

计算机学院(软件学院) SCHOOL OF COMPUTER SCIENCE AND ENGINEERING

Compilation Principle 编译原理

第17讲: 语义分析(3)

张献伟

xianweiz.github.io

DCS290, 4/20/2023





Review Questions

- Why context analysis is not performed in parsing stage?
 Parsing relies on CFG, which is context free.
- What is an synthesized attribute?
 Defined by attribute values of node N's children and N itself
- What's the usage of dependence graph?
 To decide the evaluation order of attributes.
- What is S-SDD?
 Synthesized-SDD, with only synthesized attributes.
- Is the SDD a L-SDD? $A \rightarrow X Y Z Y.i = f(Z.z, A.s)$ NO. Z is right to Y, A.s is synthesized attribute.
- S-SDD is suitable for bottom-up or top-down parsing?

 Bottom-up. Natural to evaluate the parent after seeing all children.





SDD vs. SDT

- SDD[语法制导定义]: 是CFG的推广,翻译的高层次规则说明
 - A CFG grammar together with attributes and semantic rules
 - A subset of them are also called attribute grammars[属性文法]
 - No side effects, i.e., rules are strictly local to each production
 - Semantic rules imply no order to attribute evaluation
- SDT[语法制导翻译方案]: SDD的补充,具体翻译实施方案
 - An executable specification of the SDD
 - Fragments of programs are attached to different points in the production rules
 - The order of execution is important

D -> T L
T -> int
T -> float
L ->
$$L_1$$
, id
 L_1

```
L.inh = T.type

T.type = int

T.type = float

L<sub>1</sub>.inh = L.inh

id.type = L.inh
```

D -> T { L.inh = T.type } L

T -> int { T.type = int }

T -> float { T.type = float }

L -> { L₁.inh = L.inh }L₁, id

L -> { id.type = L.inh} id

Syntax Directed Trans. Impl.[实现]

- Learnt how to specify translation: SDD and SDT[定义]
 - SDT is an executable specification of the SDD
 - CFG with <u>semantic actions</u> embedded in production bodies
- SDT can be implemented in two ways[具体实现]
 - Using a parse tree or AST[基于预先构建的分析树]
 - First build a parse tree, and then apply rules or actions at each node while traversing the tree
 - All SDDs (without cycles) and SDTs can be implemented
 - Since the tree can be traversed freely, implements any ordering
 - During parsing, without building a parse tree[语法分析过程中]
 - Apply rules or actions at each production while parsing
 - Only a subset of SDDs and SDTS can be implemented
 - Evaluation ordering restricted to parser derivation order





Syntax Directed Trans. Impl. (cont.)

- Typically, SDD (i.e., semantic analysis) is implemented during parsing[更为高效]
 - Allows compiler to skip parse tree generation
 - Saves time and memory

- Two important classes of SDD's[两个关键子类]
 - SDD is <u>S-attributed</u>, the underlying grammar is <u>LR-parsable</u>
 - SDD is <u>L-attributed</u>, the underlying grammar is <u>LL-parsable</u>
 - For both classes, semantic rules in an SDD can be converted into an SDT with actions that are executed at the right time[允许 SDD到SDT的转换]
 - During parsing, an action in a production body is executed as soon as all the grammar symbols to the left of the action have been matched





== Implement S-SDD ==

- Convert S-attributed SDD to SDT by[S-SDD->SDT的转换]
 - Placing each action at the end of the production[将每个语义动作都放在产生式的最后]
 - SDTs with all actions at the right ends of the production bodies are called postfix SDT's[后缀/尾部SDT]

S-SDD

Production Rules	Semantic Rules
(1) L -> E	print (E. <i>val</i>)
(2) $E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
(3) E -> T	E.val = T.val
(4) T -> $T_1 * F$	$T.val = T_1.val \times F.val$
(5) T -> F	T.val = F.val
(6) F -> (E)	F.val = E.val
(7) F -> digit	F.val = digit.lexval

SDT

(1) L -> E { print (E.val) } (2) E -> E₁ + T { E.val = E₁.val + T.val } (3) E -> T { E.val = T.val } (4) T -> T₁ * F { T.val = T₁.val x F.val } (5) T -> F { T.val = E.val } (6) F -> (E) { F.val = E.val } (7) F -> digit { F.val = digit.lexval }





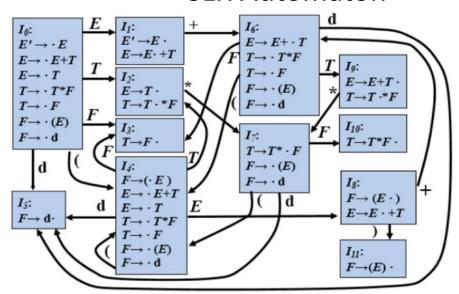
Implement S-SDD (cont.)

- If the underlying grammar of S-SDD is <u>LR parsable</u>
 - Then the SDT can be implemented during LR parsing
- Implement the converted SDT by[借助归约实现]
 - Executing the action along with the reduction of head <- body

SDT

(1) L -> E { print (E.val) } (2) E -> E₁ + T { E.val = E₁.val + T.val } (3) E -> T { E.val = T.val } (4) T -> T₁ * F { T.val = T₁.val x F.val } (5) T -> F { T.val = E.val } (6) F -> (E) { F.val = E.val } (7) F -> digit { F.val = digit.lexval }

SLR Automaton







Extend LR Parse Stack[扩展分析栈]

- Save synthesized attributes into the stack[栈中额外存放综合属性值]
 - Place the attributes along with the grammar symbols (or LR states that associated with these symbols) in records on stack
 - If there are multiple attributes
 - Make the records large enough or by putting pointers to records on the stack[栈记录足够大,或栈记录中存放指针]
- Example: A -> XYZ {action}
 - x, y, z are attributes of X, Y, Z respectively
 - After the action, A and its attributes are at the top (i.e., m-2)





Stack Manipulation[栈操作]

- Rewrite the actions to manipulate the parser stack[语义动作]
 - The manipulation can be done automatically by the parser

```
stack[top-2].symbol = A
stack[top-2].val = f( stack[top-2].val, stack[top-1].val, stack[top].val )
top = top -2
                                                                       A.a
          A \rightarrow XYZ \{ A.a = f(X.x, Y.y, Z.z) \}
                                                             X.x
       state \rightarrow S<sub>0</sub> ··· S<sub>m-2</sub> S<sub>m-1</sub> S<sub>m</sub>
                                                              state • S<sub>0</sub> ···
     symbol → $ ··· X Y Z
                                                            symbol • $ ····
    attribute \rightarrow - ... X.x Y.y Z.z
                                                                                  A.a
                                                          attribute → - ····
```





top

top

- Rewrite the actions to manipulate the parser stack
 - The manipulation can be done automatically by the parser

