

Digital Logic Design

* Number System

Normally we use decimal system :-

$$N = d_m d_{m-1} d_{m-2} \dots d_0 d_1 d_2)_b$$

d \Rightarrow digit

b \Rightarrow base / radix

d_m \Rightarrow Most Significant Digit

d_{m-2} \Rightarrow Least Significant Digit

In decimal System

$b = 10$.

$$(325)_10 = 5 \times 10^0 + 2 \times 10^1 + 3 \times 10^2$$

$$\begin{aligned} (325)_{10} &= 0 \times 2^0 + 1 \times 2^1 + 0 \times 2^2 \\ &\quad + 1 \times 2^3 \\ &= 0 + 2 + 0 + 8 \\ &= 10 \end{aligned}$$

$$(127)_8 = 7 \times 8^0 + 2 \times 8^1 + 1 \times 8^2$$

$$= 1 + 8 \underline{+ 64}$$

Hexadecimal \rightarrow 16 digits

0 1 2 3 4 5 6 7 8 9

normal till 9.

10 A
 11 B
 12 C
 13 D
 14 E
 15 F

$$(AF)_{16} = 15 \times 16^0 + 16 \times 16^1 = 175$$

Q. $(12.23)_8 \rightarrow (\quad)_{10}$

$$\Rightarrow 2 \times 8^1 + 1 \times 8^0 + 2 \times 8^{-1} + 3 \times 8^{-2}$$

* BINARY

We use binary in digital circuit comprises of 0 & 1 i.e. it follows on-off logic.

Decimal to Binary

$(17)_{10} \rightarrow (\quad)_2$

Method 1: Identify highest power of 2 $\leq N$.

$$2^4 = 16 \leq 17$$

$4 \rightarrow 5^{\text{th}}$ bit.

1 - - - -

Do $17 - 2^4 = 1$
 $2^4 = 16 \leq 17$

$$\Rightarrow 10001$$

Q. $(127)_{10} \rightarrow (\quad)_2$

$$16^2 \\ 64 \\ 64 + 2^6$$

127.
 $2^6 \Rightarrow 64$. 7th.

63.
 $32 \Rightarrow 2^5$ 6th.

31.
 $2^4 \Rightarrow 16$ 5th.

15.
 $8 \Rightarrow 2^3$ 4th.

7.
 $2^2 \Rightarrow 4$ 3rd.

3.
 $2 \Rightarrow 2^1$ 2nd.

1.
 $1 \Rightarrow 2^0$ 1st.

$$\Rightarrow 1111111$$

Method 2: dividend remainder

2	17			
2	8	1		
2	4	0		
2	2	0		
	0	0	10001	2

MORRIS MAND
AKHIL AND KUMA
R.

Q.) $(49)_{10} \rightarrow (?)_2$

$$\begin{array}{r} 2 | 49 \\ 2 | 24 \\ 2 | 12 \\ 2 | 6 \\ 2 | 3 \\ 2 | 1 \\ 1 \end{array}$$

1 0 0 1 0 0 1

Q.) $(32.1)_{10} \rightarrow (?)_8$

$$\begin{array}{r} 8 | 32 \\ 8 | 4 \\ 0 \end{array}$$

$\Rightarrow 40$

$$\begin{aligned} 0.1 \times 8 &= 0.8 \rightarrow 0. \\ 0.8 \times 8 &= 6.4 \rightarrow 6. \\ 0.4 \times 8 &= 3.2 \rightarrow 3. \\ 0.2 \times 8 &= 1.6 \rightarrow 1. \\ 0.6 \times 8 &= 4.8 \rightarrow 4. \end{aligned}$$

$\Rightarrow (40.06314)_8$

Q.) Conversion

i) $(10.12)_{10} \rightarrow (?)_2$

for 10 it's clear.

for 0.12

$$\begin{array}{r} 0.12 \times 2 = 0.24 \quad 0 \\ 0.24 \times 2 = 0.48 \quad 0 \\ 0.48 \times 2 = 0.96 \quad 0 \\ 0.96 \times 2 = 1.92 \quad 1 \end{array}$$

to till it forms a whole number
else 4-5 digits.

$\Rightarrow (1010.0001)_2$

1

* BN
BINARY to OCTAL/HEXA

Q.) $(010\ 110\ 101 \cdot 001\ 10)_2 \rightarrow (?)_8$

$2^3 \Rightarrow 8$

so take 3 bits together

$$(010 \underline{110} \underline{101} \cdot 001 \underline{10})_2$$

$\rightarrow (2 \ 6 \ 5 \cdot 1 \ 4)_8$

$$\underline{2^4 = 16.}$$

take 4 bits together

$$\begin{array}{r} \underline{0000} \quad \underline{1011} \quad \underline{0101} \cdot \quad \underline{0011} \quad \underline{0000} \\ 0 \quad B. \quad 5 \quad - \quad 3 \quad 0. \end{array}$$

O B. 5 - 3 0.

