

UNIVERSITY OF POTSDAM

MASTER'S THESIS

SoPa++: Leveraging explainability from hybridized RNN, CNN and weighted finite-state neural architectures

Author:

Atreya SHANKAR

1st Supervisor:

Dr. Sharid LOÁICIGA
University of Potsdam

2nd Supervisor:

Mathias MÜLLER
University of Zurich

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Chapter 1

Introduction

1.1 Motivation

With the recent trend of increasingly large deep learning models achieving State-Of-The-Art (SOTA) performance on a myriad of Machine Learning (ML) tasks (Figure 1), several studies argue for focused research into Explainable Artificial Intelligence (XAI) to address emerging concerns such as security risks and inductive biases associated with black-box models (Doran, Schulz, and Besold, 2017; Townsend, Chaton, and Monteiro, 2019; Danilevsky et al., 2020; Arrieta et al., 2020). Of these studies, Arrieta et al. (2020) conduct an extensive survey into the spectrum of XAI taxonomies and provide the following novel definition of XAI:

*“Given an audience, an **explainable** Artificial Intelligence is one that produces details or reasons to make its functioning clear or easy to understand.”*

In addition, Arrieta et al. (2020) explore and classify a variety of machine-learning models into transparent and black-box categories depending on their degrees of transparency. Furthermore, they explore taxonomies of post-hoc explainability methods aimed at effectively explaining black-box models. Of high relevance to this study are the local explanations, feature relevance and explanations by simplification post-hoc explainability techniques.

Through a survey of recent literature on explanations by simplification applied in the Natural Language Processing (NLP) field, we came across several prominent studies employing techniques to simplify black-box neural networks into constituent Finite-State Automata (FSAs) and/or Weighted Finite-State Automata (WF-SAs) (Schwartz, Thomson, and Smith, 2018; Peng et al., 2018; Suresh et al., 2019; Wang and Niepert, 2019; Jiang et al., 2020).

In this thesis, we build upon the work of Schwartz, Thomson, and Smith (2018) by further developing their **Soft Patterns** (SoPa) model; which represents a hybridized RNN, CNN and Weighted Finite-State Automaton neural network architecture. We modify the SoPa model by changing key aspects of its architecture which ultimately allows us to conduct effective explanations by simplification; which was not possible with the previous SoPa architecture. We abbreviate this modified model as **SoPa++**, which signifies an improvement or major modification to the SoPa model. Finally, we evaluate both the performance and explainability of the SoPa++ model on the Facebook Multilingual Task Oriented Dialog data set (FMTOD; Schuster et al. 2018); focusing on the English-language intent classification task.

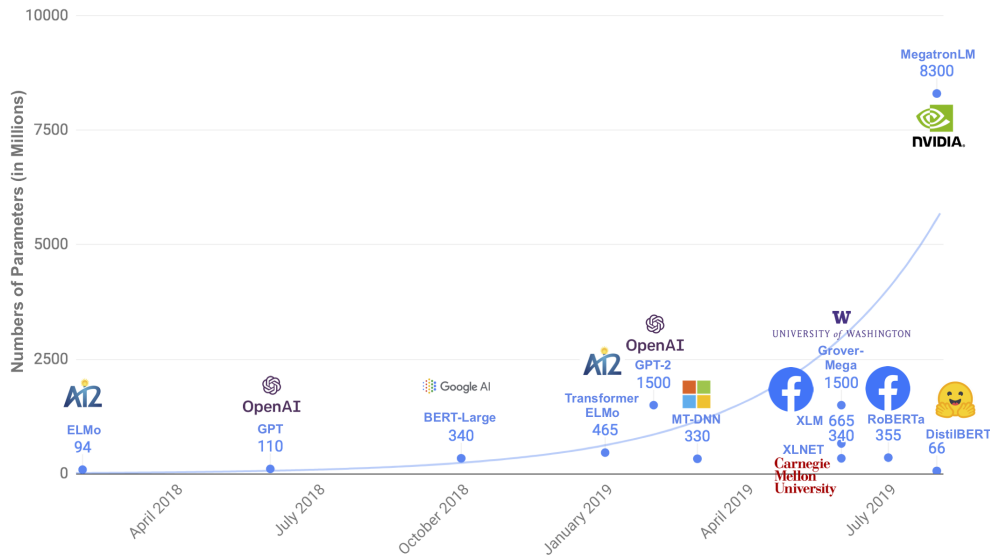


FIGURE 1: Parameter counts of recently released pre-trained language models which showed competitive or SOTA performance when fine-tuned over a range of NLP tasks (Sanh et al., 2019)

