



中山大學
SUN YAT-SEN UNIVERSITY

计算机学院（软件学院）
SCHOOL OF COMPUTER SCIENCE AND ENGINEERING

Compilation Principle 编译原理

第8讲：语法分析(5)

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DCS290, 3/21/2023



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Quiz Questions

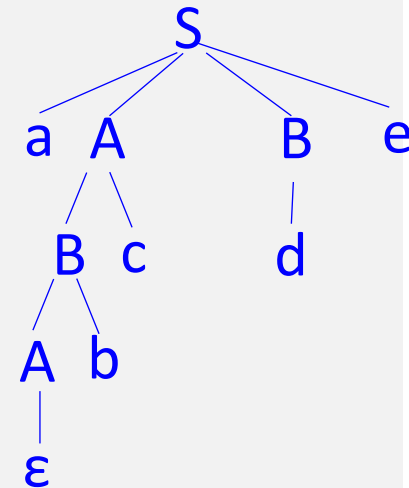


- Q1: Grammar G: $S \rightarrow aABe$, $A \rightarrow Bc \mid \epsilon$, $B \rightarrow Ab \mid d$
give a rightmost derivation of **abcde**?

$S \Rightarrow aABe \Rightarrow aAde \Rightarrow aBcde \Rightarrow aAbcde \Rightarrow abcde$

- Q2: Plot the parse tree of Q1?

See right.



- Q3: Can G be parsed by RD-backtrack? Why?

No. $A \Rightarrow Bc \Rightarrow Abc$, indirect left-recursive.

- Q4: Grammar G_2 : $S \rightarrow A \mid F$, $A \rightarrow id = exp$, $F \rightarrow id(exp)$. Can G_2 be parsed by predictive parser with one lookahead? Why?

No. A and F have a common prefix 'id'.

- Q5: Fix G_2 to make it LL(1)?

$S \rightarrow id S'$, $S' \rightarrow =exp \mid (exp)$

Cheating/Plagiarism[学术不端]

- Unauthorized use of information
 - Borrowing code: by copying, retyping, looking at a file
 - Describing: verbal desc. of code from one person to another
 - Searching the Web for solutions, discussions, tutorials, blogs ...
 - Reusing your code from a previous semester ...
 - ...
- Unauthorized supplying of information
 - Providing copy: Giving a copy of a file to someone
 - Providing access ...
 - ...
- Collaborations beyond high-level, strategic advice
 - Anything more than block diagram or a few words
 - ...

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Why a Big Deal?

- This material is best learned by doing
 - Even though that can, at times, be difficult and frustrating
 - Starting with a copy of a program and then tweaking it is very different from writing from scratch
 - Planning, designing, organizing a program are important skills
- We are the gateway to other system courses
 - Want to make sure everyone completing the course has mastered the material
- Industry appreciates the value of this course
 - We want to make sure anyone claiming to have taken the course is prepared for the real world
- Working in teams and collaboration is an important skill
 - But only if team members have solid foundations
 - This course is about foundations, not teamwork

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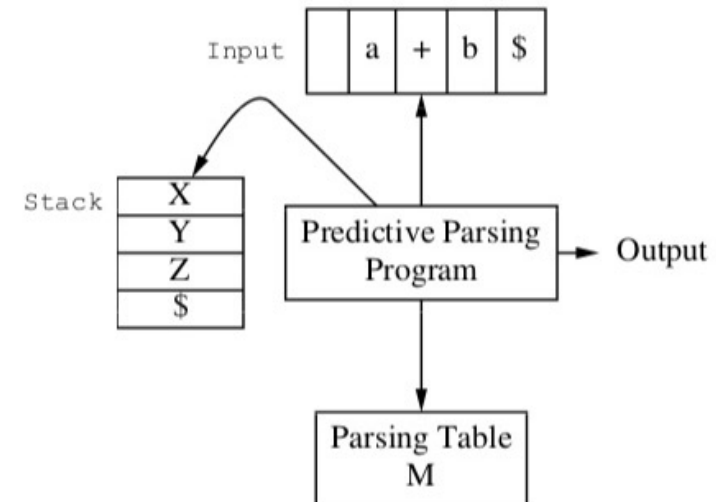
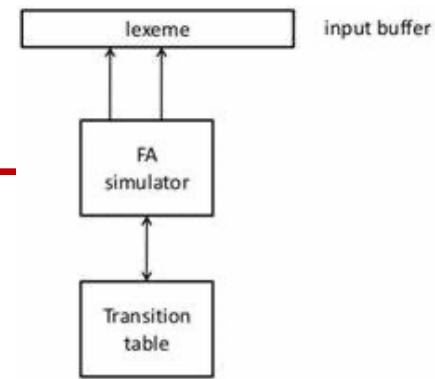
Cheating: Consequences[后果]

- Penalty for cheating:
 - Best case: -100% for assignment
 - ***You would be better off to turn in nothing***
 - Worst case: Removal from course with failing grade
 - This is the default
 - University-level involvement (from notification to serious things)
 - Loss of respect by you, the instructors and your colleagues
 - ***If you do cheat – come clean asap!***
- Detection of cheating:
 - We have sophisticated tools for detecting code plagiarism
 - In Fall 2015, 20 students were caught cheating and failed the course.
 - Some were **expelled** from the University
 - In January 2016, 11 students were penalized for cheating violations that occurred as far back as Spring 2014.
 - In May 2019, we gave an AIV to a student who took the course in Fall 2018 for unauthorized coaching of a Spring 2019 student. His grade was changed retroactively.
- Don't do it!
 - Manage your time carefully
 - Ask the staff for help when you get stuck
 - We will help you! We will give you extensions! We want you to succeed.

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LL(1) Parser[非递归]

- Table-driven parser[表驱动]: amenable to automatic code generation (just like lexers)
 - **Input buffer**: contains the string to be parsed, followed by \$
 - **Stack**: holds unmatched portion of derivation string, \$ marks the stack end
 - **Parse table** $M[A, b]$: an entry containing rule “ $A \rightarrow \dots$ ” or error
 - **Parser driver** (a.k.a., predictive parsing program): next action based on <stack top, current token>
 - ▣ **Reject** on reaching error state
 - ▣ **Accept** on end of input & empty stack



A stack records frontier of parse tree

- Non-terminals that have yet to be expanded
- Terminals that have yet to be matched against the input
- Top of stack = leftmost pending terminal or non-terminal

?: The current token is treated as lookahead token.

LL(1) Parse Table: Example

table	int	*	+	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'			$E' \rightarrow +E$		$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow \text{int } T'$			$T \rightarrow (E)$		
T'		$T' \rightarrow *T$	$T' \rightarrow \varepsilon$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$

$E \rightarrow TE'$
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- Implementation with 2D parse table

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 - One action for each <non-terminal, input> combination
 - It “predicts” the correct action based on one lookahead
 - No backtracking required

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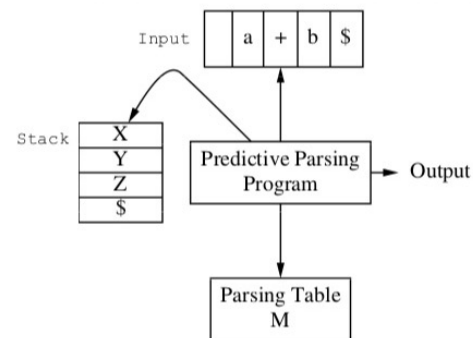
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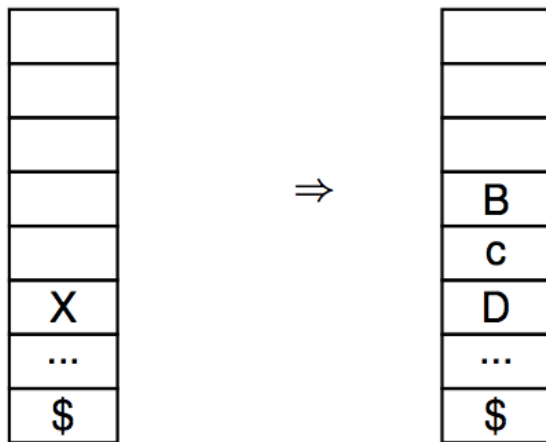
LL(1) Parsing Algorithm[算法]

- Initial state[初始态]
 - **Input** tape: input tokens followed by '\$'
 - **Stack**: start symbol followed by '\$' at bottom
- General idea[总体思路]: repeat one of two actions
 - **Expand** symbol at top of stack by applying a production
 - **Match** terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on $\langle X, a \rangle$
 - X: symbol at the top of the stack
 - a: current input token
 - If $X \in T$, then[终结符-比较]
 - If $X == a == \$$, parser halts with “success”
 - If $X == a \neq \$$, successful match, pop X from stack and advance input head
 - If $X \neq a$, parser halts and input is **rejected**
 - If $X \in N$, then[非终结符-展开]
 - If $M[X, a] == 'X \rightarrow \text{RHS}'$, pop X and push RHS to stack
 - If $M[X, a] == \text{empty}$, parser halts and input is **rejected**



Push RHS in Reverse Order[逆序入栈]

- For $\langle X, a \rangle$
 - X: symbol at the top of the stack
 - a: current input token
- If $M[X, a] = \text{"X} \rightarrow \text{BcD"}$



逆序入栈：最左符号需要被最先展开或比较（即，最左推导），因此需在靠近栈顶位置

- Performs the leftmost derivation: $\alpha \text{X} \beta \Rightarrow \alpha \text{BcD} \beta$
 - α : string that has already been matched with input
 - β : string yet to be matched, corresponding to the ... above

Apply LL(1) Parsing to Grammar[应用]