$\Rightarrow (B^5 \cdot 30)_{16}$

$$Q) \quad \begin{array}{r} 611\ 001\cdot\ 001\ 101 \\ \hline 1\ 1\ 1\ 1 \\ \hline (3\ 1\ 1\ 5)_8 \end{array}$$

$$\begin{array}{cccc} \underline{0001} & \underline{1001} & \cdot & \underline{0011} & \underline{0100} \\ (1 & 9 & \cdot & 3 & 4) \end{array}$$

Octal to Hexa.

$$Q. \quad (321 \cdot 23)_8 - ()_{15}$$

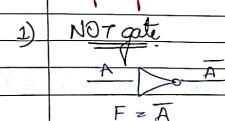
first convert to binary.

$$\begin{array}{ccccccc} & 3 & 2 & 1 & - & 2 & 3 \\ \text{(011} & \underbrace{\text{010}}_{\text{001}} & \text{)} & \cdots & \text{0010} & \underbrace{\text{011}}_{\text{1}} \end{array}_2$$

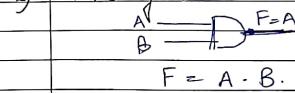
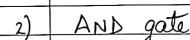
O D 1 • 4 C

$$(D_1 - 4C)_{11}$$

* Logic Gates



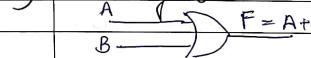
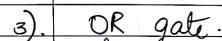
A	F
0	1
1	0



A	B	F
0	0	0
0	1	0
1	0	0
1	1	1



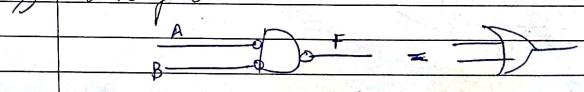
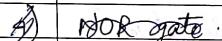
buffer

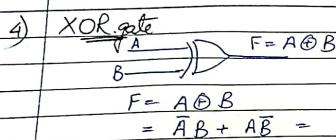


B.	A	B	F
	0	0	0
	0	-1	-1
-1		0	-1
-1			0



buffer.

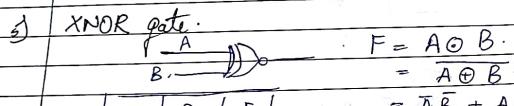




$$F = A \oplus B = \overline{A}B + A\overline{B} = A(\overline{B}) + (\overline{A})B$$

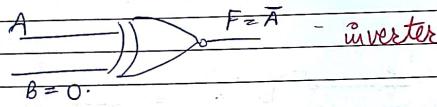
also called inequality detector.

A	B	F
0	0	0
0	1	1
1	0	1
1	1	0

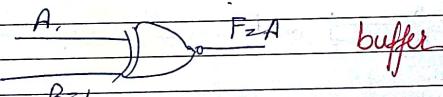


$$F = A \odot B = \overline{A} \oplus \overline{B} = \overline{A}\overline{B} + A\overline{B}$$

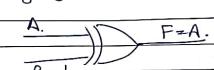
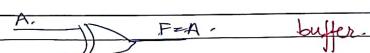
A	B	F
0	0	1
0	1	0
1	0	0
1	1	1



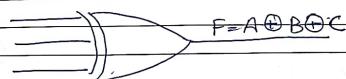
$$B=0$$



$$B=1$$



⇒ Triple Variable.



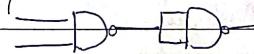
A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

⇒ for XOR → we need odd number of '1's.

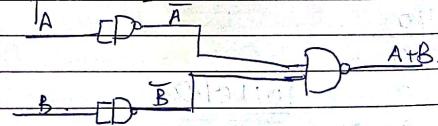
Q.) Make the following from following:
NOT from NAND



ii) AND from NAND



iii) OR from NAND



* Binary Algebra

Addition/Subtraction

$$Q. \quad \begin{array}{r} 101.11 \\ + 101.01 \\ \hline 1011.00 \end{array}$$

Add

$$\overline{0+0}=0.$$

$$1+1=10 \rightarrow 0 \text{ carry 1}$$

$$0+1=1$$

$$1+0=1$$

Sub

$$0-0=0.$$

$$1-0=1$$

$$1-1=0$$

$$0-1=-1 \Rightarrow \text{borrow}$$

$$Q. \quad \begin{array}{r} 110) 101101 (11.1 \cdot 1 \\ - 110 \\ \hline 1010 \end{array}$$

$$110$$

$$1001$$

$$110$$

$$0110$$

$$110$$

see first 8 digits
if it is smaller
take 4.