1.2 Research questions

With the aforementioned modifications to the SoPa architecture and the introduction of the SoPa++ architecture, we aim to answer the following three research questions:

1. To what extent does SoPa++ contribute to competitive performance¹ on the FMTOD data set?
2. To what extent does SoPa++ contribute to effective explanations by simplification on the FMTOD data set?
3. What interesting and relevant explanations can SoPa++ provide on the FMTOD data set?

1.3 Thesis structure

With the aforementioned research questions, we summarize the structure and contents of this thesis.

Chapter 1: Introduce this thesis, its contents and our research questions.

Chapter 2: Describe the background concepts utilized in this thesis.

Chapter 3: Describe the methodologies pursued in this thesis.

Chapter 4: Describe the results obtained from our methodologies.

Chapter 5: Discuss the implications of the aforementioned results.

Chapter 6: Conclude this thesis by answering the research questions.

Chapter 7: Document future work to expand on our research questions.

¹We define competitive performance as the scenario where a mean performance metric on a certain data set falls within the range obtained from other recent studies on the same data set

Chapter 2

Background concepts

2.1 Explainable artificial intelligence

In this section, we lay out background concepts for Explainable Artificial Intelligence (XAI) which have been largely adopted from Arrieta et al. (2020). The study is particularly helpful for us since it summarizes the findings of approximately 400 XAI contributions and presents these findings in the form of well-defined concepts and taxonomies. In addition, the study discusses future directions of XAI research. We start off by providing definitions from the study, along with accompanying remarks.

2.1.1 Interpretability and transparency

Definition 1 (Interpretability; Arrieta et al. 2020). Interpretability is defined as the ability to explain or to provide the meaning in understandable terms to a human.

Definition 2 (Transparency; Arrieta et al. 2020). A model is considered to be transparent if by itself it is understandable. Since a model can feature different degrees of understandability, transparent models are divided into three categories: simulatable models, decomposable models and algorithmically transparent models.

Remark 2.1. *Simulatability* denotes the ability of a model of being simulated or thought about strictly by a human, hence complexity takes a dominant place in this class.

Remark 2.2. *Decomposability* stands for the ability to explain each of the parts of a model (input, parameter and calculation).

Remark 2.3. *Algorithmic transparency* deals with the ability of the user to understand the process followed by the model to produce any given output from its input data.

Remark 2.4. A model is considered transparent if it falls into one or more of the aforementioned transparency categories.

Remark 2.5. If a model cannot satisfy the requirements of being transparent, then it is classified as a *black-box* model.

Examples of well-known transparent Machine Learning (ML) models are linear/logistic regressors, decision trees and rules-based learners. Similarly, common examples of non-transparent or black-box ML models are tree ensembles and deep neural networks. Arrieta et al. (2020) provide extensive justifications using the aforementioned three criteria in conducting model classifications into the transparent and black-box categories. We would direct the reader to their study for a full analysis and justification of these classifications.

