

Bug Algorithms

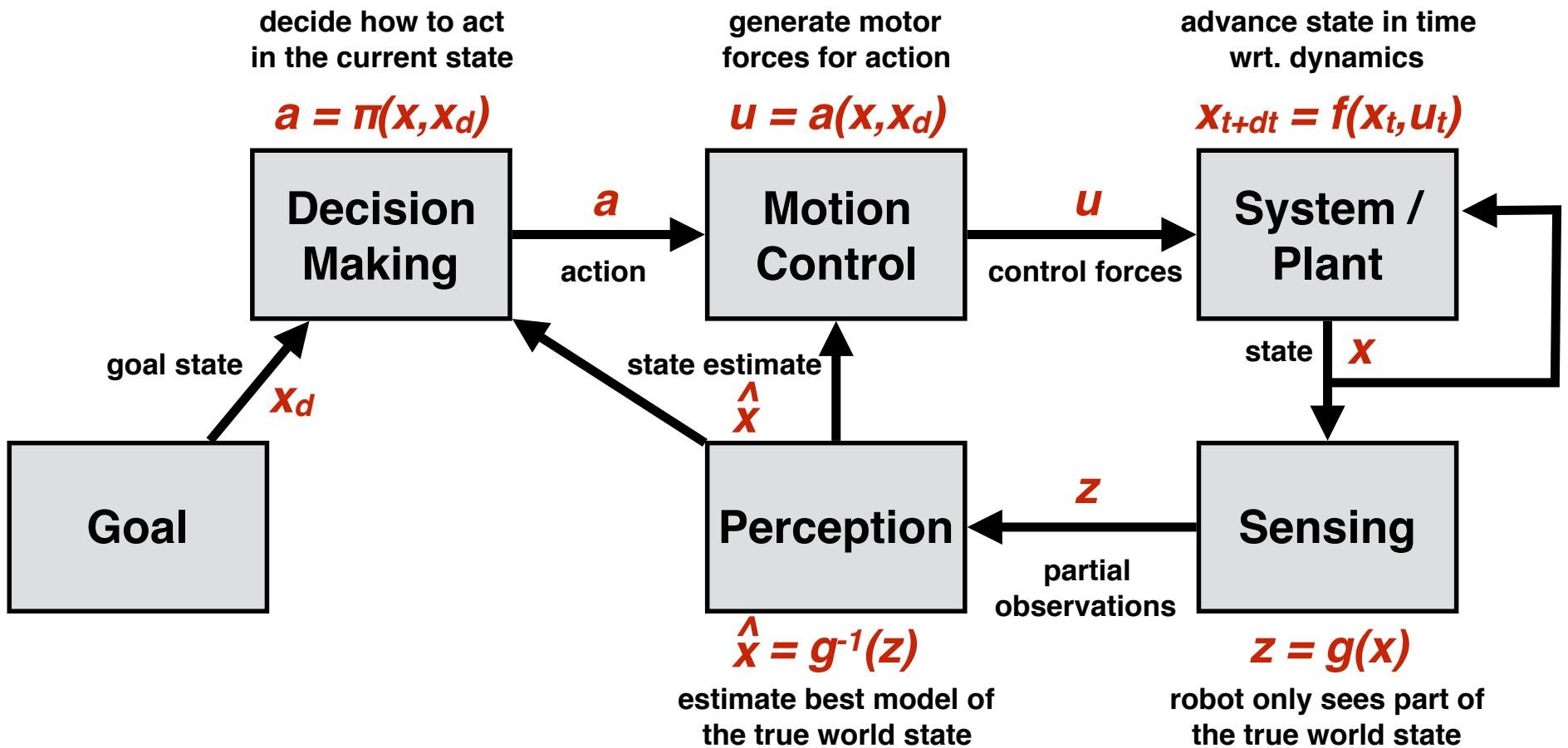
autorob.github.io

COCKROACH

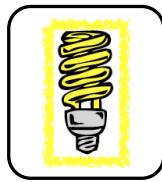


MAZE

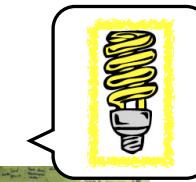
Robot Control Loop



Should your robot's decision making



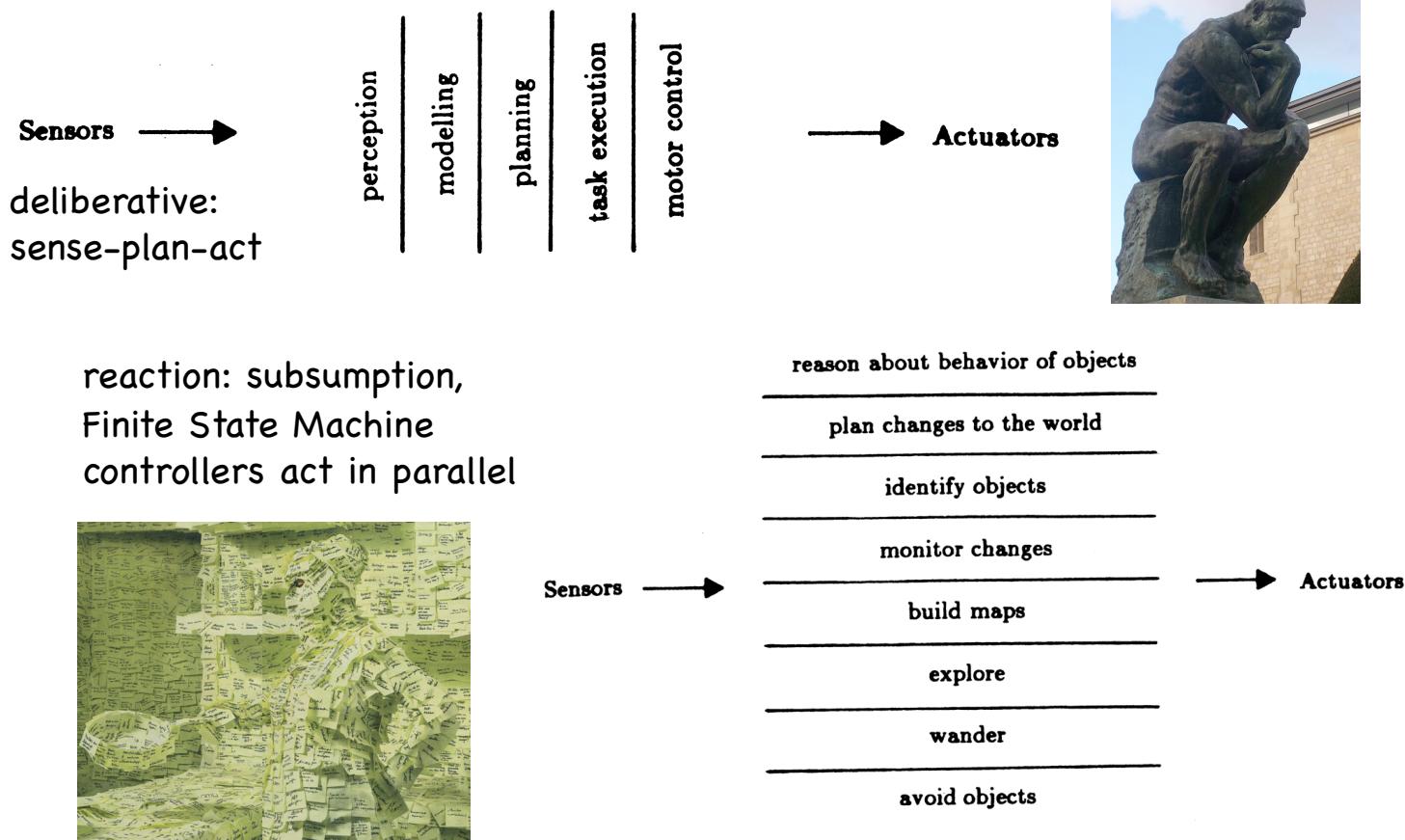
OR



fully think through
solving a problem?

react quickly to
changes in its world?

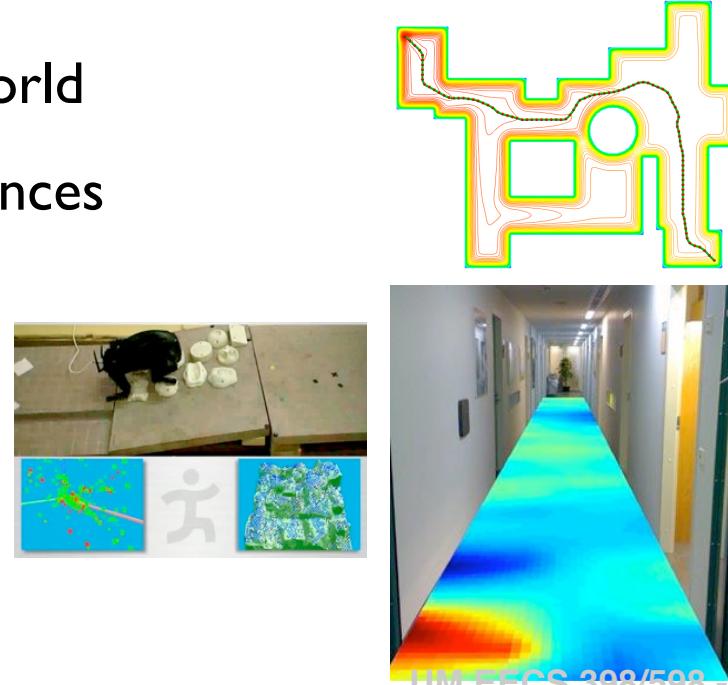
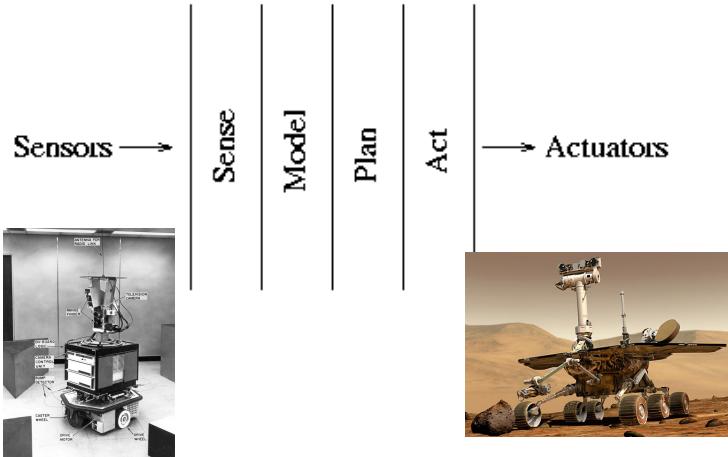
Deliberation v. Reaction



Deliberation

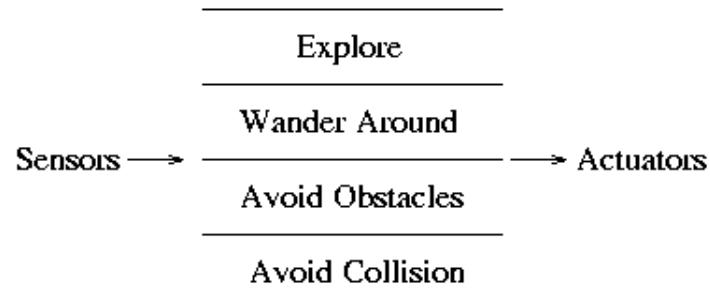
“Sense-Plan-Act” paradigm

- sense: build most complete model of world
 - GPS, SLAM, 3D reconstruction, affordances
- plan: search over all possible outcomes
 - BFS, DFS, Dijkstra, A*, RRT
- act: execute plan through motor forces



Reaction

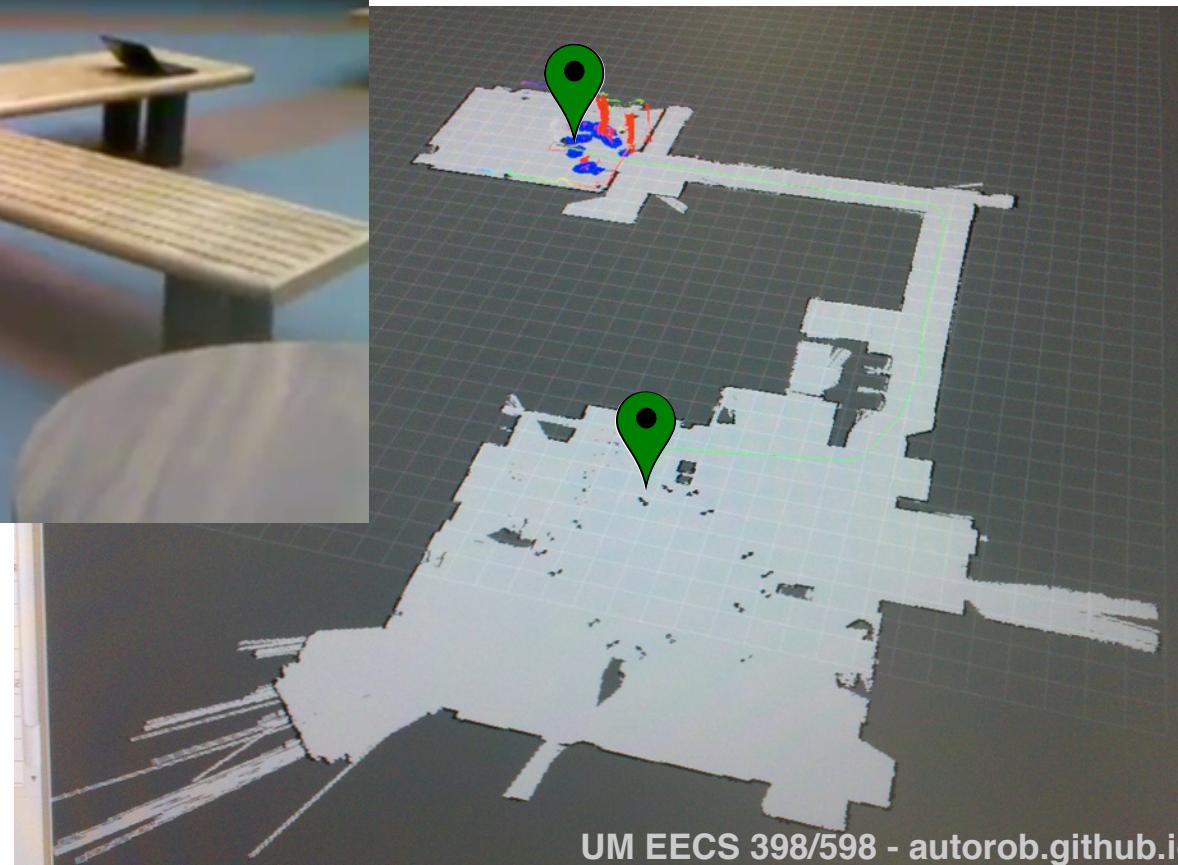
- No representation of state
- Typically, fast hardcoded rules
- Embodied intelligence
 - behavior := control + embodiment
 - ant analogy, stigmergy
- Subsumption architecture
 - prioritized reactive policies
- Ghengis hexpod video





Let's start with base navigation

How to get from Location A to
Location B?



Base Navigation

- How get from point A to point B
- **What is the simplest policy to perform navigation?**

Random Walk: Goal Seeking

- Move in a random direction until you hit something
- Then go in a new direction
- Stop when you get to the goal, assuming it can be recognized



Lisa Miller, <http://www.youtube.com/watch?v=VBzXDrz8rMI>

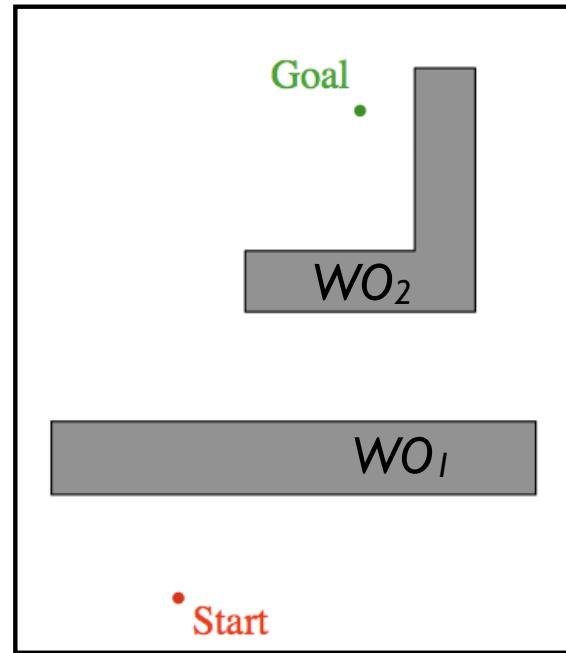
goal: exit here

Base Navigation

- How get from point A to point B
- What is the simplest policy to perform navigation?
 - random walk (2010 Enclosure Escape project)
 - reactive: embodied intelligence
- **What is a “simple” deliberative policy?**

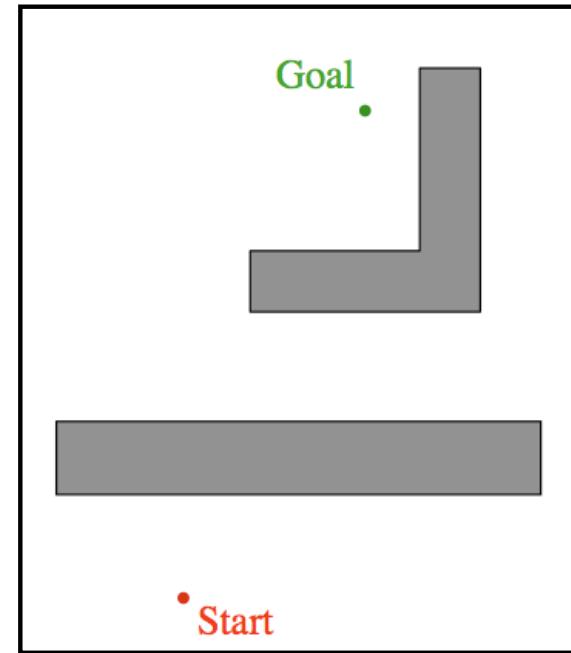
Bug Algorithms

- Assume bounded world W
- Known: global goal
- measurable distance $d(x,y)$
- Unknown: obstacles WO_i
- Local sensing
- tactile
- distance traveled



Bug Algorithms

- Assume bounded world W
- Known: global goal
 - measurable distance $d(x,y)$
- Unknown: obstacles WO_i
- Local sensing
- **bump sensor**
- distance traveled