- Consider the grammar

$$E \rightarrow T+E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

- Left recursion? **NO!**
- Left factoring? **YES.** $E \rightarrow T+E \mid T$, $T \rightarrow \text{int} * T \mid \text{int}$

- After rewriting grammar, we have

$$E \rightarrow TE'$$

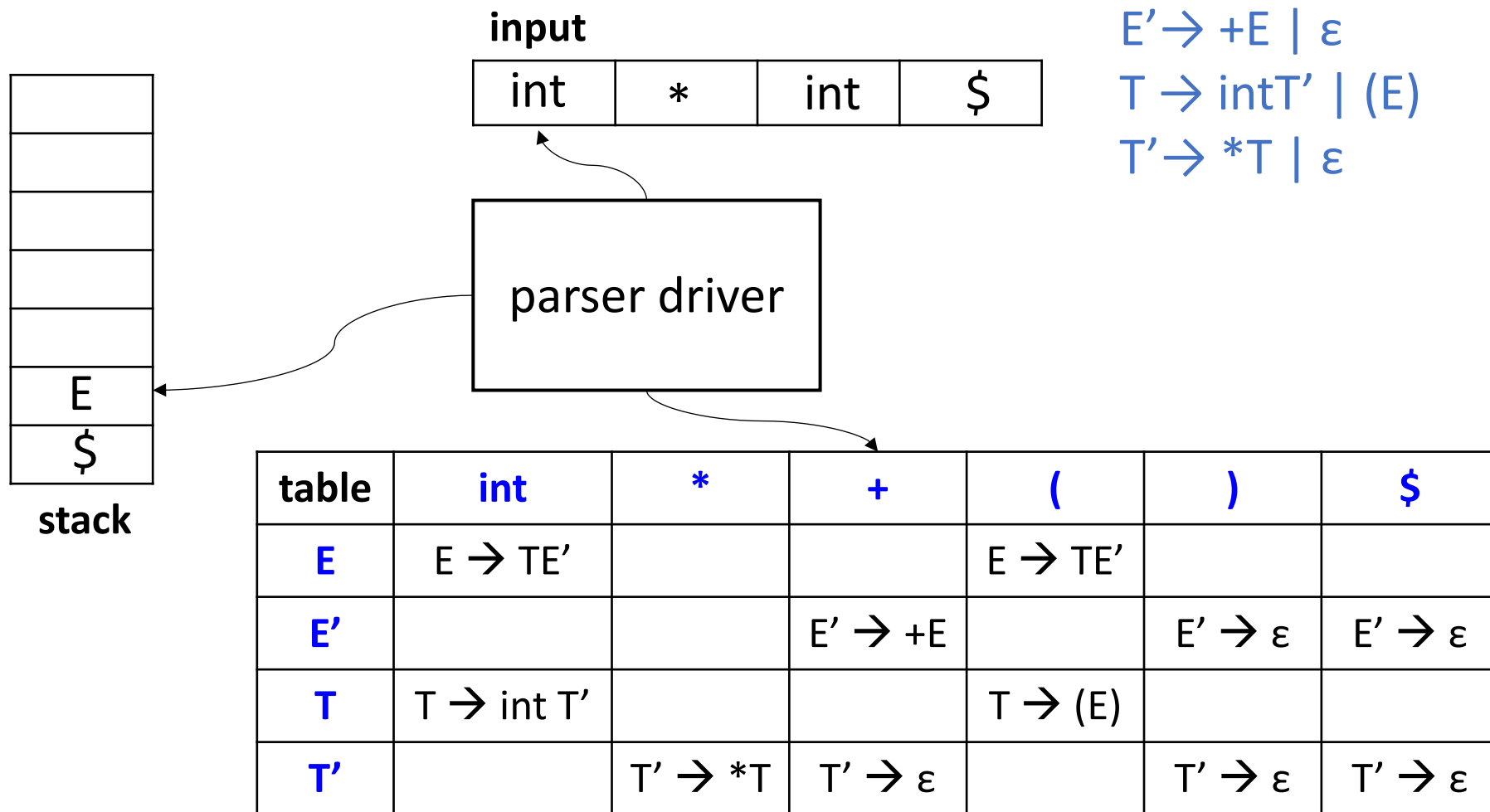
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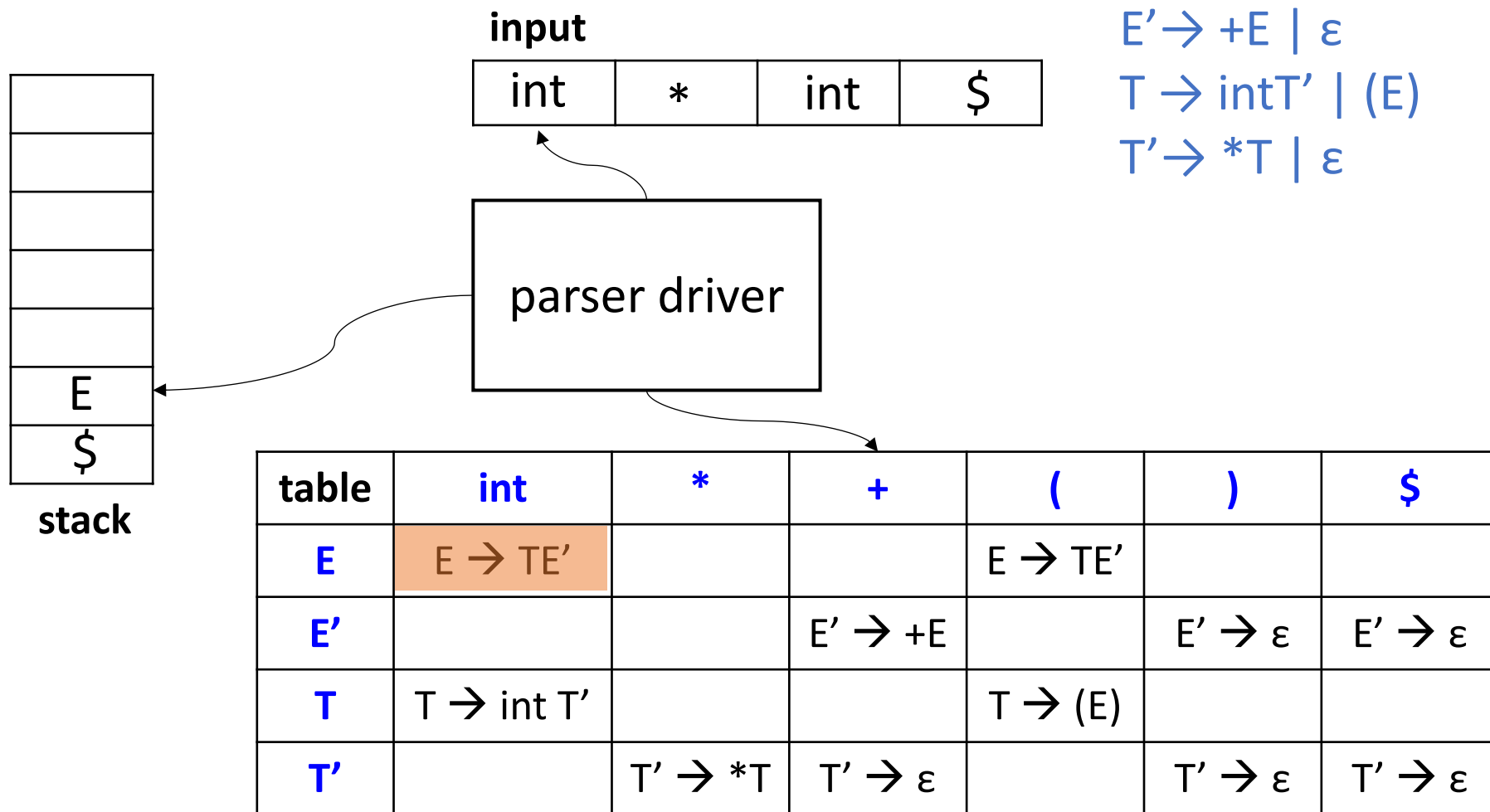
Use the Parse Table

- To recognize “int * int”



