

CS 2

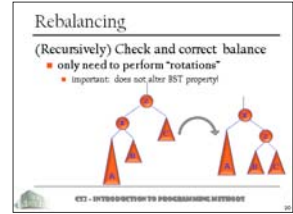
Introduction to Programming Methods



Last Time

Intro to data structures

- how to store your data in a convenient form
- finished with trees



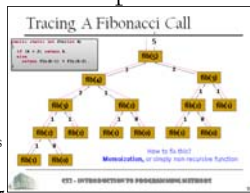
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Remember Fibonacci?

Example where recursion is hurtful

- Recursion w/ slightly smaller subproblems
 - Fib(n) calls Fib(n-1)
 - not like merge sort!
 - merge: log depth of tree
 - Fib: linear depth
 - exponential # of nodes
 - and many nodes are repeats



Dynamic programming

- used for certain optimization problems

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When Is Dynamic Prog. Useful?

Optimal substructure

- solution can be constructed efficiently from (optimal) solutions to subproblems
 - includes merge sort or towers of Hanoi, for instance

Overlapping subproblems

- recursions like Fibonacci, with redundancy

DP proceeds much faster

- through various improvements
 - including memoization (i.e., storing previous results)

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More Interesting Problem

How to reformat an image?

- scaling or cropping no good
- need to keep relevant parts



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More Interesting Problem

How to reformat an image?

- scaling or cropping no good
- need to keep relevant parts
 - or to remove old partners...



Simple Idea: Seam Carving

Remove a continuous line of pixels

- least conspicuous, from top to bottom



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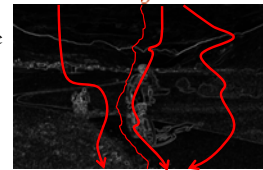
The Optimal Seam

What is a (vertical) seam?

- one pixel per row; all pixels contiguous
- with least "saliency"
 - saliency map derived from color image s^*
 - score = sum of pixels
 - best seam = min score

$$E(s) = \sum_i \text{saliency}(s_i)$$

$$E(s^*) = \min_s E(s)$$



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Computing Saliency Map

Many ways, but gradient norm G enough

- linear combos of 8 neighbors of each pixel

$$G_y = \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} * A \quad \text{and} \quad G_x = \begin{bmatrix} +1 & 0 & -1 \\ +2 & 0 & -2 \\ +1 & 0 & -1 \end{bmatrix} * A$$

$$G = \sqrt{G_x^2 + G_y^2}$$



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How to Find the Optimal Path

Seemingly, like a needle in a haystack

- for a $N \times N$ image, lots of possible seams
- brut force approach? Try and score them all
 - could use recursion
 - ex: $M(i, j) = \text{saliency}(i, j) + \min(M(i-1, j-1), M(i-1, j), M(i-1, j+1))$
 - but HUGE redundancy; & how to get seam from best score?
- can find it by dynamic programming
 - minimum path found by storing the optimal paths to reach each pixel in a cost table
 - table constructed by top-down memoizing
 - final path inferred by back tracing through the table.
 - typical when lots of overlapping sub problems



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Construction of Cost Table

Top to bottom (for vertical seams)

- from second to last row

5	8	3	9	5	8	3	9
9	2	3	9	14	8	6	12
7	3	4	2	12	8	9	8
4	5	7	8	12	13	15	16

saliency

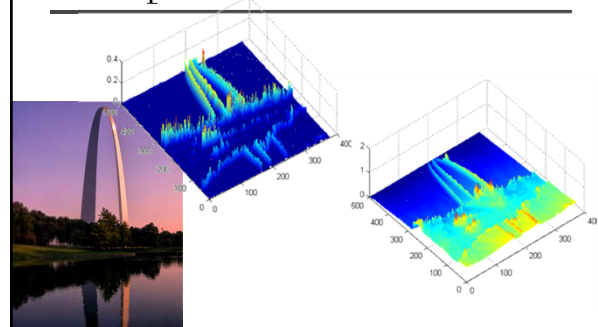
cost

$$M(i, j) = \text{saliency}(i, j) + \min(M(i-1, j-1), M(i-1, j), M(i-1, j+1))$$

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Example of Cost Table



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Finding Optimal Seam

Now just backtrace!

- start with min value on last row
 - which is the optimal cost, by the way
- ... and walk up from value to value

5	8	3	9
14	5	6	12
14	8	9	8
12	13	15	16



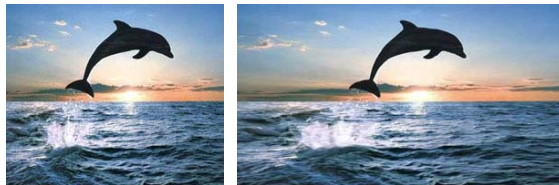
Typical Seams



Expanding an Image?

Same idea

- find optimal seam
- insert pixels (local averages)



Other Dynamic Prog Examples

Find min # of (nonUS) coins to make an amount

- to find the solution for 13€,
 - solve for all of 1€, 2€, 3€, ..., 12€
 - choose best among {solution for i€ + solution for 13-i €}

Knapsack problem

- various item types of various values & weights
- bag of limited total weight → how to make most valuable?

Gene Sequence Alignment

Shortest Path

- more on this later

