

PERFORMANCE PARAMETER

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PERFORMANCE PARAMETER

Basics

There are various parameters in Machine Learning that are useful to compare performance or score of different algorithms

Syntax : *from sklearn import metrics*
 from sklearn import stats

The parameters are used for :

- (a) Correlation between different features of the same dataset.
- (b) Comparing score of dataset with itself or other algorithms
- (c) Analyzing Statistical values of univariate, bivariate

COEFFICIENT

They are the estimators of unknown population parameters and describe relationship between predictor variable and response.

Sign indication :

“ + ” : With increase in predictor value, the response increases

“ - ” : With decrease in predictor value, the response decreases

Note, this relationship holds if others variables remain constant

Coefficient Example

Predictors			Actual Y
X1	X2	X3	Y
10	2.5	7.6	4.4125
2	1.5	2.4	2.1275
6	7.5	9.6	10.5975
4	3.5	3.7	7.9575
6	4.5	5	10.7825
6	1.5	2.3	7.1675
4	3.5	6.2	2.9575
0	7.5	7.3	7.9375
8	2.5	4.9	7.3925
2	9.5	11.2	8.5675

Coefficient

$$X1 * 1.21 + X2 * 3.005 - X3 * 2$$

INTERCEPTS



Basics

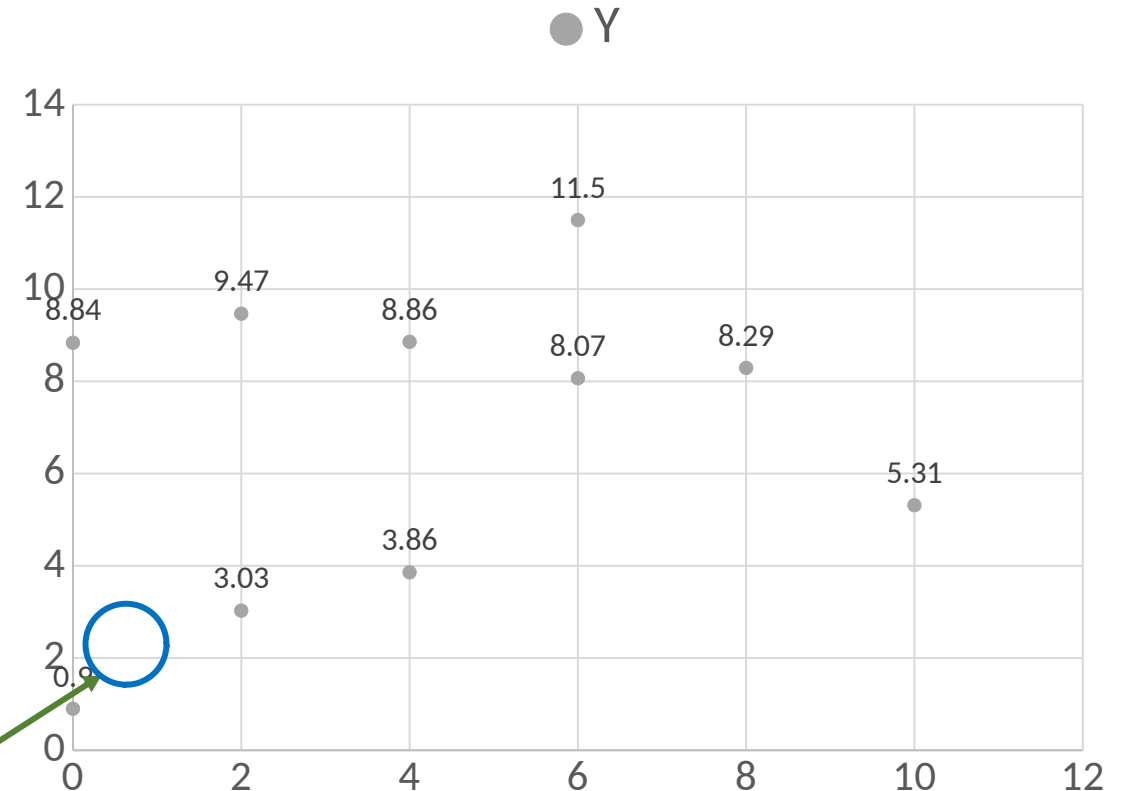
Practically, it doesn't apply anything so don't try to focus much on questions why $y = 0$ or y is negative.