Productions	Semantic Rules	Semantic Actions
(1) L -> E	print (E. <i>val</i>)	{ print(stack[top].val); }
(2) E -> E ₁ +T	$E.val = E_1.val + T.val$	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }
(3) E -> T	E.val = T.val	
(4) T -> T ₁ *F	$T.val = T_1.val \times F.val$	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }
(5) T -> F	T.val = F.val	
(6) F -> (E)	F.val = E.val	{ stack[top-2].val = stack[top-1].val;
		top = top -2; }
(7) F -> digit	F.val = digit.lexval	





Productions	Semantic Actions	$\begin{bmatrix} I_{\theta} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{I_{\theta}} \begin{bmatrix} I_{\theta} : & E \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T $ $ \begin{bmatrix} E \to E \cdot + T \\ T \to \cdot T * F \end{bmatrix} $ $ T \to \cdot T * F $ $ T \to \cdot T *$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
	top = top -2; }	$F \rightarrow (F)$ F
(3) E -> T		$ F \rightarrow \cdot d $ $T \rightarrow F$.
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow \cdot d$ I_8 :
(5) T -> F		$\begin{vmatrix} I_5 \\ \vdots \end{vmatrix}$ d $E \rightarrow T$ E
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} \hline F \rightarrow d \cdot \\ \hline T \rightarrow \cdot T^*F \\ \hline T \rightarrow \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$ $F \rightarrow (E) \cdot$

Input: 3 * 5 + 4

```
state \rightarrow S_0 symbol \rightarrow $ attribute \rightarrow -
```





		d
Productions	Semantic Actions	$ \begin{vmatrix} I_{\theta} : & E' \to E \\ E' \to -E \end{vmatrix} \xrightarrow{E} \begin{vmatrix} I_{1} : & E' \to E \\ E \to E + \cdot T \end{vmatrix} $
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_0:} T $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T \cdot $ $*$ $F \rightarrow \cdot (E)$ $*$ $T \rightarrow T \cdot *F$ $T \rightarrow T \cdot *F$
	top = top -2; }	$F \rightarrow \cdot (F)$ $F \rightarrow F$
(3) E -> T		$ F \rightarrow \cdot d $ $T \rightarrow F$.
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow (\cdot E)$ $E \rightarrow \cdot E + T$ $F \rightarrow \cdot d$ $I_8:$ $F \rightarrow (F_+)$
(5) T -> F		$\begin{bmatrix} I_5: \\ F \end{bmatrix} \qquad \begin{bmatrix} I_5: \\ I_5: \end{bmatrix} \qquad \begin{bmatrix} I_5: \\ I_$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} \hline F \rightarrow d \cdot \\ \hline T \rightarrow \cdot T * F \\ \hline T \rightarrow \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

```
state \rightarrow S_0 symbol \rightarrow $
```

attribute → -





		, d
Productions	Semantic Actions	$ \begin{vmatrix} I_{\theta} : \\ E' \to \cdot E \end{vmatrix} \xrightarrow{E} \begin{vmatrix} I_{1} : \\ E' \to E \cdot \\ E \to E + \cdot T \end{vmatrix} \xrightarrow{\mathbf{I}_{\theta}} $
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} $ $ T \longrightarrow T * F $ $ T \longrightarrow T T $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$ \begin{vmatrix} E \to T \\ T \to T^*F \\ T \to F \end{vmatrix} $
	top = top -2; }	$F \rightarrow (F)$ F
(3) E -> T		$F \rightarrow d$ $T \rightarrow F$. $T \rightarrow T \rightarrow F$.
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow (\cdot E)$ $F \rightarrow \cdot d$ $I_g:$
(5) T -> F		I_5 : d $E \rightarrow T$ E $I_{E \rightarrow E + T}$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} F \to d \cdot \\ \hline T \to \cdot T^*F \\ \hline T \to \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₅ symbol \rightarrow \$ d attribute \rightarrow - 3





		d
Productions	Semantic Actions	$\begin{bmatrix} I_{\theta} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\theta}} \begin{bmatrix} I_{\theta} : & + \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to E + T \\ E \to T \end{bmatrix} $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T \to T \to T \to T $ $ T \to T \to T \to T$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }	$ \begin{array}{c c} T \to \cdot T^*F \\ T \to \cdot F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ T \to T \cdot *F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} F \to E + T \cdot \\ T \to T \cdot *F \end{array} $
(3) E -> T		$ F \rightarrow d \nearrow I_{7}$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }	$ \begin{array}{c c} \hline d & (F) \\ \hline I_{f:} \\ F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} \hline I_{g:} \\ \hline I_{g:} \end{array} $
(5) T -> F		I_{5} : d $\begin{vmatrix} E \rightarrow E + T \\ E \rightarrow T \end{vmatrix}$ E] (d $\begin{vmatrix} F \rightarrow (E \cdot) \\ F \rightarrow F \rightarrow T \end{vmatrix}$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val; top = top -2; }	$ \begin{array}{c c} & T \to T^*F \\ & T \to F \\ & F \to \cdot (E) \end{array} $
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀
symbol \rightarrow \$
attribute \rightarrow - 3





		d
Productions	Semantic Actions	$\begin{bmatrix} I_{\theta} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\theta}} \begin{bmatrix} I_{\theta} : & + \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to E + T \\ E \to T \end{bmatrix} $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T \to T \to T \to T $ $ T \to T \to T \to T$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }	$ \begin{array}{c c} T \to \cdot T^*F \\ T \to \cdot F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ T \to T \cdot *F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} F \to E + T \cdot \\ T \to T \cdot *F \end{array} $
(3) E -> T		$ F \rightarrow d \nearrow I_{7}$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }	$ \begin{array}{c c} \hline d & (F) \\ \hline I_{f:} \\ F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} \hline I_{g:} \\ \hline I_{g:} \end{array} $
(5) T -> F		I_{5} : d $\begin{vmatrix} E \rightarrow E + T \\ E \rightarrow T \end{vmatrix}$ E] (d $\begin{vmatrix} F \rightarrow (E \cdot) \\ F \rightarrow F \rightarrow T \end{vmatrix}$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val; top = top -2; }	$ \begin{array}{c c} & T \to T^*F \\ & T \to F \\ & F \to \cdot (E) \end{array} $
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₃ symbol \rightarrow F attribute \rightarrow - 3





