic memory
    :
    void operator= (const MyVector<T>& w); // v = w;
    T operator() (int i) const;         // a = v(i);
    T& operator() (int i);              // v(i) = a;
    :
    T inner (const MyVector<T>& w) const; // a = v.inner(w);
    T norm () const;                    // a = v.norm();
};
```

Layered design

Recall definition of a vector:

A well defined mathematical quantity consisting of a set of elements (v_1, \dots, v_n) *and a set of legal operations.*

On the other hand, an array is defined as:

A collection of elements, each an object of some fixed type, and an associated dimension.

In other words,

a vector is a special array (in one dimension) with extra functionality.

This should be reflected in our design...

New array class template `MyArray<T>`

```
template <class T> class MyArray
{
protected:
    T*      A;           // vector entries (C-array)
    :
public:
    MyArray ();           // MyArray<T> v;
    MyArray (int n);      // MyArray<T> v(n);
    MyArray (const MyArray<T>& w); // MyArray<T> v(w);
    ~MyArray ();         // clean up dynamic memory
    int redim (int n);    // v.redim(m);
    int size () const { return length ; } // n = v.size ();
    void operator= (const MyArray<T>& w); // v = w;
    T operator() (int i) const;         // a = v(i);
    T& operator() (int i );             // v(i) = a;
    void print (ostream& o) const;      // v.print(cout);
};
```

MyVector<T> derived from MyArray<T>

```
template <class T> class MyVector : public MyArray<T>
{
public:
    MyVector ();                // MyVector<T> v;
    MyVector (int n);           // MyVector<T> v(n);
    MyVector (const MyVector<T>& w); // MyVector<T> v(w);
    ~MyVector ();               // clean up dynamic memory

    void operator= (const MyVector<T>& w); // v = w;
    T inner (const MyVector<T>& w) const; // a = v.inner(w);
    T norm () const ;            // a = v.norm();
};
```

Here `MyVector` inherits the data members and all the member functions from `MyArray` and provides extra functionality.

Constructors, destructors, and assignment

These are not inherited and receive special treatment. C++ automatically defines these functions unless we declare them. Constructors:

- First invoke constructor for each subobject
- Then construct members

In our case, invoke constructor for `MyArray` and do nothing else:

```
template<class T>  
MyVector<T>::MyVector(int n) : MyArray<T>(n) {}
```


Questions from the audience

Q: Referring to operator overloading of `+`; wouldn't the following construction solve the problem?

```
&MyVector MyVector::operator+(const MyVector& w)
```

A: No! What would the `&` refer to? It is not possible to return reference to a local variable. Neither is the address of the temporary memory allocated by `return` available.

Q: Can I restrict the types of T in a template class?

A: It is possible to do using various tricks such as static assertions.

Questions from the audience cont'd

Q: Is it possible to define my own operators to “overload”?

A: The only operators that may be overloaded are the following

+	-	*	/	%	
^	&		~	!	&&
	++	-	<<	>>	,
<	<=	==	!=	>	>=
=	+=	-=	*=	/0	%=
&=	=	^=	<<=	>>=	
[]	()	->	new	delete	

Book recommendations

- Timothy Budd: C++ for Java Programmers. Addison-Wesley. 1999.
- Andrei Alexandrescu. Modern C++ Design: Generic Programming and Design Patterns Applied. (C++ In-Depth Series). Addison-Wesley.
- Essential C++. Stanley B. Lippman. Addison Wesley.

ODE Solver Environment

The purpose of this example:

- OO-design for a simple problem
- Continue the overview of C++ features
- Principles apply to advanced simulations

Mathematical problem:

$$\frac{dy_i}{dt} = f_i(y_1, \dots, y_n, t), \quad y_i(0) = y_i^0, \quad i = 1, \dots, n$$

- A system of ordinary differential equations (ODEs).
- A plenitude of numerical methods exist.
- Occurs frequently in numerics

Traditional procedural solution

Typical interface in FORTRAN77:

```
SUBROUTINE RK4 (Y, T, F, WORK1, N, TSTEP, TOL1, TOL2, . . .
```

Here:

- Y is current y
- T is the value of t
- F is a function defining the f_i 's
- $WORK1$ is a work array (since runtime allocation is not allowed in F77)
- $TSTEP$ is the current time step
- $TOL1, TOL2, \dots$ are various parameters

FORTRAN 77 cont'd

For a specific ODE:

$$\ddot{y} + c_1(\dot{y} + c_2\dot{y}|\dot{y}|) + c_3(y + c_4y^3) = \sin \omega t$$

Written as a system ($\dot{y}_1 = y_2, \dot{y}_2 = \ddot{y}$)

$$f_1 = y_2,$$

$$f_2 = -c_1(y_2 + c_2y_2|y_2|) - c_3(y_1 + c_4y_1^3) + \sin \omega t$$

Possible FORTRAN function