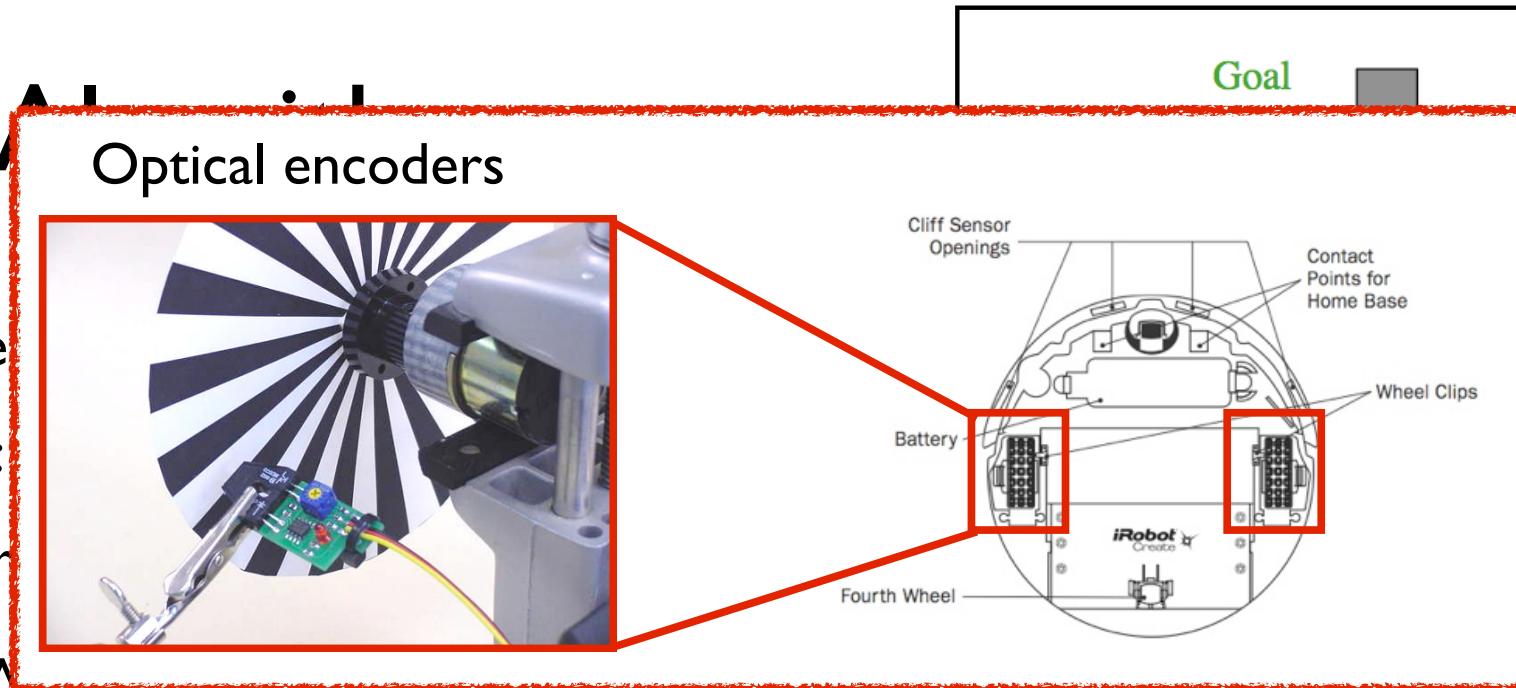


bumper is essentially an on/off button

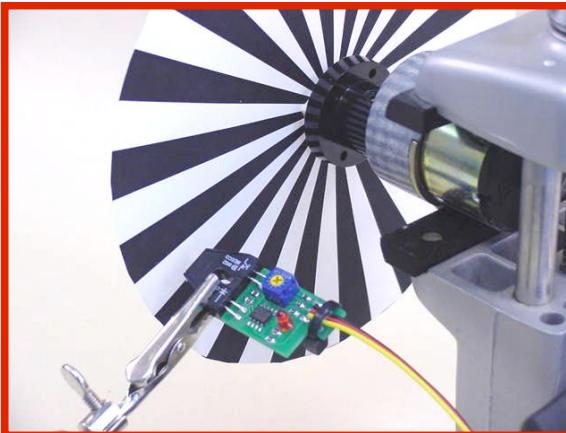
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Bug

- Assume
- Known:
- measure
- Unknown
- Local sensing
- bump
- odometry



Optical encoders



Interesting application of
Bug algorithms ?

MIT Technology Review



Wealth & Investment
Management

See how realigning
can help maximiz

Ghengis hexapod robot

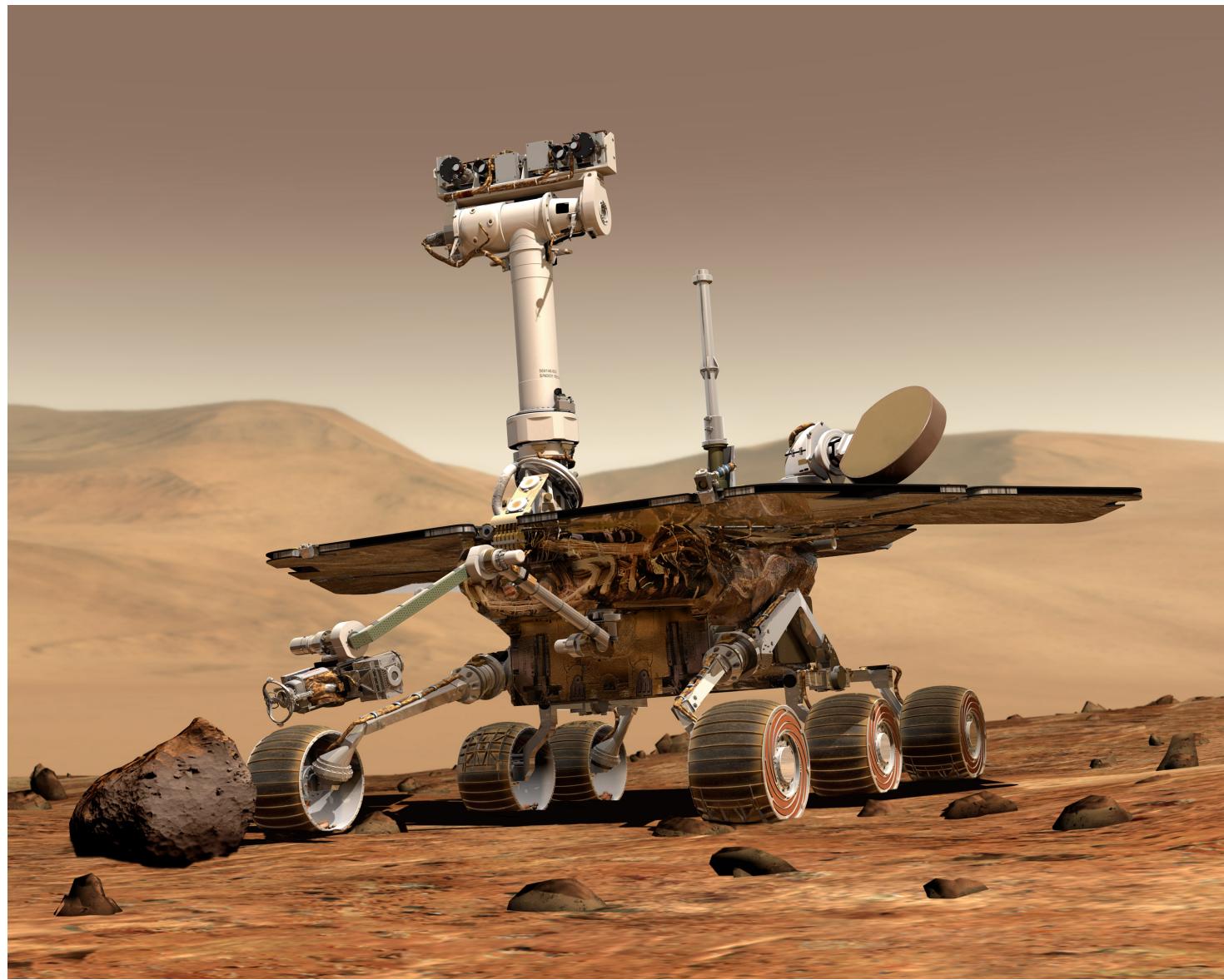


Intelligent Machines

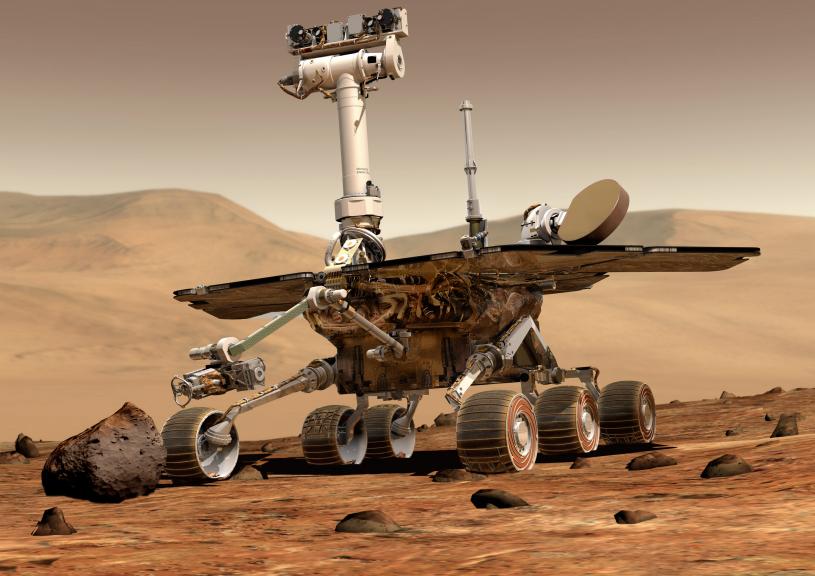
Honey, They've Shrunk the Rover

The Sojourner vehicle that trekked across the Martian surface captured the world's fancy last summer, but we haven't seen anything yet. Next will come rovers that can roam miles across Mars and "aerobots" able to survey other planets.

by Eric Scigliano January 1, 1998

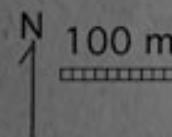


Mars Exploration Rover

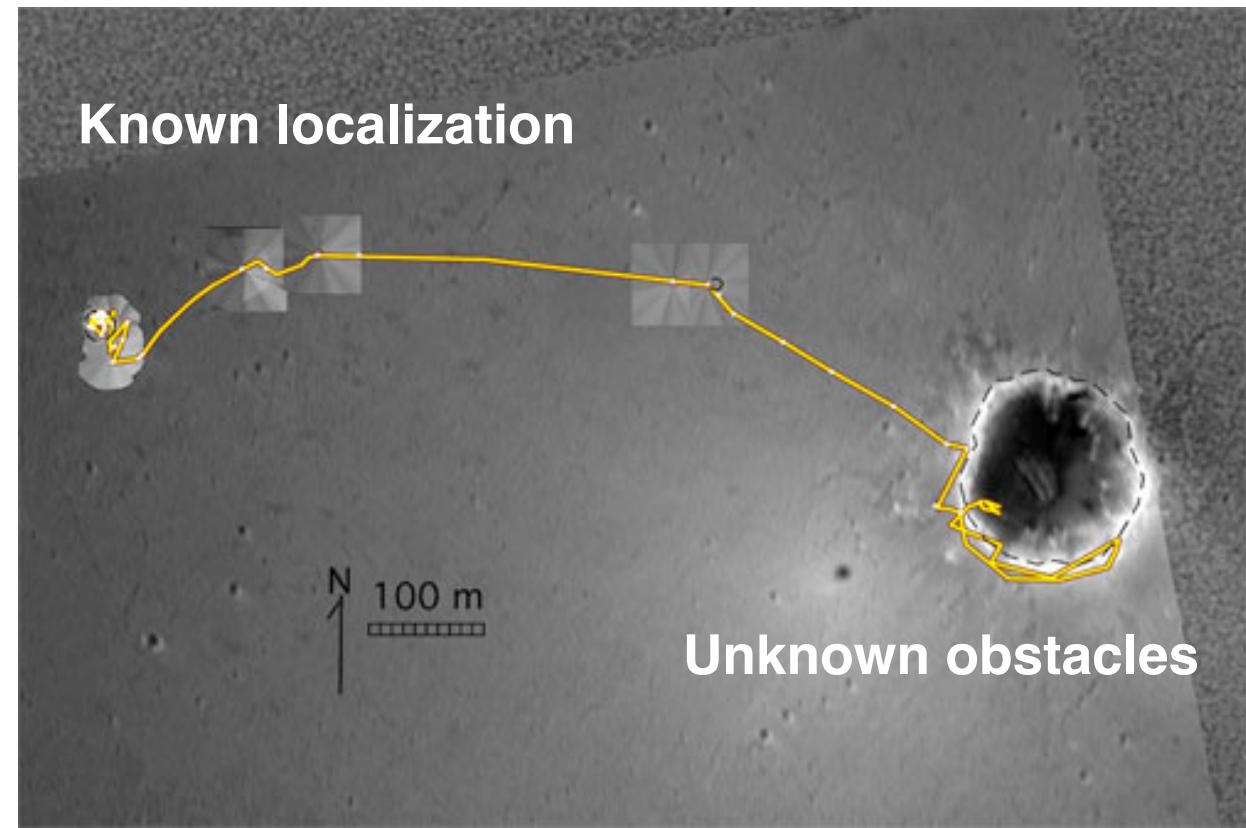


<http://mars.nasa.gov/mer/gallery/press/opportunity/20040921a.html>

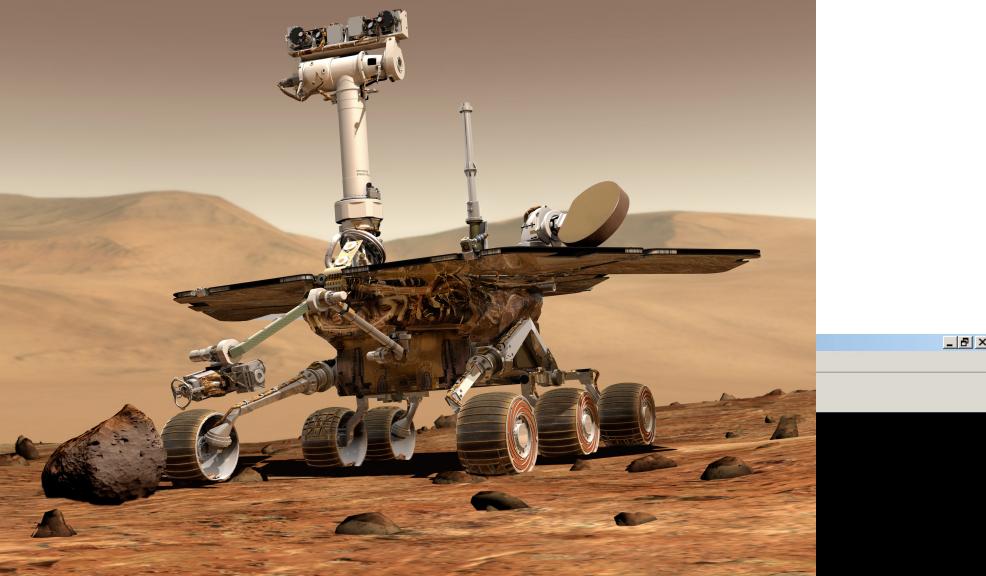
Known localization



Unknown obstacles

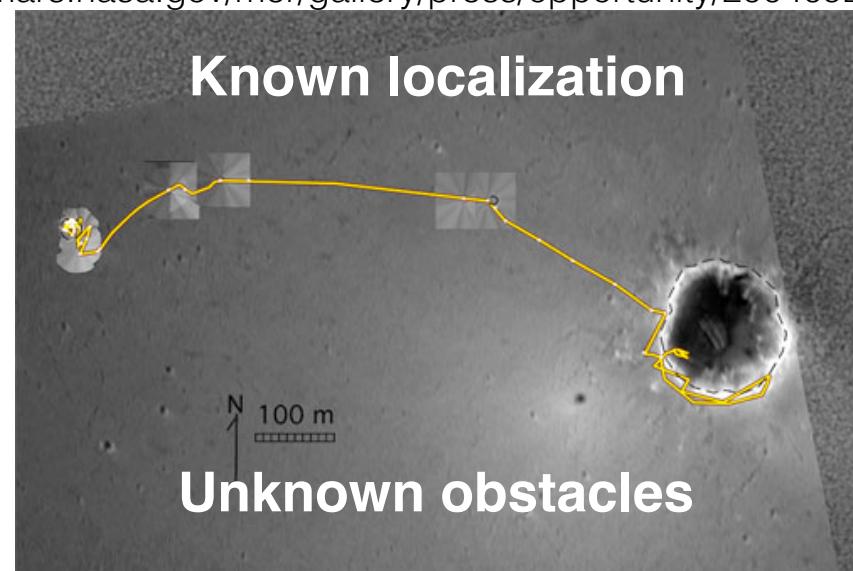


Mars Exploration Rover



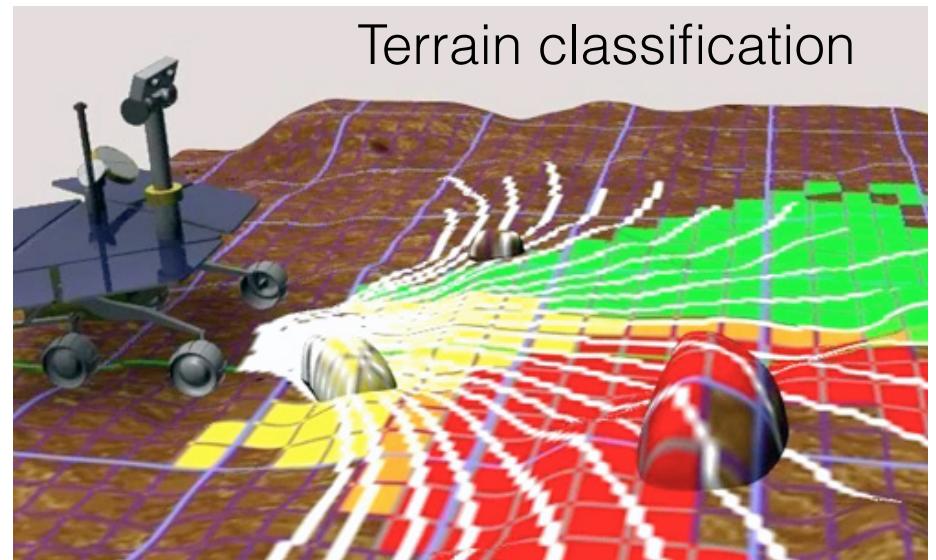
<http://mars.nasa.gov/mer/gallery/press/opportunity/20040921a.html>