		d
Productions	Semantic Actions	$\begin{bmatrix} I_{\theta} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\theta}} \begin{bmatrix} I_{\theta} : & + \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to E + T \\ E \to T \end{bmatrix} $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T \to T \to T \to T $ $ T \to T \to T \to T$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }	$ \begin{array}{c c} T \to \cdot T^*F \\ T \to \cdot F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ T \to T \cdot *F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} F \to E + T \cdot \\ T \to T \cdot *F \end{array} $
(3) E -> T		$ F \rightarrow d \nearrow I_{7}$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }	$ \begin{array}{c c} \hline d & (F) \\ \hline I_{f:} \\ F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} \hline I_{g:} \\ \hline I_{g:} \end{array} $
(5) T -> F		I_{5} : d $\begin{vmatrix} E \rightarrow E + T \\ E \rightarrow T \end{vmatrix}$ E] (d $\begin{vmatrix} F \rightarrow (E \cdot) \\ F \rightarrow F \rightarrow T \end{vmatrix}$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val; top = top -2; }	$ \begin{array}{c c} & T \to T^*F \\ & T \to F \\ & F \to \cdot (E) \end{array} $
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀
symbol \rightarrow \$
attribute \rightarrow - 3





		d
Productions	Semantic Actions	$\begin{bmatrix} I_{\theta} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\theta}} \begin{bmatrix} I_{\theta} : & + \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to E + T \\ E \to T \end{bmatrix} $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T * F $ $ T \to T \to T * F $ $ T \to T \to T \to T \to T $ $ T \to T \to T \to T$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }	$ \begin{array}{c c} T \to \cdot T^*F \\ T \to \cdot F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ T \to T \cdot *F \end{array} $ $ \begin{array}{c c} F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} F \to E + T \cdot \\ T \to T \cdot *F \end{array} $
(3) E -> T		$ F \rightarrow d \nearrow I_{7}$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }	$ \begin{array}{c c} \hline d & (F) \\ \hline I_{f:} \\ F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ \begin{array}{c c} \hline I_{g:} \\ \hline I_{g:} \end{array} $
(5) T -> F		I_{5} : d $\begin{vmatrix} E \rightarrow E + T \\ E \rightarrow T \end{vmatrix}$ E] (d $\begin{vmatrix} F \rightarrow (E \cdot) \\ F \rightarrow F \rightarrow T \end{vmatrix}$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val; top = top -2; }	$ \begin{array}{c c} & T \to T^*F \\ & T \to F \\ & F \to \cdot (E) \end{array} $
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₂ symbol \rightarrow \$ T attribute \rightarrow - 3





		F - d
Productions	Semantic Actions	$\begin{array}{c c} I_{\theta}: & E \\ E' \to \cdot E \end{array} \xrightarrow[E' \to E^{-}]{}^{+} \begin{array}{c} I_{\theta}: \\ E \to E^{+} \cdot T \end{array}$
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_0:} T $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T \cdot \qquad *$ $E \rightarrow E + T \cdot \qquad *$ $T \rightarrow T \cdot *F$
	top = top -2; }	$F \rightarrow (F)$ F
(3) E -> T		$F \rightarrow d$ I_7 : I_7 : I_7 : I_7 :
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$d \left(\begin{array}{c} I_{I_f} \\ I_{f} \end{array} \right) \left(\begin{array}{c} I_{F \to \cdot (E)} \\ I_{F \to \cdot (E)} \end{array} \right)$
	top = top -2; }	$F \rightarrow (\cdot E) \qquad F \rightarrow \cdot d \qquad I_g: \qquad$
(5) T -> F		I_5 : d $E \rightarrow T$ E $I_{E \rightarrow E + T}$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} \hline F \rightarrow d \cdot \\ \hline T \rightarrow \cdot T * F \\ \hline T \rightarrow \cdot F \end{array} $
	top = top -2; }	$ \left(\begin{array}{c} F \to \cdot (E) \\ F \to \cdot \mathbf{d} \end{array} \right) $ I_{II} :
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$

Input: 3 * 5 + 4

state
$$\rightarrow$$
 S₀ S₂ symbol \rightarrow \$ T attribute \rightarrow - 3





		,d
Productions	Semantic Actions	$ \begin{vmatrix} I_{\theta} : \\ E' \to \cdot E \end{vmatrix} \xrightarrow{E} \begin{vmatrix} I_{1} : \\ E' \to E \cdot \\ E \to E + \cdot T \end{vmatrix} \xrightarrow{\mathbf{I}_{\theta}} $
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_g:} T \xrightarrow{F} T \xrightarrow{F} T$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
(3) E -> T	top = top -2; }	$F \rightarrow \cdot (E)$ F I_3 :
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{c c} & & & & & & & & & & & & & & & & & & &$
	top = top -2; }	$F \rightarrow (\cdot E)$ $F \rightarrow \cdot d$ I_g :
(5) T -> F		I_5 : d $E \to E + I$ E) d $E \to E + I$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} F \to d \cdot \\ \hline T \to \cdot T^*F \\ T \to \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₂ symbol \rightarrow \$ T attribute \rightarrow - 3





		d
Productions	Semantic Actions	$\begin{bmatrix} I_{\emptyset} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\emptyset} : E \to E + \cdot T} $
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_0:} T $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T \cdot $ $*$ $E \rightarrow E + T \cdot $ $T \rightarrow T \cdot *F$ $*$ $T \rightarrow T \cdot *F$
	top = top -2; }	$F \rightarrow \cdot (F)$ F
(3) E -> T		$ F \rightarrow \cdot d \nearrow I_{7}: \nearrow F I_{7}: \nearrow F I_{7}: \nearrow F I_{7}: \nearrow F I_{7}: F $
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \to (\cdot E)$ $F \to \cdot d$ $I_{\mathcal{S}}$
(5) T -> F		$\begin{bmatrix} I_5: \\ T \end{bmatrix}$ d $E \rightarrow T$ E
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} \hline F \rightarrow d \\ \hline T \rightarrow \cdot T^*F \\ \hline T \rightarrow \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$

state
$$\rightarrow$$
 S₀ S₂ S₇ symbol \rightarrow \$ T * attribute \rightarrow - 3 -





		d
Productions	Semantic Actions	$\begin{vmatrix} I_{\theta} : & E \\ E' \to E \end{vmatrix} \xrightarrow{I_1} \begin{vmatrix} E' \to E \\ E' \to E \end{vmatrix} \xrightarrow{I_2} \begin{vmatrix} E \\ E \to E + \cdot T \end{vmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T $ $ \begin{bmatrix} E \to E \cdot + T \\ T \to \cdot T * F \end{bmatrix} $ $ T \to \cdot T * F $ $ T \to \cdot T *$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
(3) E -> T		$F \rightarrow \cdot (E)$ $F \rightarrow \cdot d$ $I_{3:}$ $T \rightarrow F$ $I_{10:}$ $T \rightarrow T^{*}F$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }	$ \begin{array}{c c} \hline d & (F) \\ \hline I_{f}: \\ F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ I_{g}: $
(5) T -> F		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} \hline F \rightarrow d \cdot \\ \hline T \rightarrow \cdot T * F \\ \hline T \rightarrow \cdot F \end{array} $
	top = top -2; }	$\left(\begin{array}{c} F \rightarrow \cdot (E) \\ F \rightarrow \cdot \mathbf{d} \end{array}\right) \qquad \qquad \left[I_{II} : \right]$
(7) F -> digit		$F \rightarrow c d$ $F \rightarrow (E) \cdot$

