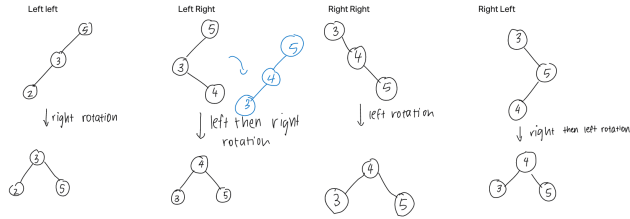


- AVL Trees**
- A self-balancing binary search tree
 - Unbalanced height: $height(left) - height(right) > 1$
 - Height of each node can be stored
 - Average and worst case search time complexity is of $O(\log n)$

```
typedef struct Node *Link; // Links are pointers to nodes
typedef struct Node *Tree; // a Tree is a pointer to its root node
struct Node { int data; int height; Link left; Link right; };

```

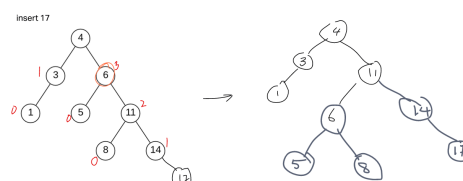
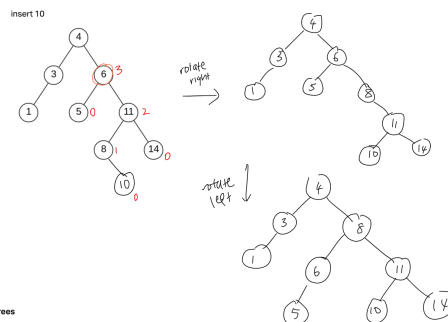
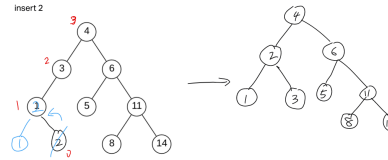
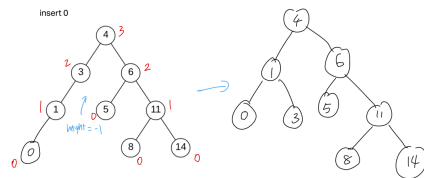
Tree rotation cases



Inserting into AVL:

1. Insert the node and update heights
2. Check if heights are balanced
3. Use one of the 4 rotations if unbalanced

1. Annotate each node with the height of its subtree, and insert the integers 0, 2, 10, 17.



2-3-4 Trees

```
typedef struct Node *Link; // Links are pointers to nodes
typedef struct Node *Tree; // a Tree is a pointer to its root node
struct Node { int order; int data[3]; Link child[4]; };

```

- Can have at a node:

- 1 item + 2 children



- 2 items + 3 children

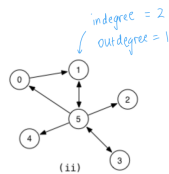
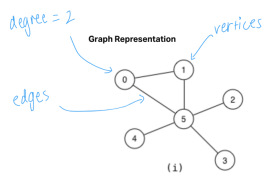
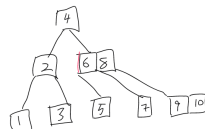


- 3 items + 4 children



- Average and worst case search time complexity is of $O(\log n)$

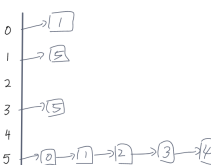
Insert 1 2 3 4 5 8 6 7 9 10 into an empty tree.



Adjacency Matrix Representation

		to					
		0	1	2	3	4	5
from	0	0	1	0	0	0	0
	1	0	0	0	0	0	1
	2	0	0	0	0	0	0
	3	0	0	0	0	0	1
	4	0	0	0	0	0	0
	5	1	1	1	1	1	0

Adjacency List Representation



	0	1	2	3	4	5
0	0	1	0	0	0	0
1	0	0	0	0	0	1
2	0	0	0	0	0	0
3	0	0	0	0	0	1
4	0	0	0	0	0	0
5	1	1	1	1	1	0