



Compilation Principle 编译原理

第7讲: 语法分析(4)

张献伟

xianweiz.github.io

DCS290, 3/15/2022





Quiz Questions



Q1: for grammar E → E-E | E+E | a | b, and input b-a+b, give one rightmost derivation.

$$E \rightarrow E - E \rightarrow E - E + E \rightarrow E - E + b \rightarrow E - a + b \rightarrow b - a + b$$

 $E \rightarrow E + E \rightarrow E + b \rightarrow E - E + b \rightarrow E - a + b \rightarrow b - a + b$

- Q2: plot parse tree of the derivation in Q1.
- Q3: briefly describe top-down parsing. b a Mimics leftmost derivation, expand the start symbol to input string.
- Q4: why top-down parsing cannot handle left recursive grammars?

Repeatedly expanding without consuming any input symbol.

Q5: is grammar S → Ta|a, T → S left recursive? Why?
 YES. S → Ta → Sa (indirect left-recursive).





Predictive Parsers[预测分析]

- In recursive descent with backtracking[有回溯]:
 - At each step, many choices of production to use
 - Backtracking used to undo bad choices
- A parser with no backtracking[无回溯]: **predict** correct next production given next input terminal(s) [以下面一些输入来预测]
 - If first terminal of every alternative production is unique, then parsing requires no backtracking[候选产生式开始符号唯一]
 - If not unique, grammar cannot use predictive parsers[不唯一]

```
A→aBD | bBB
B→c | bce
D→d
```

parsing input "abced" requires no backtracking





Predictive Parsers[预测分析]

- In recursive descent with backtracking[有回溯]:
 - At each step, many choices of production to use
 - Backtracking used to undo bad choices
- A parser with no backtracking[无回溯]: **predict** correct next production given <u>next input terminal(s)</u>?[以下面一些输入来预测]
 - If first terminal of every alternative production is unique, then parsing requires no backtracking[候选产生式开始符号唯一]
 - If not unique, grammar cannot use predictive parsers[不唯一]

```
A→aBD | bBB

B→c | bce

D→d

parsing input "abced" requires no backtracking
```





Predictive Parsers[预测分析]

- In recursive descent with backtracking[有回溯]:
 - At each step, many choices of production to use
 - Backtracking used to undo bad choices
- A parser with no backtracking[无回溯]: **predict** correct next production given next input terminal(s)?[以下面一些输入来预测]
 - If first terminal of every alternative production is unique, then parsing requires no backtracking[候选产生式开始符号唯一]
 - If not unique, grammar cannot use predictive parsers[不唯一]

```
A \rightarrow aBD \mid bBB

B \rightarrow c \mid bce

D \rightarrow d
```

parsing input "abced" requires no backtracking

?: 如果只往前看一个,那么next terminal其实就是current terminal,即要匹配的那个(注意backtrack是完全不看)



Predictive Parsers (cont.)

- A predictive parser chooses the production to apply solely on the basis of[选取产生式的依据]
 - Next input symbol(s)[下一输入符号/终结符]
 - Current nonterminal being processed[当前正处理的非终结符]
- Patterns in grammars that prevent predictive parsing[并非总是能预测分析]
 - Common prefix[共同前缀]:

$$A \rightarrow \alpha\beta \mid \alpha\gamma$$

Given input terminal(s) α , cannot choose between two rules

- Left recursion[左递归]:

$$A \rightarrow A\beta \mid \alpha$$

Lookahead symbol changes only when a terminal is matched





Predictive Parsers (cont.)

- A predictive parser chooses the production to apply solely on the basis of[选取产生式的依据]
 - Next input symbol(s)[下一输入符号/终结符]
 - Current nonterminal being processed[当前正处理的非终结符]
- Patterns in grammars that prevent predictive parsing[并非总是能预测分析]
 - Common prefix[共同前缀]:

$$A \rightarrow \alpha\beta \mid \alpha\gamma$$

Given input terminal(s) α , cannot choose between two rules

- Left recursion[左递归]:

$$A \rightarrow A\beta \mid \alpha$$

Lookahead symbol changes only when a terminal is matched

What is the language of the grammar?





Predictive Parsers (cont.)

- A predictive parser chooses the production to apply solely on the basis of[选取产生式的依据]
 - Next input symbol(s)[下一输入符号/终结符]
 - Current nonterminal being processed[当前正处理的非终结符]
- Patterns in grammars that prevent predictive parsing[并非总是能预测分析]
 - Common prefix[共同前缀]:

$$A \rightarrow \alpha\beta \mid \alpha\gamma$$

Given input terminal(s) α , cannot choose between two rules

- Left recursion[左递归]:

$$A \rightarrow A\beta \mid \alpha$$

Lookahead symbol changes only when a terminal is matched

What is the language of the grammar? $\alpha \beta^*$





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to

$$A \rightarrow \alpha A'$$

 $A' \rightarrow \beta \mid \gamma$

– After processing α , A' can can choose between β or γ (assuming β or γ do not start with α)





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow$ if expr then stmt else $stmt \mid$ if expr then $stmt \mid A \rightarrow \alpha A' \mid A' \rightarrow \beta \mid \gamma$
 - After processing α , A' can can choose between β or γ (assuming β or γ do not start with α)





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow if \ expr \ then \ stmt \ else \ stmt \ | \ if \ expr \ then \ stmt \ |$ $A \rightarrow \alpha \ A' \qquad stmt \rightarrow if \ expr \ then \ stmt \ S' \rightarrow else \ stmt \ | \ \epsilon$
 - After processing α , A' can can choose between β or γ (assuming β or γ do not start with α)





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow if \ expr \ then \ stmt \ else \ stmt \ | \ if \ expr \ then \ stmt \ |$ $A \rightarrow \alpha \ A' \qquad stmt \rightarrow if \ expr \ then \ stmt \ S' \rightarrow else \ stmt \ | \ \epsilon$
 - After processing α, A' can can choose between β or γ
 (assuming β or γ do not start with α)
 推迟选择,直到可区分





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow if \ expr \ then \ stmt \ else \ stmt \ | \ if \ expr \ then \ stmt \ |$ $A \rightarrow \alpha \ A' \qquad stmt \rightarrow if \ expr \ then \ stmt \ S' \rightarrow else \ stmt \ | \ \epsilon$
 - After processing α, A' can can choose between β or γ
 (assuming β or γ do not start with α)
 推迟选择, 直到可区分
- Left-recursion removal[左递归消除]: same as recursive descent





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow if \ expr \ then \ stmt \ else \ stmt \ | \ if \ expr \ then \ stmt \ |$ $A \rightarrow \alpha \ A' \qquad stmt \rightarrow if \ expr \ then \ stmt \ S' \rightarrow else \ stmt \ | \ \epsilon$
 - After processing α, A' can can choose between β or γ
 (assuming β or γ do not start with α)
 推迟选择, 直到可区分
- Left-recursion removal[左递归消除]: same as recursive descent
 - In previous example: $A \rightarrow A\beta \mid \alpha$
 - can be changed to