Known localization



Unknown obstacles

Terrain classification



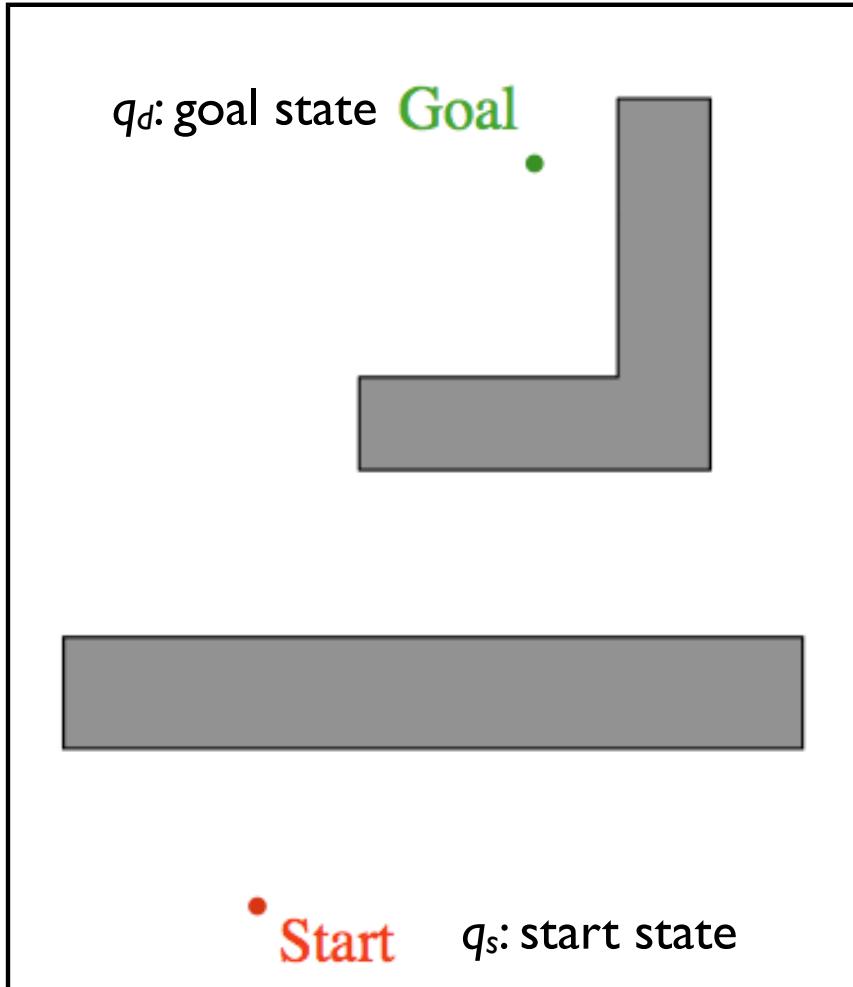
3D stereo reconstruction

University Rover Challenge



<http://urc.marsociety.org/home/photo-gallery/urc2016>

Bug Navigation

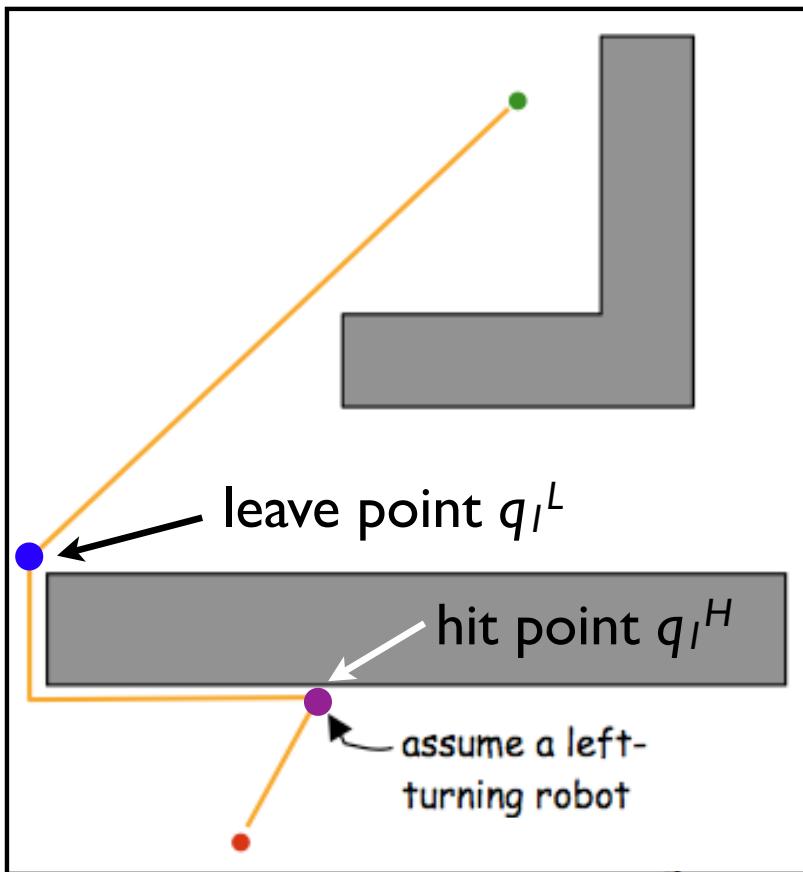


Plan navigation path from start q_s to goal q_d

as a sequence of hit/leave point pairs on obstacles

Hit point: q_i^H
Leave point: q_i^L

Bug 0



- 1) Head towards goal
- 2) When hit point set, **follow wall**, until you can move towards goal again (leave point)
- 3) continue from (1)

Wall following

follow wall



One approach:

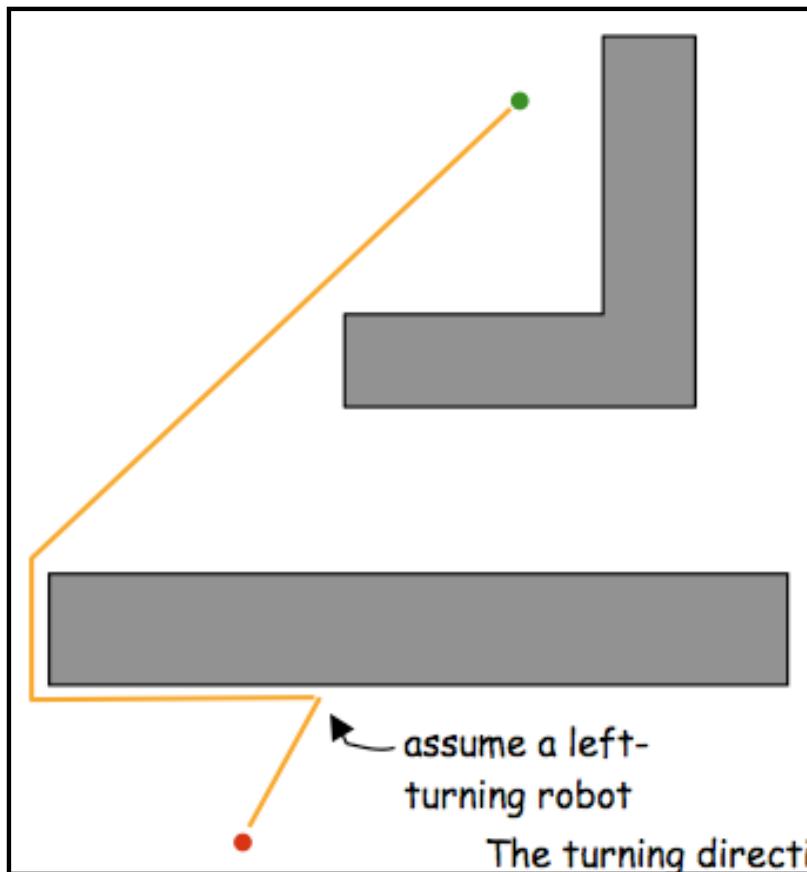
- a) move forward with slight turn
- b) when bumped, turn opposite direction
- c) goto (a)

Trevor Jay

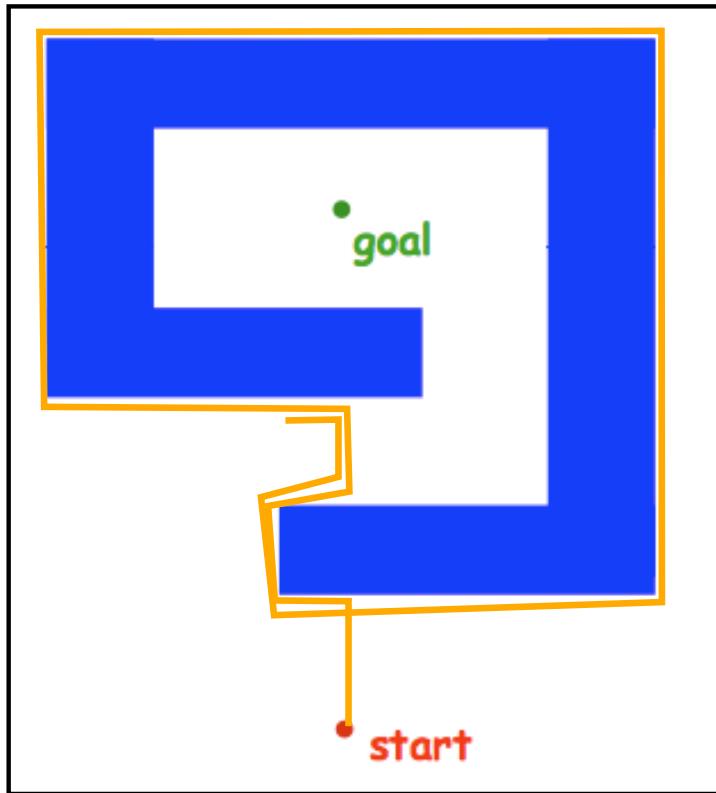
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What map would foil Bug 0?

Bug 0



- 1) Head towards goal
- 2) When hit point set, follow wall, until you can move towards goal again (leave point)
- 3) continue from (1)

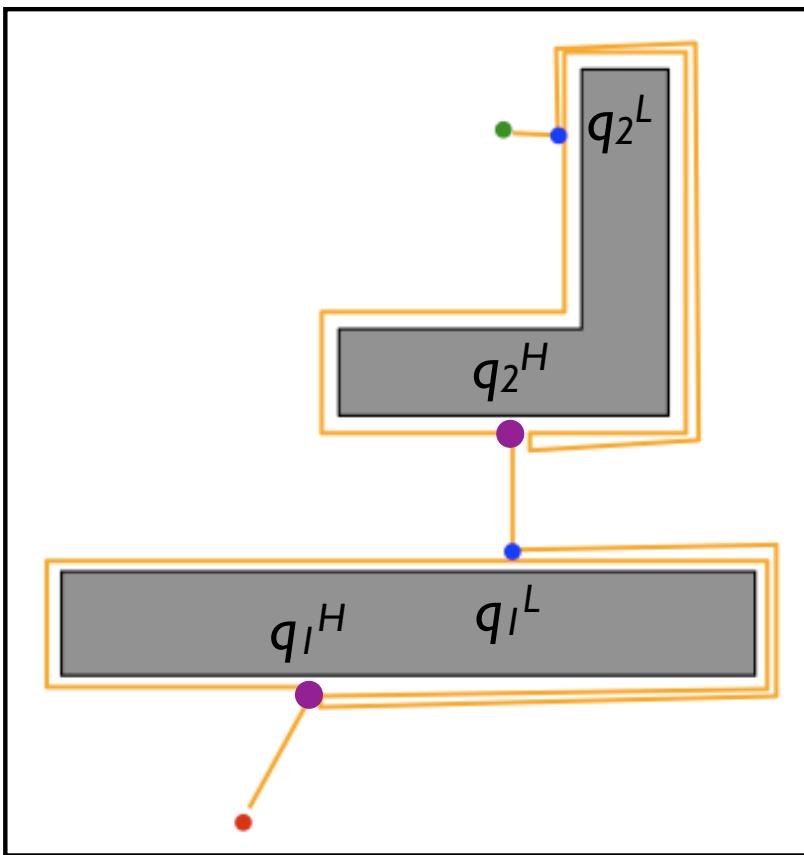


Bug 0

- 1) Head towards goal
- 2) When hit point set, follow wall, until you can move towards goal again (leave point)
- 3) continue from (1)

Can you trace the Bug 0 path?
Can we make a better bug? How?

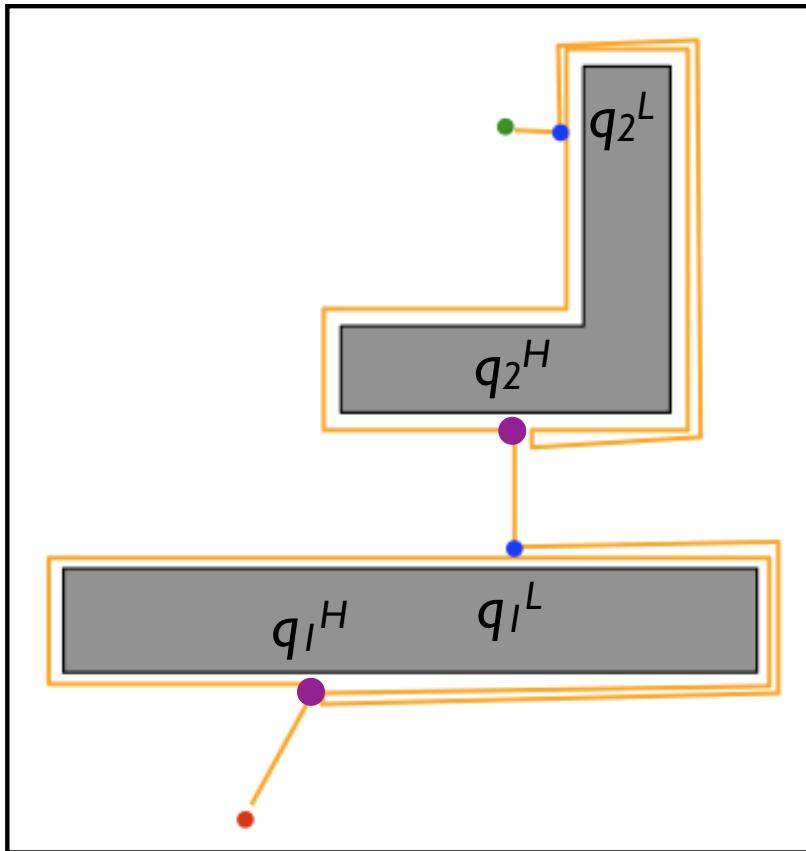
Bug I



- 1) Head towards goal
- 2) When hit point set, circumnavigate obstacle, setting leave point as closest to goal
- 3) return to leave point
- 4) continue from (1)

What map would foil Bug 1?

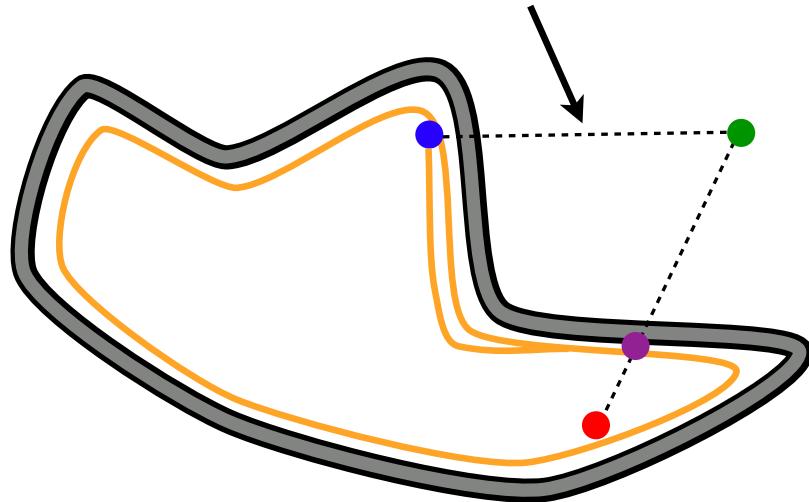
Bug 1



- 1) Head towards goal
- 2) When hit point set, circumnavigate obstacle, setting leave point as closest to goal
- 3) return to leave point
- 4) continue from (1)

What map would foil Bug 1?

no path exists: line(q_I^L, q_d) intersects current obstacle

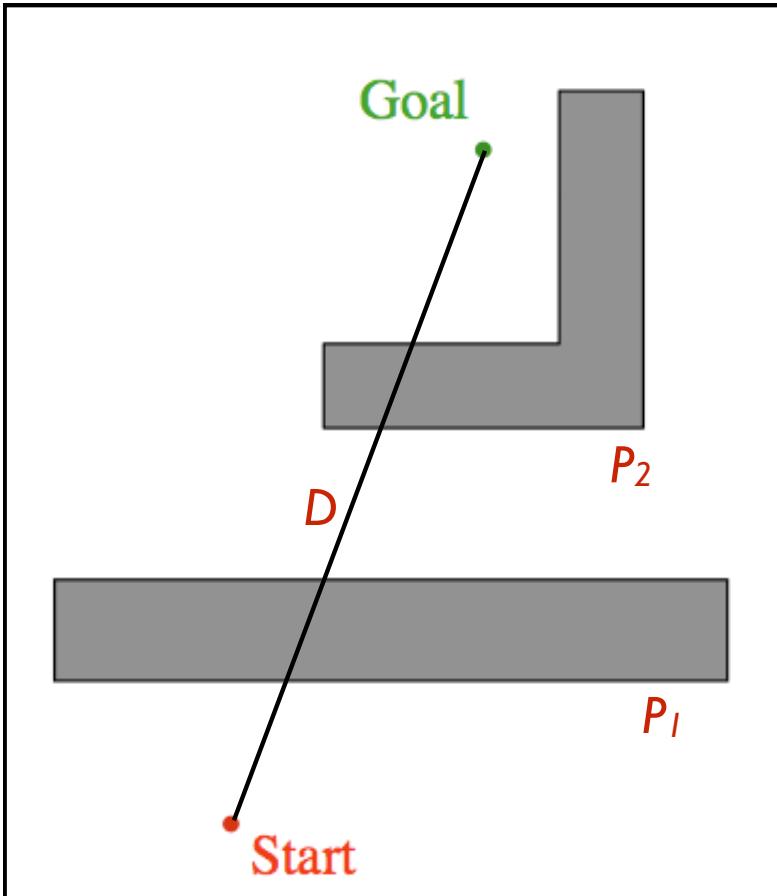


failure bump occurs immediately

Bug 1: Detecting Failure

- 1) Head towards goal
- 2) When hit point set, circumnavigate obstacle, setting leave point as closest to goal
- 3) return to leave point
- 4) if bump current obstacle,
 return **fail**;
else, continue from (1)