```
SUBROUTINE F (YDOT, Y, T, C1, C2, C3, C4, OMEGA)
```

Unfortunately this is problem dependent and cannot be used. Instead,

```
SUBROUTINE F (YDOT, Y, T)
```

with C1, C2, C3, C4, OMEGA transferred in COMMON blocks

⇒ dangerous side effects and possible hidden bugs

Object-oriented design

introduce two class hierarchies:

- `ODE_Solver` (e.g., forward Euler, Runge–Kutta , ..)
Base class with:
 - initialisation of solver
 - **virtual function** `advance` for one time step
- `ODE_Problem` (e.g., Newton's 2.law, HIV-1 virus, ..)
Base class with:
 - the generic system - **virtual function** `equation`
 - a driver function `timeLoop`
 - common data: Δt , T , name of solver, ..

`ODE_Solver` must access `ODE_Problem` and vice versa

Implementation in C++

```
class ODE_Problem;    // tell C++ that this class name exists

class ODE_Solver
{
protected:          // members only visible in subclasses
    ODE_Problem* eqdef;    // definition of the ODE in user's class

public:              // members visible also outside the class
    ODE_Solver (ODE_Problem* eqdef_)
        { eqdef = eqdef_; }
    virtual ~ODE_Solver () {} // always needed, does nothing here...
    virtual void init () {}   // initialize solver data structures
    virtual void advance (MyArray<double>& y,
                          double& t, double& dt);
};
```

Notice: `protected` means *public* access for derived classes and *private* access for others.

The ODE_Problem class

```
class ODE_Solver;    // tell C++ that this class name exists

class ODE_Problem
{
protected:
    ODE_Solver*      solver;    // some ODE solver
    MyArray<double> y, y0;      // solution (y) and initial cond. (y0)
    double           t, dt, T;  // time loop parameters
public:
    ODE_Problem () {}
    virtual ~ODE_Problem ();
    virtual void timeLoop ();
    virtual void equation (MyArray<double>& f,
                        const MyArray<double>& y, double t);
    virtual int  size  ();  // no of equations in the ODE system
    virtual void scan  ();
    virtual void print (ostream& os);
};
```

Virtual functions

C++ virtual functions are member functions, whose functionality may be overridden in derived classes

- Nonvirtual C++ member functions are resolved at compile time; this mechanism is called *static binding*.
- Virtual member functions are resolved during run-time; this mechanism is known as *dynamic binding*.

Here:

- `equation` and `size` only in subclasses
- `scan` and `print` extended in subclasses
- `timeLoop` can be written in base class

The `timeLoop` function

```
void ODE_Problem::timeLoop ()
{
    ofstream outfile ("y.out");
    t = 0;  y = y0;
    outfile << t << "┐"; y.print ( outfile );  outfile << endl;
    while (t <= T) {
        solver->advance (y, t, dt);
        outfile << t << "┐"; y.print ( outfile );  outfile << endl;
    }
}
```

This function is *generic* and can be coded in the base class.

One specific problem — oscillator

$$\dot{y}_1 = y_2, \quad \dot{y}_2 = -c_1(y_2 + c_2 y_2 |y_2|) - c_3(y_1 + c_4 y_1^3) + \sin \omega t$$

```
class Oscillator : public ODE_Problem
{
protected:
    double c1, c2, c3, c4, omega;    // problem dependent paramters
public:
    Oscillator () {}
    virtual void equation (MyArray<double>& f, const MyArray<double>& y, double t);
    virtual int size () { return 2; }
    virtual void scan ();
    virtual void print (ostream& os);
};
```

We inherit y , y_0 , t , dt , T and functions from `ODE_Problem`.
`timeLoop` can be reused and does not appear explicitly

Oscillator cont'd

```
void Oscillator :: equation(MyArray<double>& f,  
                           const MyArray<double>& y, double t)  
{  
    f(1) = y(2);  
    f(2) = -c1*(y(2)+c2*y(2)*fabs(y(2))) - c3*y(1)*(1.0+c4*y(1)*y(1))  
           + sin(omega*t);  
}
```

A specific solver – ForwardEuler

$$y_i^{\ell+1} = y_i^{\ell} + \Delta t f(y_1^{\ell}, \dots, y_n^{\ell}, t_m)$$

