$$\frac{N_0}{4} \int\limits_0^\infty r^2 dr \int\limits_0^\pi \sin\theta_1 d\theta_1 \int\limits_0^\pi \sin\theta_2 d\theta_2 \int\limits_0^{2\pi} \left(1 - \exp\left(-\frac{U\left(r,\theta_1,\theta_2,\varphi\right)}{kT}\right)\right) d\varphi$$

$$r = \tan\left(\frac{\pi}{2}\hat{r}\right)$$

$$\theta_1 = \pi\hat{\theta}_1$$

$$\theta_2 = \pi\hat{\theta}_2$$

$$\varphi = 2\pi\hat{\varphi}$$

$$\hat{\varphi} = \frac{1}{2\pi}\varphi$$

$$\frac{N_0}{4} \int\limits_0^1 \frac{\pi}{2} r^2 \left(1 + r^2\right) d\hat{r} \int\limits_0^1 \pi \sin\theta_1 d\hat{\theta}_1 \int\limits_0^1 \pi \sin\theta_2 d\hat{\theta}_2 \int\limits_0^1 2\pi \left(1 - \exp\left(-\frac{U\left(r,\theta_1,\theta_2,\varphi\right)}{kT}\right)\right) d\hat{\varphi} = \frac{N_0\pi^4}{4} \int\limits_0^1 r^2 (1 + r^2) d\hat{r} \int\limits_0^1 \sin\theta_1 d\hat{\theta}_1 \int\limits_0^1 \sin\theta_2 d\hat{\theta}_2 \int\limits_0^1 \left(1 - \exp\left(-\frac{U\left(r,\theta_1,\theta_2,\varphi\right)}{kT}\right)\right) d\hat{\varphi}$$