# ArmoredSoftware Semantics 0.0

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#### Abstract

This document describes evolving  $\ensuremath{\mathsf{ARMOREDSOFTWARE}}$  semantic definitions.

## 1 Introduction

## 2 SPI Calculus

Examples motivated by ?.

### 2.1 Wide Mouth Frog

#### 2.2 Needham Schroeder

$$A 
ightarrow B: \{A^+, N_A\}_{B^+}$$
 on  $c$   
 $B 
ightarrow A: \{N_A, N_B\}_{A^+}$  on  $c$   
 $A 
ightarrow B: \{N_B\}_{B^+}$  on  $c$ 

$$\begin{array}{rcl} A& \stackrel{\Delta}{=}& \overline{c}\langle\{(A,N_A)\}_{B^+}\rangle.\\ & c(M).\\ & case\ \{M\}_{A^-}\ \text{of}\ (N_A,nb)\ \text{in}\\ & \overline{c}\langle\{nb\}_{B^+}\rangle.\\ & A\\ B& \stackrel{\Delta}{=}& c(M).\\ & case\ \{M\}_{B^-}\ \text{of}\ (x,n)\ \text{in}\\ & \overline{c}\langle\{(n,N_B)\}_{x^+}\rangle.\\ & c(M).\\ & case\ \{M\}_{B^-}\ \text{of}\ N_B\ \text{in}\ B\\ \\ sys& \stackrel{\Delta}{=}& (\nu c)A\mid B \end{array}$$

React Inter
$$\overline{\hspace{1cm}\overline{m}\langle N\rangle.p\mid m(x).Q\to P\mid [x\to N]Q}$$

Red Replace 
$$|P>P|!P$$

Note that we may want a more general let that matches more than pairs here. We'll see what the other inference rules give us.

Red Suc case 
$$suc(M)$$
 of  $0: P \ suc(x): Q > [x \to M]Q$ 

I find the case rules over naturals quite crude.

Red Sym Decrypt case 
$$\{M\}_k$$
 of  $\{x\}_k$  in  $P > [x \to M]P$ 

Additional proposed semantic rules for public/private key encryption and signature checking

Do we really want a signature check that fails to get stuck? The M is available, but the signature check does not pass. This would work if we treat  $\{|M|\}_{k^-}$  as only the signature block and not the message. A signed message may be best represented as a pair  $(M, \{|M|\}_{k^-})$  allowing the message to be explicitly available. What that construct looks like is up in the air at this point.

This rule has a more serious problem as it allows us to reproduce a message from it's signature. Specifically, if we have  $\{|M|\}_{k^-}$  and signature match is successful, then x is bound to M. That can't happen. Possibly the rule should look like this:

where |M| is the hash and not the message itself. Maybe a signature check should look something like this:

let 
$$(m, s) = (M, \{|M|\}_{k^-})$$
 in case  $s$  of  $\{|M|\}_{k^+}$  in  $P$ 

A quick reduction gives:

$$[m \to M][s \to \{|M|\}_{k^-}]$$
 case  $s$  of  $\{|M|\}_{k^+}$  in  $P$ 

Substitution gives:

case 
$$\{|M|\}_{k^-}$$
 of  $\{|M|\}_{k^+}$  in  $[m \to M][s \to \{|M|\}_{k^-}]P$ 

Finally, using the signature reduction rule:

$$[m \to M][s \to \{|M|\}_{k^-}]P$$

If the signature does not match, the process hangs. Assume  $M \neq N$ :

$$\begin{split} &\text{let }(m,s)=(M,\{|N|\}_{k^-}) \text{ in case } s \text{ of } \{|M|\}_{k^+} \text{ in } P \\ &[m\to M][s\to\{|N|\}_{k^-}] \text{case } s \text{ of } \{|M|\}_{k^+} \text{ in } P \\ &\text{case } \{|N|\}_{k^-} \text{ of } \{|M|\}_{k^+} \text{ in } [m\to M][s\to\{|M|\}_{k^-}] P \end{split}$$

This is pretty much what we want I think other than the signature check hanging on failure. I think that's what it should be, but signature check failure still results in a message that could be processed. I suppose the way to do it would be put the signature check process in parallel with a process that does not check it.

Struct Nil 
$$\frac{P \mid \mathbf{0} \equiv P}{P \mid Q \equiv Q \mid P}$$
Struct Assoc
$$\frac{P \mid (Q \mid R) \equiv (P \mid Q) \mid R}{P \mid (Q \mid R) \equiv (P \mid Q) \mid R}$$
Struct Switch 
$$\frac{(\nu m)(\nu n)P \equiv (\nu n)(\nu m)P}{(\nu n)\mathbf{0} \equiv \mathbf{0}}$$
Struct Extrusion 
$$\frac{n \notin fv(P)}{(\nu n)(P \mid Q) \equiv P \mid (\nu n)Q}$$
Struct Red 
$$\frac{P > Q}{P \equiv Q}$$
Struct Refl 
$$\frac{P \equiv Q}{P \equiv Q}$$
Struct Symm 
$$\frac{P \equiv Q}{Q \equiv P}$$
Struct Trans 
$$\frac{P \equiv Q}{P \equiv P}$$
Struct Par 
$$\frac{P \equiv P'}{P \mid Q \equiv P' \mid Q}$$
Struct Res 
$$\frac{P \equiv P'}{(\nu n)P \equiv (\nu n)P'}$$
React Struct 
$$\frac{P \equiv P' \quad P' \rightarrow Q' \quad Q' \equiv Q}{P \equiv Q}$$
React Par 
$$\frac{P' \rightarrow P'}{P \mid Q \rightarrow P' \mid Q}$$
React Res 
$$\frac{P' \rightarrow P'}{(\nu n)P \rightarrow (\nu n)P}$$

$$A \stackrel{\Delta}{=} \overline{c}\langle \{(A, N\_A)\}_{B^+}\rangle.$$

### 2.3 Privacy CA Protocol

# A Glossary

- 0 null process
- |M| hash of M
- $K^+$  public half of asymmetric key K
- $K^-$  private half of asymmetric key K
- $\{M\}_K$  encrypt M with symmetric key K
- $\{M\}_{K^+}$  encrypt M with the public key from K
- $\{M\}_{K^-}$  decrypt M with the public key from K
- $\{|M|\}_{K^-}$  sign M with the private key from K
- $\{|M|\}_{K^+}$  check signature on M with the public key from K

- $(\nu x)P$  new variable x defined in scope of P
- $\overline{c}\langle M \rangle$  send M on channel c
- c(M) receive M on channel c
- ullet !P infinite replication of P
- $\bullet P + Q P \text{ or } Q$
- $P \mid Q$  P in parallel with Q
- $\bullet$  case  $\{M\}_k$  of x in P attempt to decrypt  $\{M\}_k$  and bind to x in P if successful. Stuck if unsuccessful
- case  $\{M\}_{k^-}$  of x in P attempt to decrypt  $\{M\}_{k^+}$  and bind to x in P if successful. Stuck if unsuccessful
- case  $\{|M|\}_{k^+}$  of x in P attempt to check signature  $\{|M|\}_{k^-}$  and bind to x in P if successful. Stuck if unsuccessful
- case x of y 0 : P suc(x) : Q case splitting over integers. x is bound in Q.
- let (x,y)=M in y match M to (x,y) binding x and y to pair elements in M
- $A \stackrel{\triangle}{=} B$  define an equivalence
- $A \rightarrow B : M$  on c A sends B message M on channel c

$$A \stackrel{\Delta}{=} (\nu c) \, \overline{c} \langle M \rangle . \mathbf{0} \mid c(M) . A$$