```
class ForwardEuler : public ODE_Solver
{
    MyArray<double> scratch1; // needed in the algorithm
public:
    ForwardEuler (ODE_Problem* eqdef_);
    virtual void init (); // for allocating scratch1
    virtual void advance (MyArray<double>& y, double& t, double& dt);
};

void ForwardEuler::advance(MyArray<double>& y, double& t, double& dt)
{
    eqdef->equation (scratch1, y, t); // evaluate scratch1 (as f)
    const int n = y.size ();
    for (int i = 1; i <= n; i++)
        y(i) += dt * scratch1(i);
    t += dt;
}
```

Another solver — RungeKutta4

$$y_i^{\ell+1/4} = y_i^\ell + \frac{\Delta t}{2} f(y^\ell, t_m)$$

$$y_i^{\ell+2/4} = y_i^{\ell+1/4} + \frac{\Delta t}{2} f(y^{\ell+1/4}, t_m + \Delta t/2)$$

$$y_i^{\ell+3/4} = y_i^\ell + \Delta t f(y^{\ell+2/4}, t_m + \frac{\Delta t}{2})$$

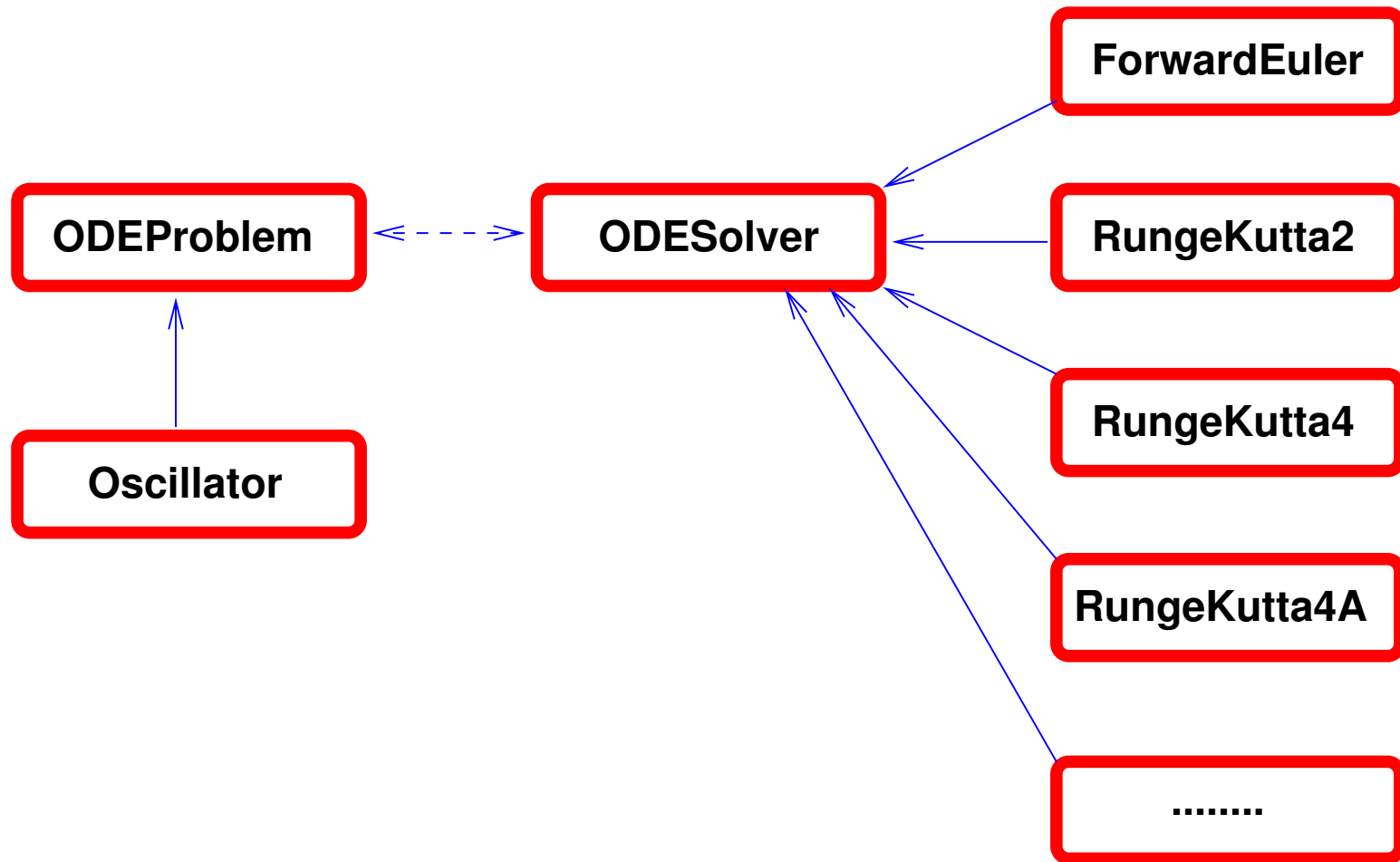
$$y_i^{\ell+1} = y_i^\ell + \frac{\Delta t}{6} \left[f(y^\ell, t_m) + 2f(y^{\ell+1/4}, t_m + \frac{\Delta t}{2}) \right. \\ \left. + 2f(y^{\ell+2/4}, t_m + \frac{\Delta t}{2}) + f(y^{\ell+3/4}, t_m + \Delta t) \right]$$

