

- The memory limit for all problems is 1024 MB.
- Beginners are recommended to start with A and M, the first and last problems respectively.



## Problem A Espresso!

Time limit: 1 second

John is a student working as a part-time barista at the micro kitchen of his school department. He operates the espresso machine at the kitchen to make espresso and latte for students seeking energy to study.

Today, there are n students coming to the micro kitchen to place an order. An order is noted with an espresso shot number x ranging between 1 and 4, and an optional letter L that indicates that the student wants to have a x-shot latte. For example, an order 2 means a 2-shot espresso, and an order 3L means a 3-shot latte.



Making an x-shot espresso consumes x ounces of water. Making a latte requires steaming milk and consumes one additional ounce of water, e.g. making a 3-shot latte consumes 4 ounces of water. The espresso machine at the micro kitchen has a water tank of s ounces that is full at the beginning of the day. John refills the water tank to s ounces whenever the remaining water in the tank is not enough to fulfill the next student's order. John fulfills the n orders one by one without changing their order.

How many times do John have to refill the water tank today in order to serve all the n students?

### Input

The first line of input has two integers n ( $1 \le n \le 100$ ) and s ( $10 \le s \le 200$ ). The next n lines each contain a digit between 1 and 4 followed by an optional letter L to describe an order. The orders are to be fulfilled in the given order as they appear in the input.

### Output

Output the number of times John has to refill the water tank of the espresso machine.

Sample Input 1	Sample Output 1	
8 10	2	
1		
2L		
3		
4		
3L		
1		
1L		
4L		
Sample Input 2	Sample Output 2	
3 12	0	
4		
4		



# Problem B Ultimate Binary Watch

Time limit: 1 second

The Ultimate Binary Watch is a maker project that uses small LEDs to display time on a watch face. The display uses four columns of four LEDs each, with each column representing one digit of the current time in hours and minutes. Time is displayed in 24-hour format, with the 1st (left-most) column displaying the tens position for hours, the 2nd column displaying the ones position for minutes, and the last (right-most) column displaying the ones position for minutes. The bottom LED of each column shows the lowest-order bit of its represented digit, with the bit positions increasing moving up the column. For example, the time 1615 would be displayed as shown in the figure.



Write a program that will take a 24-hour time and print the corresponding watch face.

### Input

The input has a single line with 4 digits describing a valid 24-hour time between 0000 and 2359.

### **Output**

Output four lines with a representation of the watch face displaying the given time. The tens of hours shall be in the 1st column, the single hours in the 3rd, the tens of minutes in the 7th, and the single minutes in the 9th. Use asterisks to represent bits that are set and periods to represent bits that are clear. Columns not used are to be filled with spaces. No extra whitespace are to appear at the beginning or end of any output line.

Sample Input 1	Sample Output 1
1615	
	. * . *
	. *
	* . * *
Sample Input 2	Sample Output 2
1900	. *
	* *
Sample Input 3	Sample Output 3
0830	. *
	* .
	* .



### Problem C

### Concert Rehearsal

Time limit: 3 seconds

A class of n music students are going to rehearse for a concert in a recital hall. In one rehearsal pass, each student will give one performance in order from student 1 to student n. Student i's performance has a duration of  $d_i$ . After the last student's performance concludes, a new rehearsal pass will start immediately, beginning with the performance of student 1.

On each day, the recital hall will be open for a fixed duration of p. At any moment if the next student's performance cannot complete before the recital hall closes, all the remaining performances within the current rehearsal pass will be moved to the next day.





### Input

The first line of input contains three integers n, p, k  $(1 \le n \le 2 \times 10^5, 1 \le p, k \le 10^9)$ . Each of the next n lines contains a single integer. The ith line gives  $d_i$   $(1 \le d_i \le p)$ .

### Output

Output the number of full rehearsal passes the class can complete in k days.

Sample Input 1	Sample Output 1
3 9 5	7
1	
2	
3	
Sample Input 2	Sample Output 2
4 10 5	2
3	
2	
4	
6	
Sample Input 3	Sample Output 3
3 10 2	0
5	
6	
7	



# Problem D Land Equality

Time limit: 1 second

There is a kingdom where the old King wants to divide his land into two pieces and give them to his two descendants. The King's land is a grid of r rows and c columns. Each cell in the grid has an integer value representing the prosperity of the cell, which can be 0 (deserted), 1 (regular), or 2 (fertile). Two cells are connected if they share a side horizontally or vertically.

Each descendant shall receive a single connected piece of land with at least one cell, in which all cells must be directly connected or indirectly connected via other cells. There shall be no leftover cells, which means that



each cell must be given to one descendant. The prosperity of a piece of land is the product of all the prosperity values of its cells. The King wants the absolute difference between the prosperity of the two descendants' land to be as small as possible. He has asked his best counselor to devise a land division plan between the two descendants.