One of the purpose of this constant is that it forces the residuals to have the crucial zero mean.

If we omit this constant, then every regression line will pass through $(0, 0)$ forcing other variables to 0 as well.

Intercept Example

X1	X2	X3	Y
10	2.5	7.6	5.3125
2	1.5	2.4	3.0275
6	7.5	9.6	11.4975
4	3.5	3.7	8.8575
0	0	0	0.9
6	1.5	2.3	8.0675
4	3.5	6.2	3.8575
0	7.5	7.3	8.8375
8	2.5	4.9	8.2925
2	9.5	11.2	9.4675



Intercept

$$0.9 + X1 * 1.21 + X2 * 3.005 - X3 * 2$$

SUM OF SQUARES



Basics

Sum of Squares (SS) is simply defined as Sum of squared differences between two values

Formula : $SS = (columnName1 - columnName2) ^ 2$

In itself, it doesn't have any information.

But, when they are applied to find errors or mean difference, they imply a significant role to find the resultant.

For SS, you just have to omit denominator part.



SS Example

Formula : $SS = (columnName1 - columnName2) ^ 2$

X	μ	$Y - \mu$	$(Y - \mu)^2$
13	15	-2	4
16	15	1	1
10	15	-5	25
20	15	5	25
13	15	-2	4
18	15	3	9
			68

SS
↓

$$\text{Variance} = \frac{\sum (Y - \mu)^2}{n} = \frac{68}{6} = 11.33$$

RESIDUAL SUM OF ERROR (RSE)

Basics

Residual Sum of Errors (RSE) is defined as Sum of errors between two features.

Formula : $RSE = (y_{test} - y_{predicted})$

A residual is defined as the error caused due to difference between 2 features.
RSE is sum of residuals.