Input: 3 * 5 + 4

state
$$\rightarrow$$
 S₀ S₂ S₇ symbol \rightarrow \$ T * attribute \rightarrow - 3 -





		, F , d
Productions	Semantic Actions	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} $ $ T \longrightarrow T * F $ $ T \longrightarrow T T \longrightarrow T * F $ $ T \longrightarrow T \longrightarrow$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow \cdot (F)$ F
(3) E -> T		$F \rightarrow \cdot d$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	I = I = I = I = I = I = I = I = I = I =
	top = top -2; }	
(5) T -> F		$ I_{\mathcal{E}} $ d $ E \rightarrow T $ $ E $ $ E $ $ E \rightarrow E + T $
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$F \to d \cdot \qquad T \to F $ $T \to \cdot F $ $T \to \cdot F$
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₂ S₇ symbol \rightarrow \$ T * attribute \rightarrow - 3 -





	-	
Productions	Semantic Actions	$\begin{vmatrix} I_{\theta} : & E' \to E \\ E' \to \cdot E \end{vmatrix} \xrightarrow{E} \begin{vmatrix} I_{1} : & F' \to E \\ E' \to E \end{vmatrix} \xrightarrow{I_{\theta}} \begin{vmatrix} I_{\theta} : & F' \to E \\ E \to E + \cdot T \end{vmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} $ $ T \longrightarrow T^*F $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
45.5	top = top -2; }	$F \rightarrow (E)$ $F \downarrow I_{3}$:
(3) E -> T		$ F \rightarrow \cdot \mathbf{d} \nearrow T \rightarrow F.$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow (\cdot E)$ $E \rightarrow \cdot E + T$ $F \rightarrow \cdot d$ $I_{\mathcal{E}}$ $F \rightarrow (F, \cdot)$
(5) T -> F		I_5 : d $\begin{vmatrix} E \rightarrow E + I \\ E \rightarrow T \end{vmatrix}$ E I
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} F \to d \\ \hline \end{array} $ $ \begin{array}{c c} T \to T^*F \\ \hline \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₂ S₇ S₅ symbol \rightarrow \$ T * d attribute \rightarrow - 3 - 5





		, F , d
Productions	Semantic Actions	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} $ $ T \longrightarrow T * F $ $ T \longrightarrow T T \longrightarrow T * F $ $ T \longrightarrow T \longrightarrow$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow \cdot (F)$ F
(3) E -> T		$F \rightarrow \cdot d$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	I = I = I = I = I = I = I = I = I = I =
	top = top -2; }	
(5) T -> F		$ I_{\mathcal{E}} $ d $ E \rightarrow T $ $ E $ $ E $ $ E \rightarrow E + T $
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$F \to d \cdot \qquad T \to F $ $T \to \cdot F $ $T \to \cdot F$
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$ $F \rightarrow (E) \cdot$

state
$$\rightarrow$$
 S₀ S₂ S₇ symbol \rightarrow \$ T * attribute \rightarrow - 3 -





		d
Productions	Semantic Actions	$\begin{bmatrix} I_{\emptyset} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\emptyset} : E \to E + \cdot T} $
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_0:} T $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T \cdot $ $*$ $E \rightarrow E + T \cdot $ $T \rightarrow T \cdot *F$ $*$ $T \rightarrow T \cdot *F$
	top = top -2; }	$F \rightarrow \cdot (F)$ F
(3) E -> T		$ F \rightarrow \cdot d \nearrow I_{7}: \nearrow F I_{7}: \nearrow F I_{7}: \nearrow F I_{7}: \nearrow F I_{7}: F $
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \to (\cdot E)$ $F \to \cdot d$ $I_{\mathcal{S}}$
(5) T -> F		$\begin{bmatrix} I_5: \\ T \end{bmatrix}$ d $E \rightarrow T$ E
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} \hline F \rightarrow d \\ \hline T \rightarrow \cdot T^*F \\ \hline T \rightarrow \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$

state
$$\rightarrow$$
 S₀ S₂ S₇ S₁₀ symbol \rightarrow \$ T * F attribute \rightarrow - 3 - 5





		,d
Productions	Semantic Actions	$\begin{bmatrix} I_{0}: & & E \\ E' \to E \end{bmatrix} \xrightarrow{E} \xrightarrow{I_{1}: & + \\ E' \to E} \xrightarrow{I_{0}: & + \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_g:} T $
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top -2; }	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
(3) E -> T		$ F \rightarrow \cdot d \nearrow T \rightarrow F \nearrow F \rightarrow T \rightarrow T \rightarrow F $
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top -2; }	$ \begin{array}{c c} \hline d & (F) \\ \hline I_{f:} \\ F \to \cdot (E) \\ F \to \cdot d \end{array} $ $ I_{g:}$
(5) T -> F		$\begin{bmatrix} I_5 : & & \\ & E \to \cdot T & \\ & & \end{bmatrix} (d \begin{bmatrix} F \to (E \cdot) \\ & F \to F \cdot + T \end{bmatrix})$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} F \to \mathbf{d} & & \\ \hline T \to T^*F \\ \hline T \to F \end{array} $
	top = top -2; }	$\begin{bmatrix} F \rightarrow \cdot (E) \\ F \rightarrow \cdot \mathbf{d} \end{bmatrix}$
(7) F -> digit		$F \rightarrow c d$ $F \rightarrow (E) \cdot$





