

Tower of Hanoi

What is the code?

The code given is to print each step of solving the problem of Tower of Hanoi.

Bugs Found:

1) Line no. 131

```
mov %rsp,%rbp # Bug 1: The current stack pointer needs to be
moved to Base pointer to access.
```

The base pointer is updated now. So stops the segmentation fault that was given by the code before.

2) Line no. 113

```
j1 .less_branch # Bug 2: If r10 is less than rax then the source
and destination need to be swapped.
```

It should be less than not greater than.

Because the switch should happen from the pole with the disk of lower Disk size to higher size.

Function and loops Definitions :

I)_start:

```
_start:
movl $3, %edi
cmpl $1, (%rsp)
jle .solve
mov 16(%rsp), %rax
movsbl (%rax), %edi
subl $'0', %edi
```

Puts the default argument in %edi. Checks if an argument was passed to the function. If Passed changes it to that. Jumps or falls to .solve that calls the solve function.

II)solve:

```
solve:
push %rdi
mov %rsp,%rbp # Bug 1: The current stack pointer needs to be moved to
Base pointer to access.
```

```

    sub $64, %rsp
    mov %rsp, %rdi
    call f1

    sub $64, %rsp
    mov %rsp, %rdi
    call f1

    sub $64, %rsp
    mov %rsp, %rdi
    call f1

    lea -64(%rbp), %rax
    mov (%rbp), %rcx
    mov %rcx, (%rax)
    add $4, %rax

```

Pushes the first argument. The bug is fixed. That is the current stack pointer is moved to %rbp.

Allocate 64 bytes to first array. This array represents the source pole. Array[0] holds the number of disks in the pole.

After solve calls f1. *f1 Initialises everything in the array to zero.*

The function does the same the same for the auxiliary pole and destination pole arrays.

So -64(%rbp) is the base address of source array,
 -128(%rbp) is the base address of auxiliary array,
 -192(%rbp) is the base address of destination array.

III) .init_s:

Now the function prepares to fall through init_s . init_s will loop through n times. Each time, it will add the discs. For example if it is 3. It will put it is 3,3,2,1 ie, Array[0] is the no. of disks. The later numbers are the disks on the pole.

Now the function stores $2^N - 1$ as %r14. That is the number of steps that are required in tower of hanoi problem. %r15 has zero it is the looping variable.

```

.init_s:
    mov %rcx, (%rax)
    add $4, %rax
    loop .init_s

```

```
call pt7

mov (%rbp), %c1
mov $1, %r14
shl %c1, %r14
dec %r14
xor %r15,%r15
```

IV) f7: The loop

```
f7:
    lea -64(%rbp), %rdi
    lea -192(%rbp), %rsi
    call f5

    inc %r15
    cmp %r14, %r15
    jge f8

    lea -64(%rbp), %rdi
    lea -128(%rbp), %rsi
    call f5

    inc %r15
    cmp %r14, %r15
    jge f8

    lea -192(%rbp), %rdi
    lea -128(%rbp), %rsi
    call f5

    inc %r15
    cmp %r14, %r15
    jge f8
    jmp f7
```

In the loop the f5 is called three times each time with the following arguments and moves

Valid move from S to D

Valid move from S to A

Valid move from A to D
And repeats this 2^N-1 times.

Each time a move is done the counter %r15 is increased and is compared to 2^N-1 and when they become equal you remove everything from stack and return and exit the program.

V)f5: The Move Function

```
f5:
    mov %rdi, %r9
    call f2
    mov %rax, %r10
    mov %rsi, %rdi
    call f2
    mov %r9, %rdi
    cmp %rax, %r10
    jl .less_branch # Bug 2: If r10 is less than rax then the source and
                    # destination need to be swapped.
.greater_branch:
    mov %rdi, %rax
    mov %rsi, %rdi
    mov %rax, %rsi
.less_branch:
    call f3
    push %rdi
    push %rsi
    mov %rsi, %rdi
    mov %rax, %rsi
    call f4
    pop %rsi
    pop %rdi
    jmp pt7
```

f5 is a move function which takes the from pole and to pole as arguments. It calls f2 function which returns the top of the disk value of the array. The function compares the top values and swaps it in the .greater branch if required before calling the f3 and f4 functions which does the actual swap.

VI) f2: The top()

It returns the value of the top element of array. If it is empty it returns 100000. Ie so that the smaller or valid is chosen.

```
f2:
    movl (%rdi), %ecx
```

```

    cmpl $0, %ecx
    jz .peek_empty
    dec %ecx
    movq 4(%rdi, %rcx, 4), %rax
    ret

```

VII) f3: The pop()

```

f3:
    movl (%rdi), %ebx
    dec %ebx
    movl 4(%rdi, %rbx, 4), %eax
    movl $0, 4(%rdi, %rbx, 4)
    mov %ebx, (%rdi)
    ret

```

F3 is like a pop(). It deletes the last element of the array and returns it. It also reduces the size of the array. Ie the number of disks in the array.

VIII)f4: The push()

```

f4:
    movl (%rdi), %ecx
    mov %rsi, 4(%rdi, %rcx, 4)
    inc %ecx
    mov %ecx, (%rdi)
    ret

```

f4 is like the push() which takes two arguments, the array and the value to be pushed. It pushes the value at the end of the array ie, add a disk. It also increases the size of the array or pole by 1. It does not return anything.

Explanation of Output:

Each three lines are the output of one valid move. Total there will $2^N - 1$ moves.

In the given case the

1 3 2 1

2

3

Is the initial state

5 3 2
6
7 1

You move 1 from Source to Destination.

9 3
10 2
11 1

You move 2 from source to Auxiliary

13 3
14 2 1
15

You move 1 from Destination to Auxiliary

17
18 2 1
19 3

You move 3 from Source to Auxiliary

21 1
22 2
23 3

You move 1 from Auxiliary to source

25 1
26
27 3 2

You move 2 from Auxiliary to Destination

29
30
31 3 2 1

You move 1 from Source to destination

The puzzle is over and you have moved everything from source to destination.