RSE Example

Syntax : $RSE = \Sigma(columnName1 - columnName2)$

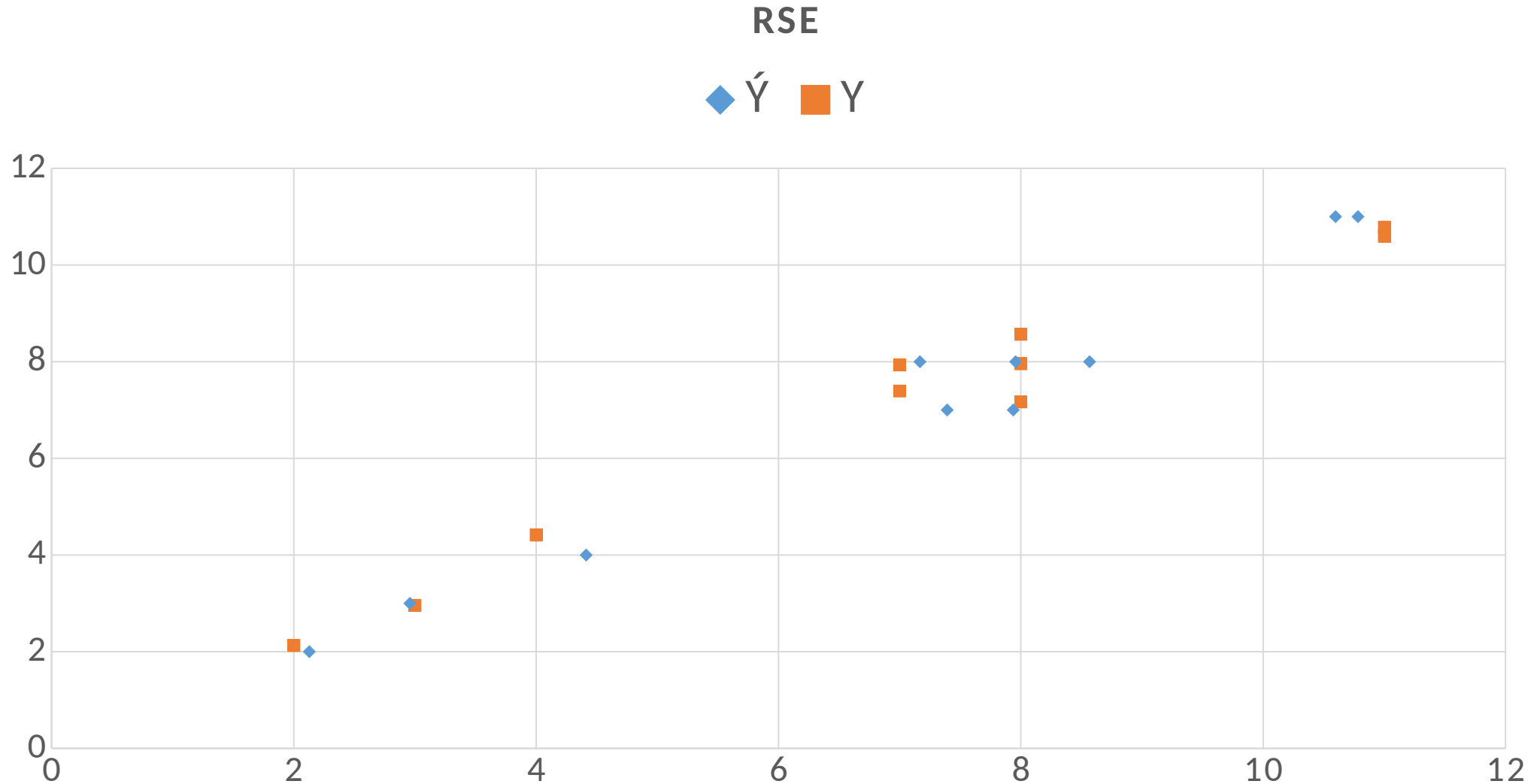
Predictors			Actual Y	Predicted Y	Error
X1	X2	X3	Y	Ŷ	Y - Ŷ
10	2.5	7.6	4.4125	4	0.4125
2	1.5	2.4	2.1275	2	0.1275
6	7.5	9.6	10.598	11	-0.4025
4	3.5	3.7	7.9575	8	-0.0425
6	4.5	5	10.783	11	-0.2175
6	1.5	2.3	7.1675	8	-0.8325
4	3.5	6.2	2.9575	3	-0.0425
0	7.5	7.3	7.9375	7	0.9375
8	2.5	4.9	7.3925	7	0.3925
2	9.5	11.2	8.5675	8	0.5675
					0.9

Residual

Residual Sum of Error (RSE)

Total

RSE Example



SUM OF SQUARED ERRORS

RSS Basics

Residual Sum of Squares (RSS) is defined as Sum of squared errors between the actual and predicted response.

Formula : $RSS = (y_{test} - y_{predicted})^2$

RSS is used to find MSE and RMSE.

Lower the value, better is the ML model.

It is the quantity used in defining an error which is not explained by the model.
We try to minimize the error as small as possible.



ESS Basics

Explained Sum of Squares (ESS) is defined as Sum of squared errors between the actual and mean response.

Formula : $ESS = (y_{test} - \text{mean}(y_{test}))^2$

Higher the value, better is the ML model.

It is the quantity used in describing the error (or irregularity or variance) which is explained by the model.



TSS Basics

Total Sum of Squares (TSS) is defined as sum of squared residual errors and sum of squared explained errors.