### Input

The first line of input contains two positive integers r and c ( $2 \le r \times c \le 64$ ). The next r lines each have c integers giving the prosperity values of the King's land. All those integers are 0, 1, or 2.

### Output

Output the smallest absolute difference between the prosperity of the two descendants' land.

Sample Input 1	Sample Output 1
3 4	8
1 2 1 1	
2 2 1 2	
1 2 2 2	
Sample Input 2	Sample Output 2
2 3	0
0 1 2	
0 1 2	
Sample Input 3	Sample Output 3
1 3	2
2 0 2	



## Problem E Even Substrings

Time limit: 7 seconds

You are given a string  $s[1\dots n]$  consisting of the first 6 lowercase English letters between a and f. A substring is called even if every distinct letter in it appears an even number of times. For example, in abbacac there are 4 even substrings: abba, bb, acac, bbacac. If a same substring appears at different locations, they shall be counted multiple times, e.g. the string aaa has 2 even substrings aa.



You are to process q queries of the following two types:

Given a range specified by two integers l and r, count the number of even substrings in  $s[l \dots r]$ , the substring of s starting at s[l] and ending at s[r] (both ends are inclusive). Given an index i and a letter x between a and f, change s[i] to x.

### Input

The first line of input has a single string  $s[1\dots n]$   $(1 \le n \le 2 \times 10^5)$  consisting of letters between a and f. The second line of input has a single integer q  $(1 \le q \le 2 \times 10^5)$ , the number of queries. Each of the next q lines gives one query:

Type 1 query has 1 l r ( $1 \le l \le r \le n$ ).

Type 2 query has 2 i x ( $1 \le i \le n$ ), where x is a letter between a and f.

There is at least one query of type 1.

### Output

For each type 1 query output the number of even substrings on a single line.

### Sample Input 1 Sample Output 1

	· · · · · · · · · · · · · · · · · · ·
abbacac	4
8	2
1 1 7	6
2 5 a	4
1 4 6	0
1 1 7	0
2 6 b	
1 2 6	
1 5 7	
1 1 1	



# Problem F Bracket Pairing

Time limit: 7 seconds

There are four types of brackets: round (), square [], curly, and angle <>. A bracket sequence is defined to be valid as follows:

An empty sequence is valid.

If X is a valid bracket sequence, then pXq is a valid bracket sequence, where p is an open bracket, q is a close bracket, and p,q are of the same type.

If X and Y are valid bracket sequences, then the concatenation of X and Y, Z = XY, is a valid bracket sequence.



You have a bracket sequence in which some brackets are given, but the others are unknown and represented by question marks ('?'). You shall fill in each unknown bracket using the four types of brackets described above and obtain a valid bracket sequence. How many different valid bracket sequences can you obtain?

#### Input

The input has a single line giving a non-empty bracket sequence. The length of the sequence is even and no larger than 20. All sequence characters are either one of the four types of open or close brackets, or a question mark denoting an unknown bracket. There is at least one question mark in the sequence.

### Output

Output the number of different valid bracket sequences you can obtain.

Sample Input 1	Sample Output 1	
(??)	5	
Sample Input 2	Sample Output 2	
(<{}>??]	1	
Sample Input 3	Sample Output 3	
(?]]	0	

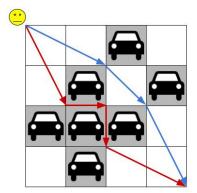


## Problem G Parking Lot

Time limit: 7 seconds

Walking across a huge parking lot is not only time consuming but also challenging because cars block your way and you may even get lost! Imagine you are walking across a parking lot of r rows and c columns of parking spots. All parking spots have a size of a unit square. A parking spot either is empty or contains a parked car. You can walk across an empty parking spot in any direction, but can only walk along the boundaries of a parking spot if there's a parked car in it. You start at the top-left corner of the parking lot and walk at a constant speed of one unit distance per second. If you pick the fastest route, in how many seconds can you walk to the bottom-right corner of the parking lot?

The image illustrates two possible routes for the parking lot in the first sample case. The blue route is the fastest route in this case. The red route shows that you can walk along the boundaries of parked cars.



### Input

The first line of input has two integers r and c ( $1 \le r, c \le 50$ ). The next r lines each have a string of c characters giving one row of parking spots from top to bottom. A dot '.' indicates an empty parking spot and a hash '#' indicates a parking spot with a parked car.

### **Output**

Sample Input 1

Output the smallest amount of time in seconds you need to walk to the bottom-right corner of the parking lot. Your answer is considered correct if it has an absolute or relative error of at most  $10^{-6}$  from the correct answer.