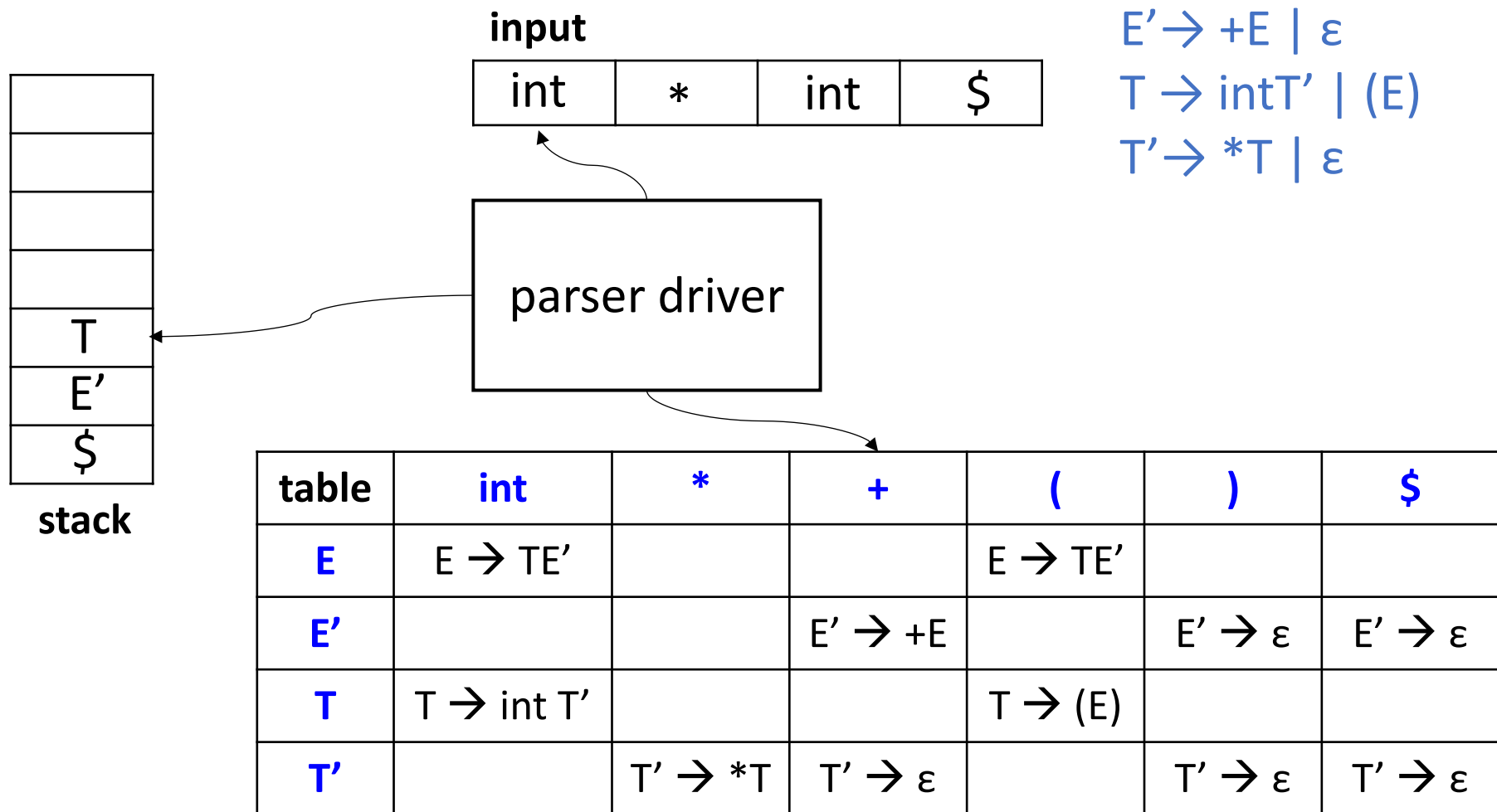
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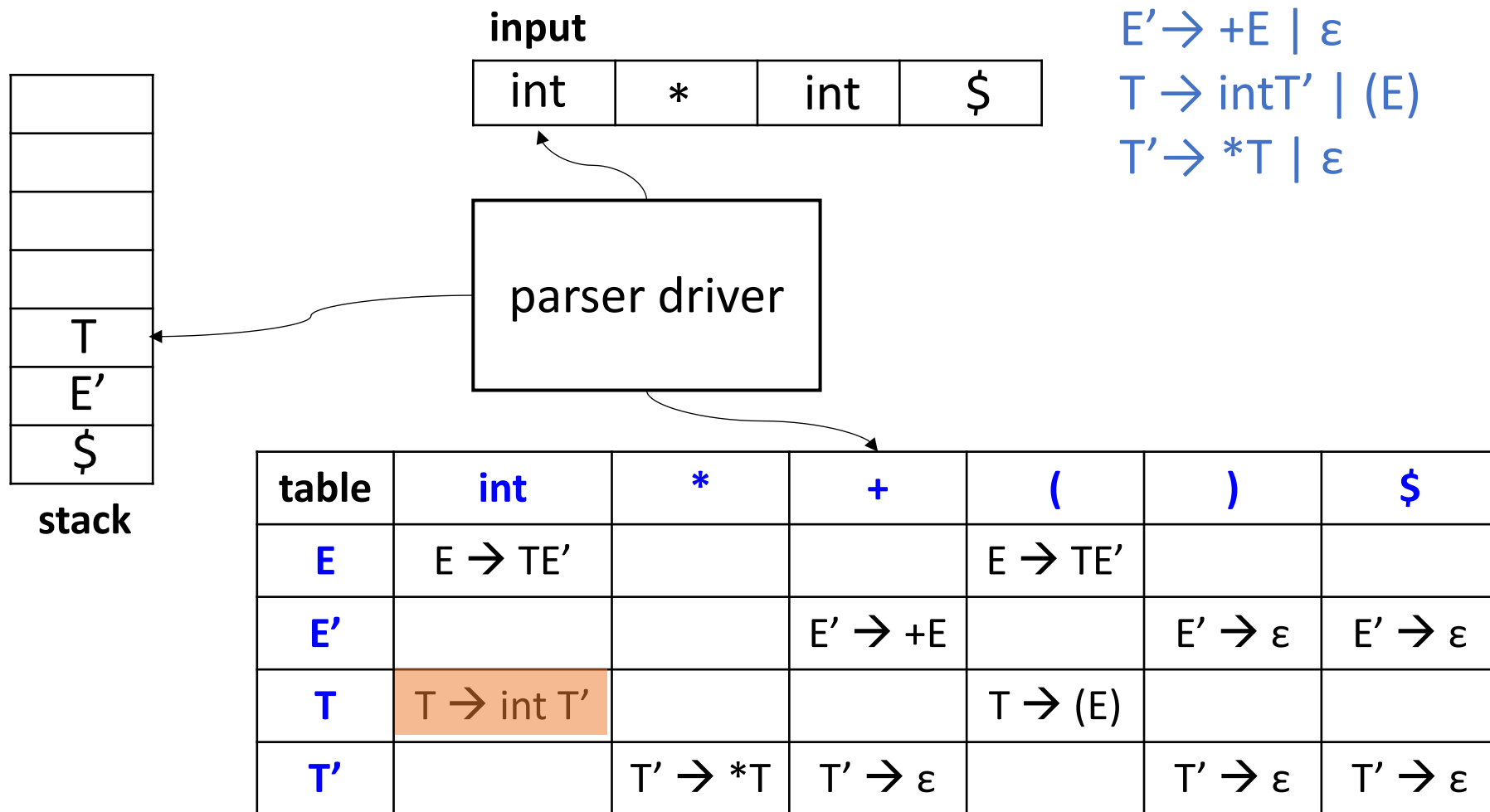
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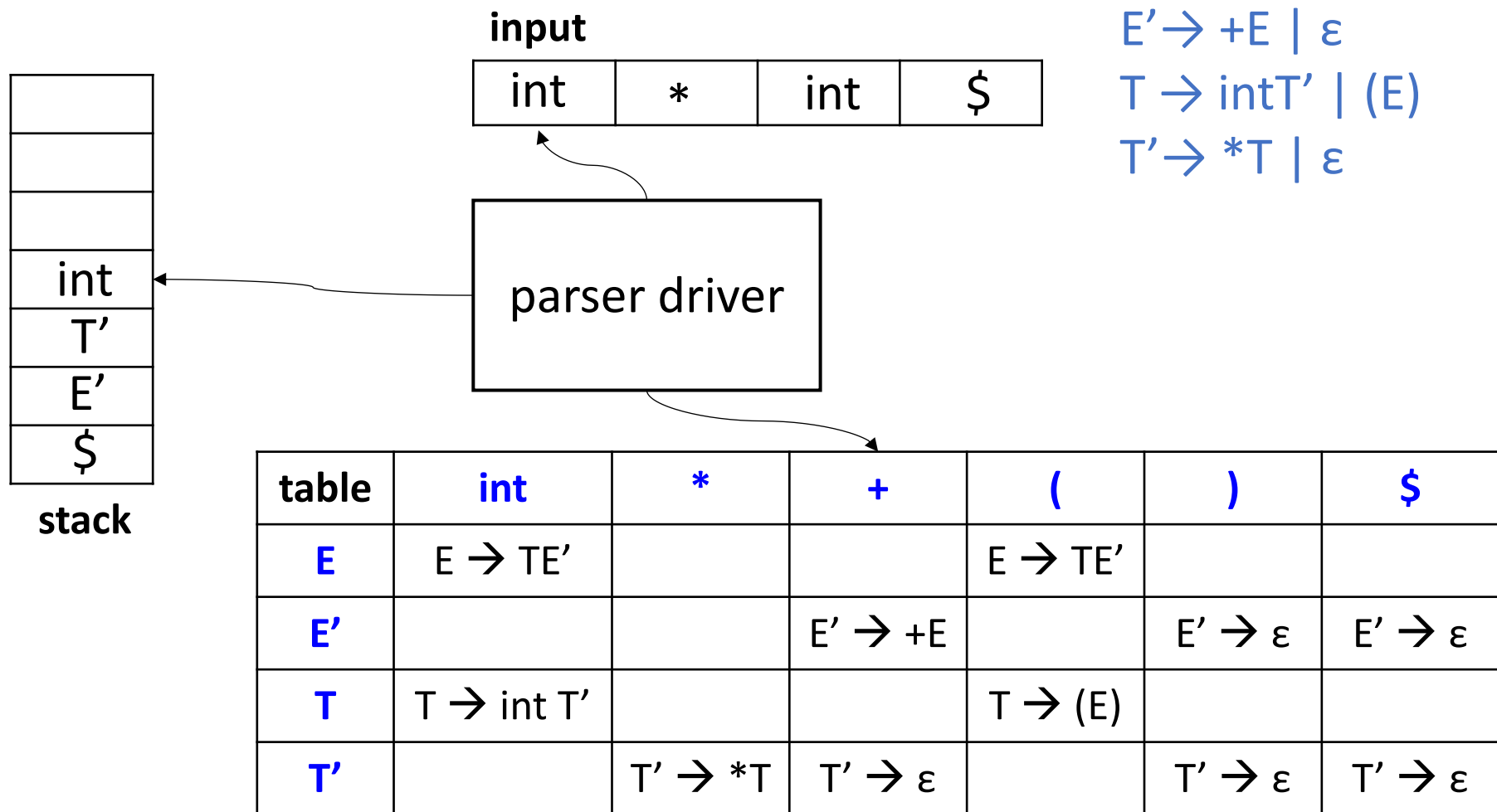
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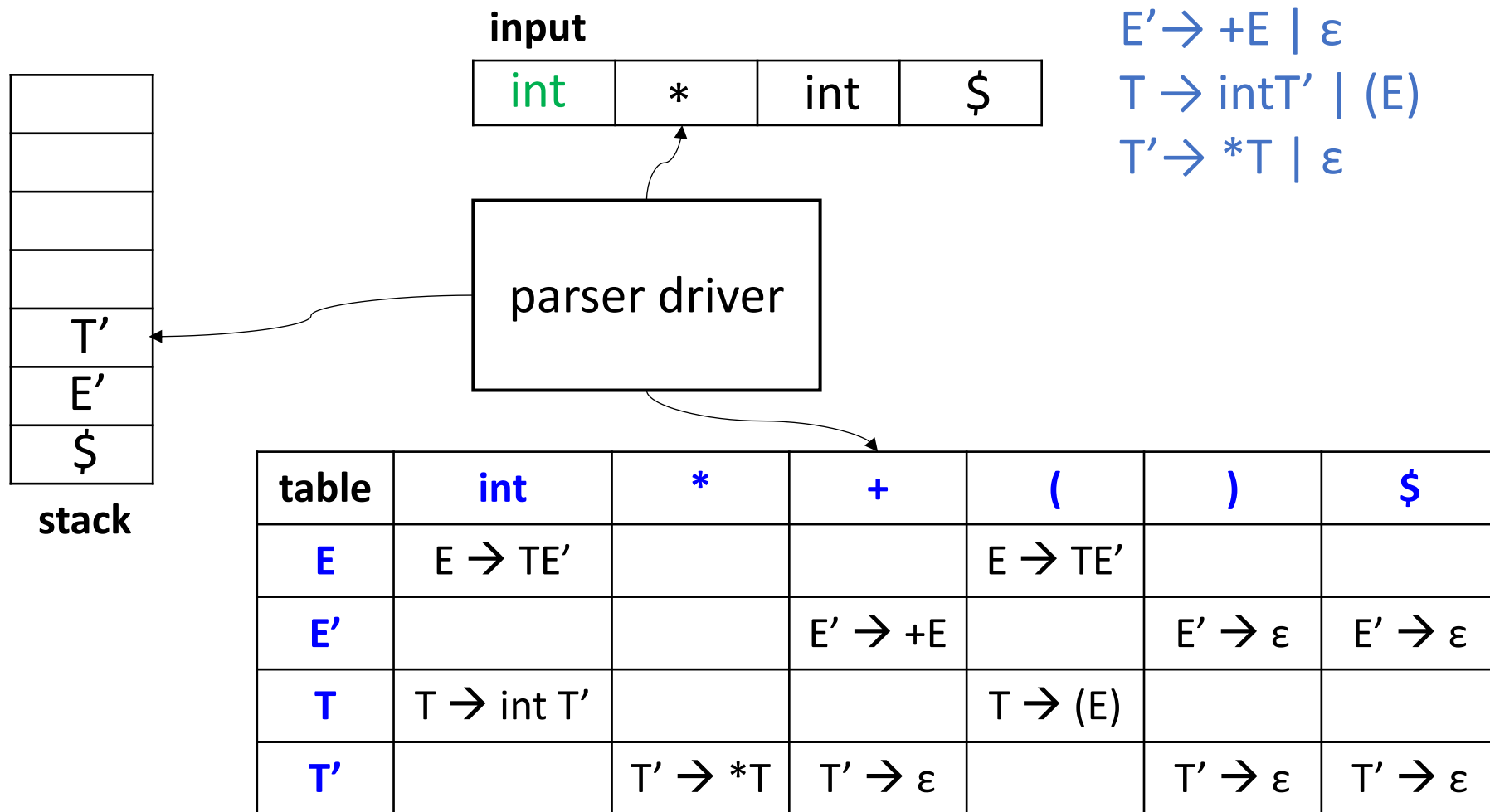