Syntax : $TSS = RSS + ESS$

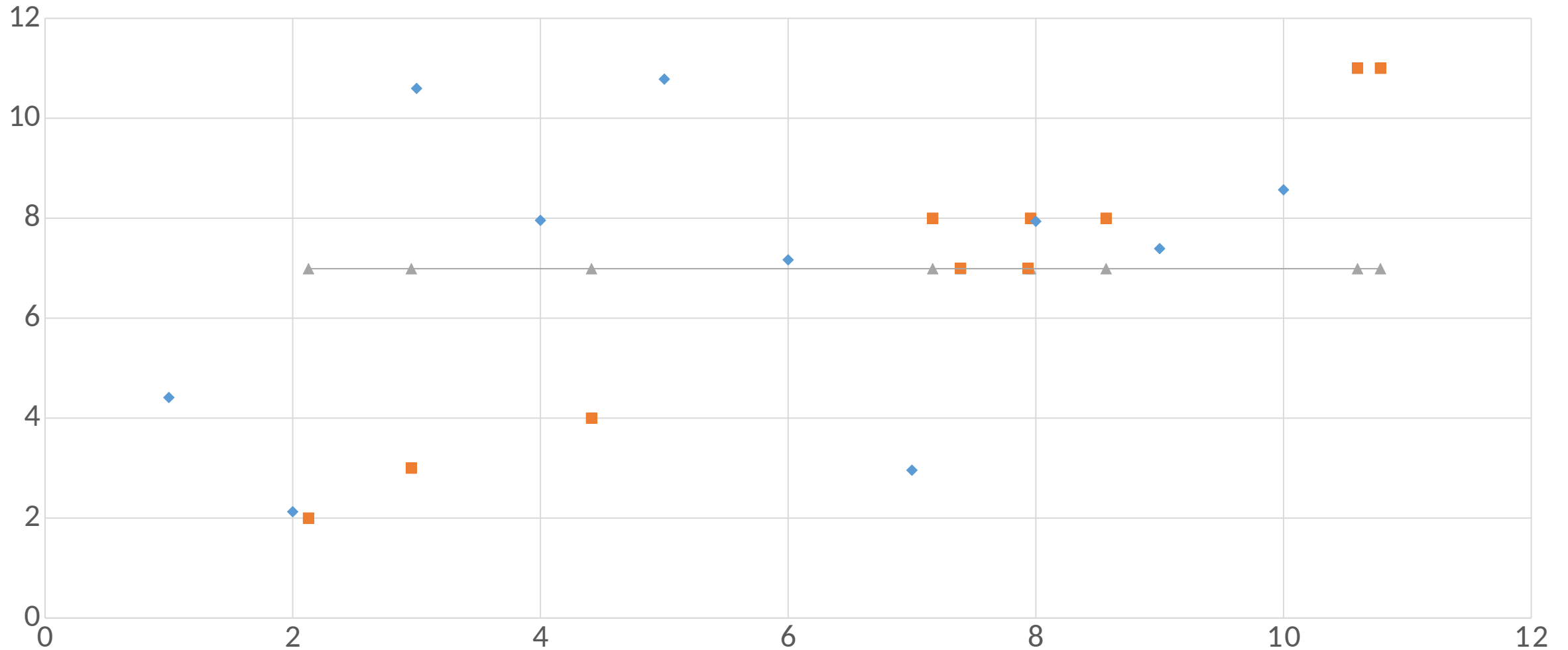
It is used to find r-squared to get the accuracy measure of model

SSE Example

Predictors			Actual Y	Mean Y	Expained Y	Expained Y^2	Predicted Y	Error	Error^2
X1	X2	X3	Y	μ	$Y - \mu$	$(Y - \mu)^2$	\hat{Y}	$Y - \hat{Y}$	$(Y - \hat{Y})^2$
10	2.5	7.6	4.4125	6.99	-2.5775	6.64350625	4	0.4125	0.17016
2	1.5	2.4	2.1275	6.99	-4.8625	23.64390625	2	0.1275	0.01626
6	7.5	9.6	10.598	6.99	3.6075	13.01405625	11	-0.4025	0.16201
4	3.5	3.7	7.9575	6.99	0.9675	0.93605625	8	-0.0425	0.00181
6	4.5	5	10.783	6.99	3.7925	14.38305625	11	-0.2175	0.04731
6	1.5	2.3	7.1675	6.99	0.1775	0.03150625	8	-0.8325	0.69306
4	3.5	6.2	2.9575	6.99	-4				
0	7.5	7.3	7.9375	6.99	0				
8	2.5	4.9	7.3925	6.99	0				
2	9.5	11.2	8.5675	6.99	1				
						RSS	ESS		TSS
						$\Sigma(Y - \hat{Y})^2$	$\Sigma(Y - \mu)^2$		RSS + ESS
						2.4474125	78.4614125		80.908825