Bug I: Search Bounds

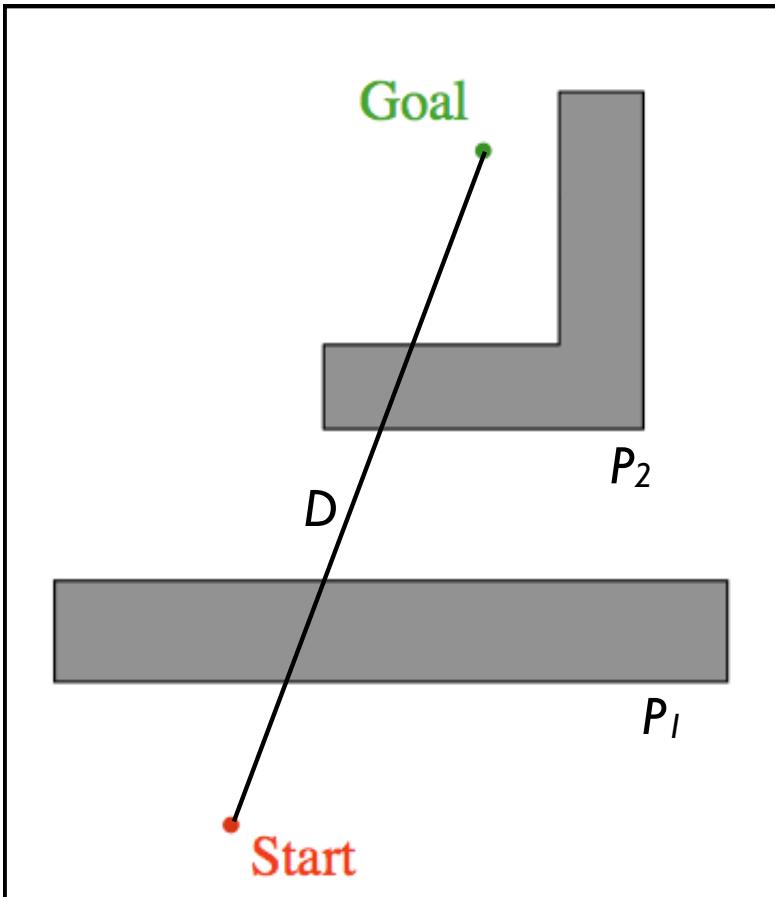


Bounds on path distance, assuming
 D : distance start-to-goal
 P_i : obstacle perimeter

Best case:

Worst case:

Bug I: Search Bounds



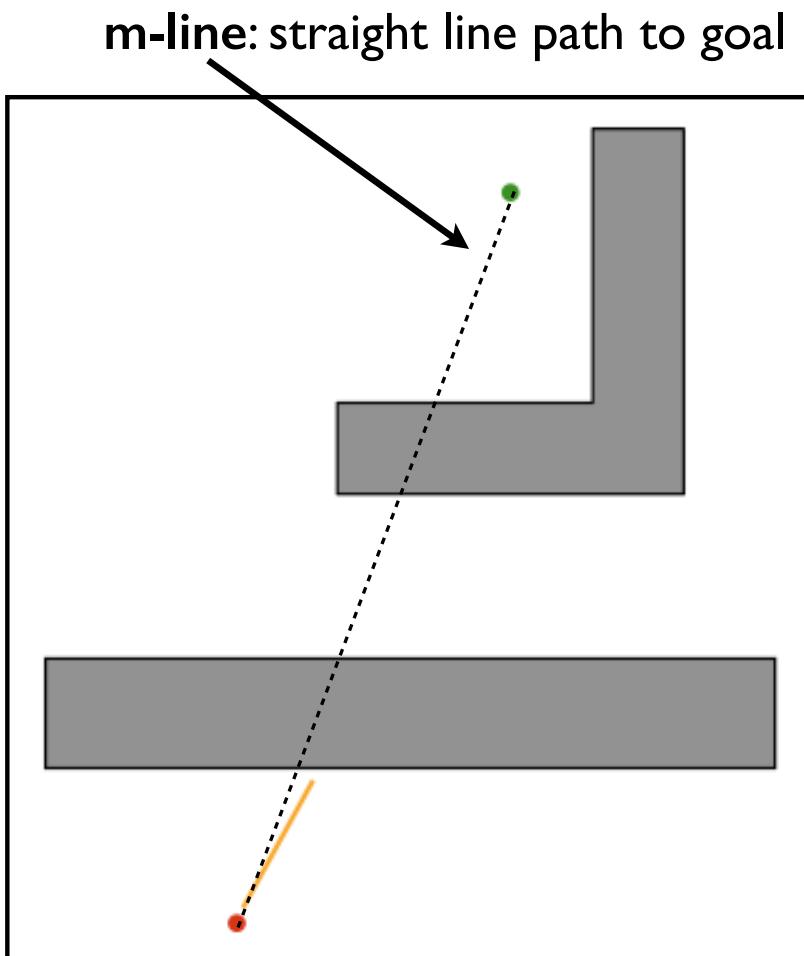
Bounds on path distance, assuming
 D : distance start-to-goal
 P_i : obstacle perimeter

Best case: D

Worst case: $D + 1.5\sum_i P_i$

Is there a faster bug?

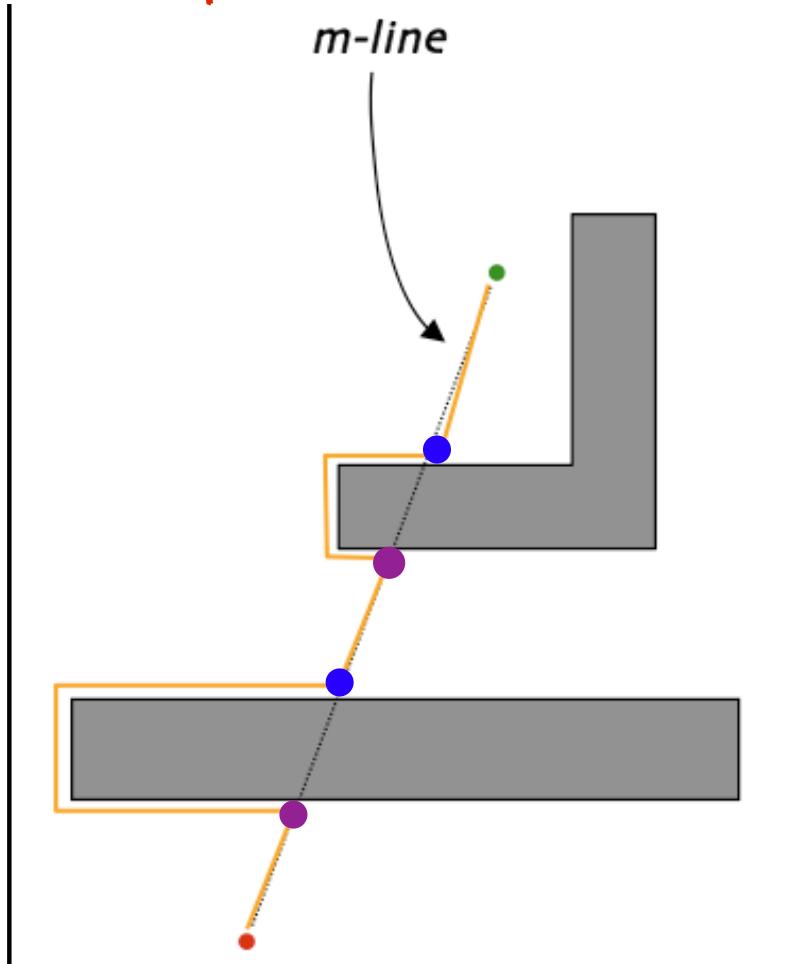
Bug 2



- 1) Head towards goal on m-line
- 2) When hit point set, traverse obstacle until m-line is encountered
- 3) set leave point and exit obstacle
- 4) continue from (1)

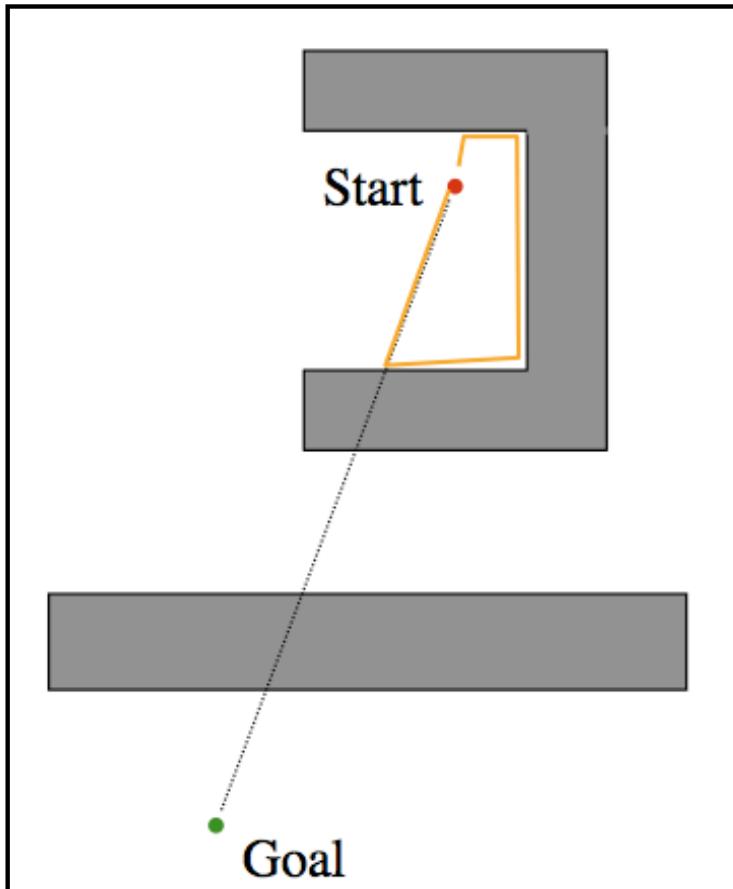
What map would foil Bug 2?

Bug 2



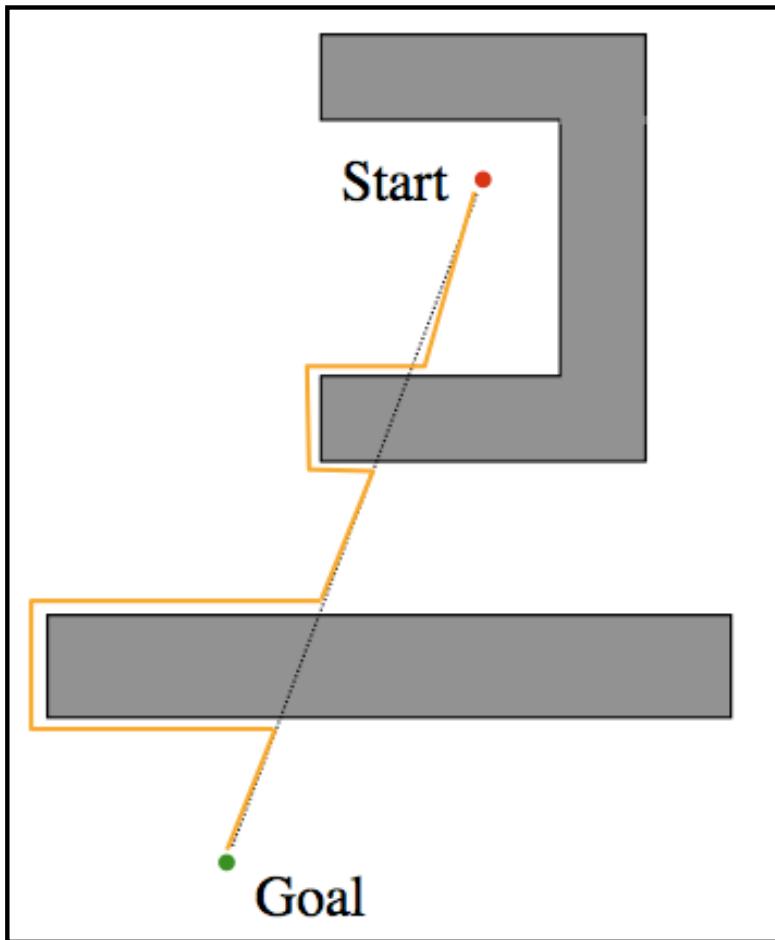
- 1) Head towards goal on m-line
- 2) When hit point set, traverse obstacle until m-line is encountered
- 3) set leave point and exit obstacle
- 4) continue from (1)

Bug 2



- 1) Head towards goal on m-line
- 2) When hit point set, traverse obstacle until m-line is encountered
- 3) set leave point and exit obstacle
- 4) continue from (1)

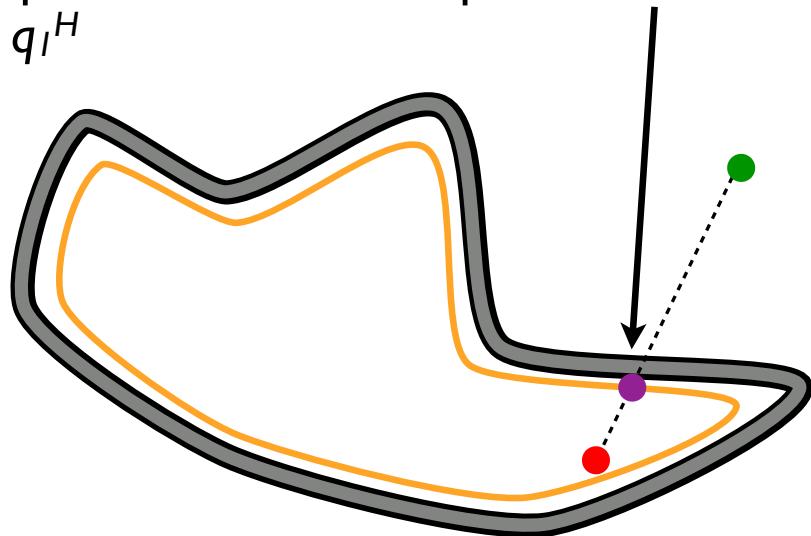
Bug 2



- 1) Head towards goal on m-line
- 2) When hit point set, traverse obstacle until m-line is encountered
& closer to the goal
- 3) set leave point and exit obstacle
- 4) continue from (1)

Bug 2: Detecting Failure

no path exists: no leave point before returning
to q_I^H

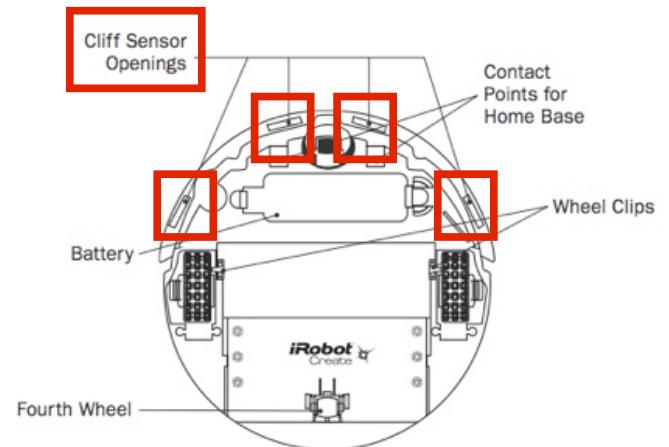


- 1) Head towards goal on m-line
- 2) When hit point set, traverse obstacle until m-line is encountered & closer to the goal
or hit point reached
- 3) **if not i^{th} hit point**, set leave pt. and exit
- 4) continue from (1)

Bug 2 in action



m-line drawn on floor
with tape recognizable by
Create cliff sensor



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Kayle Gishen

Is Bug2 better than Bug1?

Bug 1 v. Bug 2:

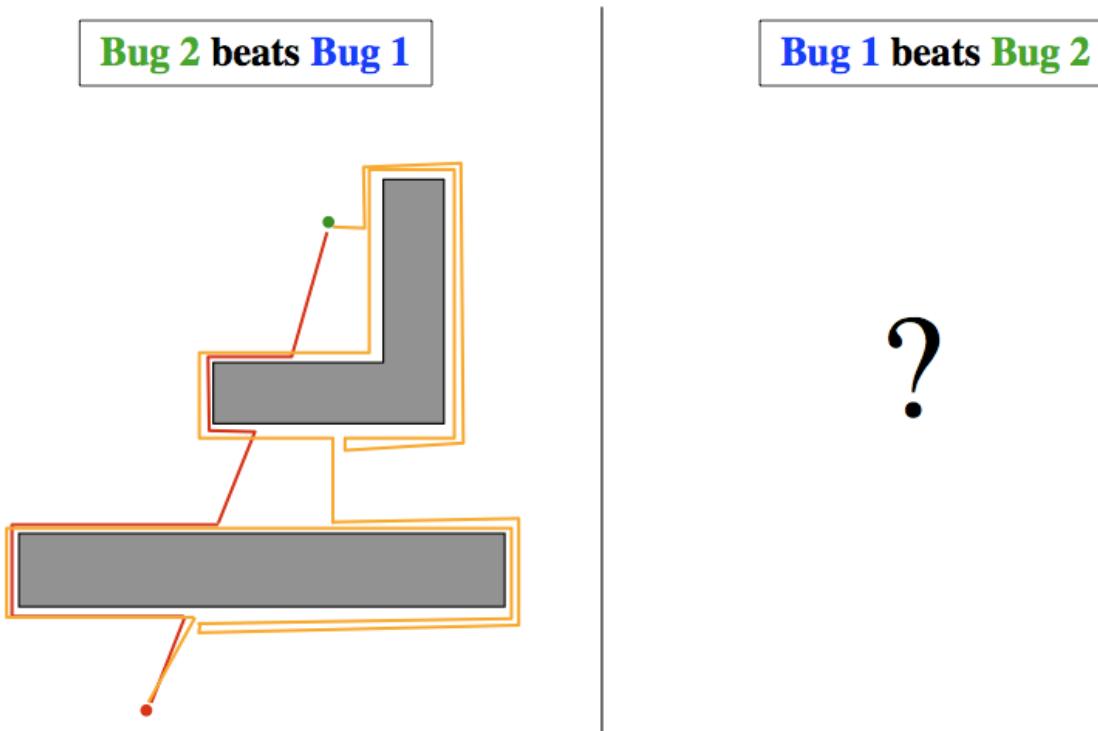
Draw worlds where Bug 2 performs better than Bug 1 (and vice versa)