* r 's complement and $(r-1)$'s complement.

Write the magnitude of the number but the first bit is reserved for sign.

1's complement

$$\begin{array}{r} 1111 \\ - 10101 \\ \hline 01010 \end{array}$$

Either subtract from 1 or
do $0 \rightarrow 1$ $1 \rightarrow 0$ these changes.

Q) $(746)_10 \rightarrow 9$'s complement.

$$999$$

$$- 746$$

$$\boxed{253}.$$

10's complement $\rightarrow ?$

9's complement + 1

Multiplication & Division

$$Q. \quad \begin{array}{r} 111.1 \\ \times 110 \\ \hline \end{array}$$

$$\begin{array}{r} ,000.0 \\ \hline \end{array}$$

$$\begin{array}{r} .1111.0 \\ \hline \end{array}$$

$$\begin{array}{r} .101101.0 \\ \hline \end{array}$$

(746) \rightarrow 253 in 9's complement
+1
[254] .

Q. $(101011)_2 \rightarrow$ 19's & 2's complement

$(010100)_2 \rightarrow$ 1's comple.

[010101] . \rightarrow 2's complement.

Signed	1's complement	2's comp.
+5	0101	0101
-5	[1] 01	[1] 010

No change in 1's comp & 2's compl.
for +ve number.

-9	[1] 1001	[1] 0110	[1] 0111
-16	[1] 10000	[1] 01111	[1] 10000

For 2^m , we can drop sign bit.
i.e., 10000 is -16 in 2's complement.

\Rightarrow We can write copy sign bit to LHS for any number.

[1] [1] 1001 ✓

So how to recognise?

[1] 11110111 \rightarrow -ve & 2's complement
↓ find 2's compliment.

000 1000

+1
000 [100] \rightarrow 9.

Ans = -9.

Q. 110001101 \rightarrow ? 2's complement.

[1] 10001101 \rightarrow -ve.

G 01110010

+1

$$01110011 = 1 + 2 + 16 + 32 + 64. \\ = -\underline{\underline{115}}$$

* Overflow

When the output cannot be represented in our bit memory,
it is called overflow.

2's complement arithmetics

13 - 12

$$(sign) 13 - 12 \Rightarrow 13 + (-12)$$

$$13 = [0] 1101$$

$$(2's comp) - 12 \Rightarrow [1] 1100 \rightarrow 0011$$

+1

[10100] .

0 1101

1 0100

~~(+) 0001~~
carry

[00001]

Rule 1: Discard the carry

Q2 -13 + 12

(-13) + 12

-13 11 1101

0010
[110011].

12 → 110

alternate

in 2's complement; sign bit can be copied.

so, -3 = 101

-4 = 100

~~(+) 001~~

001 = +1 which is wrong.

⇒ Take atleast 1 extra bit.

Q. 1) 127 - 54

2) 17 - 32

* 1's complement Arithmetic

1) 13 - 12

13 + (-12)

13 = 1101

-12 =

~~11 1100~~

10011

001101 001101
010011 110011
+100000 100000

end around.

i.e. add this carry.

000000

+1

100001 ⇒ +1 -

Q3 -3 - 4

-3 + (-4).

(-3) → 11,

~~1101~~

-4 100

011

[11100]

,

1101

1100

1001

~~carry~~

[110001] Ans = 1001

But 110001 ≠ 1.

110 11

Q. $12 - 13$ (8 bit)
 $12 + (-13)$.

13 $0000\ 0000\ 1100$
 -12 $1111\ 1111\ 0010$

$\boxed{11111110}$

$\boxed{11000000} 1$

Q. $-3 - 4$ (8 bit).

$-3 \Rightarrow 1111\ 1100$
 $-4 \Rightarrow 1111\ 1011$

$\boxed{110000} 0111$

$+1$

$1111\ 0000\ 1000$

$\boxed{1111\ 1000}$

$1000\ 0111 \rightarrow -7$

$\begin{array}{r} 1101 \\ 10010 \end{array}$

But for

$10 \rightarrow \begin{array}{r} 1 \\ 0 \end{array} \rightarrow 0001\ 0000$
 $11 \rightarrow \begin{array}{r} 1 \\ 1 \end{array} \rightarrow 0001\ 0001$
 $12 \rightarrow \begin{array}{r} 1 \\ 2 \end{array} \rightarrow 0001\ 0010$.

* Excess 3 Code.

