

AutoRob

Introduction to Autonomous Robotics
Michigan EECS 367

Robot Kinematics and Dynamics
Michigan ME 567 EECS 567 ROB 510

Fall 2019

EECS 367 Lab:
pendularm1.html support

Administrative

- Assignment #2: Pendularm
 - Due 11:59pm, Wednesday, October 2
- Regrade policy described on course website

Lab Takeaways

1) STENCIL
REVIEW

3) IMPLEMENTATION
ADVICE



2) EQUATION
TRANSLATION

4) BIG PICTURE

How to finish
assignment 2

Pendularm Overview

Assignment 2: Pendularm		
4	All	Euler integrator
4	All	Velocity Verlet integrator
4	All	PID control
1	Grad	Verlet integrator
2	Grad	RK4 integrator
3	Grad	Double pendulum

FEATURES ASSIGNED
TO ALL SECTIONS

FEATURES ASSIGNED
TO GRADUATE
SECTIONS

- FOR GRADUATE SECTIONS, ASSIGNMENT 2 STILL WORTH 18 POINTS
- 15 OF THESE POINTS CAN BE EARNED FROM LISTED FEATURES
- 3 OTHER POINTS LEFT FOR ADVANCED EXTENSIONS

Stencil Review

```
function animate() {
```

```
131 // update servo desired state from user interaction
132 if ( keyboard.pressed("e") )
133     pendulum.desired += 0.05; // move the desired angle for the servo
134 if ( keyboard.pressed("q") )
135     pendulum.desired += -0.05; // move the desired angle for the servo
136
137
138 // add user force from user interaction
139 if ( keyboard.pressed("d") )
140     pendulum.control += 50.0; // add a motor force to the pendulum motor
141 else if ( keyboard.pressed("a") )
142     pendulum.control += -50.0; // add a motor force to the pendulum motor
143
144 // STENCIL: implement servo controller
145 
$$e(t) = \theta_{desired}(t) - \theta(t)$$

146 
$$\tau(t) = K_p e(t) + K_i \int_0^t e(\alpha) d\alpha + K_d \frac{d}{dt} e(t)$$

147
148 
$$\int_0^t e(\alpha) d\alpha = \sum_{\alpha=0} e(\alpha) = e(t) + \sum_{\alpha=0} e(\alpha)$$

149
150
151
152
153
154
155
156
157
```



PID STENCIL

Stencil Review

```
function animate() {
```

```
164     if (numerical_integrator === "euler") {
165         // STENCIL: a correct Euler integrator is REQUIRED for assignment
166
167
168
169
170
171
172     }
173     else if (numerical_integrator === "verlet") {
174         // STENCIL: basic Verlet integration
175
176
177
178
179
180
181     }
182     else if (numerical_integrator === "velocity verlet") {
183         // STENCIL: a correct velocity Verlet integrator is REQUIRED for assignment
184
185
186
187
188
189
190     }
191     else if (numerical_integrator === "runge-kutta") {
192
193         // STENCIL: Runge-Kutta 4 integrator
194     }
195     pendulum.geom.rotation.y = pendulum.angle; // threejs cylinders have their
```

← FEATURE STENCILS

← DEFAULT ROTATION

← UPDATE PENDULUM

Stencil Review

```
function animate() {
```

```
164     if (numerical_integrator === "euler") {
165         // STENCIL: a correct Euler integrator is REQUIRED for assignment
166          $\theta(t + dt) = \theta(t) + \dot{\theta}(t)dt$ 
167
168          $\dot{\theta}(t + dt) = \dot{\theta}(t) + \ddot{\theta}(t)dt$ 
169
170          $\ddot{\theta}(t) = \ddot{\theta}(t) + \text{pendulum\_acceleration}(P, g, t)$ 
171     }
172     else if (numerical_integrator === "verlet") {
173         // STENCIL: basic Verlet integration
174
175
176
177
178
179
180
181     }
182     else if (numerical_integrator === "velocity verlet") {
183         // STENCIL: a correct velocity Verlet integrator is REQUIRED for assignment
184
185
186
187
188
189
190     }
191     else if (numerical_integrator === "runge-kutta") {
192
193         // STENCIL: Runge-Kutta 4 integrator
194     }
```

← FEATURE STENCILS

Stencil Review

```
function animate() {
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164     if (numerical_integrator === "euler") {
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166          $\theta(t + dt) = \theta(t) + \dot{\theta}(t)dt$ 
167
168          $\dot{\theta}(t + dt) = \dot{\theta}(t) + \ddot{\theta}(t)dt$ 
169
170          $\dot{\theta}(t + dt) = \dot{\theta}(t) + \text{pendulum\_acceleration}(P, g, t)dt$ 
171     }
172
173     else if (numerical_integrator === "verlet") {
174         // STENCIL: basic Verlet integration
175          $\theta(t + dt) = 2\theta(t) - \theta(t - dt) + \ddot{\theta}(t)dt^2$ 
176
177          $\theta(t + dt) = 2\theta(t) - \theta(t - dt) + \text{pendulum\_acceleration}(P, g, t)dt^2$ 
178
179     }
180
181     else if (numerical_integrator === "velocity verlet") {
182         // STENCIL: a correct velocity Verlet integrator is REQUIRED for assignment
183
184
185
186
187
188
189
190     }
191     else if (numerical_integrator === "runge-kutta") {
192
193         // STENCIL: Runge-Kutta 4 integrator
194     }
```

DON'T FORGET TO INITIALIZE
FOR VERLET!