Bug 2 beats Bug 1

Bug 1 beats Bug 2

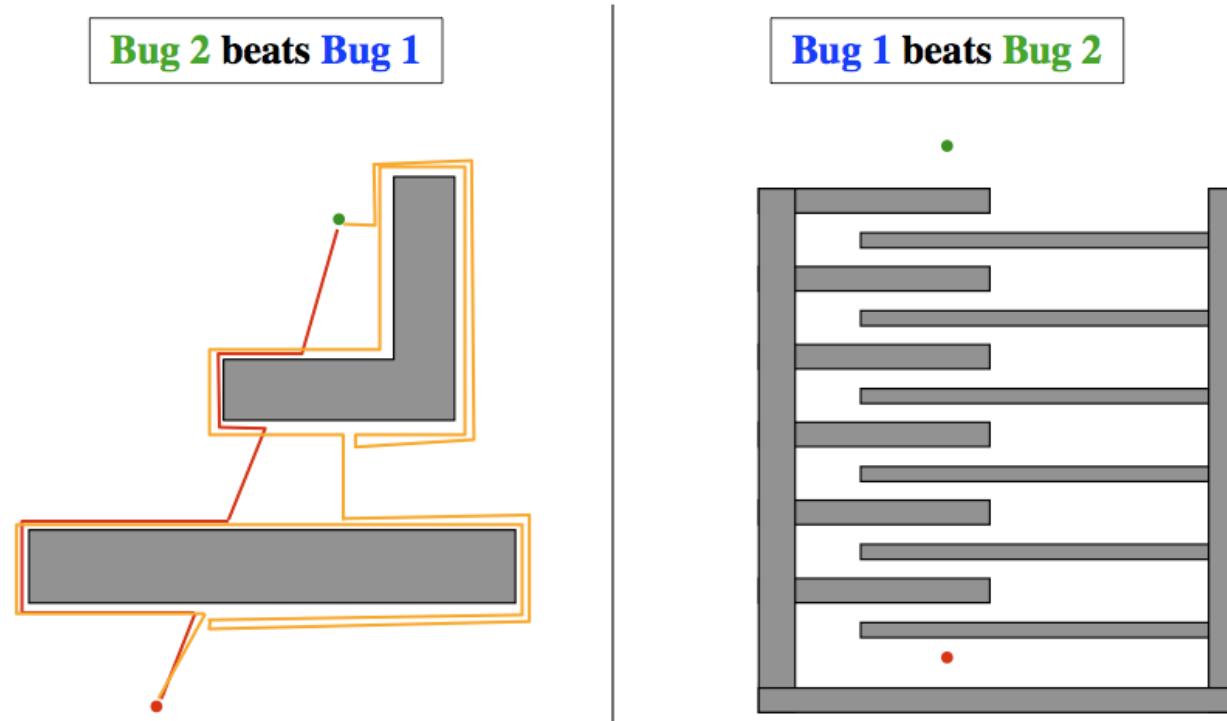
Bug 1 v. Bug 2:

Draw worlds where Bug 2 performs better than Bug 1 (and vice versa)



Bug 1 v. Bug 2:

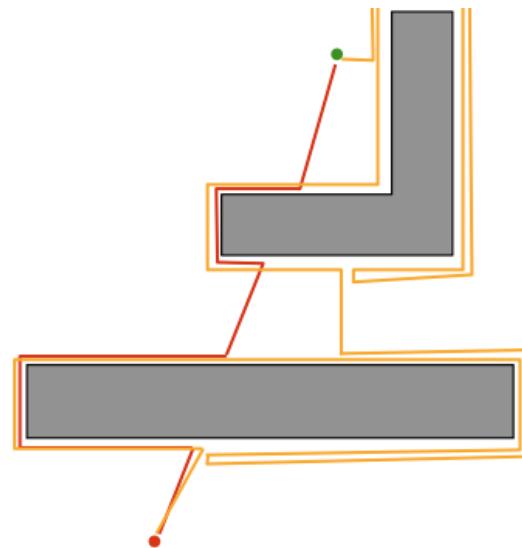
Draw worlds where Bug 2 performs better than Bug 1 (and vice versa)



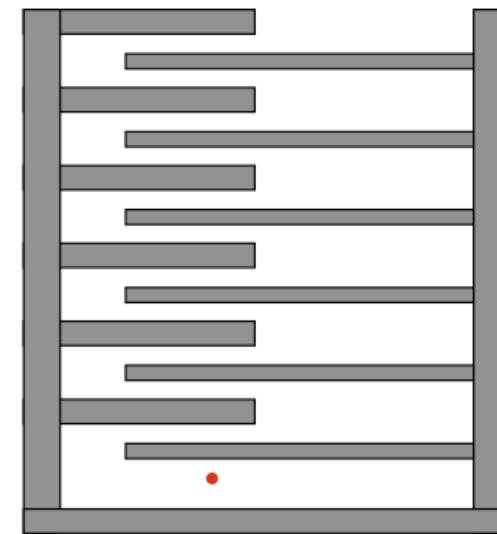
Bug 1 v. Bug 2:

Draw worlds where Bug 2 performs better than Bug 1 (and vice versa)

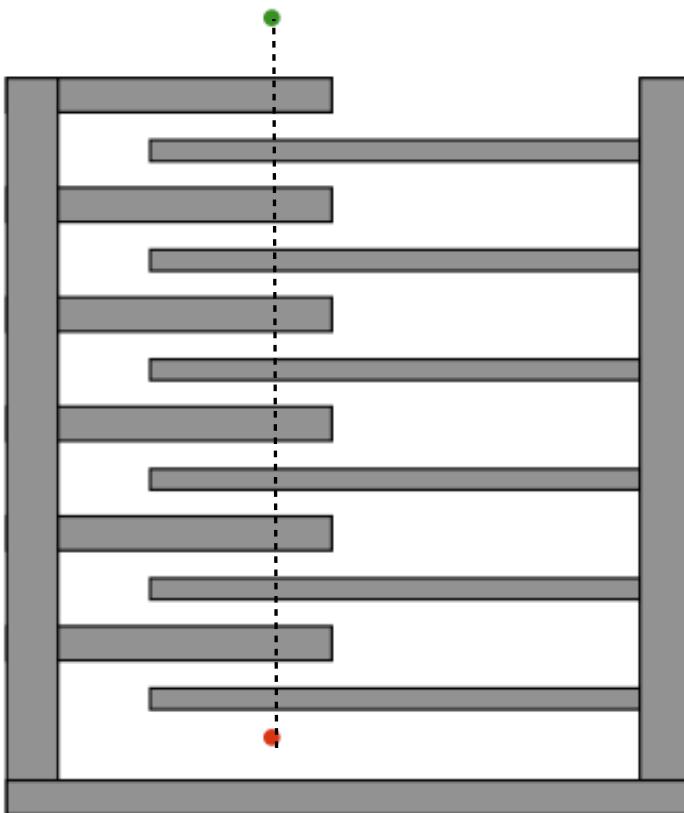
Bug 2: greedy, better typical performance



Bug 1: exhaustive search, more predictable



Bug 2: Search Bounds



Bounds on path distance, assuming

- D : distance start-to-goal
- P_i : obstacle perimeter
- n_i : number of m-line intersections for WO_i

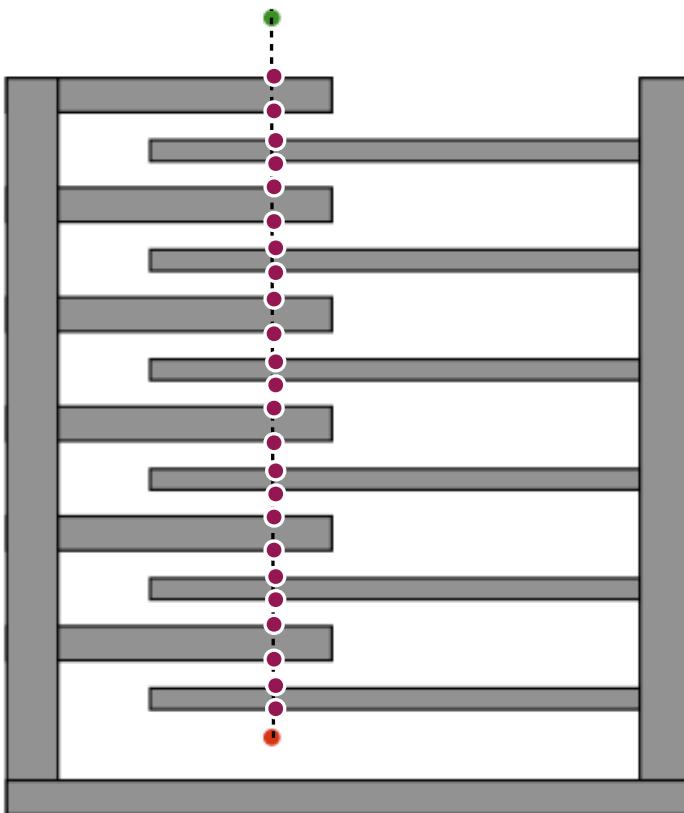
Best case:



Worst case:



Bug 2: Search Bounds



Bounds on path distance, assuming

- D : distance start-to-goal
- P_i : obstacle perimeter
- n_i : number of m-line intersections for WO_i

Best case: D

Worst case: $D + \sum_i (n_i/2)P_i$

Why?

Why?

Consider all leave points on m-line;
only half are valid



Each leave pt might require traversing entire
obstacle perimeter, including the outside

Bug 2: Search Bounds

Bounds on path distance, assuming

- D : distance start-to-goal
- P_i : obstacle perimeter
- n_i : number of m-line intersections for WO_i

Best case: D

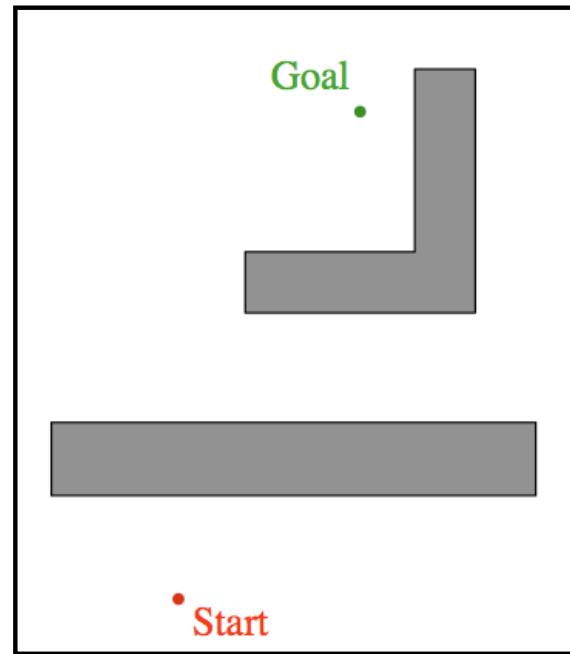
Worst case: $D + \sum_i (n_i/2)P_i$

Suppose robot has a range sensor.

Is there a better Bug algorithm?

Tangent Bug

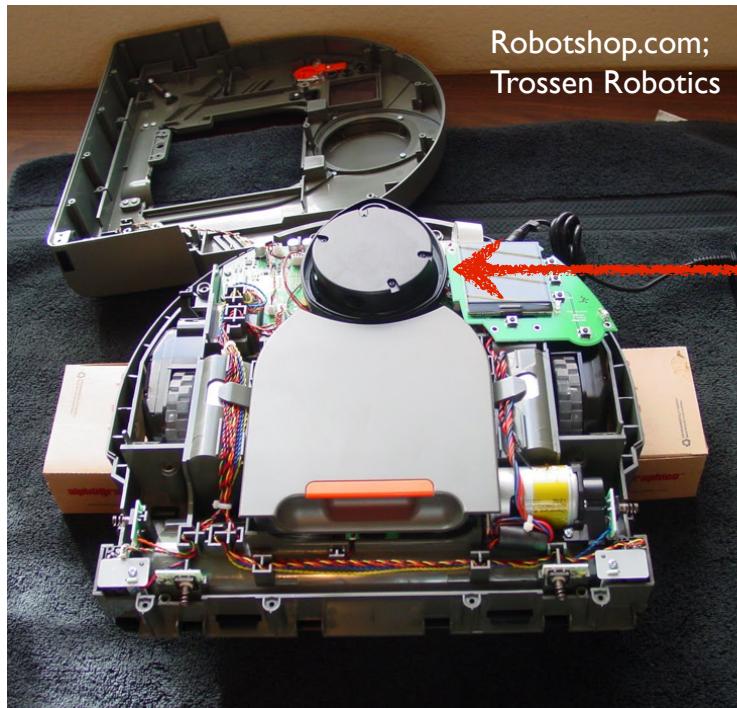
- Assume bounded world
- Known: global goal
 - measurable distance $d(x,y)$
- Local sensing
- **range finding**
- odometry



>



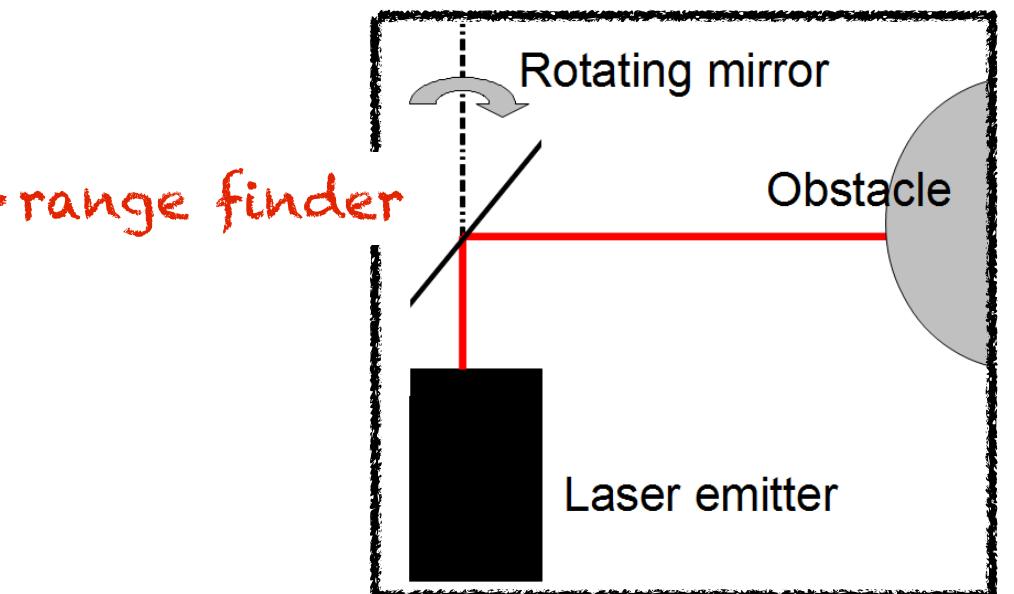
Laser Rangefinding (briefly)

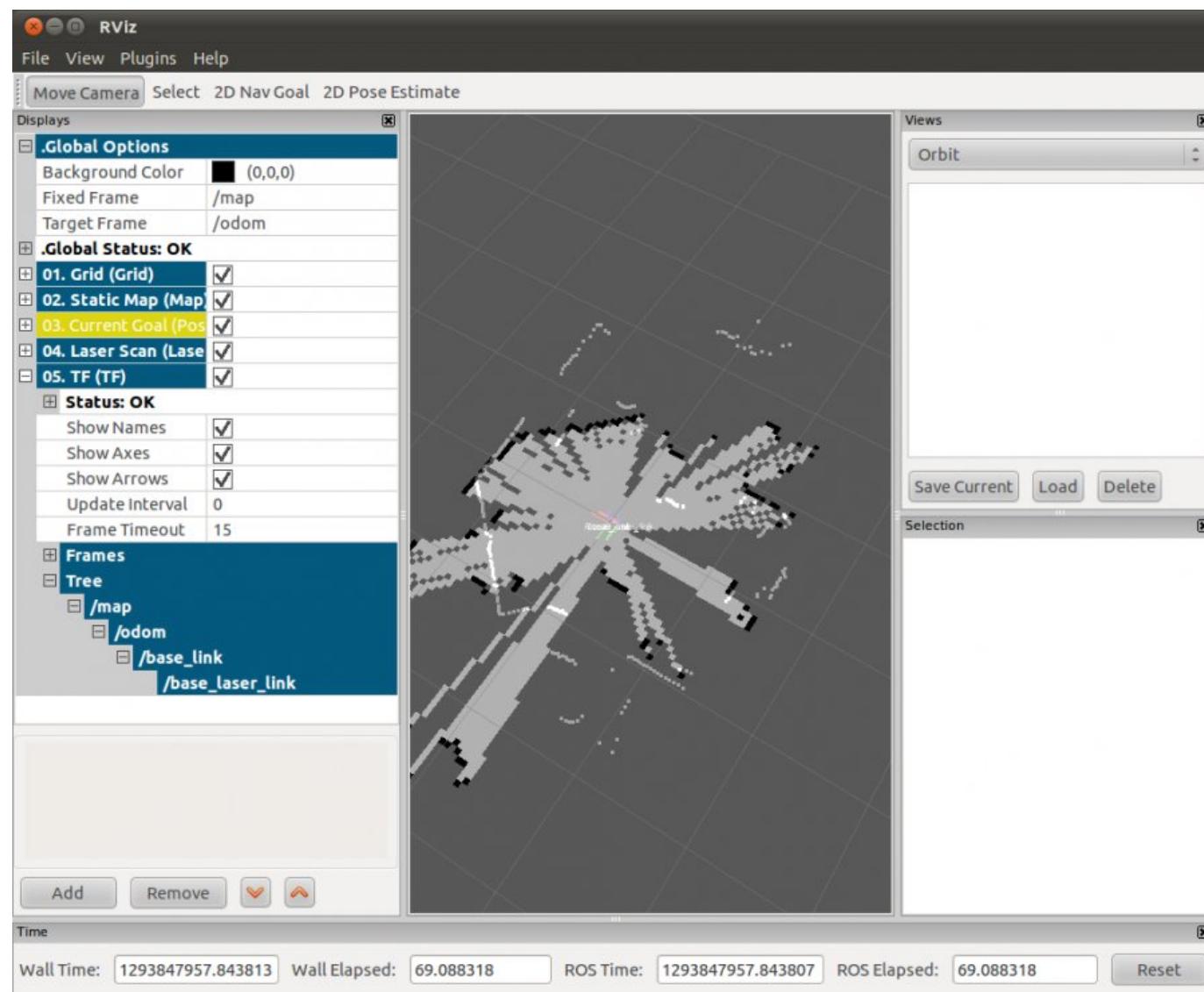


Emit laser beam in a direction

Distance to nearest object related to time from emission to sensing of beam
(assumes speed of light is known)

Planar range finding : reflect laser on spinning mirror (typically at 10Hz)