Add 3

0	0000	<u>0010</u>
1	0001	<u>0100</u>
2	0010	<u>0101</u>
3	0011	<u>1</u>
4	0100	<u>1</u>
5	0101	<u>1</u>
6	0110	<u>1</u>
7	0111	<u>1</u>
8	1000	$\rightarrow 1011$
9	1001	$\rightarrow 1100$

* BCD Codes. (Binary coded decimals)

0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001

eg 238

$\Rightarrow \begin{array}{r} 2 \\ 3 \\ 8 \end{array} \rightarrow 0101\ 0110\ 1011$

9's complement of 238 \rightarrow

$\begin{array}{r} 7 \\ 6 \\ 1 \\ \hline 1010\ 1001\ 0100 \\ \downarrow \quad \downarrow \quad \downarrow \\ 0101\ 0110\ 1011 \end{array}$
i.e. $238'$

* Gray Code

- Used in communication and error detection.
- 2 consecutive numbers differ at exactly 1 bit.
i.e. we can change only 1 bit.

0 →	0 0 0 0	8 →	1 1 0 0
1 →	0 0 0 1	9 →	1 1 0 1
2 →	0 0 1 1	10 →	1 1 1 1
3 →	0 0 1 0	11 →	1 1 1 0
4 →	0 1 0 0	12 →	0 1 0 0
5 →	0 1 0 1	13 →	0 1 0 1
6 →	0 1 1 0	14 →	0 0 0 1
7 →	0 1 1 1	15 →	0 0 0 0

Binary to Gray

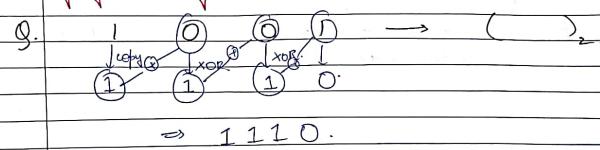


1 0 0 0

Q. 1 0 1 1 0 0 1 0

⇒ 1 1 1 0 1 0 1 1.

Gray to binary



* Sum of Product and Product of sum. and Truth Table

Q. Write a Truth-table for all numbers 0 to 7 divisible by 3.

0 → 7₃ ⇒ atleast 3 bit -

0	0 0 0	1
1	0 0 1	0
2	0 1 0	0
3	0 1 1	1
4	1 0 0	0
5	1 0 1	0
6	1 1 0	1
7	1 1 1	0

Now we can express F in 2 ways:-

Min terms / SOP
(Output = 1)

Max terms / POS
(Output = 0)

$$\Sigma (m_0, m_3, m_5)$$

$$\prod (M_1, M_2, M_3, M_4)$$

$$F = \sum (0, 3, 6)$$

$$F = m_0 + m_3 + m_6$$

$$F = \bar{A}\bar{B}\cdot\bar{C} + \bar{A}BC + A\cdot B\cdot\bar{C}$$

(Complement for '0')

$$F = \prod (M_0, M_1, M_2, M_4, M_5, M_6)$$

$$F = \prod (1, 2, 4, 5, 7)$$

$$F = M_1 \cdot M_2 \cdot M_4 \cdot M_5 \cdot M_6$$

$$F = (A+B+\bar{C}) \cdot (A+\bar{B}+C)$$

$$(A+\bar{B}+C) \cdot (\bar{A}+B+\bar{C})$$

$$(A+\bar{B}+\bar{C})$$

(Complement for '1')

* K-MAP

3 variable

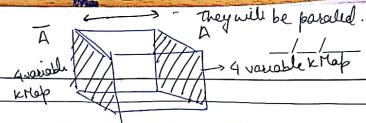
A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

A	BC			BC			BC			BC			
	$\bar{B}C$	$\bar{B}C$	BC	BC	$B\bar{C}$	$B\bar{C}$	$\bar{B}\bar{C}$	$\bar{B}\bar{C}$	$\bar{B}\bar{C}$	$\bar{B}\bar{C}$	$\bar{B}\bar{C}$	$\bar{B}\bar{C}$	
\bar{A}	000	001	011	010									
A	100	101	111	110									

* 4 variable

A	B	C	D	CD	CD	CD	CD	CD	CD	CD	CD
0	0	0	0	0	1	2	3	4	5	6	7
0	0	1	0	$\bar{A}\bar{B}$	0000	0001	0011	0010			
0	1	0	0	$\bar{A}B$	0100	0101	0111	0110			
0	1	1	0	$A\bar{B}$	1000	1001	1111	1110			
1	0	0	0	AB	1100	1101	1111	1110			
1	0	1	0	$A\bar{B}$	1000	1001	1011	1010			
1	1	0	0	AB	0100	0101	0111	0110			
1	1	1	0	$A\bar{B}$	0000	0001	0011	0010			

* 5 variable



Draw 2 K-Map, one with $x=0$ and 1 with $x=1$.