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow if \ expr \ then \ stmt \ else \ stmt \ | \ if \ expr \ then \ stmt \ |$ $A \rightarrow \alpha \ A' \qquad stmt \rightarrow if \ expr \ then \ stmt \ S' \rightarrow else \ stmt \ | \ \epsilon$
 - After processing α, A' can can choose between β or γ
 (assuming β or γ do not start with α)
 推迟选择, 直到可区分
- **Left-recursion removal**[左递归消除]: same as recursive descent
 - In previous example: $A \rightarrow A\beta \mid \alpha$
 - can be changed to

$$A \rightarrow \alpha A'$$

 $A' \rightarrow \beta A' \mid \epsilon$





- Left factoring[左公因子提取]: removes common left prefix
 - In previous example: $A \rightarrow \alpha\beta \mid \alpha\gamma$
 - can be changed to $stmt \rightarrow if \ expr \ then \ stmt \ else \ stmt \ | \ if \ expr \ then \ stmt \ |$ $A \rightarrow \alpha \ A' \qquad stmt \rightarrow if \ expr \ then \ stmt \ S' \rightarrow else \ stmt \ | \ \epsilon$
 - After processing α, A' can can choose between β or γ
 (assuming β or γ do not start with α)
 推迟选择, 直到可区分
- **Left-recursion removal**[左递归消除]: same as recursive descent
 - In previous example: $A \rightarrow A\beta \mid \alpha$
 - can be changed to

$$A \rightarrow \alpha A'$$

 $A' \rightarrow \beta A' \mid \epsilon$

– After processing α , A' can can choose between β or ϵ (assuming β doesn't start with α or A' isn't followed by α)





LL(k) Parser / Grammar / Language

• LL(k) Parser

- A predictive parser that uses k lookahead tokens
- L: scans the input from left to right[从左往右]
- L: produces a leftmost derivation[生成最左推导]
- k: using k input symbols of lookahead at each step to decide[向前看k个符号]

LL(k) Grammar

- A grammar that can be parsed using an LL(k) parser
- $-LL(k) \subset CFG$
 - Some CFGs are not LL(k): common prefix or left-recursion

LL(k) Language

- A language that can be expressed as an LL(k) grammar
- Many languages are LL(k) ...
 - In fact many are LL(1)!





LL(k) Parser Implementation[实现]

- Implemented in a recursive or non-recursive fashion[递归/ 非递归]
 - Recursive: recursive descent (recursive function calls, <u>implicit</u> stack)
 - Non-recursive: <u>explicit stack</u> to keep track of recursion[栈]
- Recursive LL(1) parser for: $A \rightarrow B \mid C, B \rightarrow b, C \rightarrow c$
 - Parser consists of small functions, one for each non-terminal

```
void A() {
  token = peekNext(); // lookahead token
  switch(token) {
    case 'b': // 'B' starts with 'b'
        B(); // call procedure B()
    case 'c': // 'C' starts with 'c'
        C(); // call procedure C()
    default: // Reject
    return;
}
```





LL(k) Parser Implementation (cont.)

• Recursive LL(1) parser for: $A \rightarrow B \mid C, B \rightarrow b, C \rightarrow c$

```
void A() {
  token = peekNext(); // lookahead token
  switch(token) {
    case 'b': // 'B' starts with 'b'
        B(); // call procedure B()
    case 'c': // 'C' starts with 'c'
        C(); // call procedure C()
    default: // Reject
    return;
}
```

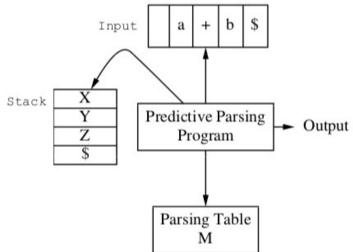
- Is there a way to express above code more concisely?[简洁]
 - Non-recursive LL(k) parsers use a state transition table (just like finite automata)[状态转换表]
 - Easier to automatically generate a non-recursive parser[自动化]





LL(1) Parser[非递归]

- Table-driven parser[表驱动]: amenable to automatic code generation (just like lexers)
 - Input buffer: contains the string to be parsed, followed by \$
 - Stack: holds unmatched portion of derivation string, \$ marks
 the stack end
 - Parse table M[A, b]: an entry containing rule " $A \rightarrow ...$ " or error
 - Parser driver (a.k.a., predictive parsing program): next action based on <stack top, current token
 - Reject on reaching error state
 - Accept on end of input & empty stack





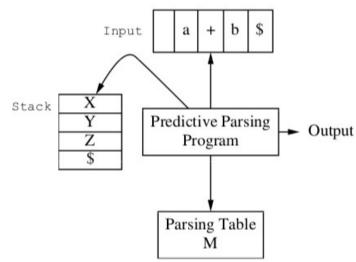


LL(1) Parser[非递归]

- Table-driven parser[表驱动]: amenable to automatic code generation (just like lexers)
 - Input buffer: contains the string to be parsed, followed by \$
 - Stack: holds unmatched portion of derivation string, \$ marks
 the stack end
 - Parse table M(A, b): an entry containing rule " $A \rightarrow ...$ " or error
 - Parser driver (a.k.a., predictive parsing program): next action based on <stack top, current token
 - Reject on reaching error state
 - Accept on end of input & empty stack

A stack records frontier of parse tree

- Non-terminals that have yet to be expanded
- Terminals that have yet to matched against the input
- Top of stack = leftmost pending terminal or non-terminal







?: The current token is treated as lookahead token.

table	int	*	+	()	\$	- >
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E' > ε	E' > ε	$E' \rightarrow +E \mid \epsilon$ T \rightarrow intT'
T	$T \rightarrow int T'$			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	

Implementation with 2D parse table





table	int	*	+	()	\$	
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E′ → ε	E' → ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' \rightarrow (E)
T	$T \rightarrow int T'$			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′ → ε	T′) ε	

Implementation with 2D parse table





table	int	*	+	()	\$	- >
E	E → TE′			E → TE′			$E \rightarrow TE'$
Ε'			E' → +E		E' → ε	E′ → ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' (E)
T	$T \rightarrow int T'$			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation





table	int	*	+	()	\$	
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E' > ε	E' > ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' (E
Т	$T \rightarrow int T'$			T → (E)			
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation





table	int	*	+	()	\$	- >!
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E′ → ε	E' > ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' \rightarrow (E)
Т	$T \rightarrow int T'$			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′) ε	T′ → ε	

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation





table	int	*	+	()	\$	- >
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E′ → ε	E' > ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' \rightarrow (E)
T	$T \rightarrow int T'$			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation
 - First row lists all possible terminals in the grammar and \$
 - I.e., next input token





table	int	*	+	()	\$	
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E' > ε	E' > ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' (E
Т	$T \rightarrow int T'$			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation
 - First row lists all possible terminals in the grammar and \$
 - I.e., next input token





table	int	*	+	()	\$	
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E′ → ε	E′ → ε	$E' \rightarrow +E \mid \epsilon$ T \rightarrow intT' (E)
Т	T \rightarrow int T'			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	. , . 0

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation
 - First row lists all possible terminals in the grammar and \$
 - I.e., next input token





table	int	*	+	()	\$	
Е	E → TE′			E → TE′			$E \rightarrow TE'$
E'	i		E' → +E		E′ → ε	E′ → ε	$E' \rightarrow +E \mid \varepsilon$ T \rightarrow intT' \rightarrow (E)
T	T \rightarrow int T'			T → (E)			$T' \rightarrow *T \mid \epsilon$
T'	I	T′ → *T	T′ → ε		T′) ε	T′) ε	. , . 0