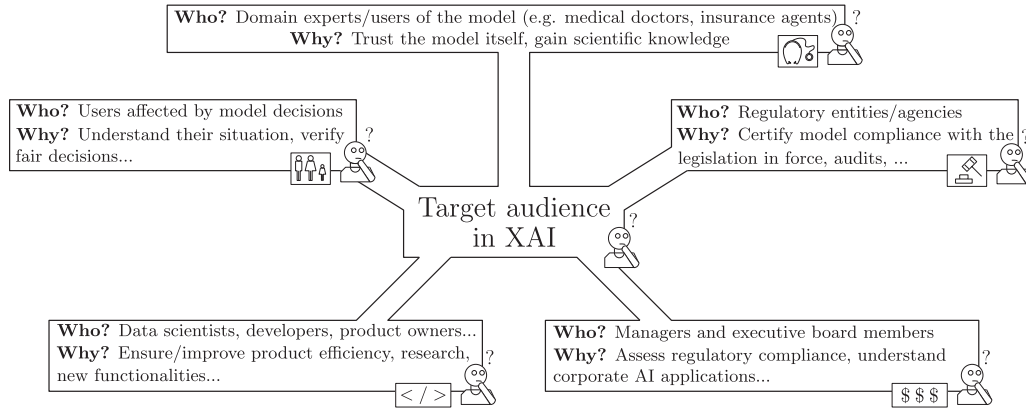


FIGURE 2: Examples of various target audiences in XAI (Arrieta et al., 2020)

2.1.2 Explainability and XAI

Definition 3 (Explainability; Arrieta et al. 2020). Explainability is associated with the notion of explanation as an interface between humans and a decision maker that is, at the same time, both an accurate proxy of the decision maker and comprehensible to humans.

Definition 4 (Explainable Artificial Intelligence; Arrieta et al. 2020). Given an audience, an **explainable** Artificial Intelligence is one that produces details or reasons to make its functioning clear or easy to understand.

Arrieta et al. (2020) observe that black-box ML models are increasingly being employed to make important predictions in critical contexts, citing high-risk areas such as precision medicine and autonomous vehicles. Of particular relevance to the field of Natural Language Processing (NLP), the study notes a myriad of issues related to inductive biases within training data sets and the ethical issues involved in using black-box models trained on such data sets. As a result, they describe an increased demand for transparency in black-box ML models from the various stakeholders in Artificial Intelligence (AI). In addition, Arrieta et al. (2020) concretize the presence of a target audience for XAI; implying that different XAI techniques should be employed for different target audiences. In their study, they provide examples of target audiences such as domain experts, end-users and managers (Figure 2).

2.1.3 Terminology clarifications

Based on an extensive literature review, Arrieta et al. (2020) observe that many studies tend to misuse the terms interpretability and explainability by using them interchangeably. To address this, they provide clear conceptual differences between the terms. For example, Arrieta et al. (2020) state that “*interpretability refers to a passive characteristic of a model referring to the level at which a given model makes sense for a human observer.*” They state that this same feature can also be expressed as transparency. In contrast, they state that “*explainability can be viewed as an active characteristic of a model, denoting any action or procedure taken by a model with the intent of clarifying or detailing its internal functions.*”

In summary, we gather that both interpretability and transparency refer to the same inherent or passive feature; and therefore we use these terms interchangeably. On the other hand, explainability refers to an active characteristic undertaken by

the model and its developers to explain the model's inner mechanisms. In addition, explainability entails the presence of a target audience; which may not necessarily be the case for interpretability or transparency.

2.1.4 Explainability techniques

Based on the aforementioned classification of ML models into transparent and black-box models, Arrieta et al. (2020) expound on explainability techniques for each of these model types. Due to their transparent nature, the study states that transparent ML models are usually explainable in themselves to most target audiences and therefore usually do not require any external technique to extract explanations. The study does however highlight some target audiences, such as non-expert users, who may require external explainability techniques such as model output visualizations in order to explain the inner workings of transparent ML models.

For the case of non-transparent or black-box models, Arrieta et al. (2020) argue that separate or external techniques must be utilized in order to reasonably explain these models. Such explainability techniques are referred to in the study as post-hoc explainability techniques; which is derived from the idea that explanations for such models are usually extracted post-modelling. Notable examples of post-hoc explainability techniques include local explanations, feature relevance and explanations by simplification. Below we provide definitions for these methods.

Definition 5 (Local explanations; Arrieta et al. 2020). Local explanations tackle explainability by segmenting the solution space and giving explanations to less complex solution subspaces that are relevant for the whole model.

Remark 5.1. Explanations can be formed by means of techniques with the differentiating property that these only explain part of the whole system's functioning.