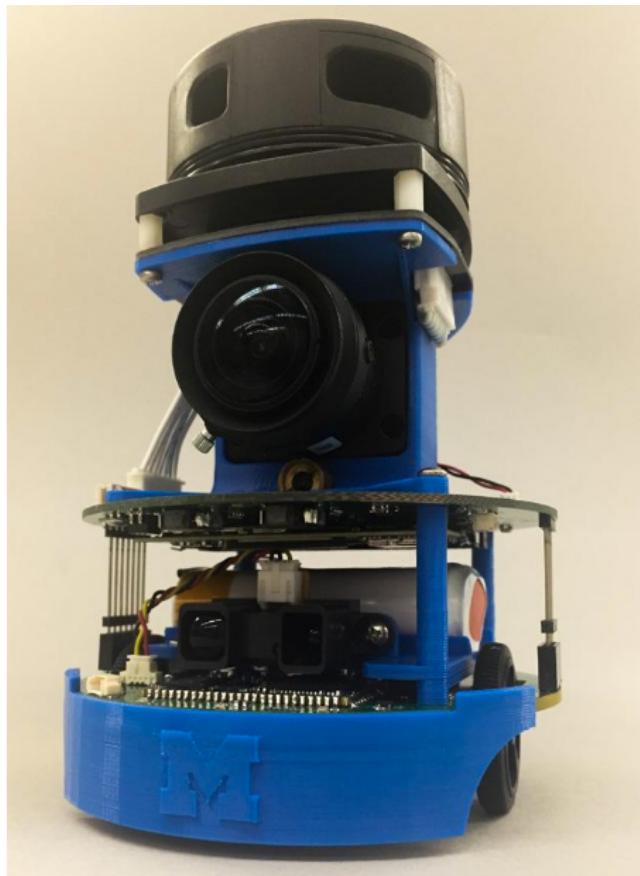


ROS LaserScan definition

LaserScan message:

```
Header header
uint32 seq
time stamp
string frame_id
float32 angle_min
float32 angle_max
float32 angle_increment
float32 time_increment
float32 scan_time
float32 range_min
float32 range_max
float32[] ranges
float32[] intensities
```

SLAM - BotLab

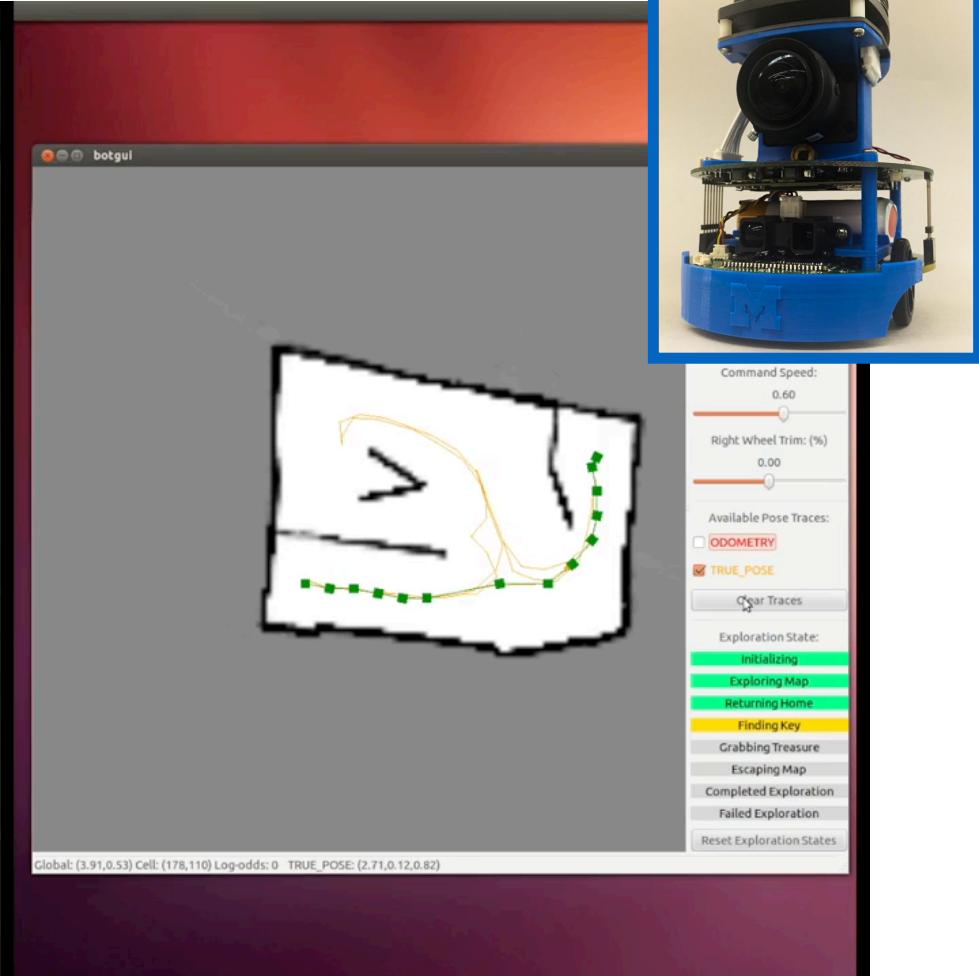
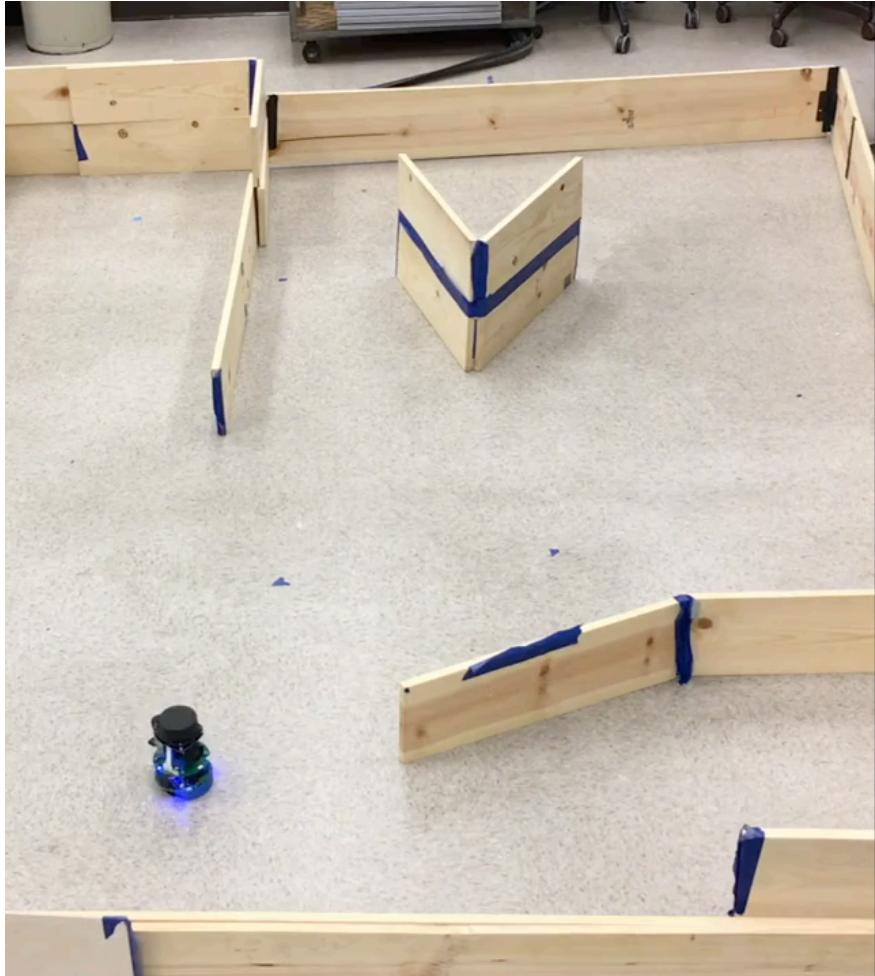


ROB 550 / EECS 467



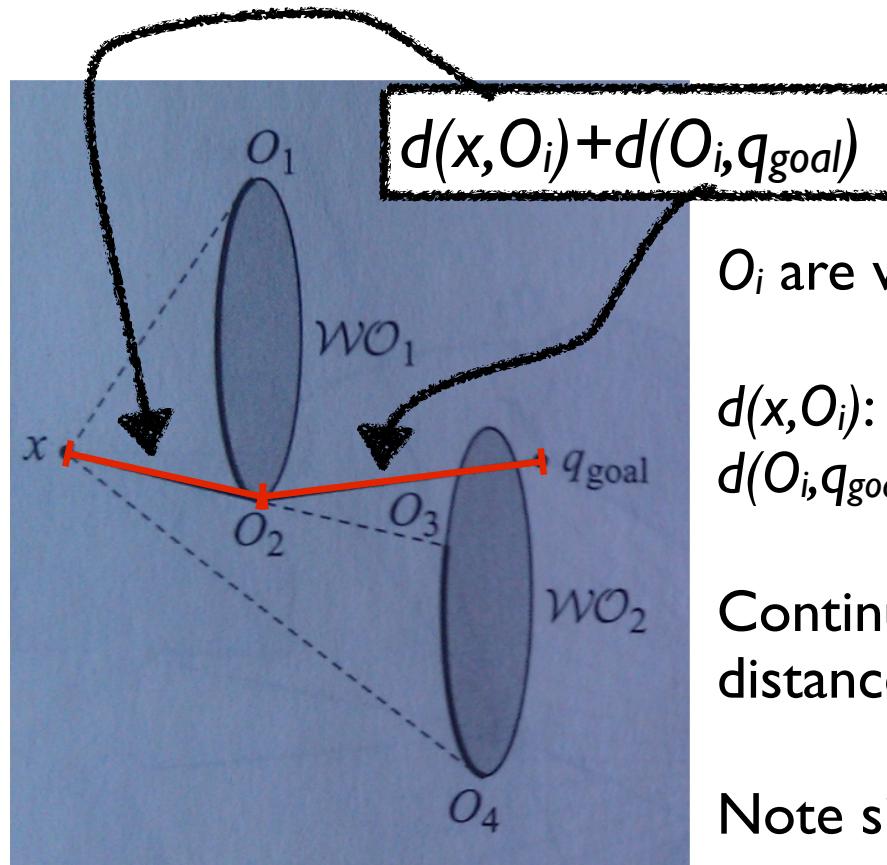
UM EECS 398/598 - autorob.github.io

ROB 550 BotLab / EECS 467 Escape Challenge



UM EECS 467 autobot.github.io Jasmine Liu et al.

Tangent Bug: Heuristic Distance-to-Goal



O_i are visible obstacle extents

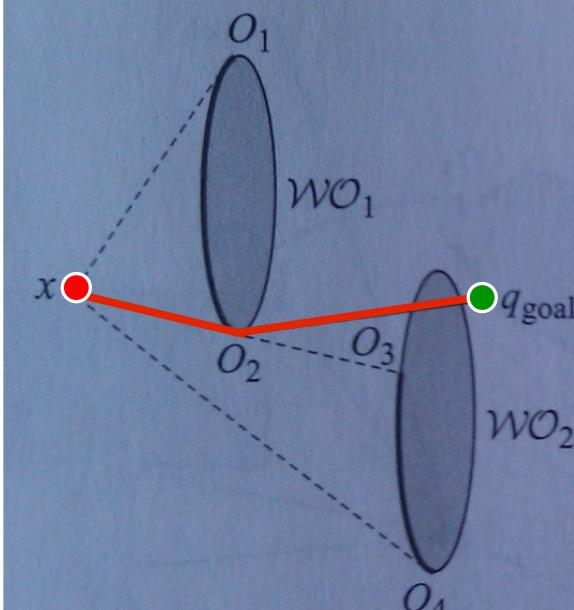
$d(x, O_i)$: robot can see

$d(O_i, q_{goal})$: best path robot cannot see

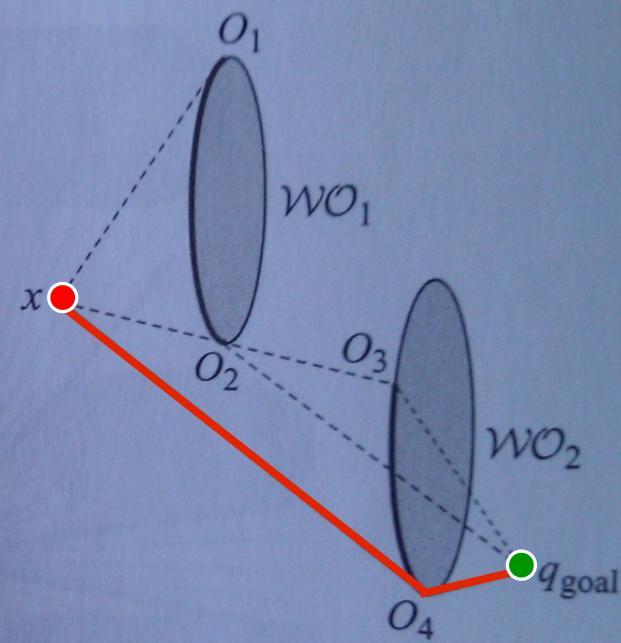
Continually move robot such that distance to goal is decreased

Note similarity to A* search heuristic

$$d(x, O_2) + d(O_2, q_{goal})$$



$$d(x, O_4) + d(O_4, q_{goal})$$

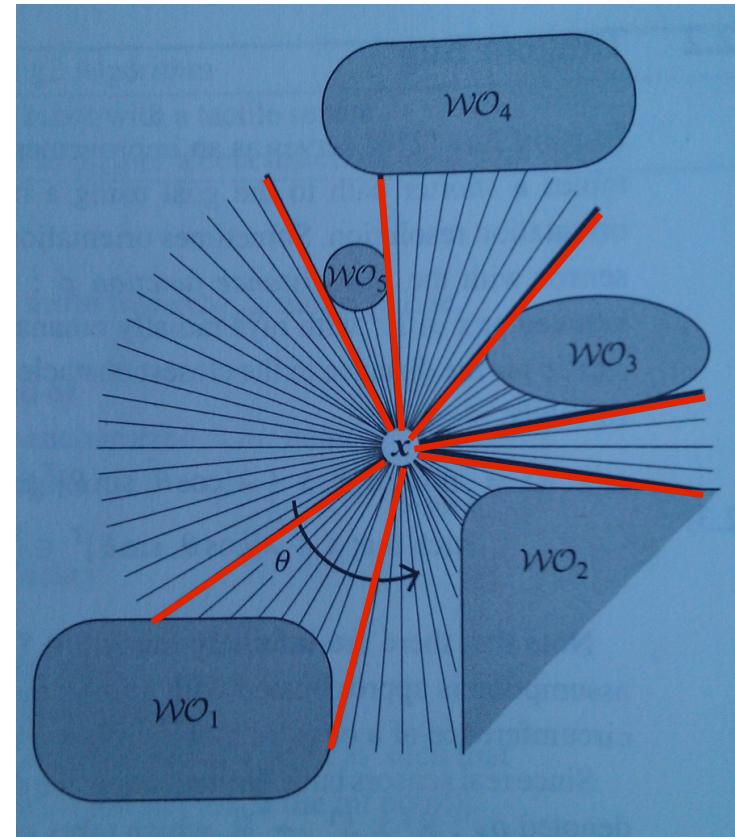


Range Segmentation

range scan $\rho(x, \Theta)$: sensed distance along ray at angle Θ within limit R

discontinuities $\{O_i\}$ in scan result from obstacles

$\{O_i\}$ segments scan into intervals of continuity, with obstacles and free space