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation
 - First row lists all possible terminals in the grammar and \$
 - I.e., next input token
 - A table entry contains one production
 - One action for each <non-terminal, input> combination
 - It "predicts" the correct action based on one lookahead
 - No backtracking required





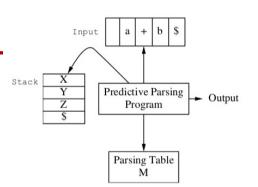
table	int	*	+	()	\$	
E	E → TE′			E → TE′			$E \rightarrow TE'$
E'			E' → +E		E′ → ε	E' > ε	$E' \rightarrow +E \mid \epsilon$ T \rightarrow intT' (E
Т	$T \rightarrow int T'$			T → (E)			
T'		T′ → *T	T′ → ε		T′ → ε	T′ → ε	

- Implementation with 2D parse table
 - First column lists all non-terminals in the grammar
 - I.e., leftmost non-terminal in derivation
 - First row lists all possible terminals in the grammar and \$
 - I.e., next input token
 - A table entry contains one production
 - One action for each <non-terminal, input> combination
 - It "predicts" the correct action based on one lookahead
 - No backtracking required





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

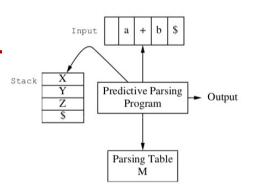


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

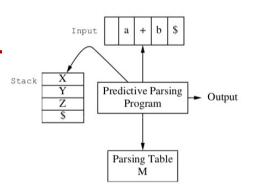


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

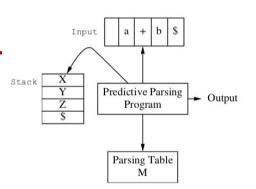


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

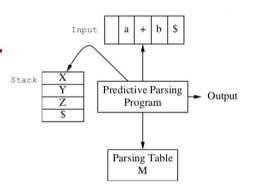


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - \blacksquare If $X \in T$, then





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

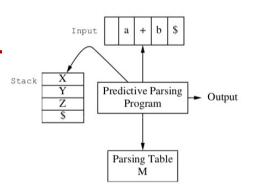


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - \blacksquare If $X \in T$, then
 - If X == a == \$, parser halts with "success"





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

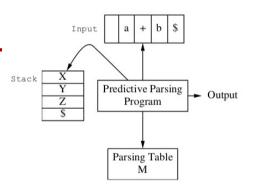


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - \blacksquare If $X \in T$, then
 - If X == a == \$, parser halts with "success"
 - If X == a != \$, successful match, pop X from stack and advance input head





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

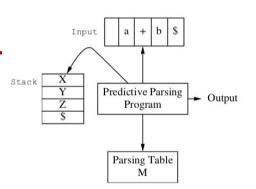


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - □ If X ∈ T, then
 - If X == a == \$, parser halts with "success"
 - If X == a != \$, successful match, pop X from stack and advance input head
 - If X != a, parser halts and input is rejected





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

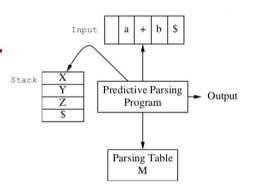


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - \blacksquare If $X \in T$, then
 - If X == a == \$, parser halts with "success"
 - If X == a != \$, successful match, pop X from stack and advance input head
 - If X != a, parser halts and input is rejected
 - □ If X ∈ N, then





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom

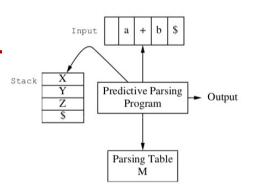


- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - \blacksquare If $X \in T$, then
 - If X == a == \$, parser halts with "success"
 - If X == a != \$, successful match, pop X from stack and advance input head
 - If X != a, parser halts and input is rejected
 - \square If $X \in \mathbb{N}$, then
 - If M[X,a] == 'X→RHS", pop X and push RHS to stack





- Initial state[初始态]
 - Input tape: input tokens followed by '\$'
 - Stack: start symbol followed by '\$' at bottom



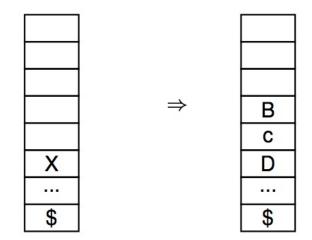
- General idea[总体思路]: repeat one of two actions
 - Expand symbol at top of stack by applying a production
 - Match terminal symbol at top of stack with input token
- Step-by-step[每步操作] parsing based on <X, a>
 - X: symbol at the top of the stack
 - a: current input token
 - \blacksquare If $X \in T$, then
 - If X == a == \$, parser halts with "success"
 - If X == a != \$, successful match, pop X from stack and advance input head
 - If X != a, parser halts and input is rejected
 - \square If $X \in \mathbb{N}$, then
 - If $M[X,a] == 'X \rightarrow RHS''$, pop X and push RHS to stack
 - If M[X,a] == empty, parser halts and input is rejected





Push RHS in Reverse Order[逆序入栈]

- For <X, a>
 - X: symbol at the top of the stack
 - a: current input token
- If $M[X,a] = "X \rightarrow BcD"$



- Performs the leftmost derivation: $\alpha \times \beta \Rightarrow \alpha \text{ BcD } \beta$
 - $-\alpha$: string that has already been matched with input
 - β: string yet to be matched, corresponding to the ... above





$$E \rightarrow T+E|T$$

T \rightarrow int*T | int | (E)





Consider the grammar

$$E \rightarrow T+E|T$$

T \rightarrow int*T | int | (E)

- Left recursion?





```
E \rightarrow T+E|T
T \rightarrow int*T \mid int \mid (E)
- Left recursion? NO!
```





```
E \rightarrow T+E|T

T \rightarrow int*T | int | (E)
```

- Left recursion? NO!
- Left factoring?





```
E \rightarrow T+E|T
T \rightarrow int*T | int | (E)
```

- Left recursion? NO!
- Left factoring? YES. $E \rightarrow T+E|T, T \rightarrow int*T| int$





Consider the grammar

```
E → T+E|T
T → int*T | int | (E)
Left recursion? NO!
Left factoring? YES. E → T+E|T, T → int*T | int
```

After rewriting grammar, we have





```
E \rightarrow T+E|T
T \rightarrow int*T | int | (E)
```

