CS351 Introduction to Computer Graphics

Test A: Shape
100 pts max.
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(netID is 6 letters + 6digits, e.g. jet861)

**INSTRUCTIONS: Edit this file in Microsoft Word or in Google Docs to enter your HIGHLIGHTED answers. Upload your own file on Canvas before the end of the day Sunday, Jan 31, 2016.**

1) Suppose that:

- Our HTML5 on-screen display canvas is square (height==width) and displays WebGL output, and we wrote a Javascript 'drawAxes()' function that causes WebGL to:
  - --draw an arrow from the origin to (+1,0,0) to depict the x axis, and
  - --draw an arrow from the origin to (0,+1,0) to depict the y axis, and
- In JavaScript we send the 4x4 'modelMatrix' as a uniform to the graphics hardware, and
- In GLSL, our Vertex shader applies that uniform matrix to all vertex positions before drawing

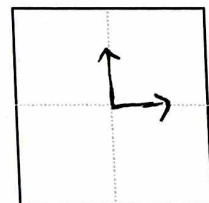The on-screen result of this sequence of statements is:

```
modelMatrix.setIdentity();  // set to identity matrix.
drawAxes();                 // draw it!
```
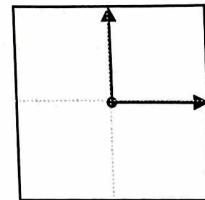
(HINT: All arrows stay entirely within the square canvas for all answers)
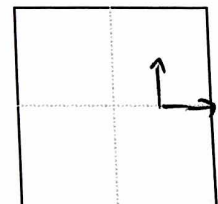
1a) (5pts) Sketch the on-screen result if you used these statements instead:

```
modelMatrix.setIdentity();
modelMatrix.scale(0.5, 0.5, 0.5);   // shrink to 50%
drawAxes();                         // draw it!  ANS: →→→
```
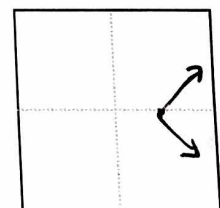
1b) (5pts) Sketch the on-screen result if you used these statements instead:

```
modelMatrix.setIdentity();
modelMatrix.scale(0.5, 0.5, 0.5);     // shrink to 50%
modelMatrix.translate(1.0, 0.0, 0.0); // move +x by 1
drawAxes();                           // draw it! ANS: →→→
```

1c) (5pts) Sketch the on-screen result if you used these statements instead:

```
modelMatrix.setIdentity();
modelMatrix.translate(0.5, 0.0, 0.0); // move +x by .5
modelMatrix.scale(0.5, 0.5, 0.5);     // shrink to 50%
modelMatrix.rotate(-45.0,0.0,0.0,1.0);// z-axis rotate
drawAxes();                           // draw it! ANS: →→→
```

1d) (5pts) Sketch the on-screen result if you used these statements instead:

```
modelMatrix.setIdentity();
modelMatrix.translate(0.5, 0.0, 0.0);  // move +x by .5
modelMatrix.scale(0.5, 0.5, 0.5);      // shrink to 50%
modelMatrix.rotate(-45.0,0.0,0.0,1.0); // z-axis rotate
modelMatrix.translate(-1.0, 0.0, 0.0); // move +x by 1
drawAxes();                            // draw it! ANS: →→→
```
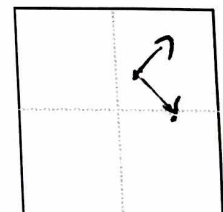
2) (16pts) TRUE/FALSE: (copy-and-paste your choice of these highlighted answers "True" or "False")

a) ___True___ Drawing commands for WebGL and drawing commands for HTML5 'canvas' elements use different on-screen drawing axes; one has its origin at the upper left corner.

b) ___True___ WebGL *requires* users to specify all vertex positions using real values (float/double). This requirement ensures that limited precision never introduces rendering flaws on-screen.

c) ___False___ WebGL provides its own built-in functions that can create a 4x4 matrix for translation, for rotation, or for scale, each from a single function call, as well as a push-down stack for them.

d) ___True___ All the many parameters kept as state variables by WebGL, such as background color, buffer bindings, depth testing, etc., are 'write-only': you can't read any of their current values.

e) ___True___ Every WebGL/HTML5/JavaScript program that can draw WebGL drawing primitives on-screen (e.g. TRIANGLES) must include both a 'Vertex Shader' and a 'Fragment Shader'.

f) ___False___ With proper selection of 'stride' and 'offset', WebGL can render the contents of a vertex buffer object (VBO) that holds 100 vertex positions, followed 100 vertex colors, followed by 100 vertex surface normals. In this VBO, the attributes are NOT interleaved!

g) ___True___ WebGL permits you to use the same 'uniform' variable to send values to both the Vertex Shader and Fragment Shader. If JavaScript sets its value, then both shaders can use it.

h) ___False___ WebGL itself provides built-in functions for mouse, keyboard, and window-system interactions. We use HTML and JavaScript functions instead because they're more convenient.