← FEATURE STENCILS

Stencil Review

```
function animate() {
```

```
164     if (numerical_integrator === "euler") {
165         // STENCIL: a correct Euler integrator is REQUIRED for assignment
166          $\theta(t + dt) = \theta(t) + \dot{\theta}(t)dt$ 
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170          $\dot{\theta}(t + dt) = \dot{\theta}(t) + \text{pendulum\_acceleration}(P, g, t)$ 
171     }
172
173     else if (numerical_integrator === "verlet") {
174         // STENCIL: basic Verlet integration
175          $\theta(t + dt) = 2\theta(t) - \theta(t - dt) + \ddot{\theta}(t)dt^2$ 
176
177          $= 2\theta(t) - \theta(t - dt) + \text{pendulum\_acceleration}(P, g, t)dt^2$ 
178
179     }
180
181     else if (numerical_integrator === "velocity verlet") {
182         // STENCIL: a correct velocity Verlet integrator is REQUIRED for assignment
183
184          $\theta(t + dt) = \theta(t) + \dot{\theta}(t)dt + \frac{1}{2}\ddot{\theta}(t)dt^2$ 
185
186          $\dot{\theta}(t + dt) = \dot{\theta}(t) + \frac{\ddot{\theta}(t) + \ddot{\theta}(t + dt)}{2}dt$ 
187
188     }
189
190     else if (numerical_integrator === "runge-kutta") {
191
192         // STENCIL: Runge-Kutta 4 integrator
193     }
194 }
```

← FEATURE STENCILS

PAY ATTENTION TO ANGLE USED
BY ACCELERATION CALCULATION

Stencil Review

```
function animate() {
```

```
225     " a/d - apply user force " +  
226     "<br>" +  
227     " q/e - adjust desired angle " +  
228     "<br>" +  
229     " c|x - toggle servo " +  
230     "<br>" +  
231     " s - disable servo "  
232  
233     ;
```

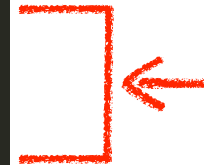
```
234  
235     // threejs rendering update  
236     renderer.render( scene, camera );  
237  
238 }
```

$$\ddot{\theta} = -\frac{g}{l} \sin(\theta) + \frac{\tau}{ml^2}$$

```
244 function createScene() {
```

```
245  
246     // instantiate threejs scene graph  
247     scene = new THREE.Scene();  
248
```

```
249     // instantiate threejs camera and set its position in the world  
250     camera = new THREE.PerspectiveCamera( 75, window.innerWidth / window.innerHeight,  
251     camera.position.y = 1;  
252     camera.position.z = 4;
```



ACCELERATION
STENCIL

Implementation Advice

- Pay attention to time index within equations!

- Ensure you're using the correct of:

$$\begin{array}{c|c|c} \text{previous} & \text{current} & \text{future} \\ \hline t - dt & t & t + dt \end{array}$$

- Parameterized helper functions can reduce code duplication
 - Like, `pendulum_acceleration(P,g,...)`
- Unnecessary global variables can be difficult to debug

Motivation of Assignment

- Desired outcome of the pendulum assignment:
 - Understand how 'error'* can be used as feedback in a closed-loop fashion to control a system
 - ↳ Implement a PID servo controller for a pendulum functioning under well defined rules (classical/Newtonian mechanics)
- Why are we working with Newton's equations of motion and numerical integrators?

*'error' referring to some measure of difference between current and goal states of some system

Motivation of Assignment

- Why are we working with Newton's equations of motion and numerical integrators?
- The real—physical—world operates under Newtonian mechanics, why not implement our pendulum and PID controller there?

↳ **Too expensive, too slow**

- How can we implement a pendulum in simulation?

Motivation of Assignment

- How can we implement a pendulum in simulation?
 - ↳ Use Newton's equations of motion to model the change of pendulum's position over time (model of the state dynamics)
 - ↳ With numerical integration techniques and an initial position, we can approximate the pendulum's position at any specific time

INSIDE OF SIMULATION

$$\theta(t + dt) = \theta(t) + \dot{\theta}(t)dt$$

OUTSIDE OF SIMULATION

$$\theta(t + dt) = \text{get_measurement}(\theta, \text{realWorld})$$

Motivation of Assignment

- Desired outcome of the pendulum assignment:
 - Understand how 'error'* can be used as feedback in a closed-loop fashion to control a system
 - ↳ Implement a PID servo controller for a pendulum functioning under well defined rules (classical/Newtonian mechanics)
 - Understand why simulations are relevant in robotics and how they can be implemented using differential equations
 - ↳ Build a digital simulation of the pendulum operating under the laws of classical mechanics

*'error' referring to some measure of difference between current and goal states of some system

Final Thoughts

- If you think of an idea for an advanced extension, **which you are excited about**, let the course staff know!
- We will consider the idea for possible extension points (following the working implementation)
- Have a great weekend!