Remark 5.2. Two well-known examples of local explainability techniques are Local Interpretable Model-Agnostic Explanations (LIME; Ribeiro, Singh, and Guestrin 2016) and G-REX (Konig, Johansson, and Niklasson, 2008).

Definition 6 (Feature relevance; Arrieta et al. 2020). Feature relevance explanation methods clarify the inner functioning of a model by computing a relevance score for its managed variables. These scores quantify the affection (sensitivity) a feature has upon the output of the model.

Remark 6.1. Feature relevance methods can be thought to be an indirect method to explain a model.

Remark 6.2. A well-known feature relevance explainability technique is known as the Shapley Additive Explanations (SHAP; Lundberg and Lee 2017). Another similar feature relevance explainability technique is known as the occlusion sensitivity method (Zeiler and Fergus, 2014).

Definition 7 (Explanations by simplification; Arrieta et al. 2020). Explanations by simplification collectively denote those techniques in which a whole new system is rebuilt based on the trained model to be explained. This new, simplified model usually attempts at optimizing its resemblance to its antecedent functioning, while reducing its complexity, and keeping a similar performance score.

Remark 7.1. We refer to the original black-box model as an *antecedent* model and the simplified version as the *proxy* model. Furthermore, we qualify that all proxy

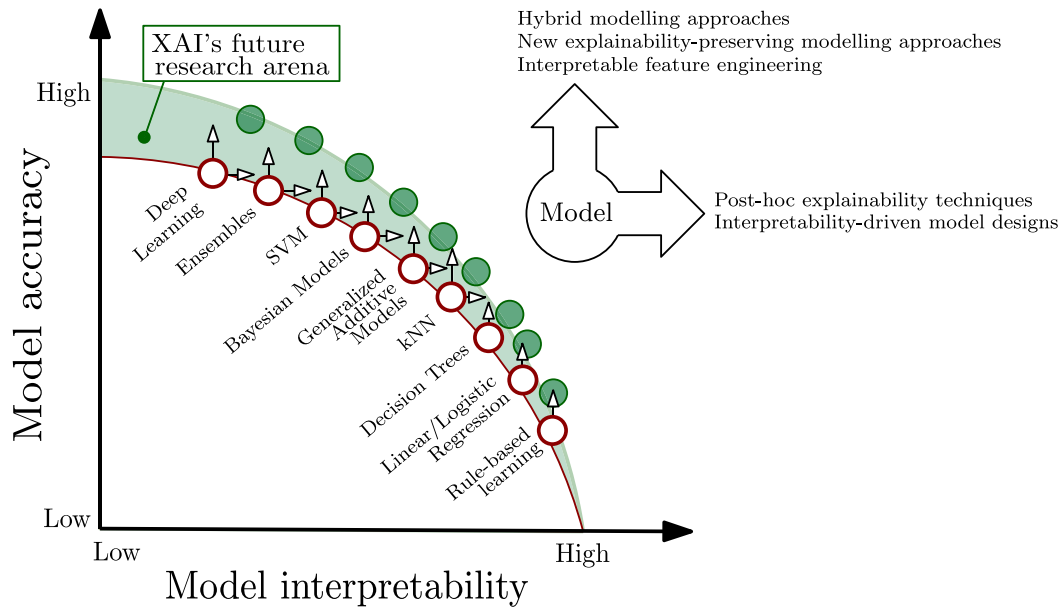


FIGURE 3: Schematic visualizing the performance-interpretability tradeoff (Arrieta et al., 2020)

models must be designed to globally approximate their respective antecedent models. This is in contrast to local explanations which require that simplified models approximate only subsets of the original black-box model.

Remark 7.2. Bastani, Kim, and Bastani (2017) and Tan et al. (2018) are examples of studies that extract and distill simpler proxy models from complex antecedent models.