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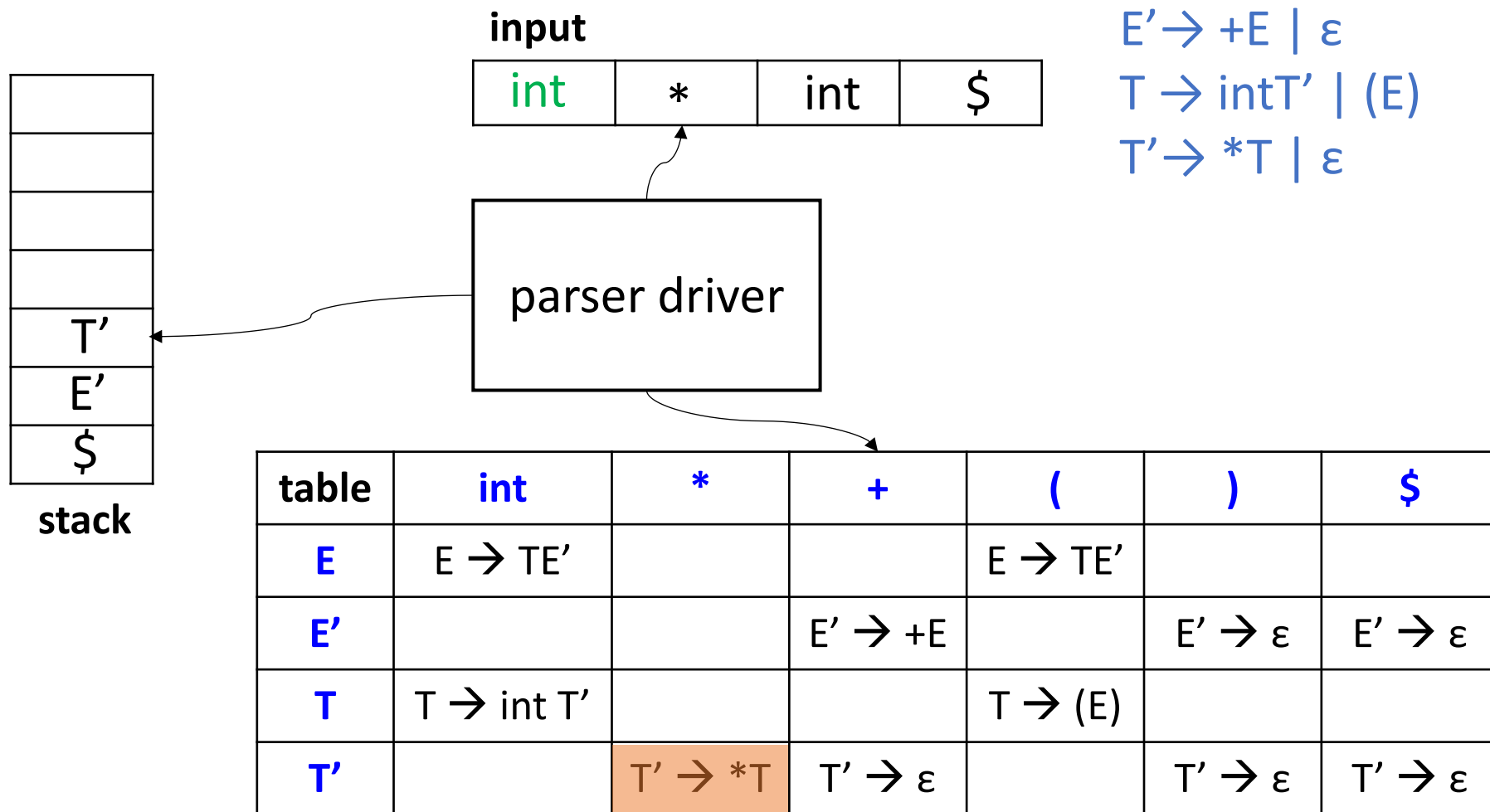
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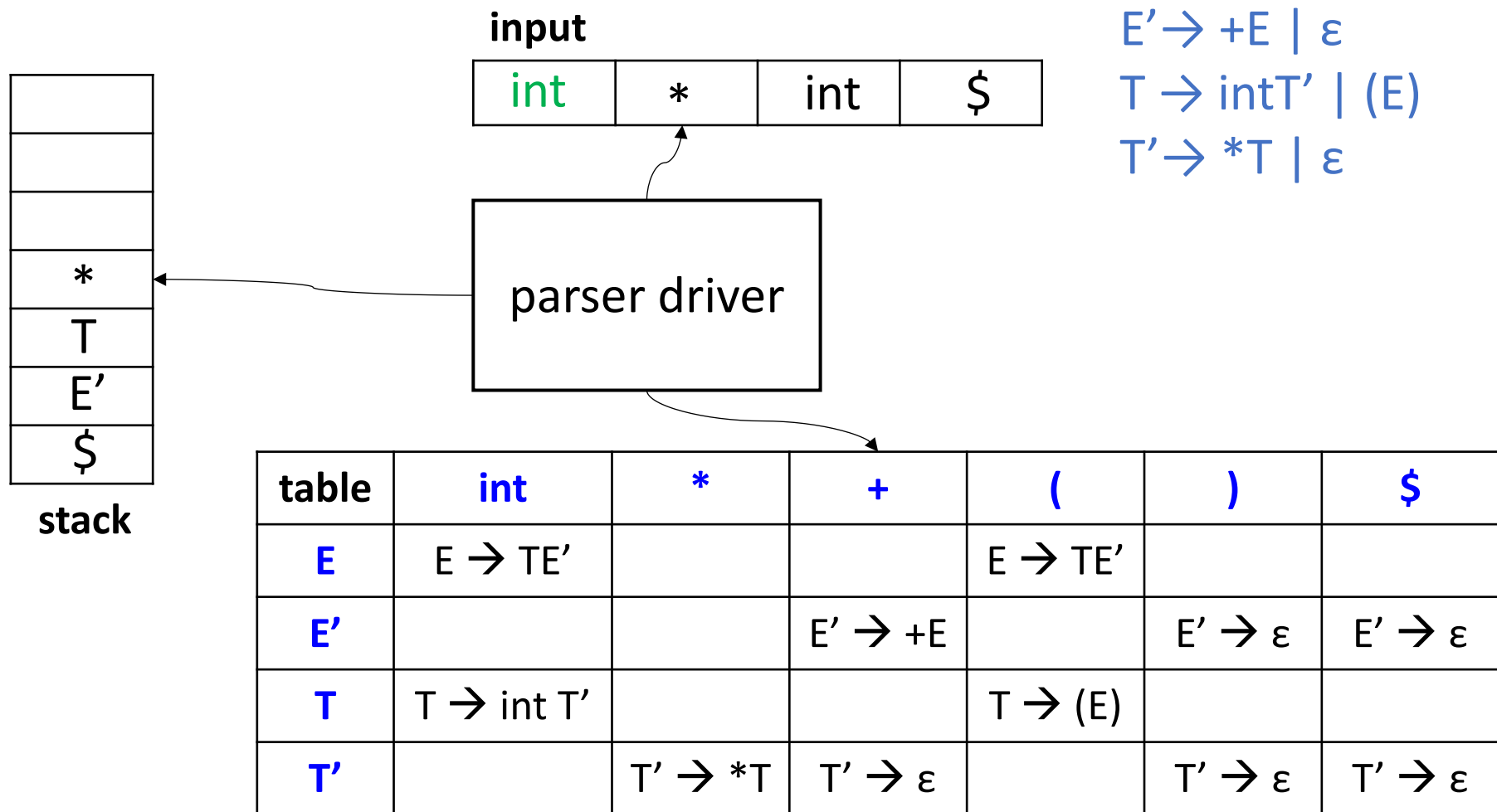
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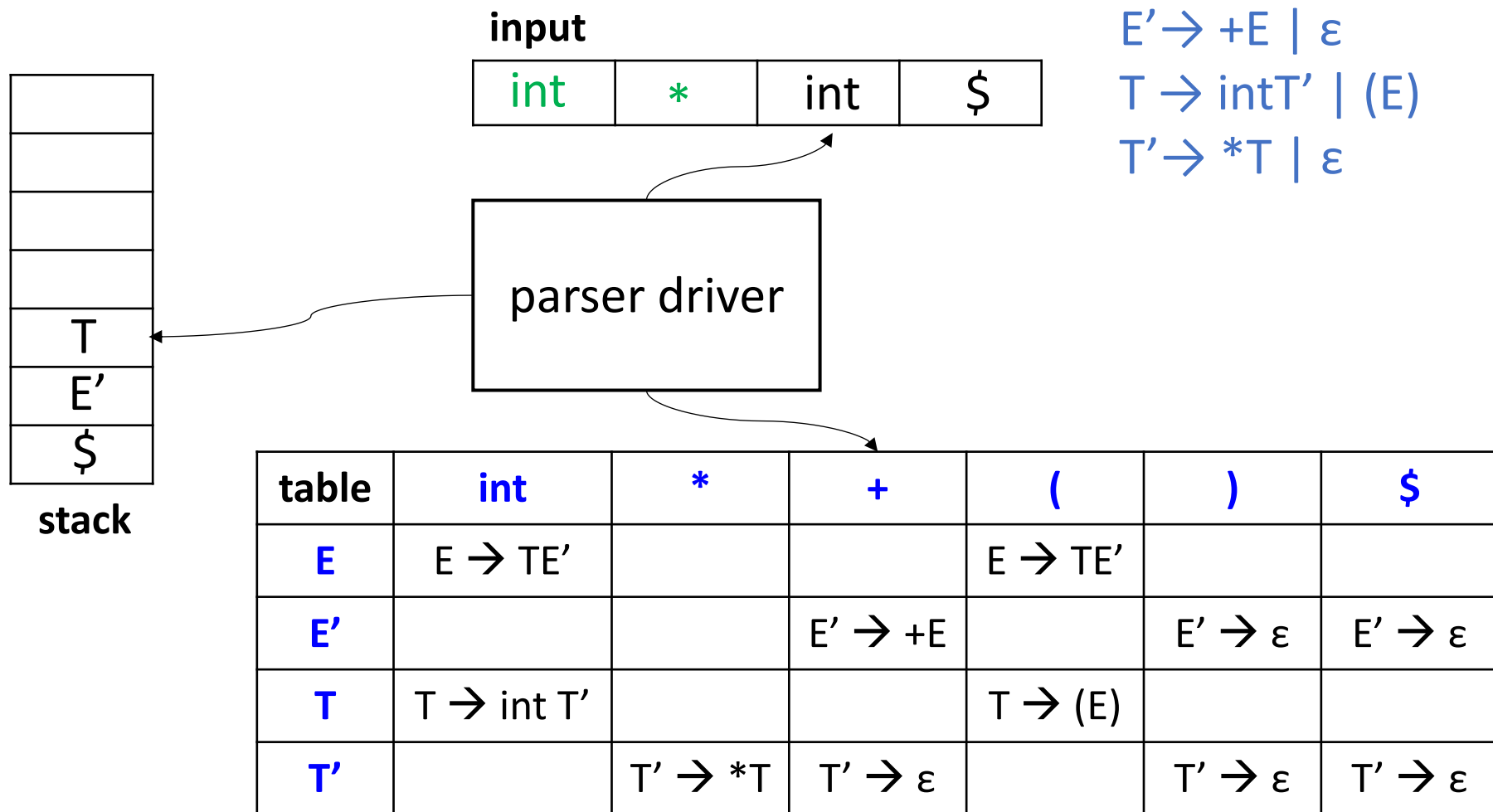
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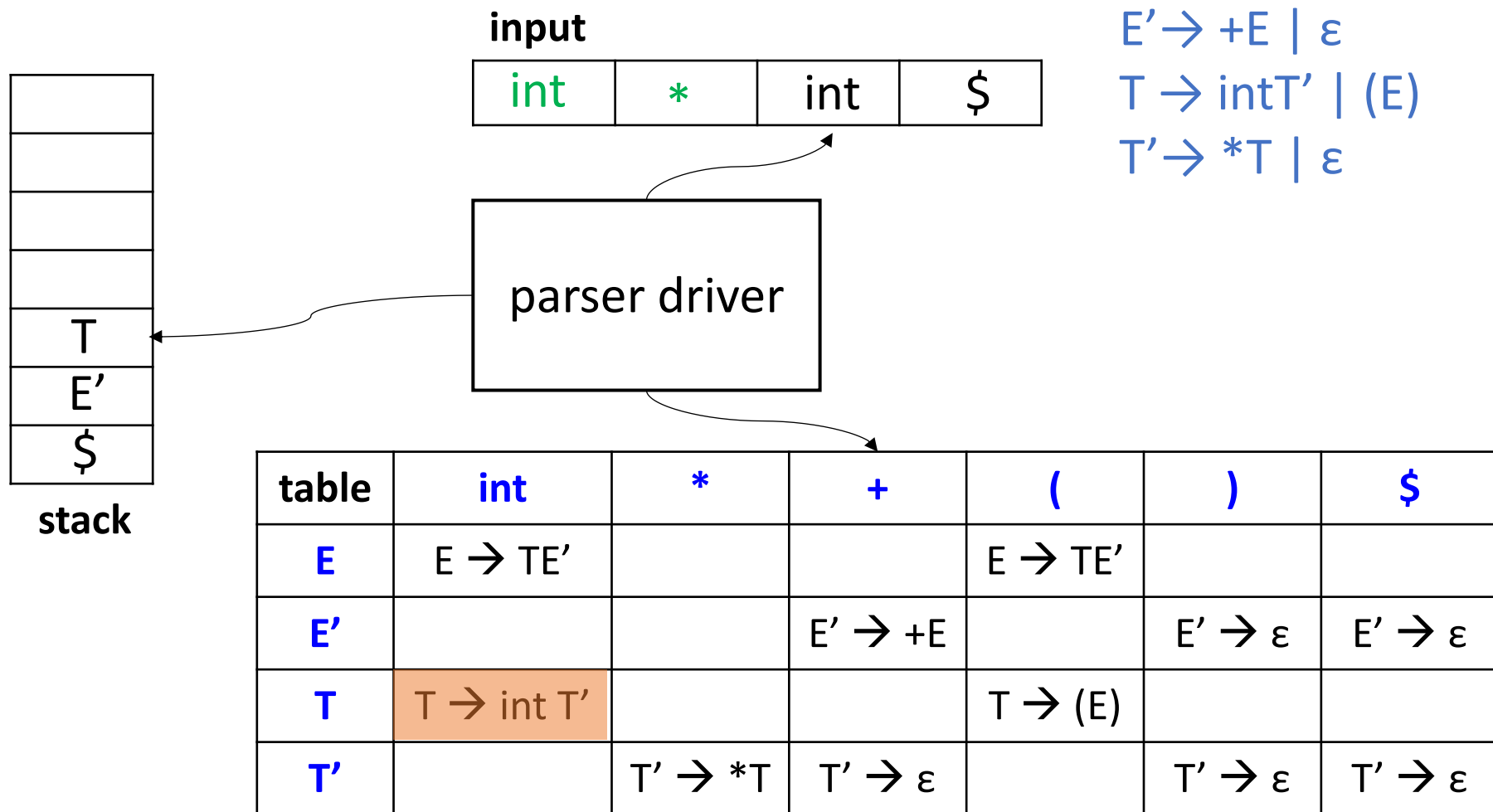