Sample Output 1

Sample Input 2	Sample Output 2
.#	
###.	
.#.#	
#.	
4 4	5.886349517

2 2	4.00000000
##	
##	



## Problem H Subprime

Time limit: 6 seconds

There is an open math problem: Is every non-negative integer a substring of at least one prime number when expressed in base ten?

A positive integer is a prime number if it is greater than one and not a product of two smaller positive integers. Integer a is a substring of integer b if it is equal to an integer derived from b by deleting zero or more consecutive digits of the most and least significant digits of b. For example, 123 is a substring of: 123, 56123, 123789, 50182312365, 41237912123.



Given two integers l and h along with an integer p, you are to check

how many primes between the lth smallest prime and the hth smallest prime (both ends are inclusive) contain a substring that equals p. We are interested in substrings that may include significant leading zeroes, and thus p may have leading zeroes. A prime shall be counted only once even if the integer p occurs more than once as its substring.

For example, consider l=1, h=10 and p=9. This is a search from the 1st smallest prime (2) to the 10th smallest prime (29) for any prime containing the substring "9". There are 2 such primes: 19 and 29.

### Input

The first line of input has two integers l and h ( $1 \le l \le h \le 10^5$ ). The second line has a sequence of 1 to 6 digits giving the integer p, which may be zero or have significant leading zeroes.

### **Output**

Output the count of prime numbers in the given range that contain p as a substring.

Sample Input 1	Sample Output 1	
1 10	2	
9		
Sample Input 2	Sample Output 2	
500 1000	26	
43		
Sample Input 3	Sample Output 3	
1 1000	10	
00		



### Problem I Word Puzzle

Time limit: 13 seconds

Young Anna recently indulges in a word puzzle app on her phone. A word puzzle is a single English word with several blanks. Each blank represents a letter to be filled. For example, the word "programming" may appear as a puzzle p\_o\_rammin\_. When solving a puzzle, Anna first clicks on a blank and then begins typing letters. The app automatically advances to the next blank once Anna types a letter. When there are no more blanks to the right of the filled letter, the app jumps back to the beginning of the word and advances from there. Anna keeps typing until all blanks are filled. To solve the puzzle p\_o\_rammin\_, Anna may click on the first blank and type rgg. Alternatively, she may click on the second blank and then type ggr.



One day Anna shows you a puzzle that she solved along with the sequence of letters she typed. Could you tell how many different puzzles can be the one that Anna solved? Two puzzles are different if they have blanks at different positions, e.g. if the puzzle word is programming and Anna typed rgg, there can be two possible puzzles:  $p_o_rammin_a$  and  $pro_ammin_a$ . As the answer can be large, output the answer modulo  $1\,000\,000\,007$ .

### Input

The first line of input has a single string p giving the puzzle word  $(1 \le |p| \le 10^5)$ . The second line has a single string s giving the letter sequence that Anna typed  $(1 \le |s| \le \min(50, |p|))$ . Both strings contain only lowercase English letters.

### **Output**

Output the number of different puzzles that can be the one solved by Anna, modulo  $1\,000\,000\,007$ . If Anna can not have typed s to solve the puzzle, output zero.

Sample Input 1	Sample Output 1
programming	2
rgg	
Sample Input 2	Sample Output 2
aabbaa	12
aba	
Sample Input 3	Sample Output 3
acca	0
acac	



# Problem J Code Guessing

Time limit: 1 second

Alice and Bob are playing a board game with a deck of nine cards. For each digit between 1 to 9, there is one card with that digit on it. Alice and Bob each draw two cards after shuffling the cards, and see the digits on their own cards without revealing the digits to each other. Then Alice gives her two cards to Bob. Bob sees the digits on Alice's cards and lays all the four cards on the table in increasing order by the digits. Cards are laid facing down. Bob tells Alice the positions of her two cards. The goal of Alice is



to guess the digits on Bob's two cards. Can Alice uniquely determine these two digits and guess them correctly?

#### Input

The input has two integers p,q ( $1 \le p < q \le 9$ ) on the first line, giving the digits on Alice's cards. The next line has a string containing two 'A's and two 'B's, giving the positions of Alice's and Bob's cards on the table. It is guaranteed that Bob correctly sorts the cards and gives the correct positions of Alice's cards.

### Output

If Alice can uniquely determine the two digits on Bob's cards, output the two digits on a single line, starting with the smaller digit. Otherwise, output -1.