AB	CD	X = 0	AB	CD	X = 1
00	00	0	00	00	1
00	01	1	00	01	2
00	10	2	00	10	3
00	11	3	00	11	4
01	00	4	01	00	5
01	01	5	01	01	6
01	10	6	01	10	7
01	11	7	01	11	8
10	00	8	10	00	9
10	01	9	10	01	10
10	10	11	10	10	12
10	11	12	10	11	13
11	00	13	11	00	14
11	01	14	11	01	15
11	10	15	11	10	16
11	11	16	11	11	17

NOTE.

for connection b/w 2 tables.
if there is just a difference of
1 bit, they can be clubbed.
 $0 \rightarrow 16$, $8 \rightarrow 24$.

Q. Draw a K-Map for ^{state} number of states T.T.

A	B	C	F	BC
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	0

Q. $\Sigma = (01, 2, 3, 4, 6, 7) = ?$

Full Subtractor

A	B	B_{in}	Diff	B_{out}
0	0	0	0	0
0	0	1	1	1
0	1	0	1	0
0	1	1	0	0
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

for Diff

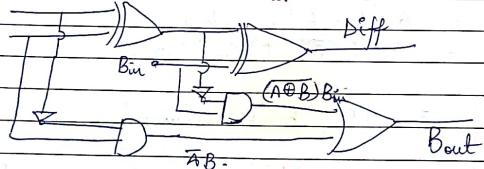
1	1	1	1
---	---	---	---

$$\Rightarrow \overline{A}B_{in} + \overline{A}B\overline{B}_{in} + A\overline{B}\overline{B}_{in} + AB_{in}$$

$$Diff = A \oplus B \oplus B_{in}$$

for B_{out}

$$B_{out} = \overline{AB} + \overline{A}B_{in} + BB_{in}$$



$$B_{out} = (A \oplus B)B_{in} + \overline{A}B.$$

$$= \overline{A}BB_{in} + \overline{A}\overline{B}B_{in} + \overline{A}B.$$

$$= ABB_{in} + \overline{A}(B + \overline{B}B_{in})$$

$$= ABB_{in} + \overline{A}B + \overline{A}B_{in}$$

$$= B(\overline{A} + A)(\overline{A} + B_{in}) + \overline{A}B_{in}$$

$$= \overline{A}B + B_{in}B + \overline{A}B_{in}.$$

$$B_{out} = \overline{A}B + B_{in}B + \overline{A}B_{in}.$$

* Comparators

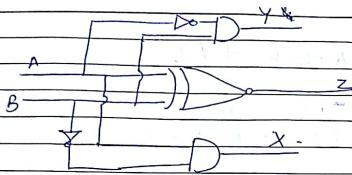
1 bit comp

A	B	$A > B$	$A < B$	$A = B$
0	0	0	0	1
0	1	0	1	0
1	0	1	0	0
1	1	0	0	1

$$x = m_2 = A\overline{B}$$

$$y = m_1 = AB$$

$$z = m_0 + m_3 = \overline{A} \cdot \overline{B} + AB \Rightarrow A \odot B \\ = A \odot B.$$



4 bit comparator.

$$\begin{array}{l} \not A \Rightarrow a_3 a_2 a_1 a_0 \\ B \Rightarrow b_3 b_2 b_1 b_0 \end{array}$$

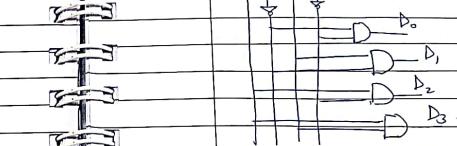
$$\Rightarrow F(A=B) = (a_3 \odot b_3) \cdot (a_2 \odot b_2) \cdot (a_1 \odot b_1) (a_0 \odot b_0)$$

$$\Rightarrow F(A \geq B) = a_3 \cdot \bar{b}_3 + (a_3 \oplus b_3) \cdot a_2 \bar{b}_2 + (a_3 \oplus b_3) \cdot (a_2 \oplus b_2) \cdot a_1 \bar{b}_1 + (a_3 \oplus b_3) \cdot (a_2 \oplus b_2) \cdot (a_1 \oplus b_1) \cdot a_0 \bar{b}_0 + (a_3 \oplus b_3) \cdot (a_2 \oplus b_2) \cdot (a_1 \oplus b_1) \cdot (a_0 \oplus b_0)$$

$$F(A \leq B) = \bar{a}_1 \cdot b_3 + (\bar{a}_2 \oplus b_3) \cdot \bar{a}_2 \cdot b_2 + (\bar{a}_3 \oplus b_3) \cdot (a_3 \oplus b_2) \\ \cdot \bar{a}_1 \cdot b_1 + (a_2 \oplus b_3) \cdot (a_3 \oplus b_1) \cdot (a_3 \oplus b_1) \cdot \bar{a}_1 \cdot b_1$$

Used to detect input combination -

A	B	D ₀	D ₁	D ₂	D ₃
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1



* Encoder

2^m input n output

	E_3	E_2	E_1	E_0	D_1	D_0	
m_8	1	0	0	0	1	1	$D_1 = E_3 \bar{E}_2 \bar{E}_1 E_0 + \bar{E}_3 E_2 \bar{E}_1 E_0$
m_7	0	1	0	0	1	0	
m_2	0	0	1	0	0	1	$D_0 = E_3 \bar{E}_2 \bar{E}_1 E_0 + \bar{E}_3 E_2 \bar{E}_1 E_0$
m_9	0	0	0	1	0	0	

e.g. if input sequence is $E_1 E_2 E_1 E_0$ not allowed.