Through a survey of recent literature on explanations by simplification applied in the Natural Language Processing (NLP) field, we came across several prominent studies employing explanations by simplification to simplify antecedent black-box neural networks into proxy Finite-State Automata (FSAs) and/or Weighted Finite-State Automata (WFSAs) (Schwartz, Thomson, and Smith, 2018; Peng et al., 2018; Suresh et al., 2019; Wang and Niepert, 2019; Jiang et al., 2020). We expound more on WFSAs and Schwartz, Thomson, and Smith (2018) in Sections 2.3 and 2.4 respectively.

2.1.5 Performance-interpretability tradeoff

An interesting and insightful contribution of Arrieta et al. (2020) is their introduction of the performance-interpretability tradeoff. According to the study, “*the matter of interpretability versus performance is one that repeats itself through time, but as any other big statement, has its surroundings filled with myths and misconceptions.*” To address some of the aforementioned myths and misconceptions, Arrieta et al. (2020) first disprove the generic statement that more complex models are always more accurate by pointing to certain case studies to support this argument. In particular, they show that complex models are not necessarily more accurate in cases where the function to be modelled is not complex, data is well-structured and input features are available with high quality.

Next, Arrieta et al. (2020) provide the case where the aforementioned statement, that complex models perform better, tends to be true. According to the study, this is

usually true when the function to be modelled is sufficiently complex and where the input data has high diversity or variance; and possibly contains significant noise. In such cases, Arrieta et al. (2020) argue that the performance-interpretability tradeoff can be observed; as exemplified in Figure 3.

2.1.6 Explainability metrics

Towards the end of their study, Arrieta et al. (2020) note two major limitations of the current state of XAI research. Firstly, they observe the lack of a unified conceptualization of explainability between various studies. They furthermore acknowledge that their study, while limited, could provide a good starting point for other XAI studies. Secondly, Arrieta et al. (2020) note the lack of a unified metric that denotes how explainable any given model is. They further explain why developing such a metric has been a difficult process for many XAI studies; particularly because such a metric would entail incorporating psychological, sociological and cognitive elements to accomodate the goodness of fit of an explainability method to a certain target audience. Furthermore, incorporating such elements might involve significant amounts of subjectivity in the desired metric.

To reduce some of the aforementioned subjectivity involved, Miller (2019) and Arrieta et al. (2020) provide basic guidelines of what could constitute a good explanation based on human psychology, sociology and cognitive sciences. Firstly, they observe that explanations are better when *constrictive*; meaning an explanation is good if it not only explains why a model made decision X, but also why it made decision X over decision Y. Next, they suggest that good explanations should be able to communicate causal links over probabilities; which could be a challenge for black-box models which generally compute aggregate probabilities without necessarily considering causal links. Finally, they recommend that explanations are better when *selective*; meaning that a good explanation should be able to selectively provide the most important causal links instead of all possible causal links as these might be irrelevant or confusing to the target audience.

2.2 Straight-through estimator

Activation quantized neural networks refer to neural networks that contain layers which transmit piecewise discrete signals. One of the main challenges in training such activation quantized neural networks is that their gradients tend to vanish almost everywhere because their derivatives typically default to zero. (Bengio, Léonard, and Courville, 2013; Courbariaux et al., 2016; Yin et al., 2019).

One significant workaround for this issue was proposed by Bengio, Léonard, and Courville (2013) through the introduction of the Straight-Through Estimator (STE). In the vanilla version of the STE, the STE neuron emits a signal of 1 when its input is strictly positive, and emits a zero signal in all other cases (Equation 1). The STE then uses a simple identity function to estimate the gradient during the backward pass (Equation 2). The vanilla STE is visualized through a schematic in Figure 4.