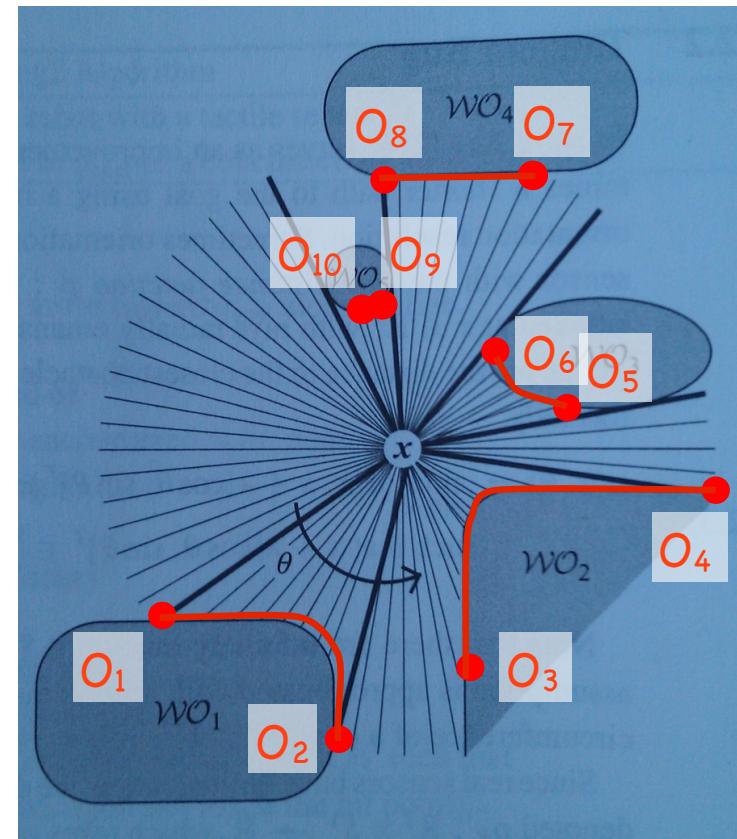


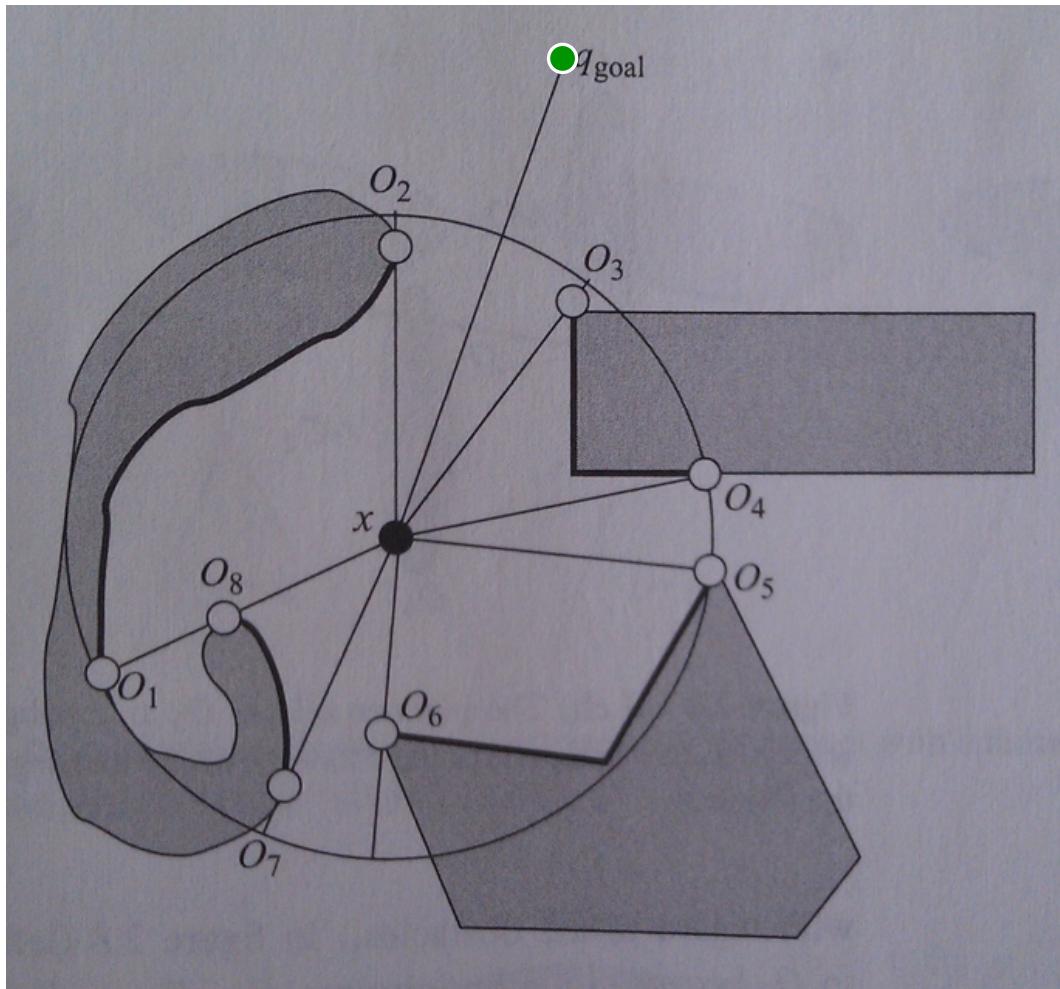
Range Segmentation

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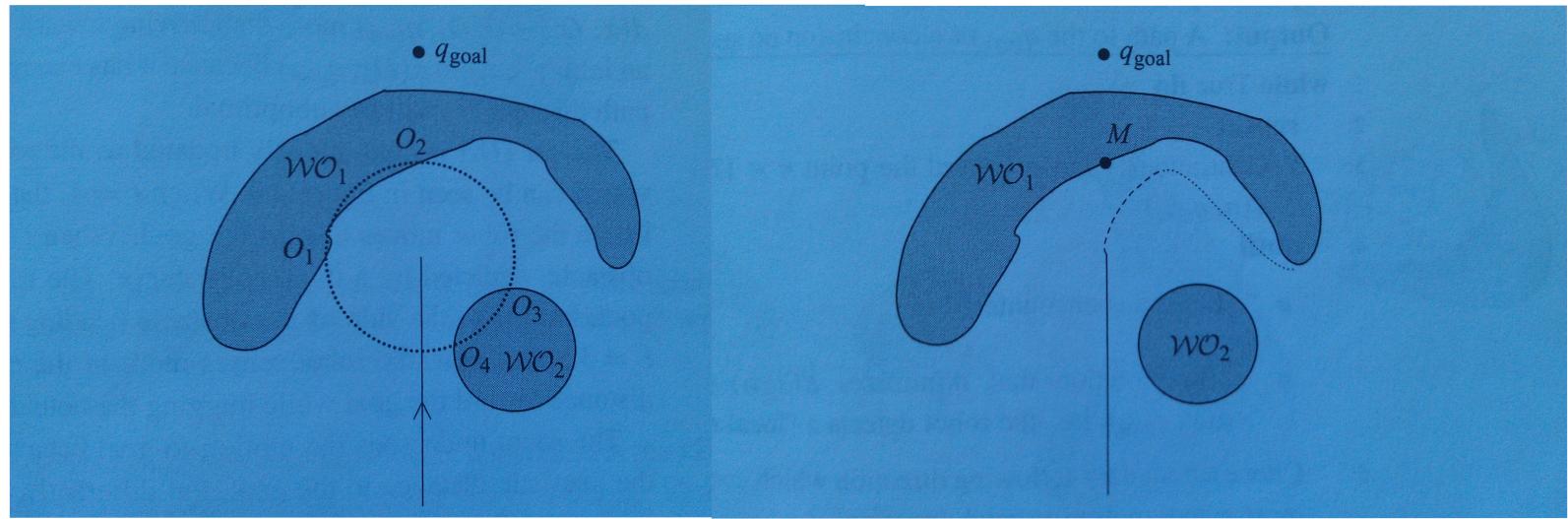
$\{O_i\}$ segments scan into intervals
continuity, with obstacles and free space





Tangent Bug Behaviors

Similar to other bug algorithms, Tangent Bug uses two behaviors:

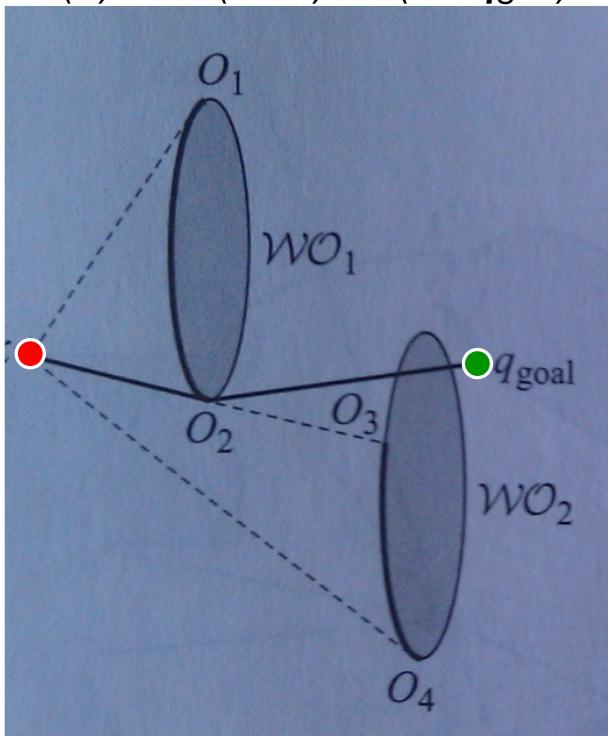


motion-to-goal

boundary-follow

Tangent Bug

$$G(x) = d(x, O_i) + d(O_i, q_{goal})$$



1) motion-to-goal: Move to current O_i to minimize $G(x)$, until goal (success) or $G(x)$ increases (local minima)

2) boundary-follow: move in while loop:

a) repeat updates

$$d_{reach} = \min d(q_{goal}, \{\text{visible } O_i\})$$

$$d_{follow} = \min d(q_{goal}, \text{sensed}(WO_j))$$

$$O_i = \operatorname{argmin}_i d(x, O_i) + d(O_i, q_{goal})$$

b) until

goal reached, (**success**)

robot cycles around obstacle, (**fail**)

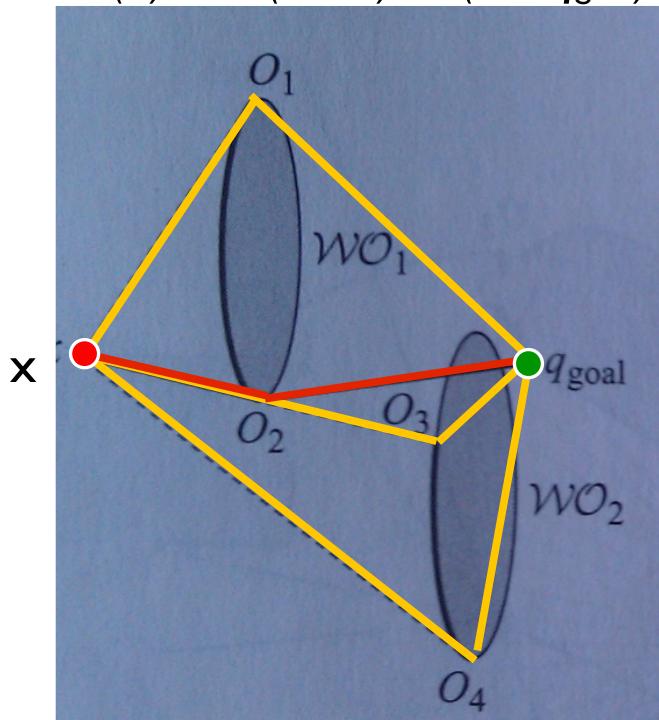
$$d_{reach} < d_{follow},$$

(**cleared obstacle or local minima**)

3) continue from (1)

Tangent Bug

$$G(x) = d(x, O_2) + d(O_2, q_{goal})$$



$\min G(x)$ in red, others in yellow

1) motion-to-goal: Move to current O_i to minimize $G(x)$, until goal (success) or $G(x)$ increases (local minima)

2) boundary-follow: move in while loop:

a) repeat updates

$$d_{reach} = \min d(q_{goal}, \{\text{visible } O_i\})$$

$$d_{follow} = \min d(q_{goal}, \text{sensed}(WO_j))$$

$$O_i = \operatorname{argmin}_i d(x, O_i) + d(O_i, q_{goal})$$

b) until

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robot cycles around obstacle, (**fail**)

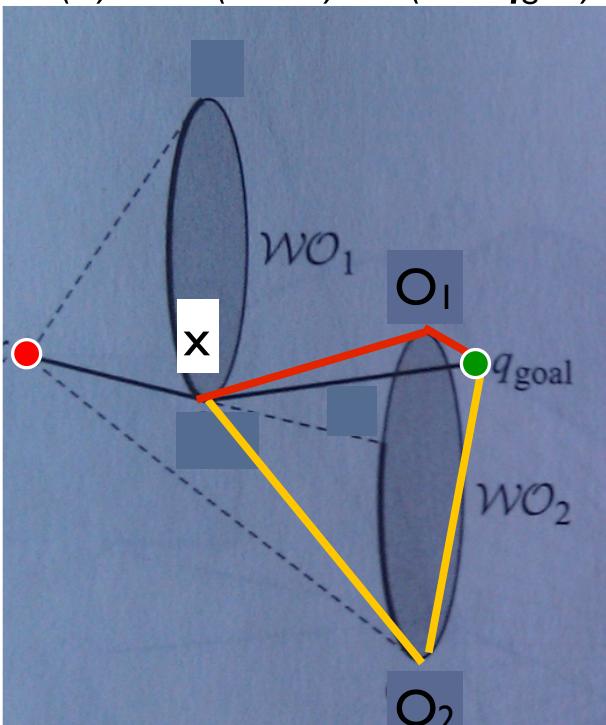
$$d_{reach} < d_{follow},$$

(**cleared obstacle or local minima**)

3) continue from (1)

Tangent Bug

$$G(x) = d(x, O_1) + d(O_1, q_{goal})$$



$\min G(x)$ in red, others in yellow

1) motion-to-goal: Move to current O_i to minimize $G(x)$, until goal (success) or $G(x)$ increases (local minima)

2) boundary-follow: move in while loop:

a) repeat updates

$$d_{reach} = \min d(q_{goal}, \{\text{visible } O_i\})$$

$$d_{follow} = \min d(q_{goal}, \text{sensed}(WO_j))$$

$$O_i = \operatorname{argmin}_i d(x, O_i) + d(O_i, q_{goal})$$

b) until

goal reached, (**success**)

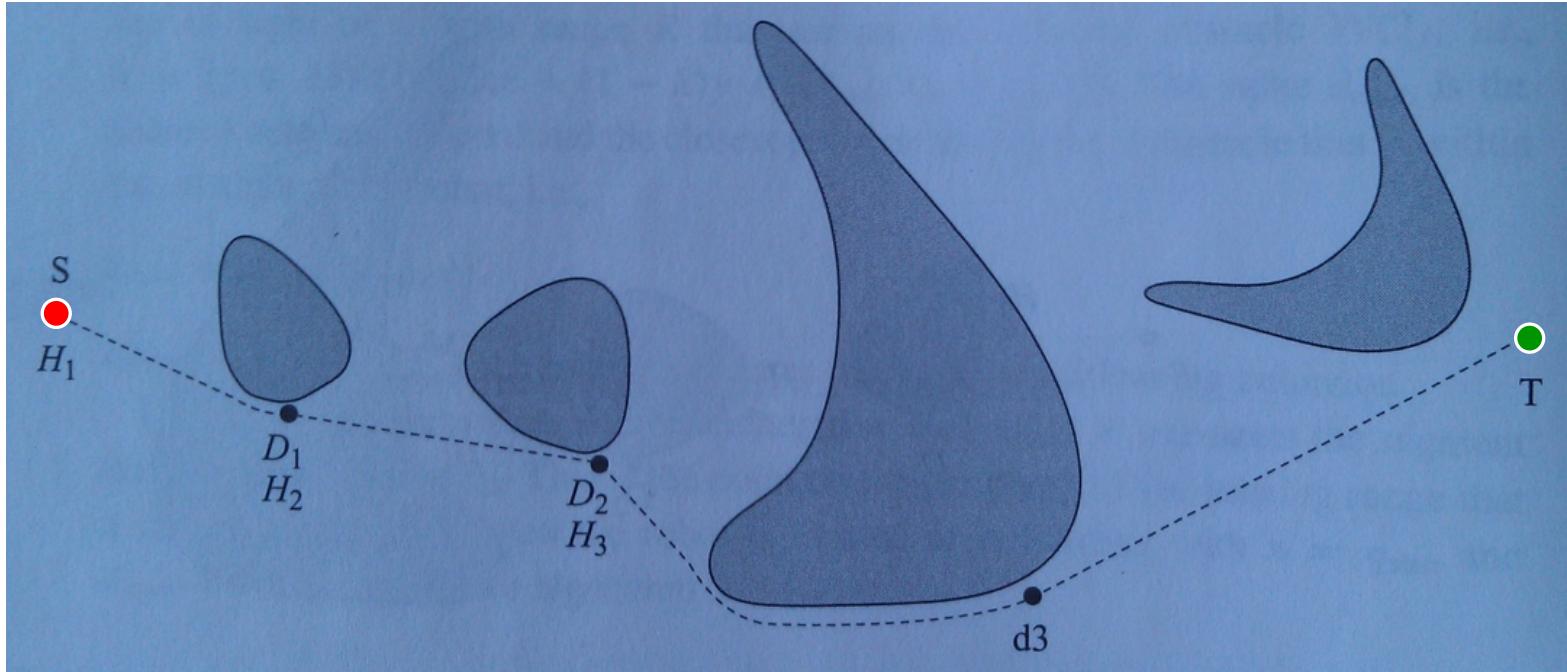
robot cycles around obstacle, (**fail**)

$$d_{reach} < d_{follow},$$

(**cleared obstacle or local minima**)

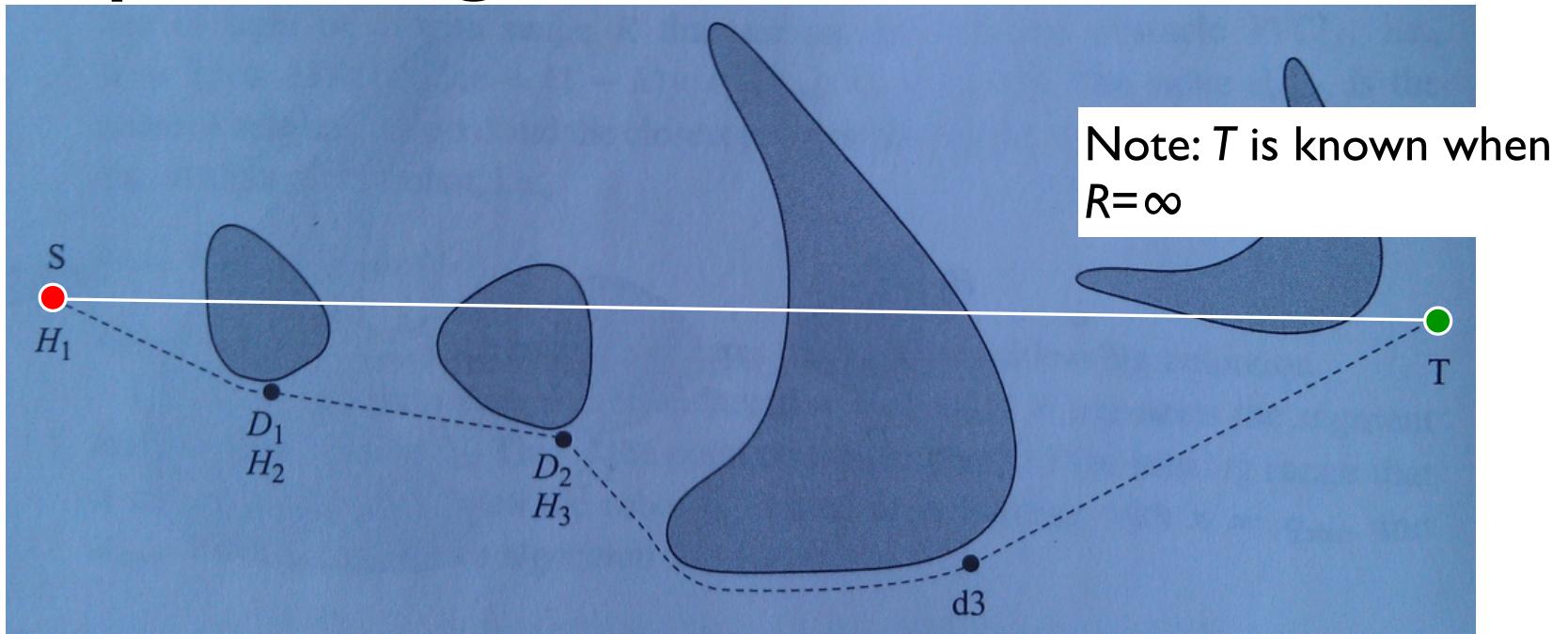
3) continue from (1)

Example: range $R=\infty$



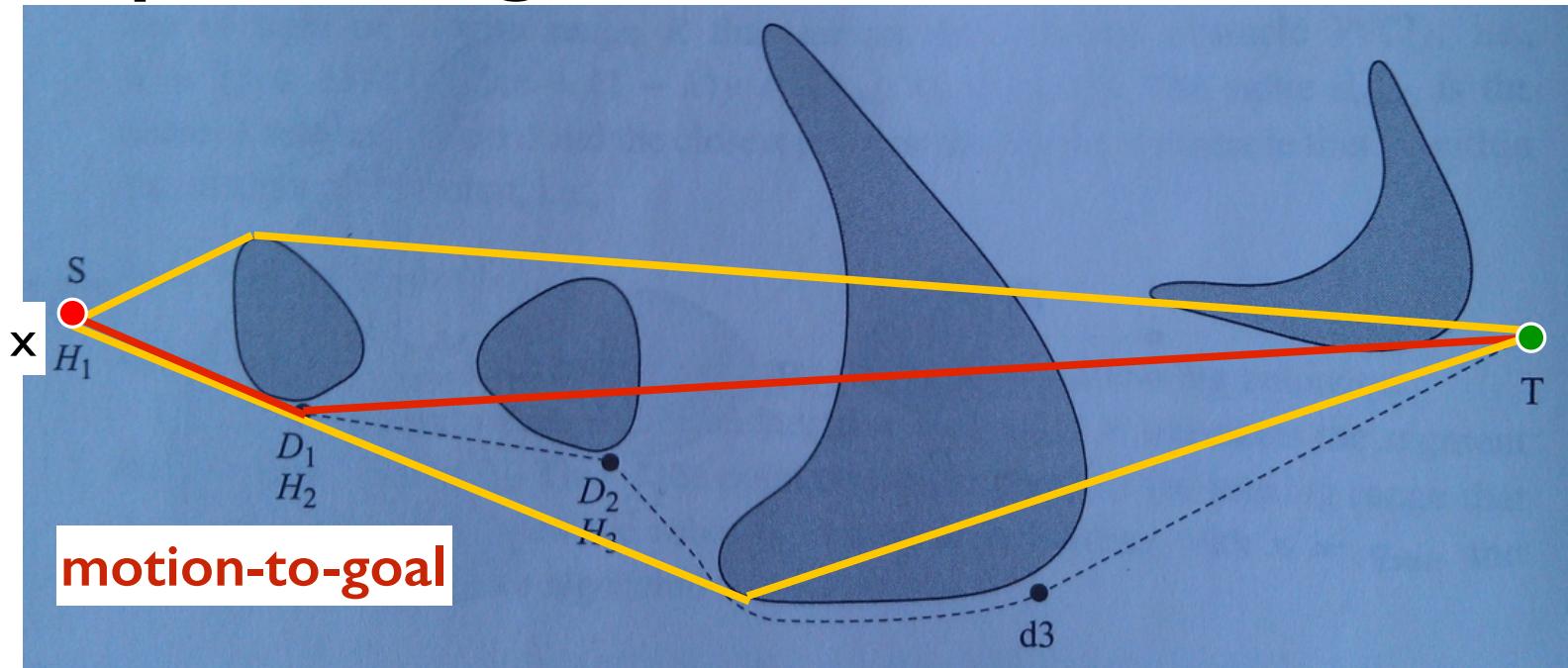
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