Decoders



* Priority Encoder
Works on priority.

Priority is directly related to significance of bits.

E_3	E_2	E_1	E_0	D_1	D_0
1	X	X	X	1	1
0	1	X	X	1	0
0	0	1	X	0	1
0	0	0	1	0	0

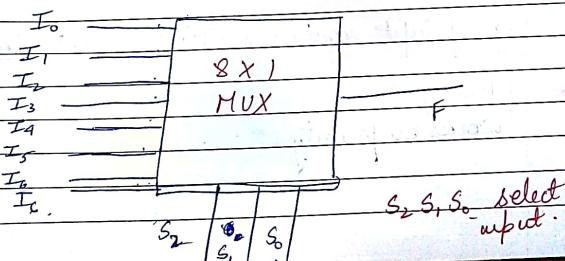
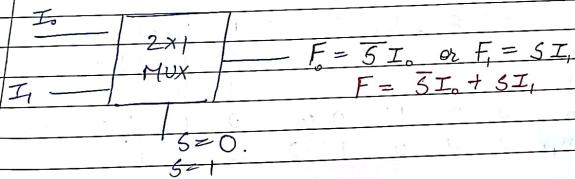
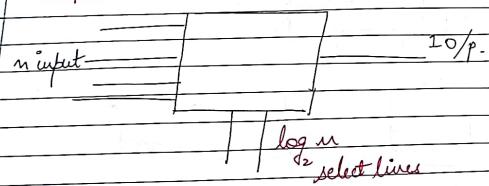
x doesn't matter

$$F = I_0 \cdot \bar{S}_2 \bar{S}_1 \bar{S}_0 + I_1 \cdot \bar{S}_2 \bar{S}_1 S_0 + I_2 \cdot \bar{S}_2 S_1 \bar{S}_0 \\ + I_3 \cdot \bar{S}_2 \bar{S}_1 S_0 + I_4 \cdot S_2 \bar{S}_1 \bar{S}_0 + I_5 \cdot S_2 \bar{S}_1 S_0 \\ + I_6 \cdot S_2 S_1 \bar{S}_0 + I_7 \cdot S_2 S_1 S_0$$

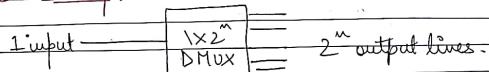
$$D_1 = E_3 + \bar{E}_3 E_2 \quad D_0 = E_3 + \bar{E}_3 \bar{E}_2 \cdot E_1$$

in truth table consider all possible case of X.

~~Multiplexers~~ Multiplexers (Data Selectors)

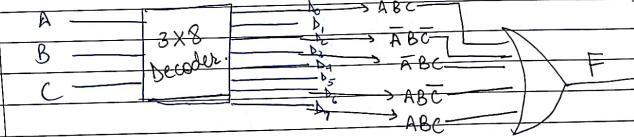


* De Multiplexer

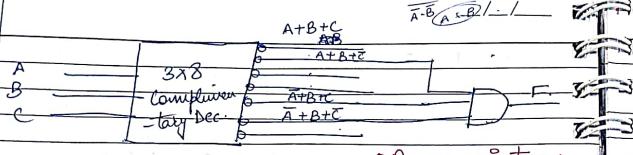


m select lines
the select lines select a output line and reflect input on that output line.

$$Q_i = \sum_m (0, 2, 3, 6, 7) \text{ in Decoder.}$$



→ Complementary Decoder.