		F - d
Productions	Semantic Actions	$\begin{bmatrix} I_{\theta} : & E' \to E \\ E' \to E \end{bmatrix} \xrightarrow{E} \begin{bmatrix} I_{1} : & + \\ E' \to E \end{bmatrix} \xrightarrow{I_{\theta} : E} \begin{bmatrix} I_{\theta} : & + \\ E \to E + \cdot T \end{bmatrix}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T $ $ \begin{bmatrix} E \to E \cdot + T \\ T \to \cdot T * F \end{bmatrix} $ $ T \to \cdot T * F $ $ T \to \cdot T *$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T$ $*$ $T \rightarrow T^*F$ $*$ $T \rightarrow T^*F$ $*$ $T \rightarrow T^*F$
(2) F . T	top = top -2; }	$F \rightarrow \cdot (E)$ F I_{10} :
(3) E -> T		$T \rightarrow T \rightarrow$
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{c c} \hline d & (& F & \hline \\ \hline & I_f & \hline \\ \hline \end{array} $
	top = top -2; }	$F \rightarrow (\cdot E)$ $F \rightarrow \cdot d$ I_8 :
(5) T -> F		I_5 : d $E \to E + I$ E] (d $F \to (E \cdot)$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} F \to d \cdot \\ \hline T \to \cdot T^*F \\ T \to \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$





		d
Productions	Semantic Actions	$\begin{vmatrix} I_{\theta} : & E \\ E' \to \cdot E \end{vmatrix} \xrightarrow{E} \begin{vmatrix} I_{1} : & + \\ E' \to E \cdot & E \end{vmatrix} \xrightarrow{I_{\theta}} \begin{vmatrix} I_{\theta} : & E \\ E \to E + \cdot T \end{vmatrix}$
(1) L -> E	{ print(stack[top].val); }	$\begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} T \xrightarrow{E \to E \cdot + T} \begin{bmatrix} F & T \to \cdot T^*F \\ T \to \cdot F \end{bmatrix} \xrightarrow{I_0:} T \xrightarrow{F} T \xrightarrow{F} T$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T$ $E \rightarrow T$ $T \rightarrow T^*F$ $T \rightarrow T^*F$ $T \rightarrow T^*F$
40	top = top -2; }	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
(3) E -> T	L	$ F \rightarrow \cdot G $ $T \rightarrow F$. $ F $ $ F $
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	top = top -2; }	$F \rightarrow \cdot $
(5) T -> F		$ I_5:$ d $ E_{\rightarrow T} E$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$F \to d \cdot \qquad T \to T^*F$ $T \to F$ $T \to F$
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$





Productions	Semantic Actions	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
(1) L -> E	{ print(stack[top].val); }	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T \cdot $ $*$ $T \rightarrow T^*F$ $*$ $T \rightarrow T^*F$ $*$
40	top = top -2; }	$F \rightarrow (F)$ F
(3) E -> T		$ F \rightarrow \cdot 0 $ $ T \rightarrow F \cdot F $ $ T \rightarrow T * F \cdot F $
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$\boxed{\boxed{\begin{matrix} I_{I:} \end{matrix}} \boxed{\begin{matrix} I_{I:} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \end{matrix}} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \end{matrix}} \end{matrix}} \boxed{\begin{matrix} I_{J:} \end{matrix}} \end{matrix}}$
	top = top -2; }	$F \rightarrow \cdot \cdot \cdot E$
(5) T -> F		$ I_5:$ d $ E \rightarrow E + I \mid E$] (d $ F \rightarrow (E \cdot) \mid E \mid E \mid E \mid E$
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$ \begin{array}{c c} F \to d \cdot \\ \hline T \to \cdot T^*F \\ T \to \cdot F \end{array} $
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot d$ $F \rightarrow (E) \cdot$





4		F G d
Productions	Semantic Actions	$\begin{bmatrix} I_0 : & & E \\ E' \to \cdot E & & E' \to E \cdot \end{bmatrix} \xrightarrow{I_1 : E \to E + \cdot T} \xrightarrow{I_2 : E \to E + \cdot T}$
(1) L -> E	{ print(stack[top].val); }	$ \begin{bmatrix} E \to \cdot E + T \\ E \to \cdot T \end{bmatrix} $ $ T \to T * F $ $ T \to T = T \to T * F $ $ T \to T \to$
(2) E -> E ₁ +T	{ stack[top-2].val = stack[top-2].val + stack[top].val;	$T \rightarrow T^*F$ $E \rightarrow T \cdot $ $*$ $E \rightarrow E + T \cdot $ $T \rightarrow T \cdot F$
	top = top -2; }	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
(3) E -> T	L	$ F \rightarrow \cdot \mathbf{d} \nearrow T \rightarrow F$. $ F \mid I^{7/2}$. $ F \rightarrow T + F$.
(4) T -> T ₁ *F	{ stack[top-2].val = stack[top-2].val x stack[top].val;	$ \begin{array}{c c} & & & & & & & & & & & & & & & & & & &$
1 /	top = top -2; }	$F \rightarrow \cdot d$ I_8 :
(5) T -> F		$ I_{\mathcal{S}}:$ $ \mathbf{d} _{E \to T} E $ $ \mathbf{d} _{E \to E \to T} E $
(6) F -> (E)	{ stack[top-2].val = stack[top-1].val;	$F \to d \cdot \qquad T \to F $ $T \to F \cdot F \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to E \to F \cdot + I \cdot \qquad D \to E \to$
	top = top -2; }	
(7) F -> digit		$F \rightarrow \cdot \mathbf{d}$ $F \rightarrow (E) \cdot$





== Implement L-SDD ==

- We have examined S-SDD -> SDT -> implementation
 - S-SDD can be converted to SDT with actions at production end
 - The SDT can be parsed and translated <u>bottom-up</u>, as long as the underlying grammar is LR-parsable
- What about the more-general **L-attributed SDD**?[L-属性文法]
 - Rules for turning L-SDD into an SDT
 - Embed the semantic rule that computes the inherited attributes for a nonterminal A immediately before that occurrence of A in the production body

[将计算某个非终结符A的继承属性的语义规则插入到产生式右部中<u>紧靠在A的本次出现</u> 之前的位置上] 综合属性呢??? 综合属性在A→xxx那个产生式处理!

 Place the rules that compute a synthesized attribute for the head of a production at the end of the body of that production

[将计算一个产生式左部符号的综合属性的规则放在这个产生式右部的末尾]





A -> B,C

- C的继承属性: 出现之前

- A的综合属性: 末尾

Production Rules	Semantic Rules
(1) T -> F T'	T'.inh = F.val
	T.val = T'.syn
(2) T' -> * $F T_1'$	T_1 '.inh = T '.inh x F.val
	$T'.syn = T_1'.syn$
(3) T' -> ε • ·	T'.syn = T'.inh
(4) F -> digit ←	

SDT

(1)
$$T \rightarrow F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}$$

(2)
$$T' -> * F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}$$

- (3) $T' -> \varepsilon \{ T'.syn = T'.inh \}$
- (4) F -> digit { F.val = digit.lexval }





Implement the SDT of L-SDD

• If the underlying grammar is <u>LL-parsable</u>, then the SDT can be implemented during <u>LL or LR parsing</u>[若文法是LL可解析的,则可在LL或LR语法分析过程中实现]