```
class RungeKutta4 : public ODE_Solver
{
    MyArray<double> y1, y2, y3; // needed in algorithm
public:
    RungeKutta4 (ODE_Problem* eqdef_);
    virtual void init ();
    virtual void advance (MyArray<double>& y, double& t, double& dt);
};
```

RungeKutta4 cont'd

```
void RungeKutta4::advance(MyArray<double>& y,double& t, double& dt) {  
    const double dt2 = 0.5*dt;  
    const double dt6 = dt/6.0;  
    const int n = y.size (); int i;  
    eqdef->equation (y1, y, t);  
    for ( i = 1; i <= n; i++)  
        y2(i) = y(i) + dt2 * y1(i);  
    eqdef->equation (y1, y2, t+dt2);  
    for ( i = 1; i <= n; i++)  
        y2(i) = y(i) + dt2 * y1(i);  
    eqdef->equation (y3, y2, t+dt2);  
    for ( i = 1; i <= n; i++) {  
        y2(i) = y(i) + dt * y3(i);  
        y3(i) = y1(i) + y3(i); }  
    eqdef->equation (y1, y2, t+dt);  
    eqdef->equation (y2, y, t);  
    for ( i = 1; i <= n; i++)  
        y(i) = y(i) + dt6*(y1(i) + y2(i) + 2*y3(i));  
    t += dt;  
}
```


The class hierarchy



How to connect and initialize?

```
class ODE_Solver_prm {
public:
    char          method[30]; // name of subclass in ODESolver hierarchy
    ODE_Problem* problem;    // pointer to user's problem class
    ODE_Solver* create ();   // create correct subclass of ODESolver
};

ODE_Solver* ODE_Solver_prm::create () {
    ODE_Solver* ptr = NULL;
    if      (strcmp(method, "ForwardEuler") == 0)
        ptr = new ForwardEuler (problem);
    else if (strcmp(method, "RungeKutta4") == 0)
        ptr = new RungeKutta4 (problem);
    else {
        cout << "\n\nODESolver_prm::create:\n\t"
              << "Method_" << method << "_is_not_available\n\n";
        exit (1); }
    return ptr;
}
```

Initialisation of ODE_Problem

```
void ODE_Problem::scan ()
{
    const int n = size ();    // call size in actual subclass
    y.redim(n); y0.redim(n);
    cout << "Give_" << n << "_" initial _conditions:_" ;
    // y0.scan(cin);
    int i ;
    for(i =1; ( i<=n) && (cin>>y0(i)); i++);
    cout << "Read_" << i-1 << "elements";
    y0.print (cout); cout<<endl;
    cout << "Give_time_step:_" ;    cin >> dt;
    cout << "Give_final_time_T:_" ; cin >> T;
    ODE_Solver_prm solver_prm;
    cout << "Give_name_of_ODE_solver:_" ;
    cin >> solver_prm.method;
    solver_prm.problem = this;
    solver = solver_prm.create();
    solver->init ();
    // more reading in user's subclass
}
```

Initialization of a specific problem

```
void Oscillator :: scan ()
{
    // first we need to do everything that ODE_Problem::scan does:
    ODE_Problem::scan();
    // additional reading here:
    cout << "Give _c1, _c2, _c3, _c4, _and _omega: _";
    cin >> c1 >> c2 >> c3 >> c4 >> omega;
    print(cout); // convenient check for the user
}
```

... and finally the main program

```
#include "Oscillator.h"

int main (int argc, const char* argv[])
{
    Oscillator problem;
    problem.scan();      // read input data and initialize
    problem.timeLoop(); // solve problem
}
```

Conclusion:

- a flexible ODE library
- introduction to general code design principles
- faster start for the next ODE we wish to solve....