OR use minterms with NAND gate

$$\star \Sigma_m(0, 2, 3, 6, 7) = \pi_M(1, 4, 5)$$

as $\overline{D} = D$

Q. $F = \Sigma_m(0, 2, 3, 4, 7)$ implement by Mux

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

$$F = I_0 \cdot \overline{ABC} + I_1 \cdot \overline{AB}\overline{C}$$

4x1 MUX

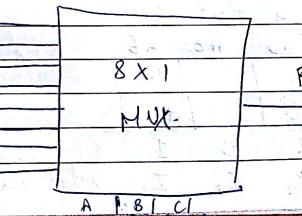
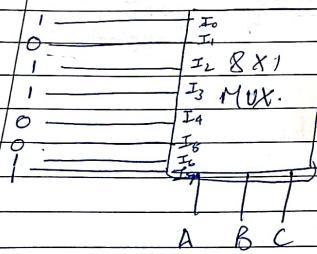
I ₀	I ₁	I ₂	I ₃
0	0	1	0
1	0	0	1
0	1	0	0
1	1	0	1

A B
any two input

pair input where A & B same & represent output
in terms of 0, 1, C

Q. $F = \pi_M(0, 1, 6, 7, 12, 15)$. 8x1 MUX

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1



$\sim \times 8c$

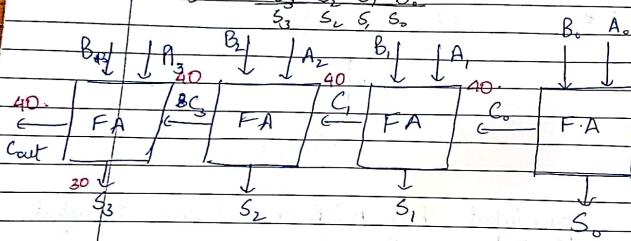
* 4 bit parallel adder.

C_0, C_1, C_2, C_3

A A_3, A_2, A_1, A_0

B B_3, B_2, B_1, B_0

S_3, S_2, S_1, S_0



If sum takes 30 ns

carry takes 40 ns

Total time = ?

$$\Rightarrow \text{sum} = 30 + 40 + 40 + 30$$

$$= 150 \text{ ns}$$

$$\text{carry} = 40 + 40 + 40 + 40$$

$$= 160 \text{ ns}$$

NOTE

for a 4×1 MUX in Question

$\Sigma_m (0, 2, 3, 6, 7)$

To choose select lines

$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
1	0	1	0
0	1	0	1
1	1	1	1

I_0, I_1, I_2, I_3 . select line $A \& B$.

-/-

-/-

$\bar{A}\bar{C}, \bar{A}C, AC, A\bar{C}$

\bar{B}, B, B, B

I_0, I_1, I_2, I_3

select line = AC

* Decoder using Enable

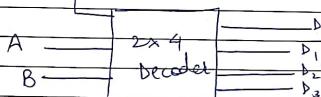
2 kinds of enable

high (1)

low (0)

decoder works - output always

eg. 2×4



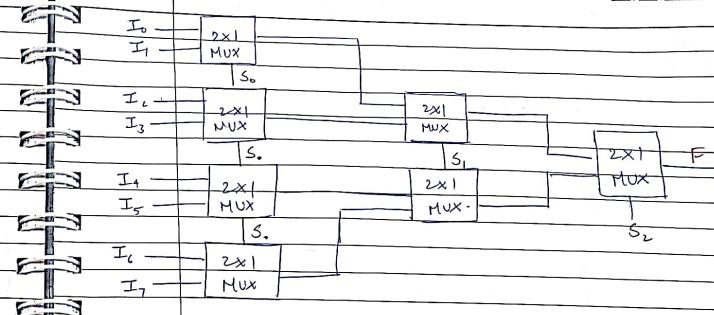
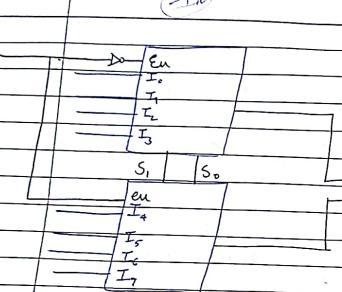
\bar{E}_n	A	B	D ₀	D ₁	D ₂	D ₃
1	X	X	0	0	0	0
0	0	0	1	0	0	0
0	0	1	0	1	0	0
0	1	0	0	0	1	0
0	1	1	0	0	0	1

8x1 MUX by 4×1 MUX.

Now, in 8x1 MUX we need 3 select lines.

S_2, S_1, S_0

Selecting S_2, S_1, S_0 for 4×1



but we need to select 1 number so we need 3 bit.

(for 0 & 4
0/00 1/00)

8x1 using 2x1 MUX.