- Semantic translation during **LL parsing**, using[LL方式]
 - A recursive-descent parser[LL递归下降]
 - Augment non-terminal functions to both parse and handle attributes
 - A predictive parser[LL非递归的预测分析]
 - Extend the parse stack to hold actions and certain data items needed for attribute evaluation
- A LR parser[LR方式]
 - Involve marker to rewrite grammars





L-SDD in LL Parsing[非递归预测]

- Extend the parse stack to hold **actions** and certain **data items** needed for attribute evaluation[扩展语法分析栈]
 - Action-record[动作记录]: represent the actions to be executed
 - Synthesize-record[综合记录]: hold synthesized attributes for non-terminals
 - Typically, the data items are copies of attributes[属性备份]
- Manage attributes on the stack[管理属性信息]
 - The inherited attributes of a nonterminal A are placed in the stack record that represents that terminal[符号位放继承属性]
 - Action-record to evaluate these attributes are immediately <u>above</u> A
 - The synthesized attributes of a nonterminal A are placed in a separate synthesize-record that is immediately below A[综合属

性另存放]

A Inh Attr.

A.syn Syn Attr.





L-SDD in LL Parsing (cont.)

- Table-driven LL-parser
 - Mimics a leftmost derivation --> stack expansion
- A -> BC, suppose nonterminal C has an inherited attr C.i
 - C.i may depend not only on the inherited attr. of A, but on all the attrs of B
 - Extra care should be taken on the attribute values
 - Since SDD is L-attributed, surely that the values of the inherited attrs of A are available when A rises to stack top $(X \rightarrow \alpha A\beta)$
 - Thus, available to be copied into C
 - A's synthesized attrs remain on the stack, below B and C when expansion happens

action	Code
Α	Inh Attr.
A.syn	Syn Attr.





L-SDD in LL Parsing (cont.)

- A -> BC: C.i may depend not only on the inherited attr. of A, but on all the attrs of B
 - Thus, need to process B completely before C.i can be evaluated
 - Save temporary copies of all attrs needed by evaluate C.i in the action-record that evaluates C.i; otherwise, when the parser replaces A on top of the stack by BC, the inherited attrs of A will be gone, along with its stack record
 - <u>变量展开</u>时 (i.e., <u>变量本身的记录出栈</u>时),若其含有<u>继承属性</u>,则要将继承属性<u>复制</u>给后面的动作记录
 - <u>综合记录出栈</u>时,要将<u>综合属性值复制</u>给后面的动作记录

action	Code
Α	Inh Attr.
A.syn	Syn Attr.





Example

(1)
$$T \rightarrow F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}$$

(2)
$$T' \rightarrow F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}$$

- (3) $T' -> \varepsilon \{ T'.syn = T'.inh \}$
- (4) F -> digit { F.val = digit.lexval }

Three kinds of symbols:

- 1) terminal
- 2) non-terminal
- 3) action



$$\begin{array}{ll} (1) \ T -> F \left\{ \, a_{1} \, \right\} \ T' \left\{ \, a_{2} \, \right\} \\ (2) \ T' -> * F \left\{ \, a_{3} \, \right\} \ T_{1}' \left\{ \, a_{4} \, \right\} \\ (3) \ T' -> \epsilon \left\{ \, a_{5} \, \right\} \\ (4) \ F -> \ digit \left\{ \, a_{6} \, \right\} \\ \end{array} \quad \begin{array}{ll} a_{1} : \ T'.inh = F.val \\ a_{2} : \ T.val = T'.syn \\ a_{3} : \ T_{1}'.inh = T'.inh \times F.val \\ a_{4} : \ T'.syn = T_{1}'.syn \\ a_{5} : \ T'.syn = T'.inh \\ a_{6} : \ F.val = \ digit.lexval \\ \end{array}$$





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow \epsilon \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

- o <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录





```
(1) T -> F { a_1 } T' { a_2 } a_1: T'.inh = F.val a_2: T.val = T'.syn a_3: T<sub>1</sub>'.inh = T'.inh x F.val a_4: T'.syn = T<sub>1</sub>'.syn a_4: T'.syn = T<sub>1</sub>'.syn a_5: T'.syn = T'.inh a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

- o 变量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

Т	Tsyn	\$
	val	





```
(1) T -> F { a_1 } T' { a_2 } a_1: T'.inh = F.val a_2: T.val = T'.syn a_3: T<sub>1</sub>'.inh = T'.inh x F.val a_4: T'.syn = T<sub>1</sub>'.syn a_4: T'.syn = T<sub>1</sub>'.syn a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

- 。 <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录







```
(1) T -> F { a_1 } T' { a_2 } a_1: T'.inh = F.val a_2: T.val = T'.syn a_3: T'.inh = T'.inh x F.val a_3: T'.syn = T'.inh x F.val a_4: T'.syn = T'.syn a_4: T'.syn = T'.inh a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

- o 变量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

F	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
	val		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

- o 变量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
val		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

- o 变量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录
- 综合记录出栈时,要将 综合属性值复制给后面 的动作记录

digit	{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
lexv=3		val		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code		
Α	Inh Attr.		
A.syn	Syn Attr.		

Input: 3 * 5

Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

- <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

digit	{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
lexv=3		val		inh	val		val	





(1) T -> F {
$$a_1$$
 } T' { a_2 } a_1 : T'.inh = F.val a_2 : T.val = T'.syn a_3 : T₁'.inh = T'.inh x F.val a_4 : T'.syn = T₁'.syn a_4 : T'.syn = T₁'.syn a_5 : T'.syn = T'.inh a_6 : F.val = digit.lexval

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

- <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

lexv=3 d_lexv=3 val inh val val	C	digit	{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
	le	exv=3	d_lexv=3	val		inh	val		val	





```
(1) T -> F { a_1 } T' { a_2 } a_1: T'.inh = F.val a_2: T.val = T'.syn a_3: T<sub>1</sub>'.inh = T'.inh x F.val a_4: T'.syn = T<sub>1</sub>'.syn a_4: T'.syn = T<sub>1</sub>'.syn a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

- 。 <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
d_lexv=3	val		inh	val		val	





(1)
$$T \rightarrow F \{a_1\} T' \{a_2\}$$
 $a_1: T'.inh = F.val$ $a_2: T.val = T'.syn$ (2) $T' \rightarrow F \{a_3\} T_1' \{a_4\}$ $a_3: T_1'.inh = T'.inh \times F.val$ $a_4: T'.syn = T_1'.syn$ (3) $T' \rightarrow E \{a_5\}$ $a_5: T'.syn = T'.inh$ $a_6: F.val = digit.lexval$