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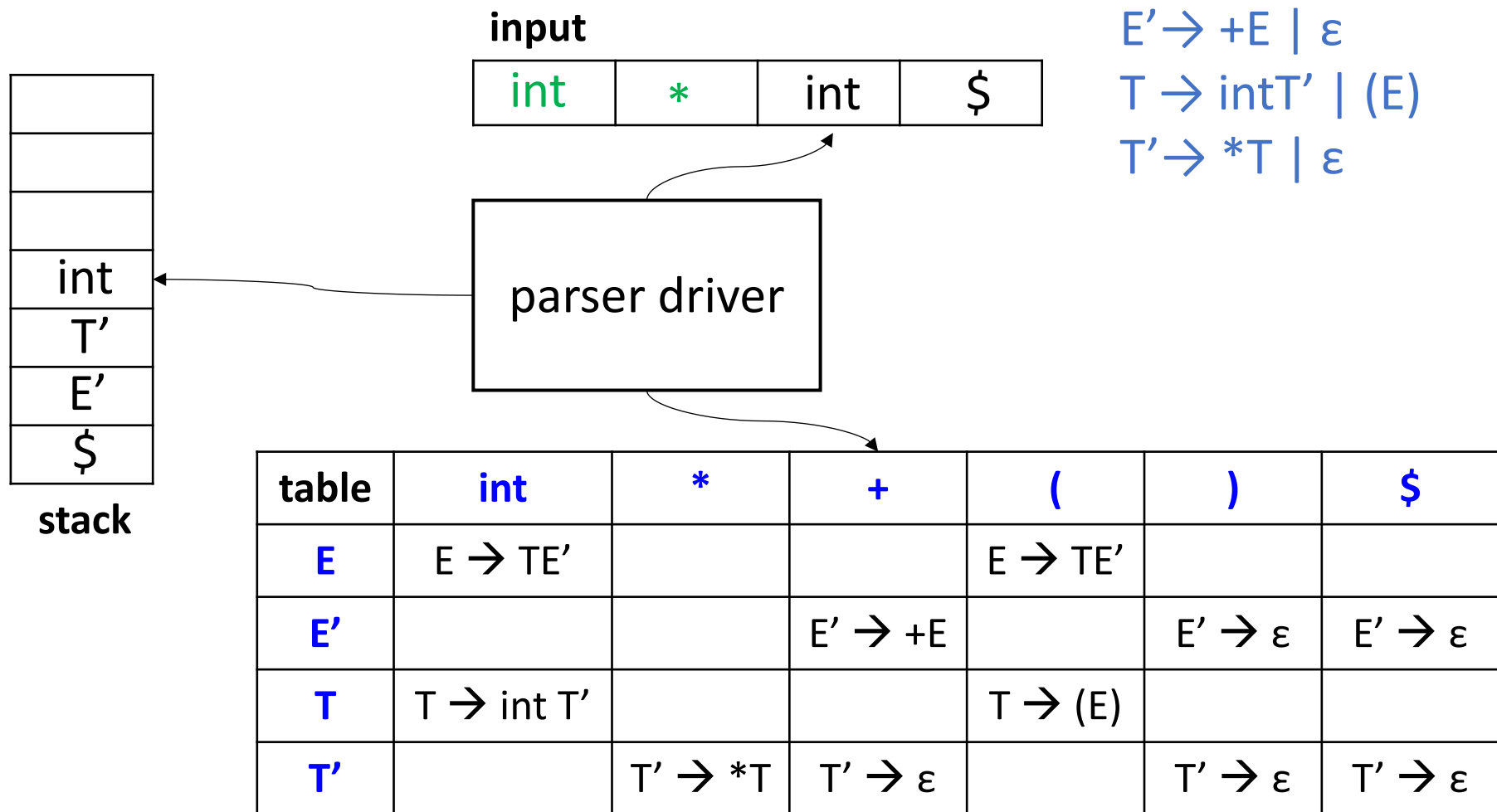
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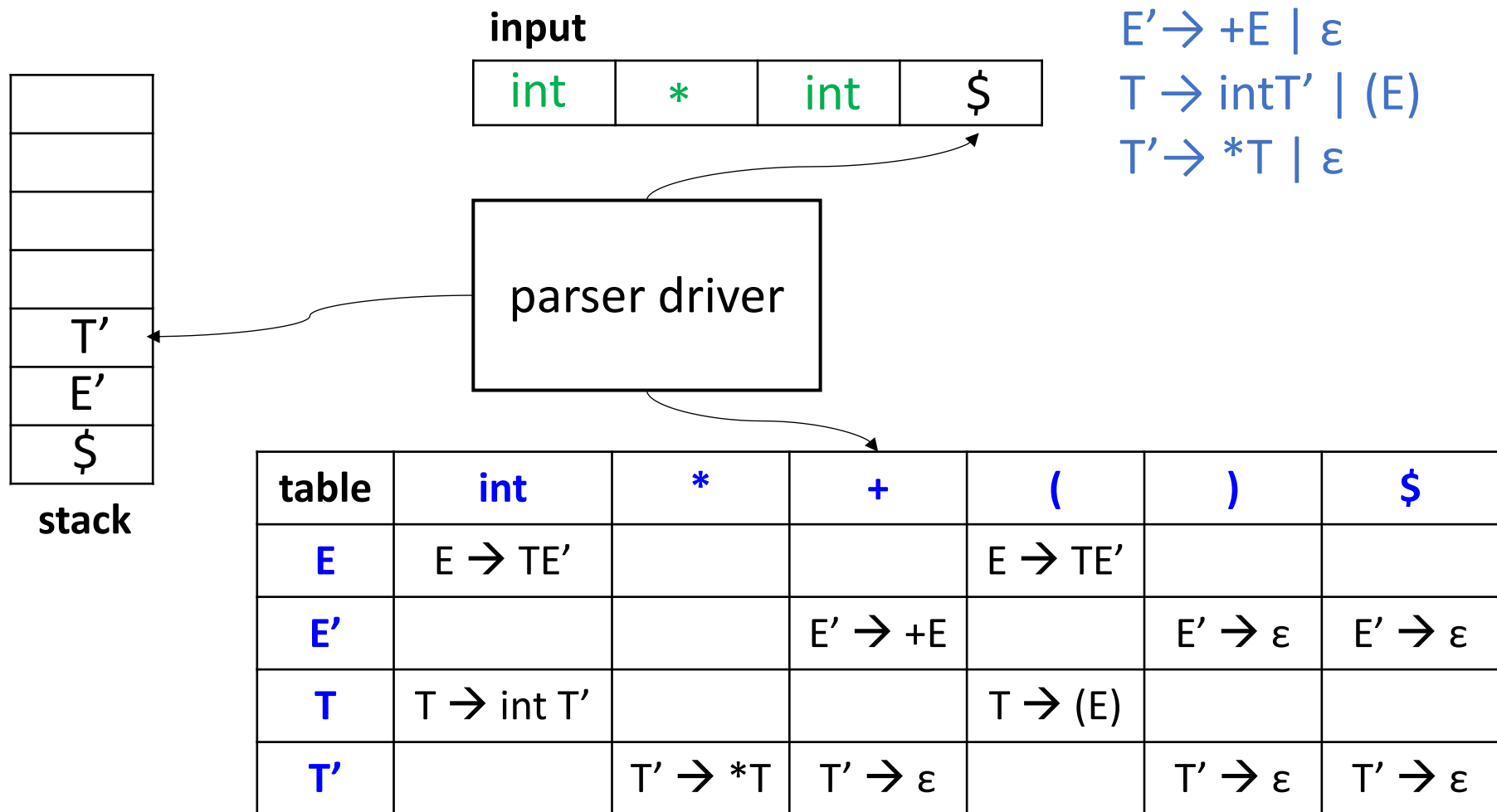
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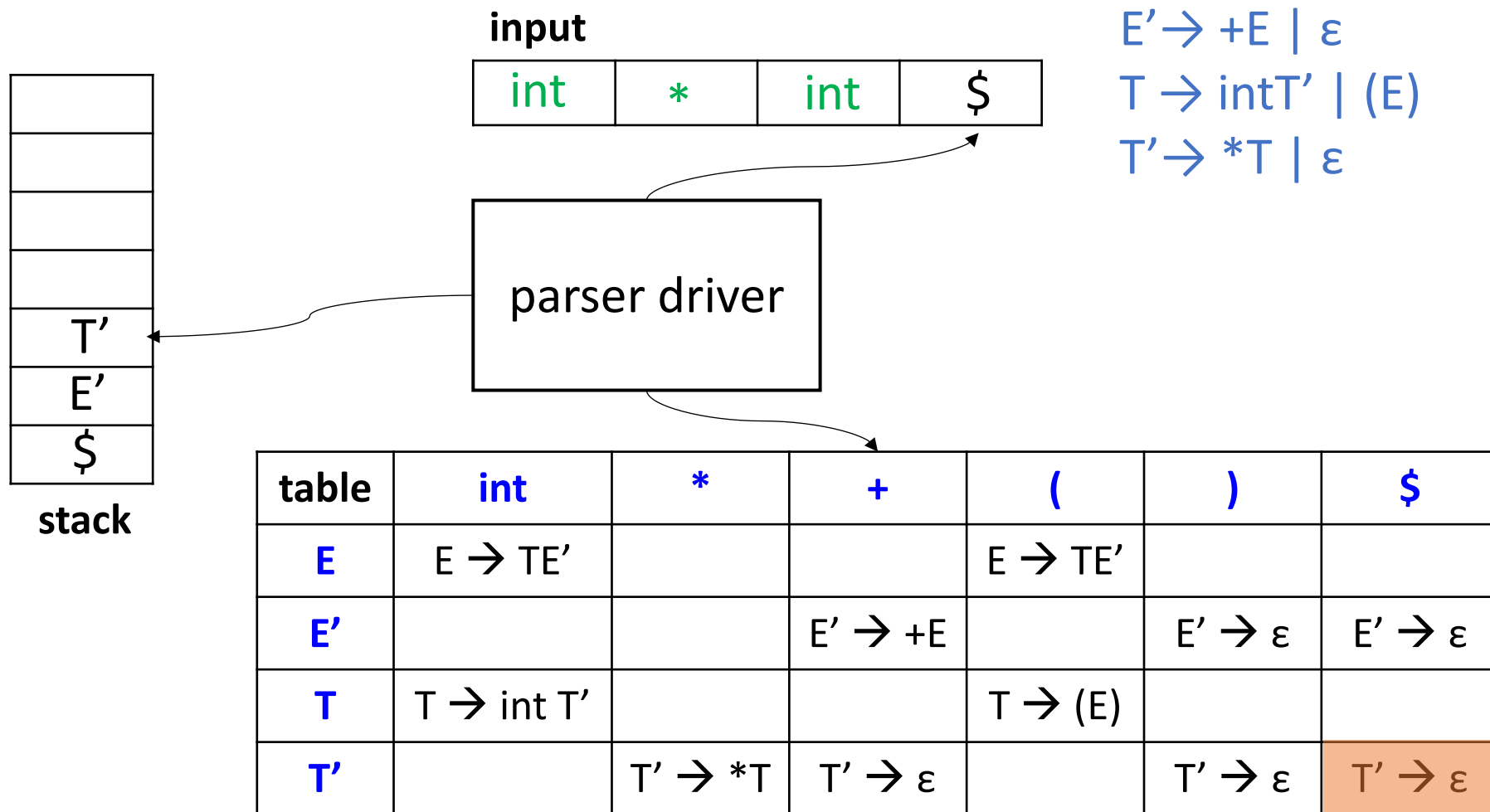
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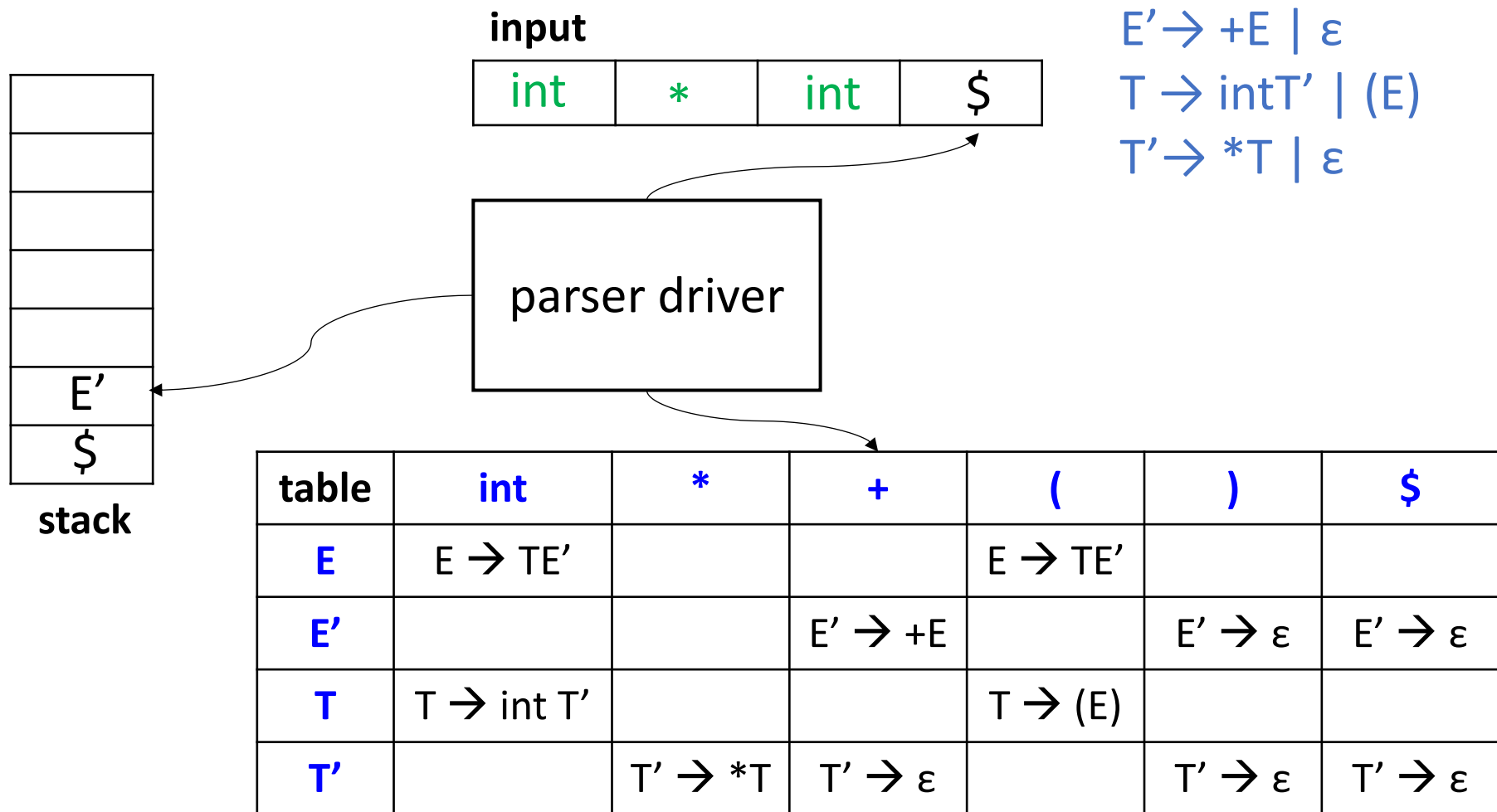