- Left recursion? NO!
- Left factoring? YES. $E \rightarrow T+E|T, T \rightarrow int*T| int$
- After rewriting grammar, we have

$$E \rightarrow TE'$$

 $E' \rightarrow +E \mid \epsilon$





Consider the grammar

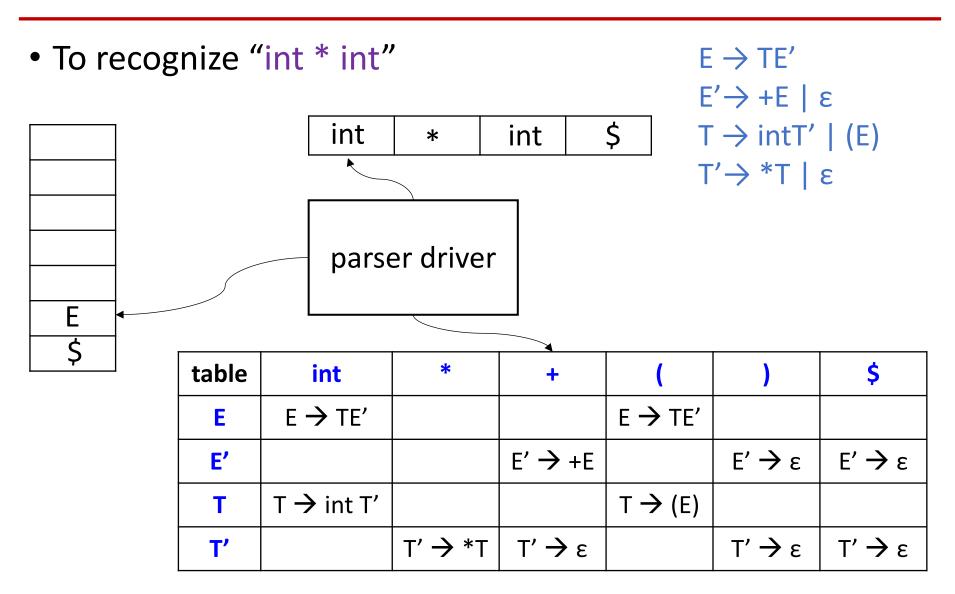
```
E \rightarrow T+E|T
T \rightarrow int*T \mid int \mid (E)
- Left recursion? NO!
- Left factoring? YES. E \rightarrow T+E|T, T \rightarrow int*T \mid int
```

After rewriting grammar, we have

```
E \rightarrow TE'
E' \rightarrow +E \mid \epsilon
T \rightarrow intT' \mid (E)
T' \rightarrow *T \mid \epsilon
```