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

。 <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录

。 <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录 Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
d_lexv=3	val		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

- 。 <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录
- o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录

Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
d_lexv=3	val		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

交量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录

o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录 Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

a₆: stack[top-1].*val* = stack[top].*d_lexval*

{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
d_lexv=3	val		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

o 变量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录

o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录 Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

a₆: stack[top-1].val = stack[top].d_lexval

{ a ₆ }	Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
d_lexv=3	val =3		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

o <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录

o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录 Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

a₆: stack[top-1].val = stack[top].d_lexval

Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
val =3		inh	val		val	





```
(1) T \rightarrow F \{a_1\} T' \{a_2\} a_1: T'.inh = F.val a_2: T.val = T'.syn (2) T' \rightarrow F \{a_3\} T_1' \{a_4\} a_3: T_1'.inh = T'.inh \times F.val a_4: T'.syn = T_1'.syn (3) T' \rightarrow E \{a_5\} a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code
Α	Inh Attr.
A.syn	Syn Attr.

Input: 3 * 5

 变量展开时(i.e., 变量 本身的记录出栈时), 若其含有继承属性,则 要将继承属性复制给后 面的动作记录

o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录 Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

a₆: stack[top-1].val = stack[top].d_lexval

Fsyn	{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
val =3	val=3	inh	val		val	
	4		·	•		•





```
(1) T -> F { a_1 } T' { a_2 } a_1: T'.inh = F.val a_2: T.val = T'.syn a_3: T<sub>1</sub>'.inh = T'.inh x F.val a_4: T'.syn = T<sub>1</sub>'.syn a_4: T'.syn = T<sub>1</sub>'.syn a_5: T'.syn = T'.inh a_6: F.val = digit.lexval
```

action	Code	
Α	Inh Attr.	
A.syn	Syn Attr.	

Input: 3 * 5

o <u>变量展开</u>时(i.e., <u>变量</u> <u>本身的记录出栈</u>时), 若其含有<u>继承属性</u>,则 要将继承属性<u>复制</u>给后 面的动作记录

o <u>综合记录出栈</u>时,要将 <u>综合属性值复制</u>给后面 的动作记录 Stack top 'digit' matches the input '3' - pop 'digit', but value copy is needed

a₆: stack[top-1].val = stack[top].d_lexval

{ a ₁ }	T'	T'syn	{ a ₂ }	Tsyn	\$
val=3	inh	val		val	





L-SDD in LR Parsing[LR解析]

- What we already learnt
 - LR > LL, w.r.t parsing power
 - We can do bottom-up every translation that we can do top-down[所有的 LL都可以LR]
 - S-attributed SDD can be implemented in bottom-up way
 - All semantic actions are at the end of productions, i.e., triggered in reduce
- For L-attributed SDD on an LL grammar, can it be implemented during bottom-up parsing?
 - Problem: semantic actions can be in anywhere of the production body

```
(1) T \to F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \to F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \to \varepsilon \{ T'.syn = T'.inh \}

(4) F \to \text{digit } \{ F.val = \text{digit.} lexval \}
```





LALR(1

- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh

```
(1) T \to F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \to F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \to \epsilon \{ T'.syn = T'.inh \}

(4) F \to \text{digit} \{ F.val = \text{digit}.lexval \}
```





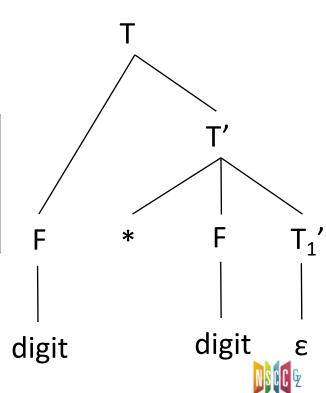
- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh

```
(1) T \to F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \to F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

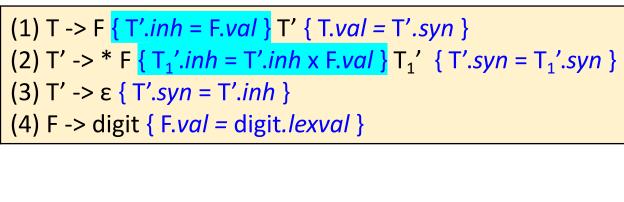
(3) T' \to \varepsilon \{ T'.syn = T'.inh \}

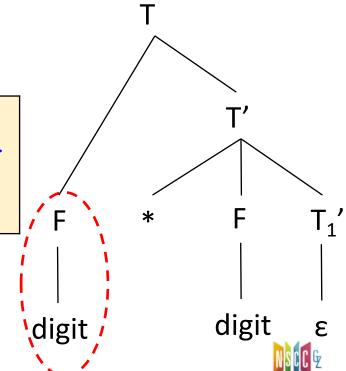
(4) F \to \text{digit} \{ F.val = \text{digit}.lexval \}
```





- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh







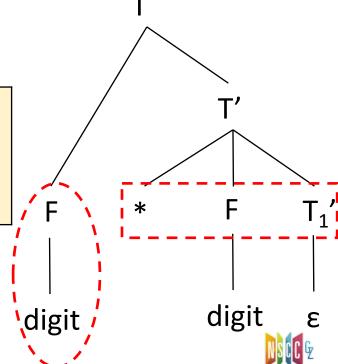
- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh

```
(1) T \rightarrow F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \rightarrow F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \rightarrow \varepsilon \{ T'.syn = T'.inh \}

(4) F \rightarrow \text{digit} \{ F.val = \text{digit}.lexval \}
```





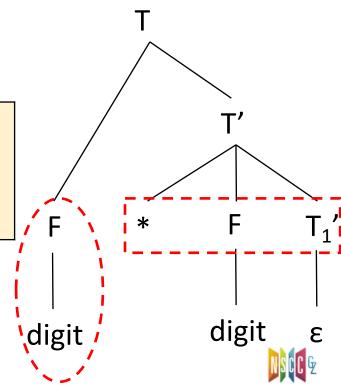
- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh

```
(1) T \to F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \to F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \to \varepsilon \{ T'.syn = T'.inh \}

(4) F \to \text{digit } \{ F.val = \text{digit.} lexval \}
```





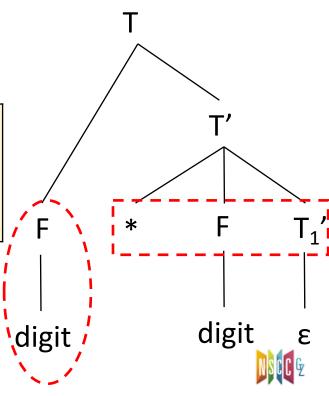
- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh
- Claim: inherited attributes are on the stack
 - Left attributes guarantee they've already been computed
 - But computed by previous productions deep in the stack