Sample Input 1	Sample Output 1
6 9	7 8
ABBA	
Sample Input 2	Sample Output 2
Sample Input 2	Sample Output 2
Sample Input 2  2 5	Sample Output 2



### Problem K

### Tree Number Generator

Time limit: 13 seconds

One day Young Anna comes up with a whimsical idea of using a tree to create a number generator. The generator is created with a modulus m and an internal tree of n nodes numbered from 1 to n. Each tree node is assigned a single digit between 0 to 9. The generator provides a method Get(a,b) that can be used to produce an integer in [0,m). The two arguments a and b specify two tree nodes. The generator walks the path from a to b in the tree, concatenates all the digits along the path (including the digits of node a and b), and obtains a decimal integer v as a result of such digit concatenation.



Note that v can be quite large and may contain leading zeroes. The return value of Get(a, b) is v modulo m.

Given a tree and the value of m to be used by Anna's number generator, calculate the return values of q queries Get(a,b).

### Input

The first line of input has three integers n ( $2 \le n \le 2 \times 10^5$ ), m ( $1 \le m \le 10^9$ ), and q ( $1 \le q \le 2 \times 10^5$ ).

The next n-1 lines describe the tree edges. Each line has two integers x,y  $(1 \le x,y \le n)$  listing an edge connecting node x and node y. It is guaranteed that those edges form a tree.

The next n lines each have a single digit between 0 to 9. The ith digit is assigned to node i.

The next q lines each have two integers a, b  $(1 \le a, b \le n)$  specifying a query Get(a, b).

#### **Output**

For each Get(a, b) query output its return value on a single line.

Sample Input 1	Sample Output 1
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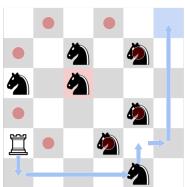
5 100 4	34
1 2	31
1 3	12
1 4	3
5 3	
1	
2	
3	
0	
4	
1 5	
5 1	
4 2	
3 3	



### Problem L Lone Rook

Time limit: 11 seconds

On a chess board of r rows and c columns there is a lone white rook surrounded by a group of opponent's black knights. Each knight attacks 8 squares as in a typical chess game, which are shown in the figure—the knight on the red square attacks the 8 squares with a red dot. The rook can move horizontally and vertically by any number of squares. The rook can safely pass through an empty square that is attacked by a knight, but it must move to a square that is not attacked by any knight. The rook cannot jump over a knight while moving. If the rook moves to a square that contains a knight, it may capture it and remove it from the board. The black knights never move. Can the rook eventually safely move to the designated target square?



The figure illustrates how the white rook can move to the blue target square at the top-right corner in the first sample case. The rook captures one black knight at the bottom-right of the board on its way.

### Input

The first line of input contains two integers r and c ( $2 \le r, c \le 750$ ). Each of the next r lines describes one row of the board using c characters: the letter 'R' represents the white rook, a 'K' represents a black knight, a dot '.' represents an empty square, and the letter 'T' represents the white rook's target square. There is exactly one 'R', exactly one 'T', and at least one 'K' on the board. It is guaranteed that the white rook starts in a square that is not attacked by any knight. The target square may be attacked by a knight, in which case the knight must be captured before the rook can safely move to the target square.

#### **Output**

Output "yes" if the white rook can move to the target square, or "no" otherwise.

Sample Input 1	Sample Output 1
6 6	yes
T	
K.K.	
K.K	
K.	
RK	
K.	
Sample Input 2	Sample Output 2
3 4	yes
RK	
KK	
T	
Sample Input 3	Sample Output 3
4 4	no
.K	
KR	
K	
.K.T	



## Problem M Marvelous Marble Machine

Time limit: 1 second

Mary and Marty have finished work on their Marvelous Marble Machine. The machine takes in a mountain of marbles, mixes them up, and then ejects the marbles out one at a time. Mary and Marty's marbles come in three types: single stripe, double stripe, and triple stripe.

Mary and Marty have been testing their Marvelous Marble Machine and they want to know if the machine is working properly. The machine is working properly as long as the marbles put in are the same as the ones the machine ejected. This means that the counts of each type are the same. Is Mary and Marty's Marvelous Marble Machine working properly?



### Input

The first line of input contains a single integer n ( $1 \le n \le 100$ ), which is the number of marbles Mary and Marty put into their machine.

The second line contains n integers describing the marbles that were put into the machine. Each integer is either 1, 2, or 3 representing the number of stripes on the marble.

The third line contains n integers describing the marbles that the machine ejected. Each integer is either 1, 2, or 3 representing the number of stripes on the marble.

### **Output**

Sample Input 1

2 3 1 2 3

Display marvelous if the machine is working properly. Otherwise, display error.

5		
	error	
Sample Input 2	Sample Output 2	
2 3 1 1 3		
1 2 3 1 3		
5	marvelous	

Sample Output 1