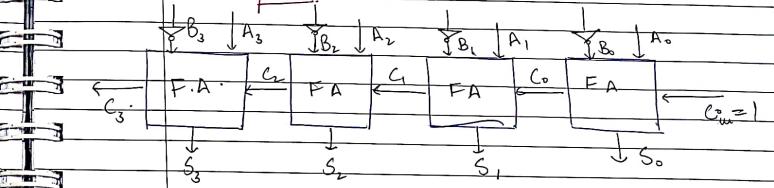
$$\text{making } n \times 1 \text{ MUX from } m \times 1 \text{ MUX.} \\ = \left(\frac{n \times 1}{m} \right) \times 1 + \left(\frac{n \times 1}{m \times 1} \right) \text{ MUX needed.} \\ \pm 1 \text{ OR gate.}$$

$$\text{eg } \left(\frac{8 \times 1}{2 \times 1} \right) \times 1 + \left(\frac{8 \times 1}{2 \times 1} \right)$$

$$= 2 + 4$$

$$= 6 \quad 2 \times 1 \text{ MUX.}$$

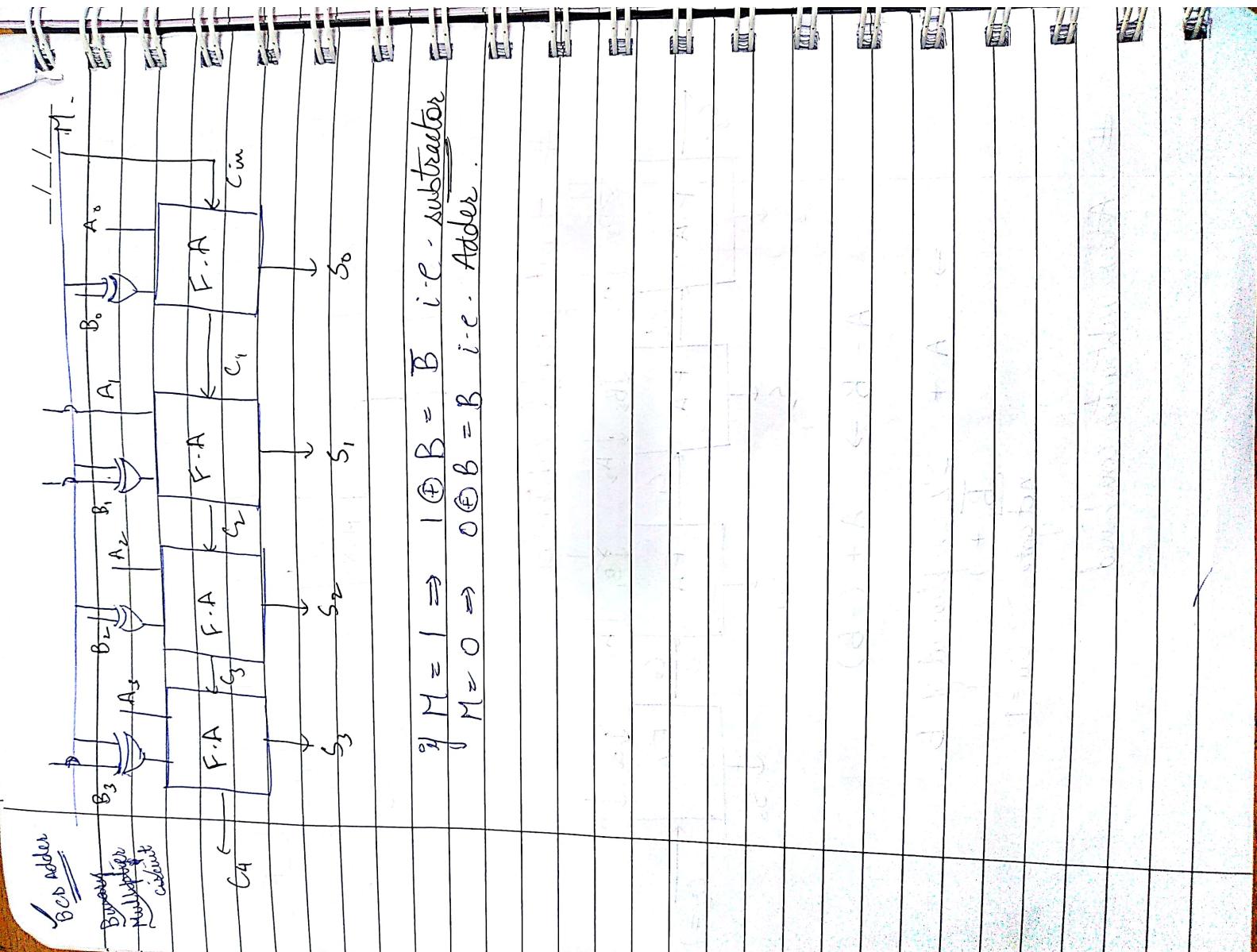
4 bit parallel subtractor



$$A - B \Rightarrow A + (-B)$$

$$\Rightarrow A + 2^{\text{bit}} \text{ complement of } B. \\ \overline{B + } \text{ not gate } \rightarrow C_{in} = 1.$$

Adder subtractor combined



$\text{if } M = 1 \Rightarrow 1 \oplus B = \bar{B} \text{ i.e. subtractor}$
 $M = 0 \Rightarrow 0 \oplus B = B \text{ i.e. Adder.}$