HIGHLIGHT your one choice to mark your answer.
3) (4pt) What are the dimensions of the 'Canonical View Volume' (CVV) in openGL?
   a) adjustable—specified indirectly HTML commands for 'canvas' object where WebGL renders.
   b) adjustable—call the ~~gl.setCVV~~() command. Default is unit cube: (+/-1, +/-1, +/-1))
   c) Fixed—a unit cube centered at the origin: (+/-1, +/-1, +/-1)
   d) Fixed—a unit cube, with x,y,z origin shown at the lower-left corner of the display window.
   e) Fixed—a unit cube, with x,y,z origin shown at the upper-left corner of the display window.

4)(3pt) Calculate the area of a triangle whose sequence of vertices lie at these three (x,y,z) positions:
   (1,2,3), (-3,3,-4), (3,-4, 5). Briefly, show your work in the space below.
   (HOW? see assigned readings: Chap 2,3 Lengyel " Math for 3D…" posted on Canvas)

$$A = \sqrt{s(s-a)(s-b)(s-c)}, \quad s = \frac{a+b+c}{2}$$

distance formula: $\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2 + (z_2-z_1)^2}$

$a = \sqrt{4^2 + 1^2 + 7^2} = \sqrt{66} = 8.12$ (etc for b, c)

$b = 6.63 \quad c = 12.88 \quad s = 13.82$

AREA = (23.07   )

5)(3pt) Calculate the surface normal vector for that same triangle: be sure to 'normalize' the vector to ensure its length is 1.0. (Again, see Lengyel "Math for 3D…" reading posted on Canvas).

normal vector (nx,ny,nz) == (-.87, -.13, .49)   (write 3 numbers, not expressions!)

$Normal = A \times B$

$A = (1+3)\hat{i} + (2-3)\hat{j} + (3+4)\hat{k} = 4\hat{i} - \hat{j} + 7\hat{k}$

$B = (1-3)\hat{i} + (2+4)\hat{j} + (3-5)\hat{k} = -2\hat{i} + 6\hat{j} - 2\hat{k}$

$= -40\hat{i} - 6\hat{j} + 22\hat{k}$

→ normalize $\frac{v}{|v|}$

Scene Graph: This 'scene graph' describes a jointed 3D object:
--Each **letter** is a transformation node (*e.g.* holds a 4x4 matrix that combines rotation, translation, scale, etc.)
--Each **gridded ellipse** is a 'group' node, where we have uniquely defined 'drawing axes' (a coordinate system)
--Each **square** holds vertices (fixed, in a VBO) & shape-drawing fcns (*e.g.* 'drawAxes()', 'drawCube()', etc.)

The root of the tree shown begins in the 'CVV' coordinate system, and each leaf of the tree ends in its own separate coordinate system where we draw a shape (s0,s1,s2, etc.), defined by fixed sets of vertices.
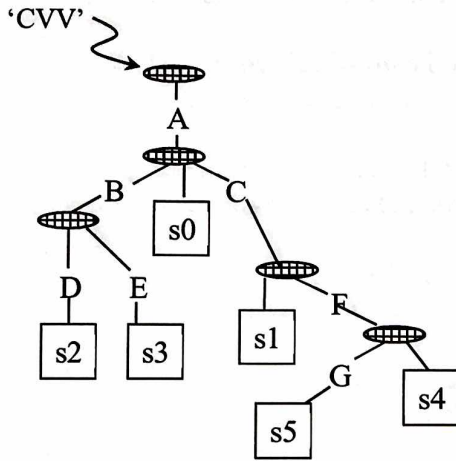
RECALL THAT:
All our matrix transformation commands presume:
a) Vertices are 4-element column vectors;
b) When the current transform matrix [M] multiplies a given vertex v to make v', we get v' = [M]v, and
c) Any transform command (*e.g.* `rotate()`, `translate()`, `scale()`) multiplies the current matrix M with a new matrix that 'precedes' it's effect on vertices. Thus a call to `rotate()` will replace current matrix [M] with the result of this matrix multiply: [M][R], which we write as [MR].   If applied to the *coordinate values* for a vertex, the result is the same as multiplying by [R], and then by [M].
BUT we could also interpret these same calculations as: "Starting from the CVV, we first transform the drawing axes by [M], then transform these new drawing axes by [R]."