```
(1) T \rightarrow F \{T'.inh = F.val\} T' \{T.val = T'.syn\}

(2) T' \rightarrow F \{T_1'.inh = T'.inh \times F.val\} T_1' \{T'.syn = T_1'.syn\}

(3) T' \rightarrow \varepsilon \{T'.syn = T'.inh\}

(4) F \rightarrow \text{digit} \{F.val = \text{digit}.lexval}
```





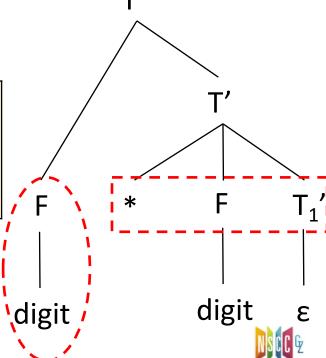
- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh
- Claim: inherited attributes are on the stack
 - Left attributes guarantee they've already been computed
 - But computed by previous productions deep in the stack
- Solution
 - Hack the stack to dig out those values

```
(1) T \to F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \to F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \to \epsilon \{ T'.syn = T'.inh \}

(4) F \to \text{digit} \{ F.val = \text{digit}.lexval \}
```





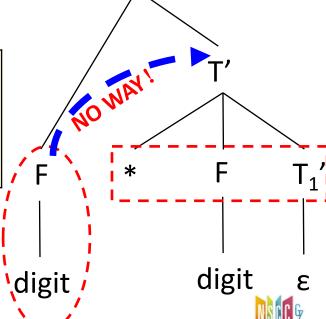
- It is not natural to evaluate inherited attributes
 - Example: how to get T'.inh
- Claim: inherited attributes are on the stack
 - Left attributes guarantee they've already been computed
 - But computed by previous productions deep in the stack
- Solution
 - Hack the stack to dig out those values

```
(1) T \to F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \to F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \to \epsilon \{ T'.syn = T'.inh \}

(4) F \to \text{digit} \{ F.val = \text{digit}.lexval \}
```





Marker[标记符号]

• Given the following SDD, where $|\alpha| \neq |\beta|$

```
A -> X \alpha { Y.in = X.s } Y | X \beta { Y.in = X.s } Y 
Y -> \gamma { Y.s = f(Y.in) }
```

- Problem: cannot generate stack location for Y.in
 - Because X.s is at different relative stack locations from Y
- Solution: insert markers M₁, M₂ right before Y

```
A -> X \alpha M<sub>1</sub> Y | X \beta M<sub>2</sub> Y

Y -> \gamma { Y.s = f(stack[top - |\gamma|].s) } // Y.s = M<sub>1</sub>.s or Y.s = M<sub>2</sub>.s

M<sub>1</sub> -> \epsilon { M<sub>1</sub>.s = stack[top - |\alpha|].s } // M<sub>1</sub>.s = X.s

M<sub>2</sub> -> \epsilon { M<sub>2</sub>.s = stack[top - |\beta|].s } // M<sub>2</sub>.s = X.s
```

- Marker: a non-terminal marking a location equidistant from the symbol that has an inherited attribute
 - Always produces ε since its only a placeholder for an action



Modify Grammar with Marker[文法修改]

- Given an L-SDD on an LL grammar, we can adapt the grammar to compute the same SDD during a LR parsing
 - Introduce into the grammar a marker nonterminal[标记非终结符] in place of each embedded action
 - □ Each such place gets a distinct marker, and there is one production for any marker M, M -> ε[空产生式]
 - Modify the action α if marker nonterminal M replaces it in some production $A \rightarrow \alpha$ { a } β , and associate with $M \rightarrow \epsilon$ an action a' that
 - \square Copies, as <u>inherited</u> attrs of M, any attrs of A or symbols of α that action a needs (e.g., M.i = A.i)[左侧]
 - \Box Computes attrs in the same way as a, but makes those attrs be synthesized attrs of M (e,.g., M.s = f(M.i))

$$A \rightarrow \{ B.i = f(A.i); \} B C$$

A -> M B C
M ->
$$\varepsilon$$
 { M. i = A. i ; M. s = f(M. i); }





Example

```
(1) T \rightarrow F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}

(2) T' \rightarrow F \{ T_1'.inh = T'.inh \times F.val \} T_1' \{ T'.syn = T_1'.syn \}

(3) T' \rightarrow \varepsilon \{ T'.syn = T'.inh \}

(4) F \rightarrow \text{digit} \{ F.val = \text{digit}.lexval \}
```

```
(1) T \rightarrow F M T' \{ T.val = T'.syn \}

M \rightarrow \epsilon \{ M.i = F.val; M.s = M.i \}

(2) T' \rightarrow F N T_1' \{ T'.syn = T_1'.syn \}

N \rightarrow \epsilon \{ N.i_1 = T'.inh; N.i_2 = F.val; N.s = N.i_1 x N.i_2 \}

(3) T' \rightarrow \epsilon \{ T'.syn = T'.inh \}

(4) F \rightarrow \text{digit } \{ F.val = \text{digit.lexval } \}
```





Stack Manipulation[栈操作]

```
(1) T \rightarrow F \{ T'.inh = F.val \} T' \{ T.val = T'.syn \}
(2) T' -> * F \{T_1'.inh = T'.inh \times F.val\} T_1' \{T'.syn = T_1'.syn\}
(3) T' -> \varepsilon \{ T'.syn = T'.inh \}
(4) F \rightarrow digit \{ F.val = digit.lexval \}
```

```
(1) T \rightarrow F M T' \{ T.val = T'.syn \}
    M \rightarrow \varepsilon \{ M.i = F.val; M.s = M.i \}
(2) T' \rightarrow F N T_1' \{ T'.syn = T_1'.syn \}
    N \rightarrow \epsilon \{ N.i1 = T'.inh; N.i2 = F.val; N.s = N.i1 x N.i2 \}
(3) T' -> \varepsilon \{ T'.syn = T'.inh \}
(4) F -> digit { F.val = digit.lexval }
```

```
(1) T -> F M T' { stack[top-2].val = stack[top].syn; top = top - 2; }
    M \rightarrow \varepsilon \{ stack[top+1].T'inh = stack[top].val; top = top + 1; \}
(2) T' -> * F N T_1' { stack[top-3].syn = stack[top].syn; top = top -3; }
    N \rightarrow \varepsilon \{ stack[top+1].T'inh = stack[top-2].T'inh \times stack[top].val; top = top + 1; \}
(3) T' -> \varepsilon { stack[top+1].syn = stack[top].T'inh; top = top + 1; }
(4) F -> digit { stack[top].val = stack[top].lexval; }
```