$$\text{STE}(x) = \begin{cases} 1 & x > 0 \\ 0 & x \leq 0 \end{cases} \quad (1)$$

$$\text{STE}'(x) = x \quad (2)$$

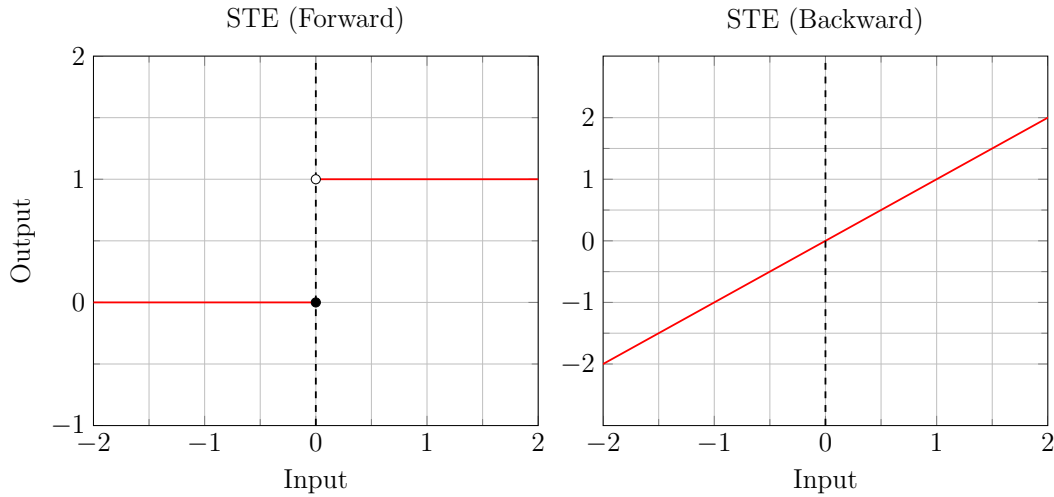


FIGURE 4: Schematic visualizing the vanilla STE (Bengio, Léonard, and Courville, 2013)

Aside from the vanilla STE, several other flavours of STEs have been proposed by studies such as Courbariaux et al. (2016) and Yin et al. (2019). In general, these studies have shown that activation quantized neural networks perform competitively with their non-quantized counterparts; while providing performance-related benefits related to lower precision computing as well as enabling further research into threshold driven neural activation functions.

2.3 Weighted finite-state automaton

Definition 8 (Semiring; Kuich and Salomaa 1986). A semiring is a set \mathbb{K} along with two binary associative operations \oplus (addition) and \otimes (multiplication) and two identity elements: $\bar{0}$ for addition and $\bar{1}$ for multiplication. Semirings require that addition is commutative, multiplication distributes over addition, and that multiplication by $\bar{0}$ annihilates, i.e., $\bar{0} \otimes a = a \otimes \bar{0} = \bar{0}$.

Remark 8.1. Semirings follow the following generic notation: $\langle \mathbb{K}, \oplus, \otimes, \bar{0}, \bar{1} \rangle$.

Remark 8.2. A simple and common semiring is the real or sum-product semiring: $\langle \mathbb{R}, +, \times, 0, 1 \rangle$. Two important semirings for this thesis are shown below.

Remark 8.3. **Max-sum** semiring: $\langle \mathbb{R} \cup \{-\infty\}, \max, +, -\infty, 0 \rangle$

Remark 8.4. **Max-product** semiring: $\langle \mathbb{R}_{>0} \cup \{-\infty\}, \max, \times, -\infty, 1 \rangle$

Definition 9 (Weighted finite-state automaton; Peng et al. 2018). A weighted finite-state automaton over a semiring \mathbb{K} is a 5-tuple $\mathcal{A} = \langle \Sigma, \mathcal{Q}, \mathcal{T}, \lambda, \rho \rangle$, with:

- a finite input alphabet Σ ;
- a finite state set \mathcal{Q} ;
- transition weights $\mathcal{T} : \mathcal{Q} \times \mathcal{Q} \times (\Sigma \cup \{\epsilon\}) \rightarrow \mathbb{K}$;
- initial weights $\lambda : \mathcal{Q} \rightarrow \mathbb{K}$;
- and final weights $\rho : \mathcal{Q} \rightarrow \mathbb{K}$.

Remark 9.1. $\epsilon \notin \Sigma$ refers to special ϵ -transitions that may be taken without consuming any input.

Remark 9.2. Self-loop transitions in \mathcal{A} refer to special transitions which consume an input while staying at the same state.

Remark 9.3. Σ^* refers to the (possibly infinite) set of all strings over the alphabet Σ .

