HW #10

10.3, 10.10, 10.13, 10.19, 10.28, 10.32

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10.3

In both (a) and (b), the t-test cannot be used because there are multiple parameters.

10.10

| Model | RSS | DF | Mean Sq | Extra SS | Extra DF |
|-----------------|------|----|---------|----------|----------|
| Full | 6.00 | 32 | 0.187 | 2.38 | 2 |
| No Interactions | 8.38 | 34 | 0.247 | | |

The F-statistic is therefore $\frac{2.38/2}{0.187}=6.36$, and $P(F_{2,32}>6.36)=0.005$. This gives evidence that the slopes are different for the different species.

10.13

a

| term | estimate | std.error | statistic | p.value |
|-------------|----------|-----------|-----------|---------|
| (Intercept) | -1.576 | 0.287 | -5.49 | 0.000 |
| log(Mass) | 0.815 | 0.045 | 18.30 | 0.000 |
| Typebird | 0.102 | 0.114 | 0.90 | 0.384 |
| Typeebat | 0.079 | 0.203 | 0.39 | 0.703 |

b

The slope of log(Energy) on log(Mass) is 0.815 for all subjects. The intercept is -1.576 for nbats, -1.576 + 0.079 = -1.497 for ebats, and -1.576 + 0.102 = -1.474.

C

| term | estimate | std.error | statistic | p.value |
|-------------|----------|-----------|-----------|---------|
| (Intercept) | -1.498 | 0.150 | -9.99 | 0.000 |
| log(Mass) | 0.815 | 0.045 | 18.30 | 0.000 |
| Typebird | 0.024 | 0.158 | 0.15 | 0.883 |
| Typenbat | -0.079 | 0.203 | -0.39 | 0.703 |

d

This gives the same slope as in (b), and the intercepts are -1.498 for ebat, -1.474 for birds, and -1.577 for nbat.

e

The test that the intercepts for ebat and birds are the same is given from the table in (c). This intercept has a p-value of 0.883, which gives no evidence that the difference in intercepts is not 0.

10.19

a

| term | df | sumsq | meansq | statistic | p.value |
|-----------|----|--------|--------|-----------|---------|
| Time | 1 | 887.0 | 887.0 | 21.4 | 1e-04 |
| Intensity | 1 | 2579.8 | 2579.8 | 62.2 | 0e+00 |
| Residuals | 21 | 871.2 | 41.5 | | |

b

| term | df | sumsq | meansq | statistic | p.value |
|----------------|----|--------|--------|-----------|---------|
| Time | 1 | 887.0 | 887.0 | 16.2 | 0.0017 |
| Intensity | 5 | 2683.5 | 536.7 | 9.8 | 0.0006 |
| Time:Intensity | 5 | 111.5 | 22.3 | 0.4 | 0.8342 |
| Residuals | 12 | 655.9 | 54.7 | | |

C

| term | df.residual | rss | df | sumsq | statistic | p.value |
|--------------------------------|-------------|-------|----|--------|-----------|---------|
| Flowers ~ (Time + Intensity)^2 | 12 | 655.9 | | | | |
| Flowers ~ Time + Intensity | 21 | 871.2 | -9 | -215.3 | 0.438 | 0.889 |

10.28

We start by analyzing the models with all potential explanatory variables (El Nino, West African wetness and Year):

Table 1: Effect on Storms

| term | estimate | std.error | statistic | p.value |
|---------------|----------|-----------|-----------|---------|
| (Intercept) | -105.945 | 65.882 | -1.608 | 0.115 |
| ElNinoneutral | -0.219 | 1.022 | -0.214 | 0.832 |
| ElNinowarm | -3.288 | 1.019 | -3.227 | 0.002 |
| WestAfrica | 2.373 | 0.987 | 2.404 | 0.021 |
| Year | 0.059 | 0.033 | 1.763 | 0.085 |

Table 2: Effect on Hurricanes

| term | estimate | std.error | statistic | p.value |
|---------------|----------|-----------|-----------|---------|
| (Intercept) | -3.044 | 48.670 | -0.063 | 0.950 |
| ElNinoneutral | -0.297 | 0.755 | -0.393 | 0.696 |
| ElNinowarm | -2.417 | 0.753 | -3.212 | 0.003 |
| WestAfrica | 1.392 | 0.729 | 1.908 | 0.063 |
| Year | 0.005 | 0.025 | 0.189 | 0.851 |

Table 3: Effect on Storm Index

| term | estimate | std.error | statistic | p.value |
|---------------|----------|-----------|-----------|---------|
| (Intercept) | -102.794 | 992.740 | -0.104 | 0.918 |
| ElNinoneutral | -24.347 | 15.405 | -1.580 | 0.121 |
| ElNinowarm | -57.673 | 15.350 | -3.757 | 0.001 |
| WestAfrica | 47.549 | 14.877 | 3.196 | 0.003 |
| Year | 0.108 | 0.501 | 0.216 | 0.830 |

We remove the Year variable from the latter two models as it is not at all shown to be different from 0:

Table 4: Effect on Hurricanes

| term | estimate | std.error | statistic | p.value |
|---------------|----------|-----------|-----------|---------|
| (Intercept) | 6.172 | 0.628 | 9.835 | 0.000 |
| ElNinoneutral | -0.336 | 0.719 | -0.468 | 0.642 |
| ElNinowarm | -2.420 | 0.744 | -3.253 | 0.002 |
| WestAfrica | 1.325 | 0.630 | 2.103 | 0.041 |

Table 5: Effect on Storm Index

| term | estimate | std.error | statistic | p.value |
|---------------|----------|-----------|-----------|---------|
| (Intercept) | 111.321 | 12.803 | 8.695 | 0.000 |
| ElNinoneutral | -25.254 | 14.659 | -1.723 | 0.092 |
| ElNinowarm | -57.756 | 15.178 | -3.805 | 0.000 |
| WestAfrica | 45.987 | 12.853 | 3.578 | 0.001 |

10.32

| term | estimate | std.error | statistic | p.value |
|-------------|----------|-----------|-----------|----------|
| (Intercept) | 16.43 | 2.728 | 6.02 | 2.46e-09 |
| Gendermale | 5.22 | 0.142 | 36.78 | 0.00e+00 |
| Father | 0.39 | 0.029 | 13.72 | 0.00e+00 |
| Mother | 0.32 | 0.031 | 10.26 | 0.00e+00 |

a

$$h_c = 16.43 + 0.39 h_f + 0.32 h_m + 5.22 (?\mathrm{male})$$

b

5.22 inches

c

| fit | lwr | upr |
|------|------|------|
| 65.1 | 60.9 | 69.4 |