SSE Example

◆ Y ■ \hat{Y} ▲ μ — Linear (μ)



R SQUARED (R^2)

R² Basics

It is also known as the coefficient of determination.

It simply measures how close the data are to the fitted regression line, ie, it is the percentage of the response variable explained by the model.

It is the statistical tool used for indicating the variance of the dependent variable that is to be predicted from the independent variable.

Formula : $R^2 =$ n = observations

Syntax : `from sklearn import metrics`
`metrics.r2_score(y_test - y_predicted)`

R² Basics

R² varies from 0% to 100%.

0% means that model explains none of the variability of response data around its mean.

100% means that model explains all variability of response data around its mean.

In general, higher the R² better the model fits the data.

Limitation :

1. R² can't determine if coefficient estimator and predictor are biased. This is because, R² increases with increase in number of predictors. (so, watch residual plots also before making a decision)
2. We can have low R² for good model or high R² for not a good model.

CONFUSION MATRIX



Basics

Confusion Matrix gives the metrics output that describes the complete performance of the model.

It helps to determine in predicting the few parameters that defines accuracy of the model.

Syntax : *from sklearn import metrics*
metrics.confusion_matrix(y_test , y_predicted)

	Predicted 'Yes'	Predicted No'
Actual 'Yes'	True Positive	False Negative
Actual 'No'	False Positive	True Negative

Important Terms :

True Positives : The cases in which we predicted YES and the actual output was also YES.

True Negatives : The cases in which we predicted NO and the actual output was NO.

False Positives (Type 1 Error) : The cases in which we predicted YES and the actual output was NO.

False Negatives (Type 2 Error) : The cases in which we predicted NO and the actual output was YES.

Confusion Matrix Example

Age	Education	Gender	Pocket Money	Hobby	Will Invest	Predicted
19	Graduation	Girl	100	Cooking	Yes	Yes
20	Graduation	Boy	200	Cooking	Yes	Yes
20	Graduation	Boy	100	Jogging	No	No
16	Graduation	Girl	100	Jogging	No	No
16	Graduation	Girl	300	Jogging	No	No
19	Graduation	Boy	100	Jogging	Yes	Yes
20	Graduation	Girl	200	Dancing	No	Yes
19	Graduation	Girl	500	Cooking	Yes	No
22	Post Graduation	Girl	200	Jogging	No	Yes
22	Post Graduation	Boy	500	Dancing	Yes	Yes
22	Post Graduation	Girl	500	Dancing	Yes	No
19	Graduation	Boy	500	Jogging	No	Yes
19	Graduation	Girl	200	Dancing	No	Yes
16	Graduation	Girl	100	Cooking	No	Yes
22	Post Graduation	Boy	200	Dancing	No	No
16	Graduation	Boy	300	Dancing	Yes	Yes

Confusion Matrix Example

Age	Education	Gender	Pocket Money	Hobby	Will Invest	Predicted
19	Graduation	Girl	100	Cooking	Yes	Yes
20	Graduation	Boy	200	Cooking	Yes	Yes
20	Graduation	Boy	100	Jogging	No	No
16	Graduation	Girl	100	Jogging	No	No
16	Graduation	Girl	300	Jogging	No	No
19	Graduation	Boy	100	Jogging	Yes	Yes
20	Graduation	Girl	200	Dancing	No	Yes
19	Graduation	Girl	500	Cooking	Yes	No
22	Post Graduation	Girl	200	Jogging	No	Yes
22	Post Graduation	Boy	500	Dancing	Yes	Yes
22	Post Graduation	Girl	500	Dancing	Yes	No
19	Graduation	Boy	500	Jogging	No	Yes
19	Graduation	Girl	200	Dancing	No	Yes
16	Graduation	Girl	100	Cooking	No	Yes
22	Post Graduation	Boy	200	Dancing	No	No
16	Graduation	Boy	300	Dancing	Yes	Yes