Definition 10 (Path score; Peng et al. 2018). Let $\pi = \langle \pi_1, \pi_2, \dots, \pi_n \rangle$ be a sequence of adjacent transitions in \mathcal{A} , with each $\pi_i = \langle q_i, q_{i+1}, z_i \rangle \in \mathcal{Q} \times \mathcal{Q} \times (\Sigma \cup \{\epsilon\})$. The path π derives the ϵ -free string $\mathbf{x} = \langle x_1, x_2, \dots, x_m \rangle \in \Sigma^*$; which is a substring of the ϵ -containing string $\mathbf{z} = \langle z_1, z_2, \dots, z_n \rangle \in (\Sigma \cup \{\epsilon\})^*$. π 's score in \mathcal{A} is given by:

$$\mathcal{A}[\pi] = \lambda(q_1) \otimes \left(\bigotimes_{i=1}^n \mathcal{T}(\pi_i) \right) \otimes \rho(q_{n+1}) \quad (3)$$

Definition 11 (String score; Peng et al. 2018). Let $\Pi(\mathbf{x})$ denote the set of all paths in \mathcal{A} that derive \mathbf{x} . Then the string score assigned by \mathcal{A} to string \mathbf{x} is given by:

$$\mathcal{A}[\mathbf{x}] = \bigoplus_{\pi \in \Pi(\mathbf{x})} \mathcal{A}[\pi] \quad (4)$$

Remark 11.1. Since \mathbb{K} is a semiring, $\mathcal{A}[\mathbf{x}]$ can be efficiently computed using the Forward algorithm (Baum and Petrie, 1966). Its dynamic program is summarized below without ϵ -transitions for simplicity. $\Omega_i(q)$ gives the aggregate score of all paths that derive the substring $\langle x_1, x_2, \dots, x_i \rangle$ and end in state q :

$$\Omega_0(q) = \lambda(q) \quad (5a)$$

$$\Omega_{i+1}(q) = \bigoplus_{q' \in \mathcal{Q}} \Omega_i(q') \otimes \mathcal{T}(q', q, x_i) \quad (5b)$$

$$\mathcal{A}[\mathbf{x}] = \bigoplus_{q \in \mathcal{Q}} \Omega_n(q) \otimes \rho(q) \quad (5c)$$

Remark 11.2. The Forward algorithm can be generalized to any semiring (Eisner, 2002) and has a runtime of $O(|Q|^3 + |Q|^2|\mathbf{x}|)$ (Schwartz, Thomson, and Smith, 2018); notably with a linear runtime with respect to the length of the input string \mathbf{x} .

Remark 11.3. A special case of Forward is the Viterbi algorithm, where the addition \oplus operator is constrained to the maximum function (Viterbi, 1967). Viterbi therefore returns the highest scoring path π that derives the input string \mathbf{x} .

2.4 Soft patterns

Schwartz, Thomson, and Smith (2018) presented a novel hybridized RNN, CNN and WFSAs-based neural architecture called **Soft Patterns** (SoPa). This architecture resembles a RNN because it processes text sequentially and can encode strings of arbitrary lengths. Similarly, the architecture contains a variable number of constrained linear-chain WFSAs with variable pattern lengths or window sizes; which resembles both one-layer CNNs and an ensemble of constrained linear-chain WFSAs. The combination of the aforementioned neural features allows SoPa to learn soft versions of traditional textual surface patterns.

In their study, Schwartz, Thomson, and Smith (2018) test the SoPa architecture on three separate sentiment classification tasks and compared the results with four baselines which included a bidirectional LSTM and a CNN. With their results, they