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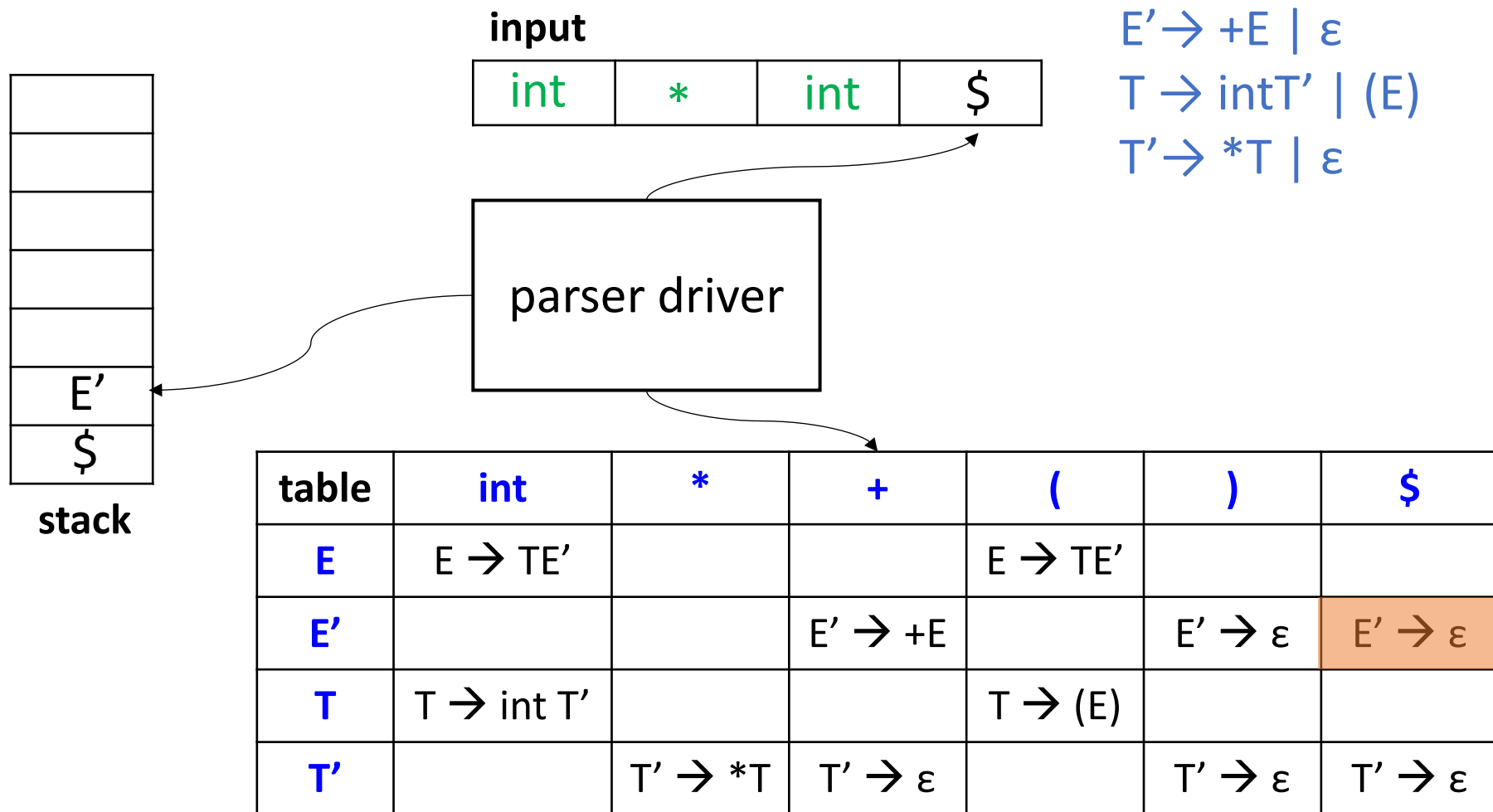
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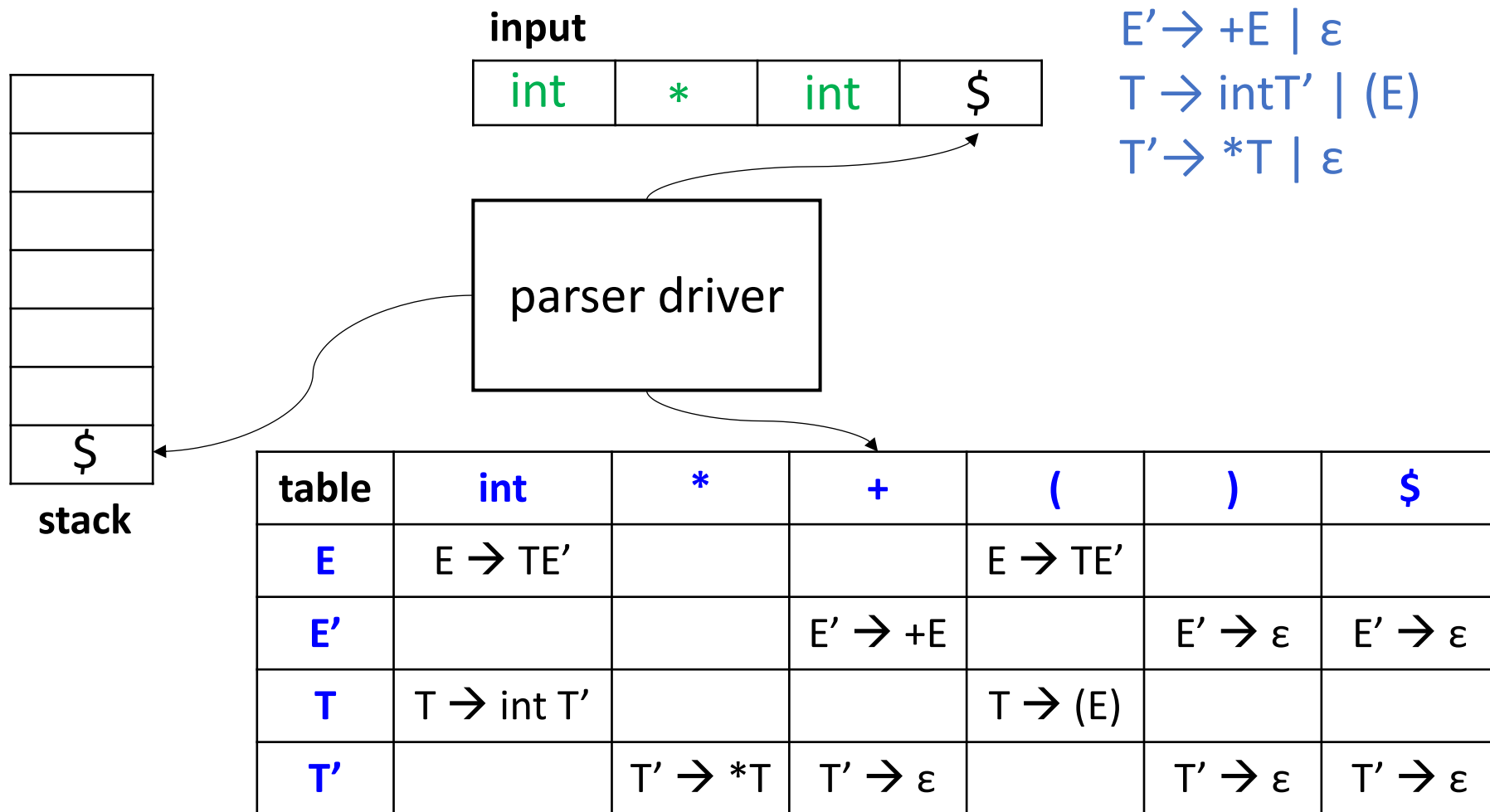
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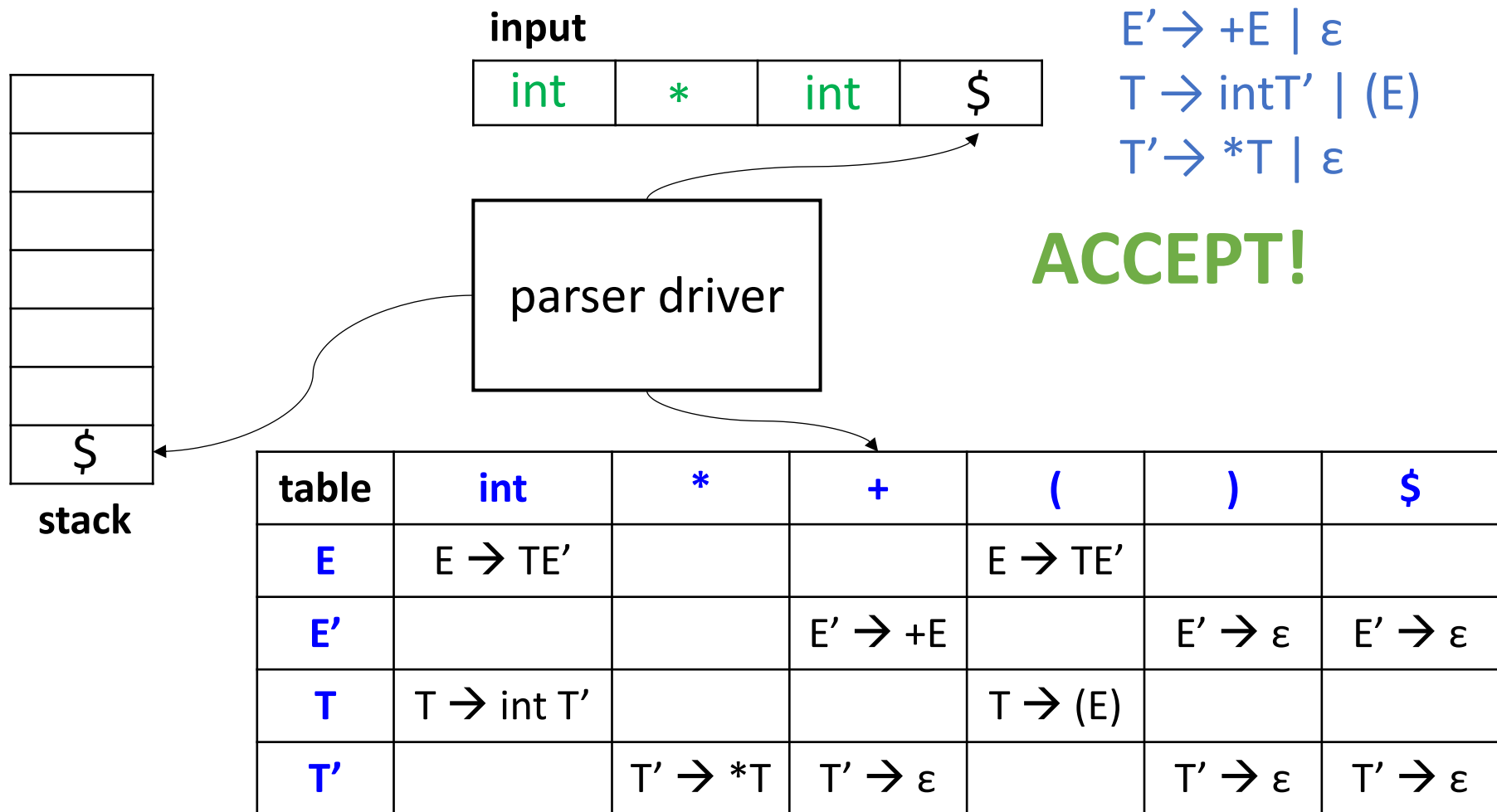
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Recognize Sequence[解析过程]

Matched	Stack (unmatched)	Input	Action
	E \$	int * int \$	$E \rightarrow TE'$
	T E' \$	int * int \$	$T \rightarrow \text{int } T'$
int	int T' E' \$	int * int \$	match
int	T' E' \$	* int \$	$T' \rightarrow *T$
int	* T E' \$	* int \$	match
int *	T E' \$	int \$	$T \rightarrow \text{int } T'$
int *	int T' E' \$	int \$	match
int * int	T' E' \$	\$	$T' \rightarrow \epsilon$
int * int	E' \$	\$	$E' \rightarrow \epsilon$
int * int	\$	\$	Halt-accept

$E \rightarrow TE'$

$E' \rightarrow +E \mid \epsilon$

$T \rightarrow \text{int } T' \mid (E)$

$T' \rightarrow *T \mid \epsilon$

Input: int * int

- 'Matched + Stack' constructs the sentential form[句型]
- Actions correspond to productions in leftmost derivation