True Positive

Confusion Matrix Example

Age	Education	Gender	Pocket Money	Hobby	Will Invest	Predicted
19	Graduation	Girl	100	Cooking	Yes	Yes
20	Graduation	Boy	200	Cooking	Yes	Yes
20	Graduation	Boy	100	Jogging	No	No
16	Graduation	Girl	100	Jogging	No	No
16	Graduation	Girl	300	Jogging	No	No
19	Graduation	Boy	100	Jogging	Yes	Yes
20	Graduation	Girl	200	Dancing	No	Yes
19	Graduation	Girl	500	Cooking	Yes	No
22	Post Graduation	Girl	200	Jogging	No	Yes
22	Post Graduation	Boy	500	Dancing	Yes	Yes
22	Post Graduation	Girl	500	Dancing	Yes	No
19	Graduation	Boy	500	Jogging	No	Yes
19	Graduation	Girl	200	Dancing	No	Yes
16	Graduation	Girl	100	Cooking	No	Yes
22	Post Graduation	Boy	200	Dancing	No	No
16	Graduation	Boy	300	Dancing	Yes	Yes

True Negative



Confusion Matrix Example

Age	Education	Gender	Pocket Money	Hobby	Will Invest	Predicted
19	Graduation	Girl	100	Cooking	Yes	Yes
20	Graduation	Boy	200	Cooking	Yes	Yes
20	Graduation	Boy	100	Jogging	No	No
16	Graduation	Girl	100	Jogging	No	No
16	Graduation	Girl	300	Jogging	No	No
19	Graduation	Boy	100	Jogging	Yes	Yes
20	Graduation	Girl	200	Dancing	No	Yes
19	Graduation	Girl	500	Cooking	Yes	No
22	Post Graduation	Girl	200	Jogging	No	Yes
22	Post Graduation	Boy	500	Dancing	Yes	Yes
22	Post Graduation	Girl	500	Dancing	Yes	No
19	Graduation	Boy	500	Jogging	No	Yes
19	Graduation	Girl	200	Dancing	No	Yes
16	Graduation	Girl	100	Cooking	No	Yes
22	Post Graduation	Boy	200	Dancing	No	No
16	Graduation	Boy	300	Dancing	Yes	Yes

False Positive

Confusion Matrix Example

Age	Education	Gender	Pocket Money	Hobby	Will Invest	Predicted
19	Graduation	Girl	100	Cooking	Yes	Yes
20	Graduation	Boy	200	Cooking	Yes	Yes
20	Graduation	Boy	100	Jogging	No	No
16	Graduation	Girl	100	Jogging	No	No
16	Graduation	Girl	300	Jogging	No	No
19	Graduation	Boy	100	Jogging	Yes	Yes
20	Graduation	Girl	200	Dancing	No	Yes
19	Graduation	Girl	500	Cooking	Yes	No
22	Post Graduation	Girl	200	Jogging	No	Yes
22	Post Graduation	Boy	500	Dancing	Yes	Yes
22	Post Graduation	Girl	500	Dancing	Yes	No
19	Graduation	Boy	500	Jogging	No	Yes
19	Graduation	Girl	200	Dancing	No	Yes
16	Graduation	Girl	100	Cooking	No	Yes
22	Post Graduation	Boy	200	Dancing	No	No
16	Graduation	Boy	300	Dancing	Yes	Yes

False Negative

CLASSIFICATION REPORT

Classification Report is used to measure the quality of predictions.