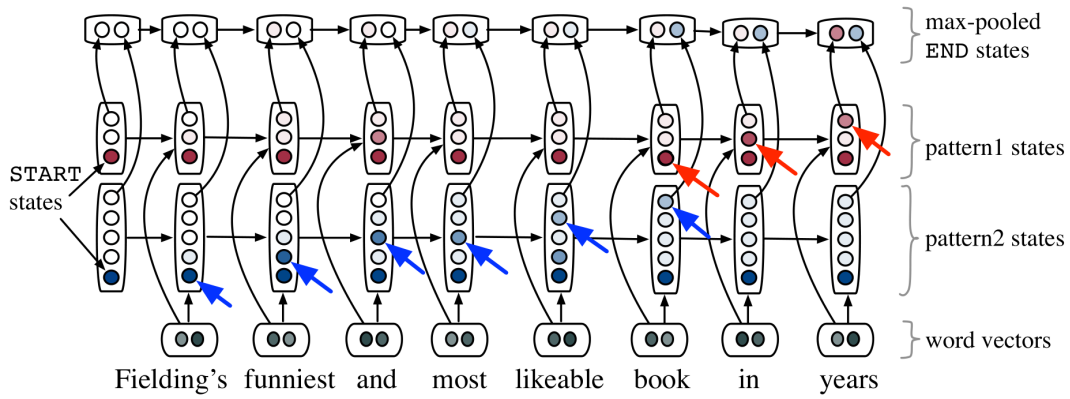


FIGURE 5: Schematic visualizing the SoPa model framework (Schwartz, Thomson, and Smith, 2018)

were able to show that SoPa performed on par or better than all baselines on all tasks. Additionally, they were able to show that SoPa outperformed all baselines significantly in low-data settings. Finally, the authors presented a simple method to explain the SoPa model using both local explanations and feature relevance.

2.4.1 Model specifications

WFSAs: In regards to the WFSAs used in SoPa, Schwartz, Thomson, and Smith (2018) only utilized the max-sum and max-product semirings. Next, they employed constraints on the model's WFSAs in order to reduce the runtime of SoPa further. Firstly, they fixed the initial λ and final ρ weights to static vectors instead of state-dependent vectors found in Definition 9. Next, they constrained ϵ -transitions to only occur at most once in each transition. Finally, they enforced a linear-chain WFSAs structure which only allows consecutive-state transitions and therefore disallows transitions to previous states. This results in the transition matrix \mathcal{T} becoming a sparse diagonal matrix. These constraints resulted in the runtime of the linear-chain WFSAs being reduced to $O(|Q||\mathbf{x}|)$ compared to the original runtime in Remark 11.2.

String vs. document score: Definition 11 describes how a WFSAs can be used to compute a string score. Since SoPa was intended to compute scores for entire documents and not just short strings, Schwartz, Thomson, and Smith (2018) proposed computing the string score over all consecutive fixed-length strings in the document. The document score would represent an aggregated score over all consecutive substrings and would therefore also depend on the semiring used in the WFSAs. In the case of max-based semirings using the Viterbi algorithm, the document score would reflect the highest scoring substring.

Computational graph: Figure 5 shows a sample computational graph for the SoPa model with two WFSAs highlighted in blue and red. The WFSAs compute consecutive string scores as they traverse the document. Given max-based semirings, the max-pooled scores accumulate in an output layer as shown on the top of Figure 5. After traversing the full document, the max-pooled scores are passed through a Multi-Layer Perceptron (MLP) which conducts the final classification to an output label. It is worth noting that without ϵ -transitions and self-loops, a pattern with length d should always consume $d - 1$ tokens. However, by allowing the aforementioned

special transitions; it is possible that strings of variable lengths match the pattern since an ϵ -transition can reduce the match length while a self-loop can increase it. This is indeed the case for Pattern 2 when a self-loop is encountered between the tokens “and” and “most” in Figure 5.

Hyperparameters: The SoPa model requires both commonly used and special hyperparameters. Commonly used hyperparameters include the learning rate, neuron dropout and word dropout. A special hyperparameter in the SoPa model is the pattern hyperparameter and it contains information on the number of patterns or WFSAs allowed, as well as the lengths of the patterns. This hyperparameter is encoded as a string with the following syntax: $\text{Length}_1\text{-Count}_1 \dots \text{Length}_n\text{-Count}_n$. An example of this hyperparameter could be 3-5_4-10_5-15, which would signify 5 patterns of length 3, 10 patterns of length 4 and 15 patterns of length 5.

2.4.2 Explainability

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