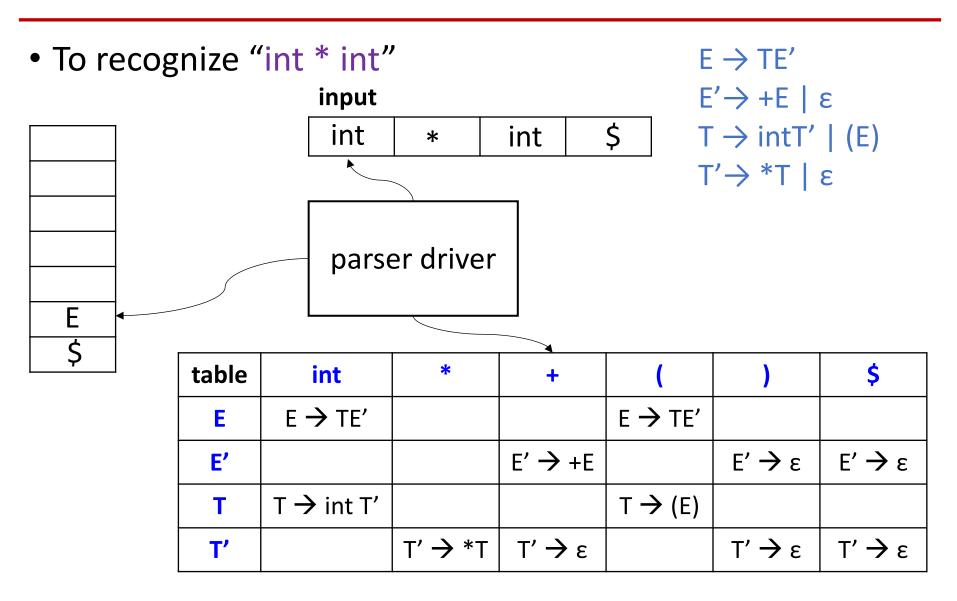






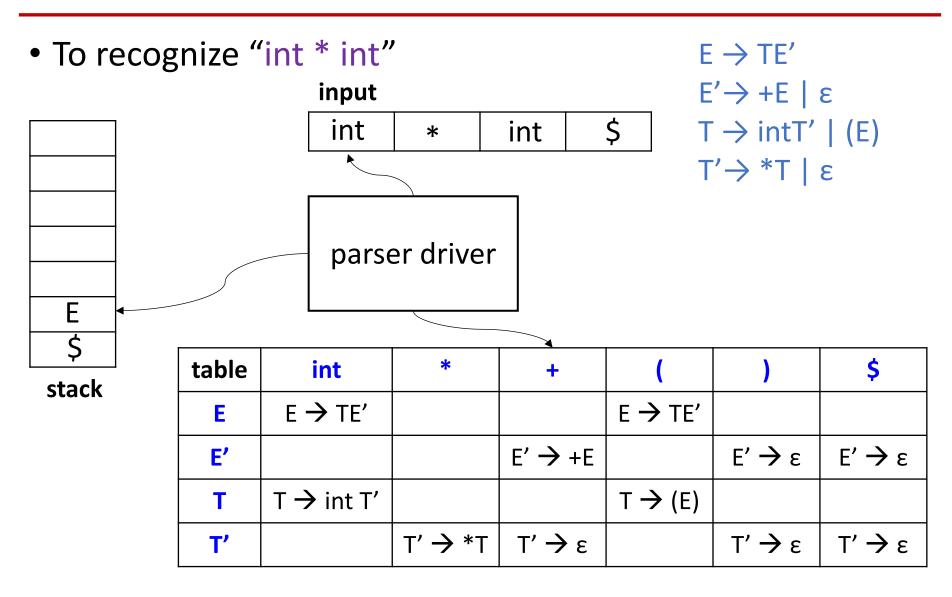






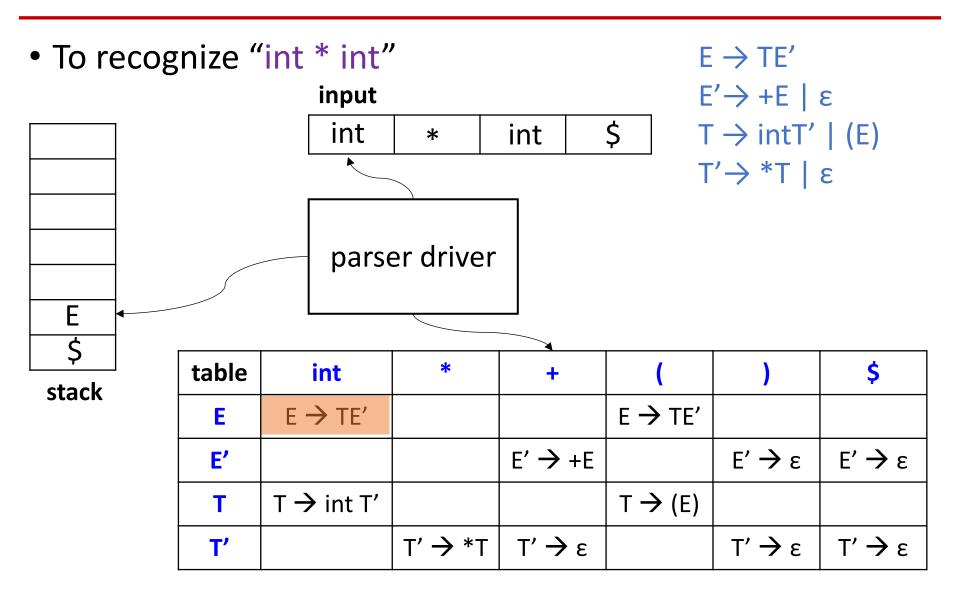






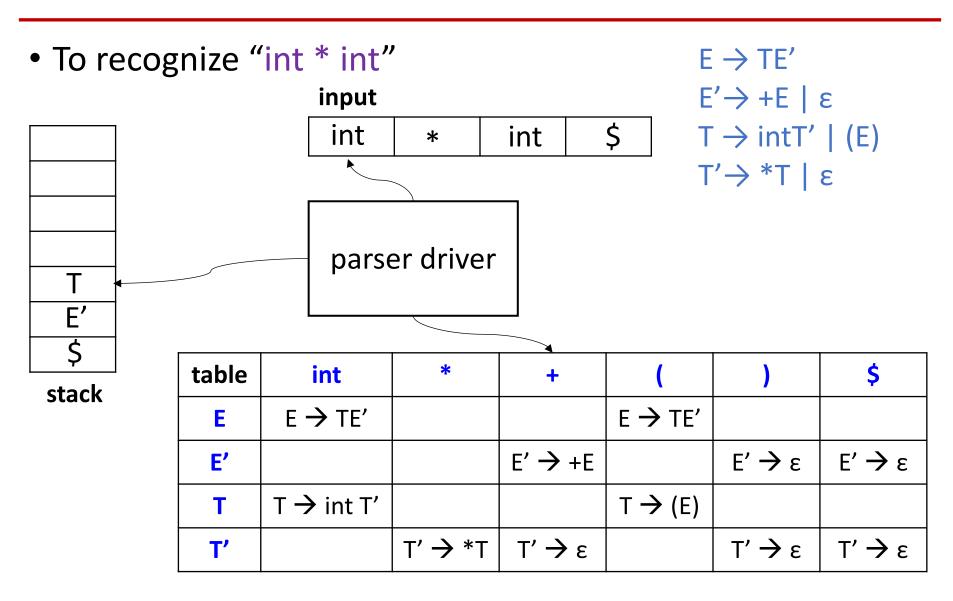






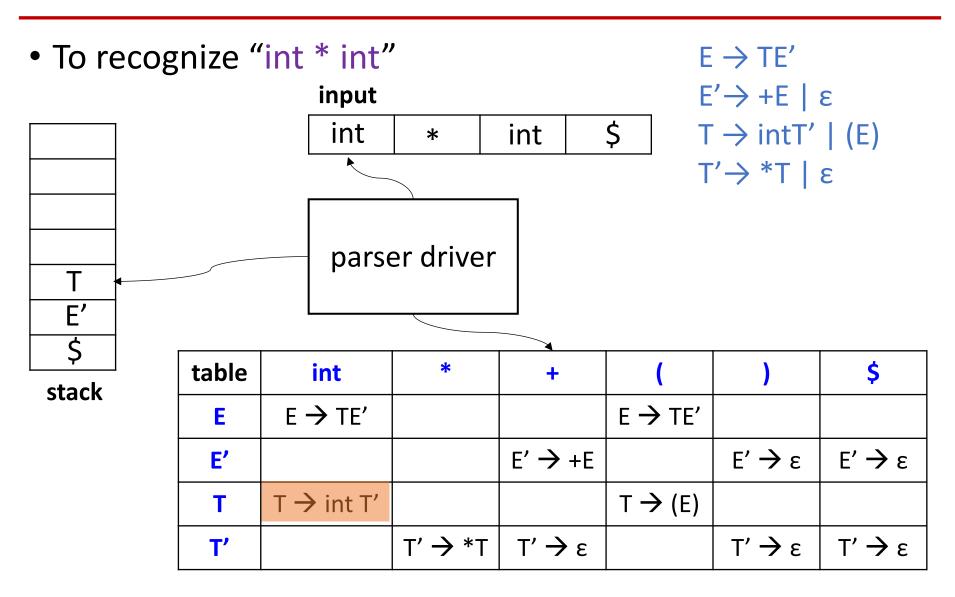






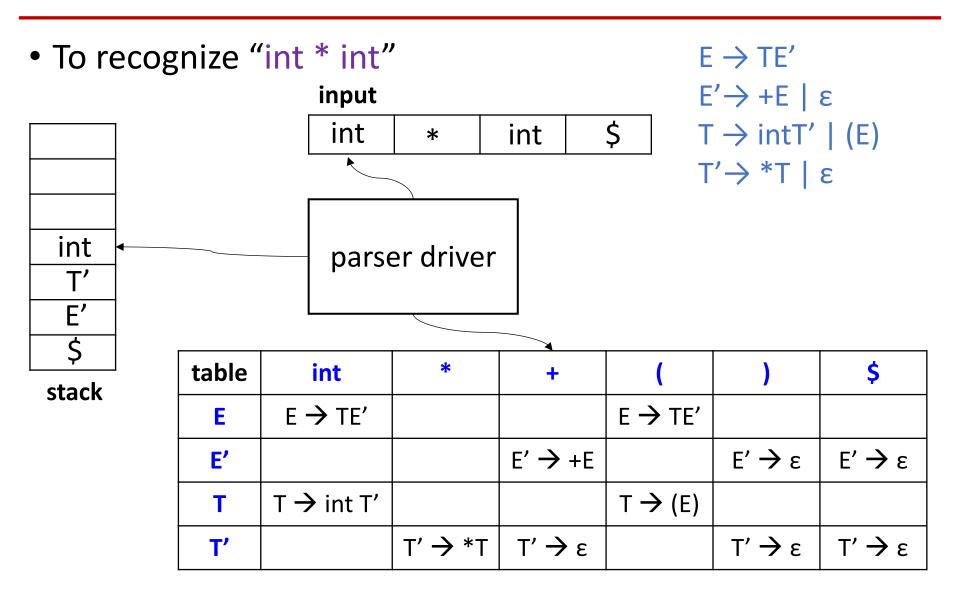






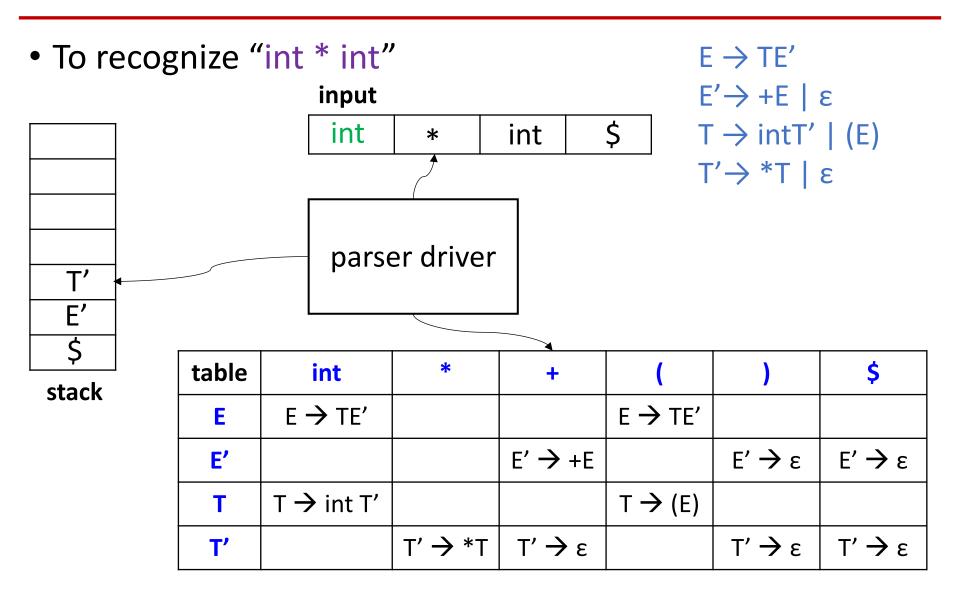






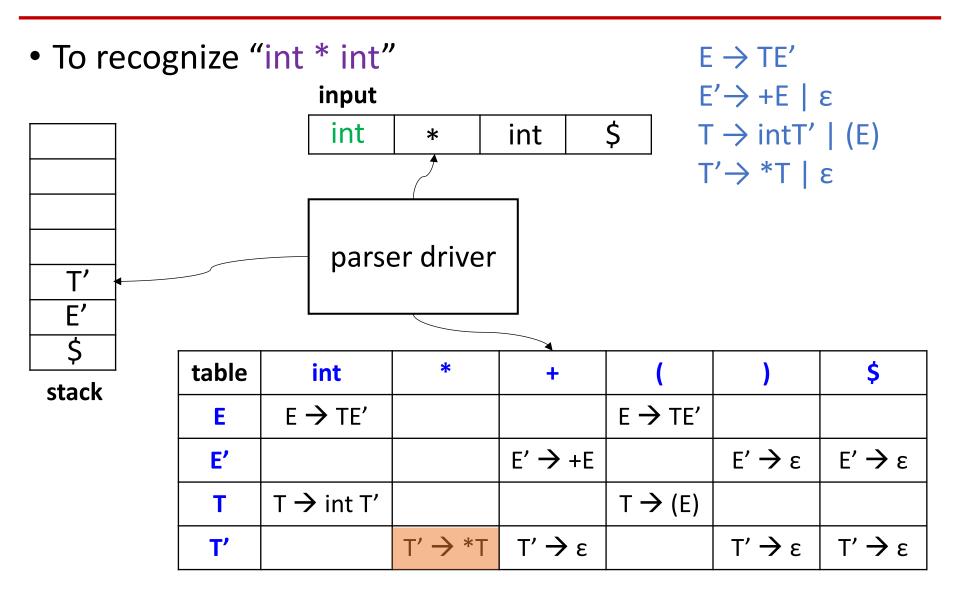