6) (8pts) Suppose we write software that traverses the tree and draws the entire scene, using pushMatrix() and popMatrix() as necessary.   When we issue the drawing commands contained in scene-graph node s5,
what are the contents of our current matrix?
(HIGHLIGHT YOUR ONE ANSWER)
a)   [A]
b)   [G]
c)   [ACFG]
d)   [GFCA]
e)   [AGCF]
f)   [GAFC]
g)   Something else:_____

7) (6pts) List *all* transform nodes that can modify the on-screen result for each shape. For example, shape s2 *might* change on-screen if we modified transform D, but G can't change s2.
Write your answers as comma-separated lists of letters, such as (A,B,C,D,E).

s0: A   s3: A B E

s1: A C   s4: A C F

s2: A B D   s5: A C F G

VERTEX / VECTOR MATH:
Use these x,y,z coordinates for the 3D points **P0, P1**, the origin, and the 3D vectors **V0,V1**:

```
NAME:   x,  y,  z,  w          NAME:  x,  y,  z,  w
  P0:   1,  2,  3   ?            V0:   3,  2,  1   ?
  P1:  -1,  1,  0   ?            V1:   0,  4,  3   ?
Orig:   0,  0,  0   ?
```

8)(4pts) What are the correct 'w' values for **P0** and **P1**?   w == 1

What are the correct 'w' values for **V0** and **V1**?   w == 0

What is the correct 'w' value for   **(P0 – P1)**?   w == 0

What is the correct 'w' value for   **(P0 – V0)**?   w == 1

9) Find your answer using 3-D homogeneous coordinates (e.g. a 4-tuple; a column of 4 numbers):

a) **(3pts)** Find a new vector that points from P1 to P0:   (P1→P0)

(2 , 1 , 3 , 0)   (write 4 real numbers, not expressions!)

b) **(3pts)** Find the length of vector V1 given above:

(5 . 0   )   (write one real number w/ decimal point,
                        not an expression!)

$\sqrt{3^2 + 4^2}$

c) **(3pts)** Find the point halfway between points P0 and P1:

(0 , 1.5 , 1.5 , 1)   (write 4 real numbers, not an expression)

d) **(3pts)** Find the dot product of vectors v0 and v1:

(11 . 0   )   (write a real number w/ decimal point,
                        not an expression

$2 \cdot 4 + 3 \cdot 1$

e) **(4pts)** Find vector perpendicular to both v0 and v1, with z <0

(2 , -9 , 12 , 0)   (write 4 numbers, not expressions!)

$v_0 \times v_1$

10) (20pts) True/False (copy-and-paste your choice of these highlighted answers "True" or "False")

a) _False_ Support for programmable shaders written in GLSL has always been available on almost all
implementations OpenGL since 1992, and part of the standard from version 1.0 onwards.

b) _False_ Each GLSL vertex shader program receives *sets* of vertices as inputs. For example, when a WebGL
program draws a TRIANGLES primitive, it calls the vertex shader once, and supplies three vertices as input.

indices ?

c) _True_ GLSL vertex program performs only geometric calculations, and never any color calculations,
because it has no way to affect the on-screen colors of any pixels: only the fragment shader can set pixel colors.

d) _True_ GLSL fragment shader programs cannot change the on-screen position of a vertex;
only the vertex shaders can modify vertex positions.

e) _True_ In a GLSL vertex shader, global variables preceded by the 'attribute' qualifier
may be different for each vertex.

f) _True_ The GLSL qualifier 'uniform' for a variable
means the GLSL value cannot change while processing a single drawing primitive.

g) _True_ The GLSL qualifier 'varying' used within a vertex shader means that variable's values get
rasterized. The graphics hardware computes interpolated values for each pixel within the drawing primitive and
each fragment shader receives a separately-computed value, which may be different for each pixel.

h) _True_ The GLSL 'swizzling' capability lets you re-arrange and/or exclude vector elements;
it can convert a color vector expressed in r,g,b,a order to a new color vector in b,g,r,a order.

j) _False_ As GLSL offers built-in vector and matrix types, it does NOT permit fixed-sized arrays
(e.g. you cannot declare: float myArray[7]; inside a GLSL shader).

k) _False_ The GLSL language permit use of the 'varying' qualifier for both local variables and global
variables in both the vertex shader and the fragment shader. Your JavaScript code can set their values, too.