The report shows the main classification metrics precision, recall and f1-score on a per-class basis. The metrics are calculated by using true and false positives, true and false negatives.

Syntax : *from sklearn import metrics*
 metrics.classification_report(y_test , y_predicted)

Basics

Age	Education	Gender	Pocket Money	Hobby	Will Invest	Predicted
19	Graduation	Girl	100	Cooking	Yes	Yes

	Predicted 'Yes'	Predicted No'
Actual 'Yes'	TP = 5	FN = 2
Actual 'No'	FP = 5	TN = 4

Type II Error

Type I Error

22	Post Graduation	Boy	500	Dancing	Yes	Yes
22	Post Graduation	Girl	500	Dancing	Yes	No
19	Graduation	Boy	500	Jogging	No	Yes
19	Graduation	Girl	200	Dancing	No	Yes
16	Graduation	Girl	100	Cooking	No	Yes
22	Post Graduation	Boy	200	Dancing	No	No
16	Graduation	Boy	300	Dancing	Yes	Yes

Classification Report Parameters

(a) Accuracy : It is defined as the total number of correct predictions to the total number of sample size

Age	Education	Predicted 'Yes'	Predicted No'	
19	Graduate	5	2	7 TP + FN
20	Graduate			
20	Graduate			
16	Graduate	5	4	9 FP + TN
16	Graduate			
19	Graduate			
20	Graduate	10	6	16
19	Graduate	TP + FP	FN + TN	
22	Post Graduate			
22	Post Graduate			
22	Post Graduate			
19	Graduate			
19	Graduate			
16	Graduate			
22	Post Graduate			
16	Graduate			

Accuracy / Classification Rate / Support		
TP + TN	=	9
TP + TN + FP + FN	=	16

Accuracy

Classification Report Parameters

(b) Misclassification Rate : It is defined as the total number of incorrect predictions to the total number of sample size

Age Education		Predicted 'Yes' Predicted No'				
19	Graduation	Actual 'Yes'	5	2	7 TP + FN	
20	Graduation					
20	Graduation	Actual 'No'	5	4	9 FP + TN	
16	Graduation					
16	Graduation		10	6	16	
19	Graduation		TP + FP	FN + TN		
20	Graduation					
19	Graduation					
22	Post Graduation					
22	Post Graduation					
22	Post Graduation					
19	Graduation					
19	Graduation					
16	Graduation					
22	Post Graduation					
16	Graduation					

Misclassification Rate		
FP + FN	=	7
		0.44
TP + TN + FP + FN		16

classification Rate

Misclassification Rate

$$\frac{FP + FN}{TP + TN + FP + FN} = \frac{7}{16} = 0.44$$



Classification Report Parameters

(c) Recall : It is defined as the fraction of actual positives that were correctly identified.

Age	Educa		Predicted 'Yes'	Predicted No'	
19	Grad	Actual 'Yes'	5	2	7 TP + FN
20	Grad				
20	Grad	Actual 'No'	5	4	9 FP + TN
16	Grad				
16	Grad		10	6	16
19	Grad		TP + FP	FN + TN	
20	Grad				
19	Grad				
22	Post Gr				
22	Post Gr				
22	Post Gr				
19	Grad	Recall			
19	Grad				
16	Grad	TP	=	5	0.71
22	Post Gr	TP + FN		7	
16	Grad				

➤ **Recall**



Classification Report Parameters

(d) Precision : It is defined as accuracy of positive predictions.

Age Educ		Predicted 'Yes'	Predicted No'	
19 Gra	Actual 'Yes'	5	2	7 TP + FN
20 Gra	Actual 'No'	5	4	9 FP + TN
20 Gra				
16 Gra				
16 Gra		10	6	16
19 Gra				
20 Gra		TP + FP	FN + TN	
19 Gra				
22 Post C				
22 Post C				
22 Post C				
19 Gra	Precision			
19 Gra	TP =	5	0.50	
16 Gra				
22 Post C				
16 Gra	TP + FP	10		

► **Precision**

THANK YOU

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