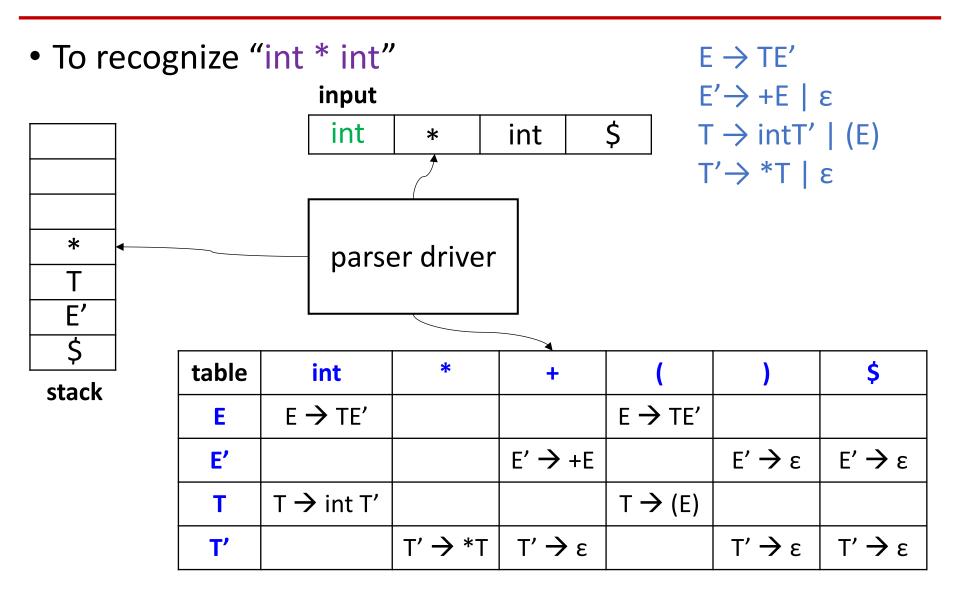






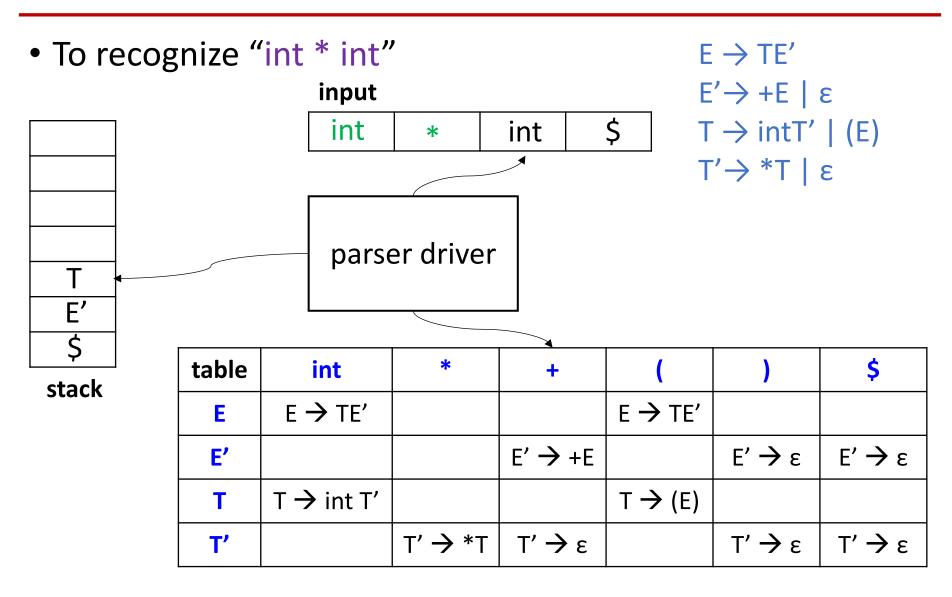






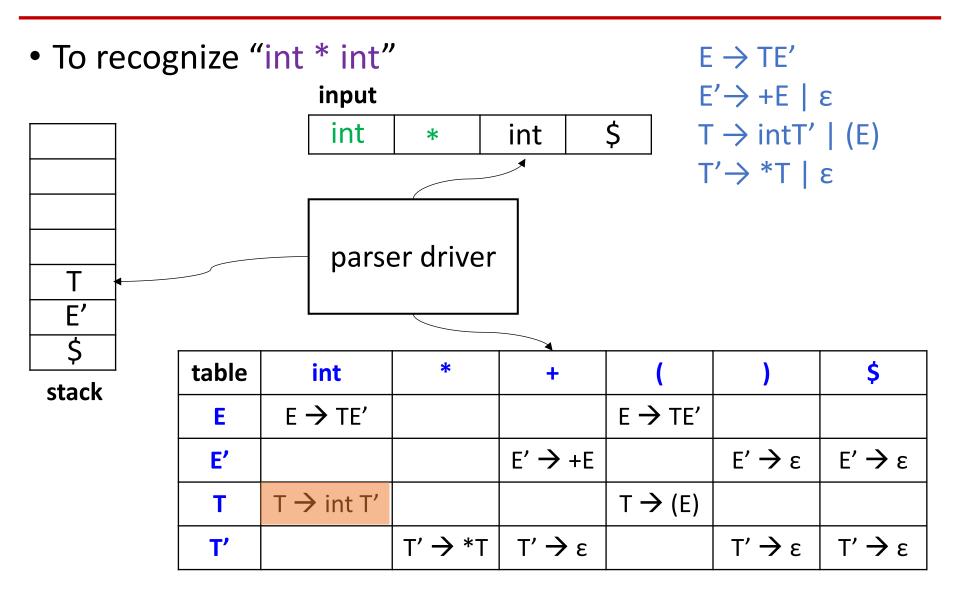






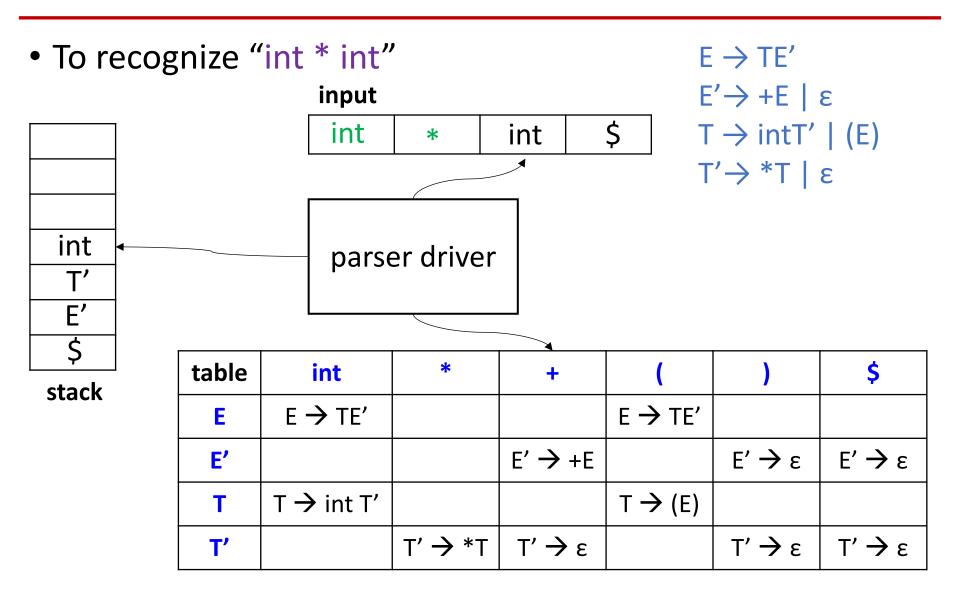






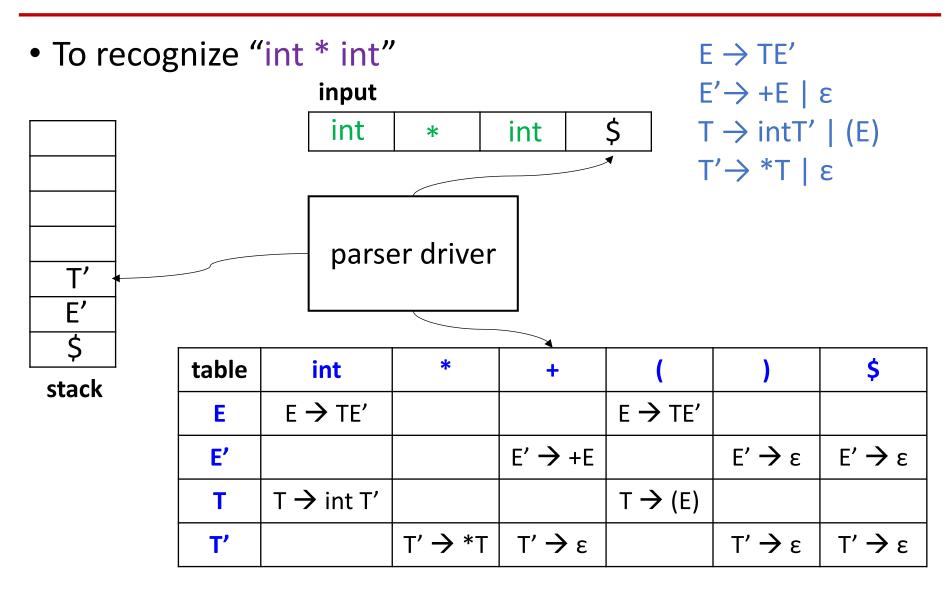






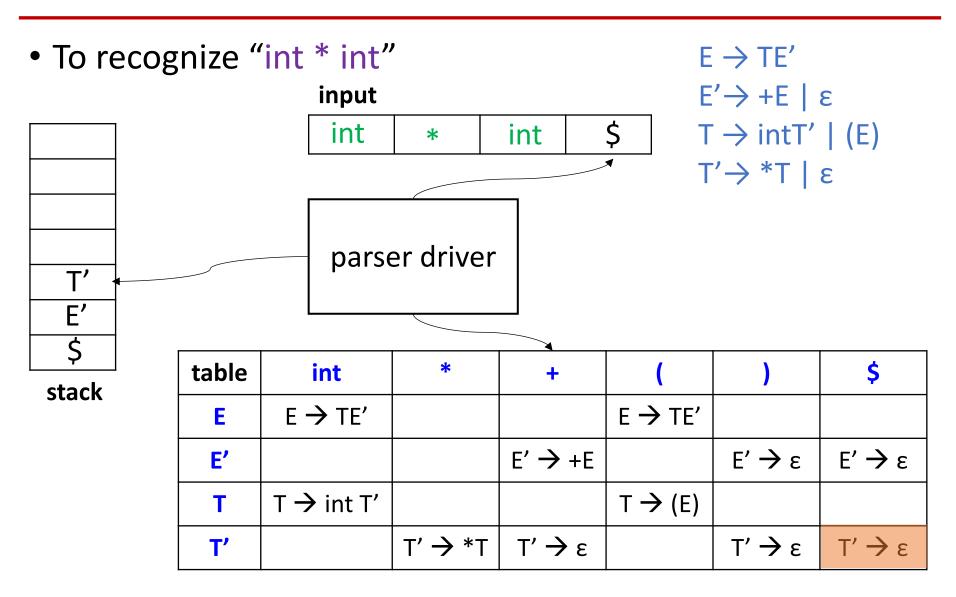






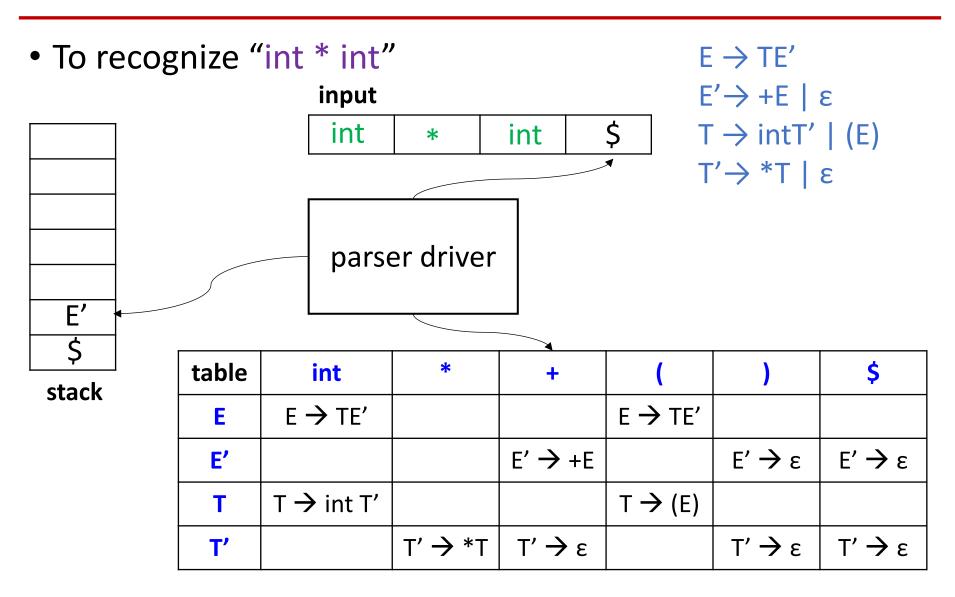






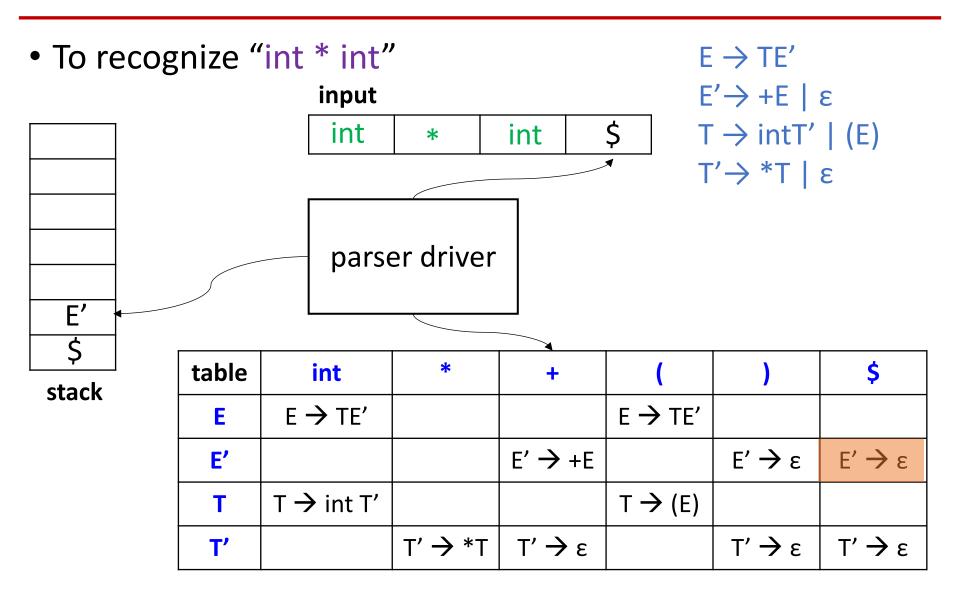






