CS 334: Homework #3

Submission Instructions: The homework is due on Oct 11th at 11:59 PM ET. Make sure your program uses Python 3.7. Your submission should consist of two steps (detailed in Homeworks #1, #2). If either of the two steps are late, then your assignment is late.

Dataset Description: For this homework, you will be predicting the energy usage of appliances in a low energy house. The dataset (energydata.zip) contains measurements of temperature and humidity sensors from a wireless network, weather from a nearby airport station, and the recorded energy use of lighting fixtures to predict the energy consumption of appliances in a low energy house. There are 27 attributes for each 10 minute interval¹. Details of the column attributes are described in detail on the University of California, Irvine Machine Learning repository (https://archive.ics.uci.edu/ml/datasets/Appliances+energy+prediction).

The dataset has been split into three subsets: training data from measurements up to 5/7/16 4:30, and test data from measurements after 5/7/16 4:30.

- 1. Feature Extraction + Feature Selection (8+5+7+5=25 points): For this problem, you will consider performing some feature selection and extraction of the data. The template code for this problem is found in selFeat.py.
 - (a) The first column of the energy data has a date and timestamp (e.g., 3/20/16 5:30). What are features that you can extract from this data that might be useful for predicting energy usage? Choosing to only drop the column is not an acceptable answer. Implement your feature extraction in extract_features to add the new features to the pandas dataframe and to remove the date column.
 - (b) Calculate the Pearson correlation between the features themselves and the features with the target as a correlation matrix $((d+1) \times (d+1) \text{ matrix})$. Note that a value close to 0 implies almost no correlation while a value close to 1 and -1 implies strong positive and negative correlation, respectively. Plot the correlation matrix using a heatmap (Hint: use seaborn.heatmap).
 - (c) Using (b), identify the features that you think should be used to train a linear regression model and your reasoning for using them. You must justify your feature selection to get full points. Implement your feature selection in select_features.
 - (d) What other preprocessing steps do you need to do to the data? Implement your preprocessing steps in the preprocess_data function in the selFeat.py. Now use selFeat.py to preprocess both the training and test data and save it to new files. The main program will (1) extract the features from the date and timestamp (a); (2) select the features (c); and (3) preprocess the remaining columns (d). You can do this from the command line by doing the following:

\$python selFeat.py new_xTrain.csv new_xTest.csv

You'll be using these two new files (new_xTrain.csv and new_xTest.csv) to train the linear regression models in the subsequent questions. Note that you need not adhere to the naming convention specified for your new filenames, you just need to ensure the selFeat.py script properly processes the data.

¹We have removed the last two random variables and log transformed the energy usage.

- 2. (3+7=10 pts) Linear Regression: Single Unique Solution For this problem, you will implement the closed form solution for linear regression without using scikit-learn. Since you will be implementing two algorithms for Linear Regression, we've created an Abstract class, LinearRegression, to standardize the functions and to share code². The two classes that will implement the LinearRegression class are StandardLR and SgdLR. The template code for this problem is found in lr.py, standardLR.py.
 - (a) Implement the predict function in the LinearRegression class object (file lr.py). Given the coefficients (stored in the class variable beta) and a feature matrix xFeat, predict the response for each sample.
 - (b) Implement the closed form solution of linear regression in the train_predict function of the StandardLR object. The idea is to train the model on the training data and also simultaneously evaluate it on the test data. The parameter specifications are:
 - xTrain is a numpy $n \times d$ array where each row represents a sample and each column a feature,
 - yTrain is a numpy 1-D array of size $n \times 1$ that contains which class (0 or 1)
 - xTest is a numpy $m \times d$ array where each row represents a sample and each column a feature,
 - yTest is a numpy 1-D array of size $m \times 1$ that contains which class (0 or 1)

The output of the function is a single dictionary with the statistics on the data. The key is the iteration number and the value is a dictionary with the time elapsed, the training mean squared error, and the testing mean squared error. For example in the closed form solution, we might get something like:

Run the closed form regression on the energy dataset. You can run it from the command line using the new files from 1(d):

\$python standardLR.py new_xTrain.csv eng_yTrain.csv new_xTest.csv eng_yTest.csv

3. (25+10+5=40 pts) Linear Regression using SGD

For this problem, you will implement the solution to linear regression using permutation-based stochastic gradient descent, a variant of stochastic gradient descent. Instead of randomly selecting the samples, you will randomly shuffle the dataset to create a random permutation. The template code is found in sgdLR.py. Similar to the previous problem, you ARE NOT allowed to use any existing toolbox / implementation.

(a) Implement the train_predict function in the linear regression using stochastic gradient descent. Your implementation should use a user-specified fixed learning rate (η) , the mini-batch size $(b \in [1, n])$, and the maximum number of epochs. For the output dictionary, the key should be the batch number that also reflects the epoch. For example,

²The abstract class in Python is very similar to Java except that Python objects can implement multiple abstract classes if needed. The annotation @abstractmethod and the inheritance of the abstract class from ABC lets the interpreter known that this is the intention of the class.

if the total number of batches is 40, and the algorithm just completed the 2nd epoch, then it would start at batch number 80:

- (b) For a batch size of 1 (i.e., b = 1) and a random subset of 40% of the training data, try various learning rates and plot the mean squared error on the training data as a function of the epoch (i.e., one epoch = one pass through the training data). What seems to be an optimal learning rate? Justify your answer based on the plot.
- (c) Using the optimal learning rate from (b), train the model on the entire dataset and plot the mean squared error on the training data and the test data as a function of the epoch.

Algorithm 1 Stochastic Gradient Descent

```
1: for epoch = 1 : MAX EPOCH do
```

- 2: Randomly shuffle training data and break into B = N/BatchSize batches
- 3: **for** b = 1 : B **do**
- 4: Compute the gradients associated with samples in batch $b, \nabla f$
- 5: Take the average of the gradients in the batch
- 6: Update the parameters based on the gradient
- 7: end for
- 8: end for

4. (20+5=25 pts) Comparison of Linear Regression Algorithms using SGD and Closed Form solutions

For this problem, you will compare the results of the linear regression algorithm using SGD (problem 3) and the closed form solution (problem 2).

- (a) Explore the impact of batch sizes on the computation time and convergence of the SGD algorithm. Choose a variety of batch sizes (it should include 1, and n, and a few more, where the training size is divisible by the number). For each batch size, find a reasonable learning rate and then run SGD using that batch size. Plot the mean squared error of the training data and the test data as a function of the total time for different batch sizes. To make it easier, you may want to split training and test into two different plots. The plots should also include the point reflecting the closed form solution.
- (b) What are your observations based on the plot in (a)? What are the trade-offs between different batch sizes as well as the closed form solution?