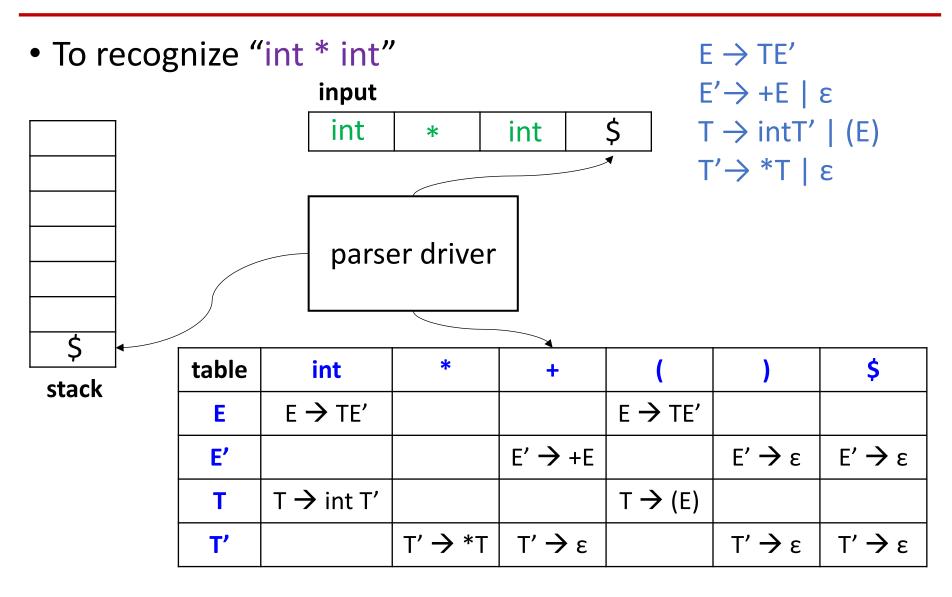






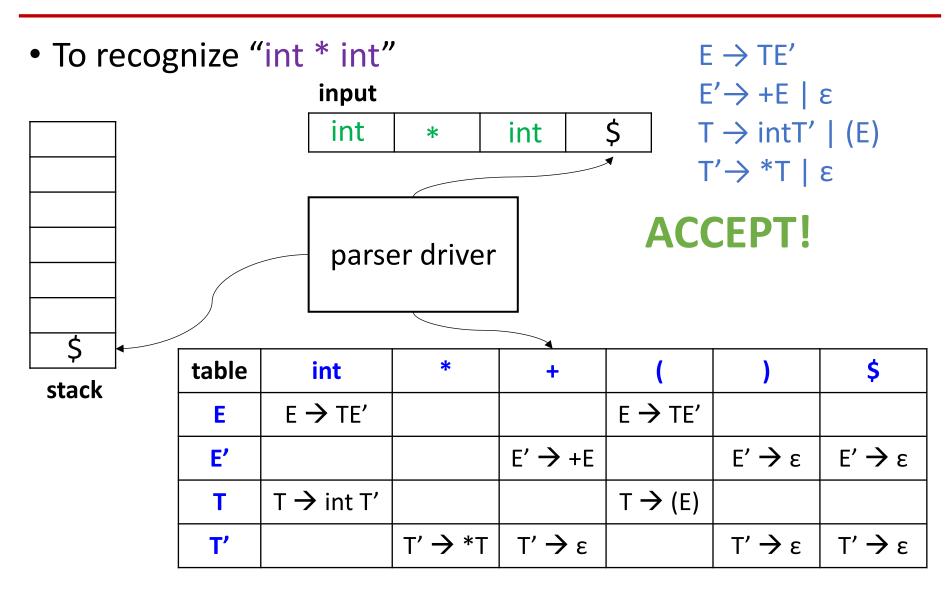
















Recognize Sequence[解析过程]

Matched	Stack	Input	Action
	E \$	int * int \$	E → TE'
	T E'\$	int * int \$	T → int T'
int	int T' E' \$	int * int \$	match
int	T' E' \$	* int \$	T' → *T
int	* T E' \$	* int \$	match
int *	T E' \$	int \$	$T \rightarrow int T'$
int *	int T' E' \$	int \$	match
int * int	T' E' \$	\$	T' → ε
int * int	E' \$	\$	E' → ε
int * int	\$	\$	Halt and accept

$E \rightarrow TE'$	
$E' {\to} + E \mid \epsilon$	
$T \rightarrow intT' \mid$	(E)
$T' {\to} *T \mid \epsilon$	

Input: int * int

- 'Matched + Stack' constructs the sentential form[句型]
- Actions correspond to productions in leftmost derivation