Example: range $R=\infty$



H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

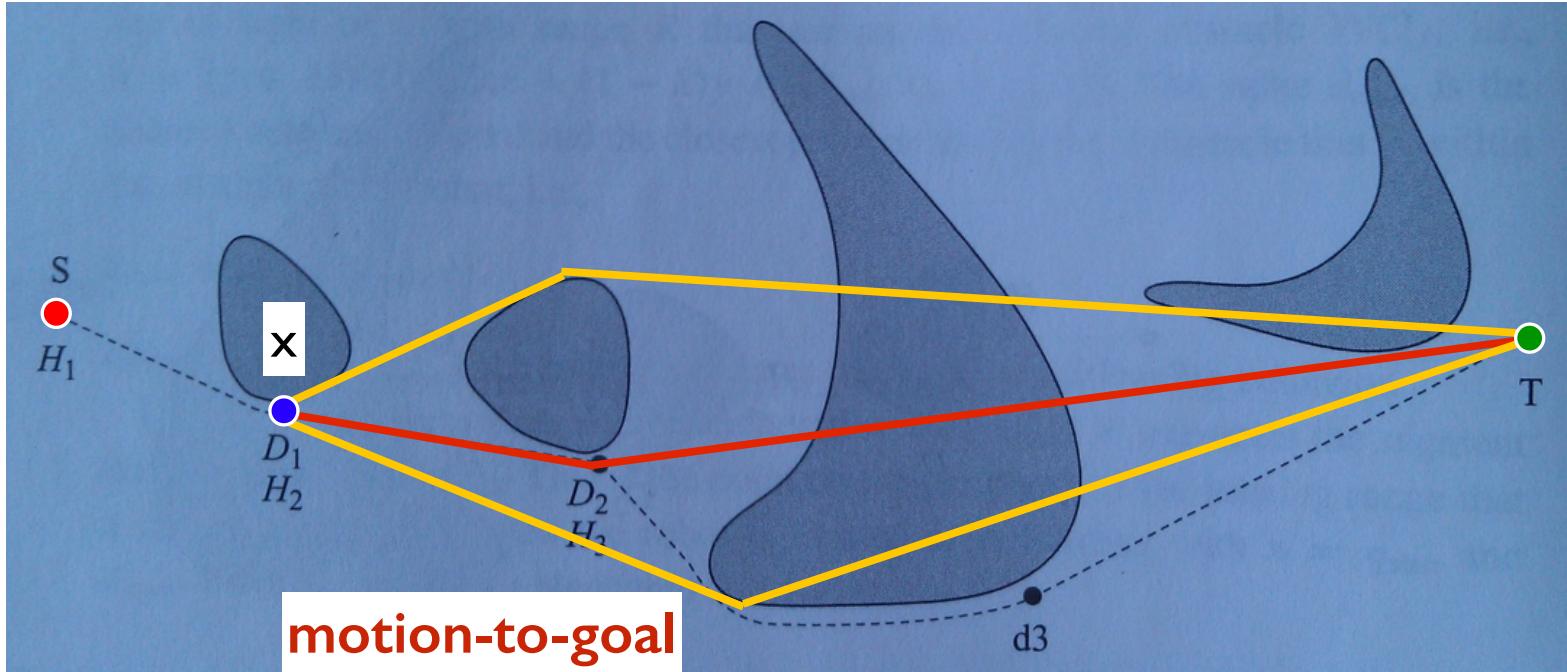
Example: range $R=\infty$



$\min G(x)$ in red, others in
yellow

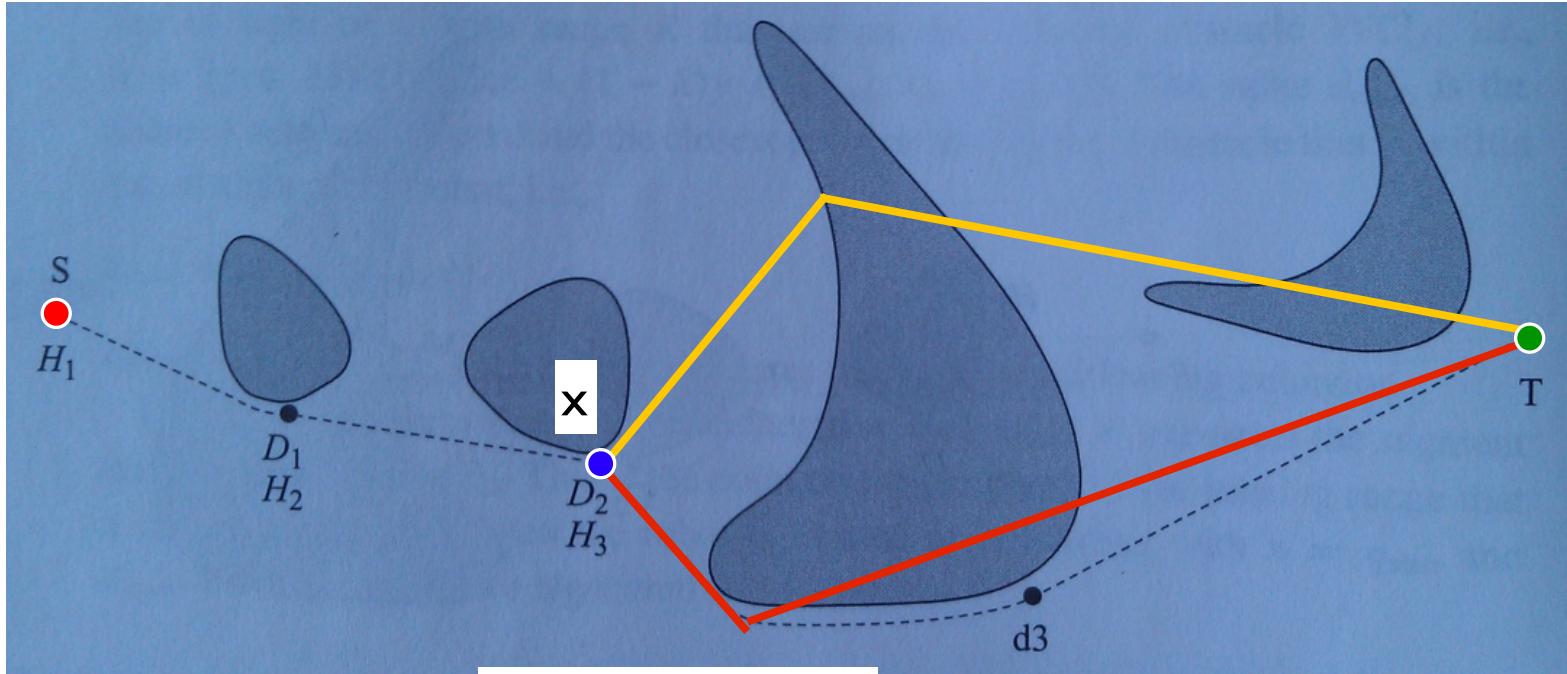
H_i : hit point
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Example: range $R=\infty$



H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

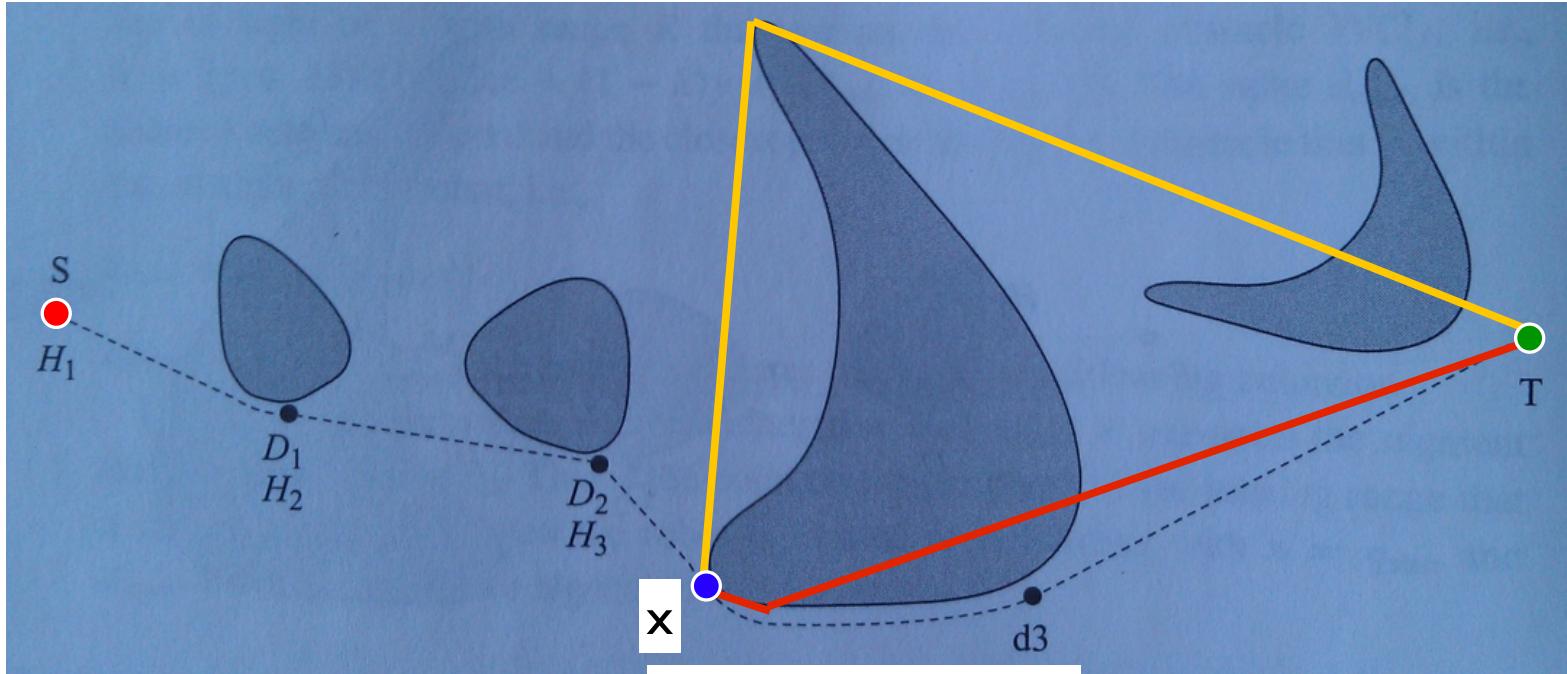
Example: range $R=\infty$



motion-to-goal

H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

Example: range $R=\infty$



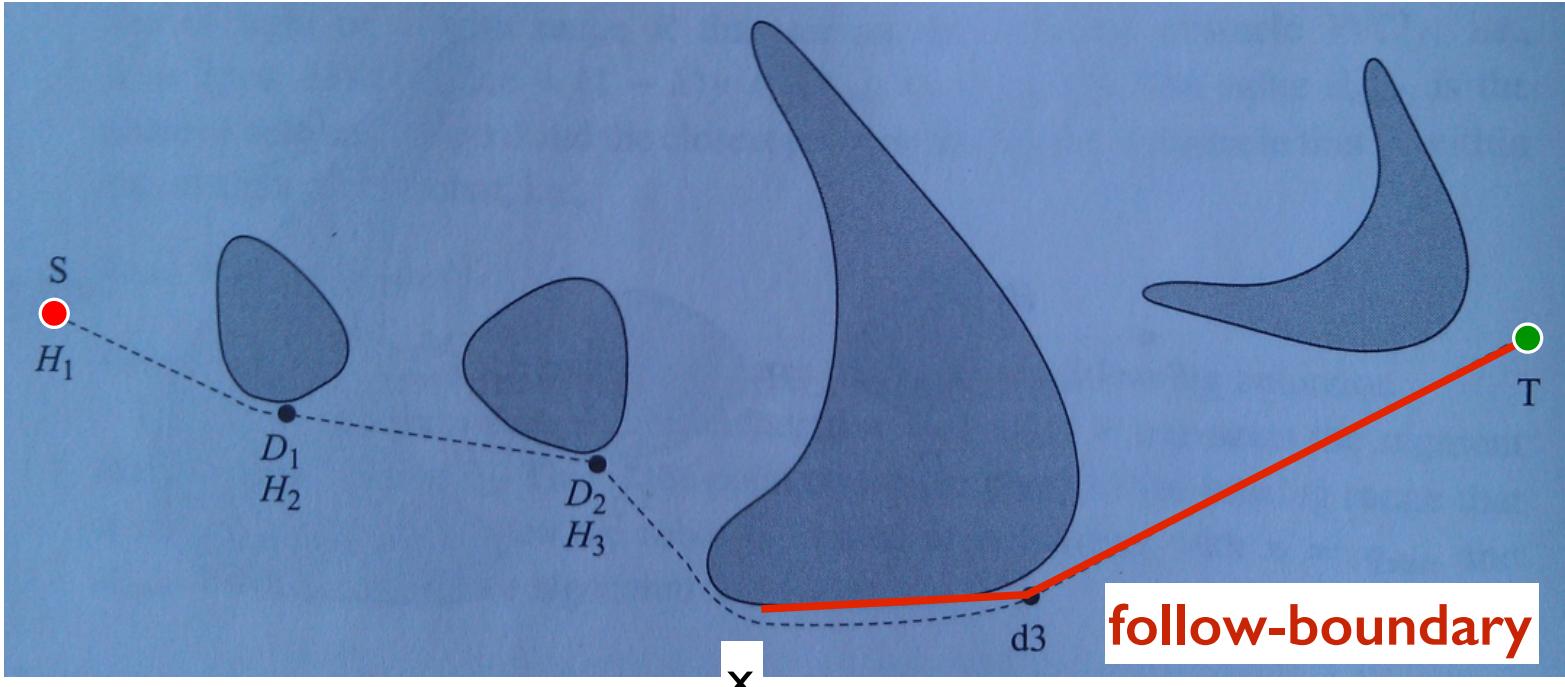
follow-boundary

start following:

$$\min d(q_{goal}, \{\text{visible } O_i\}) < \min d(q_{goal}, \text{sensed}(WO_j))$$

H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

Example: range $R=\infty$

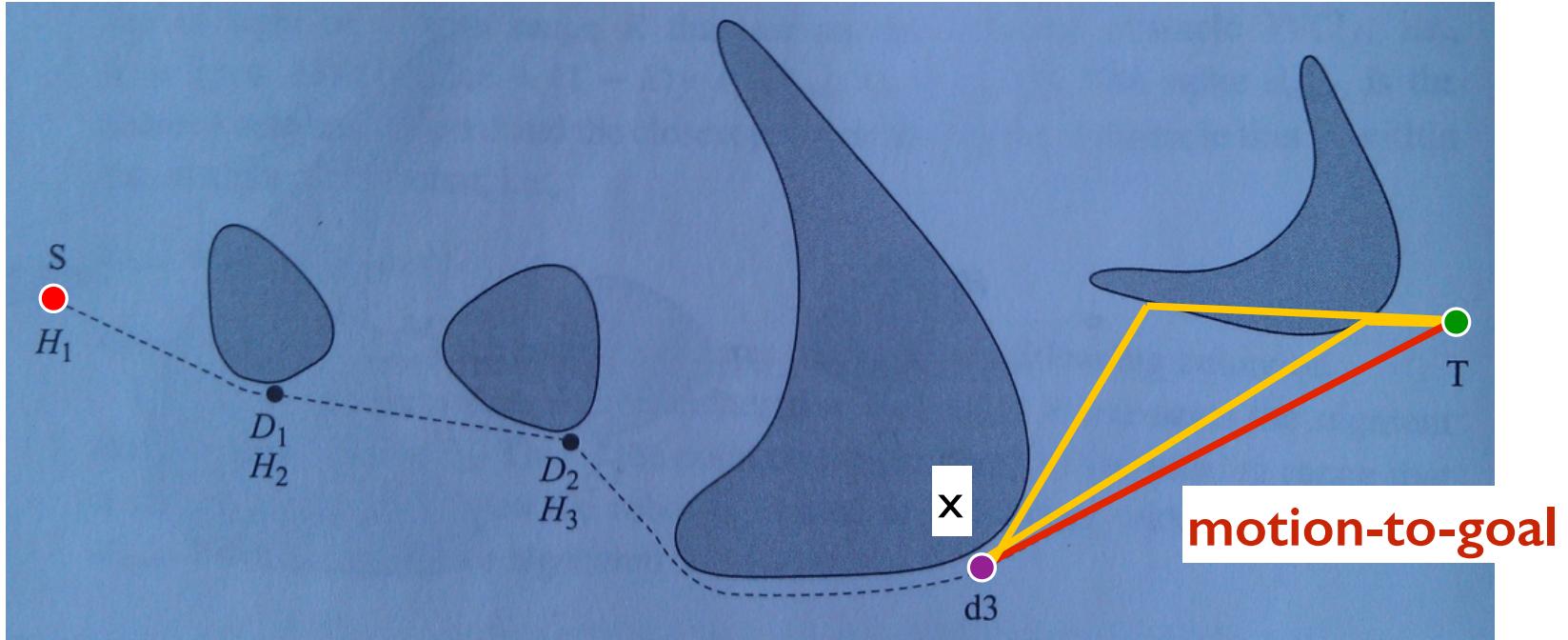


end following:

$$\min d(q_{goal}, \{\text{visible } O_i\}) < \min d(q_{goal}, \text{sensed}(WO_j))$$

H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

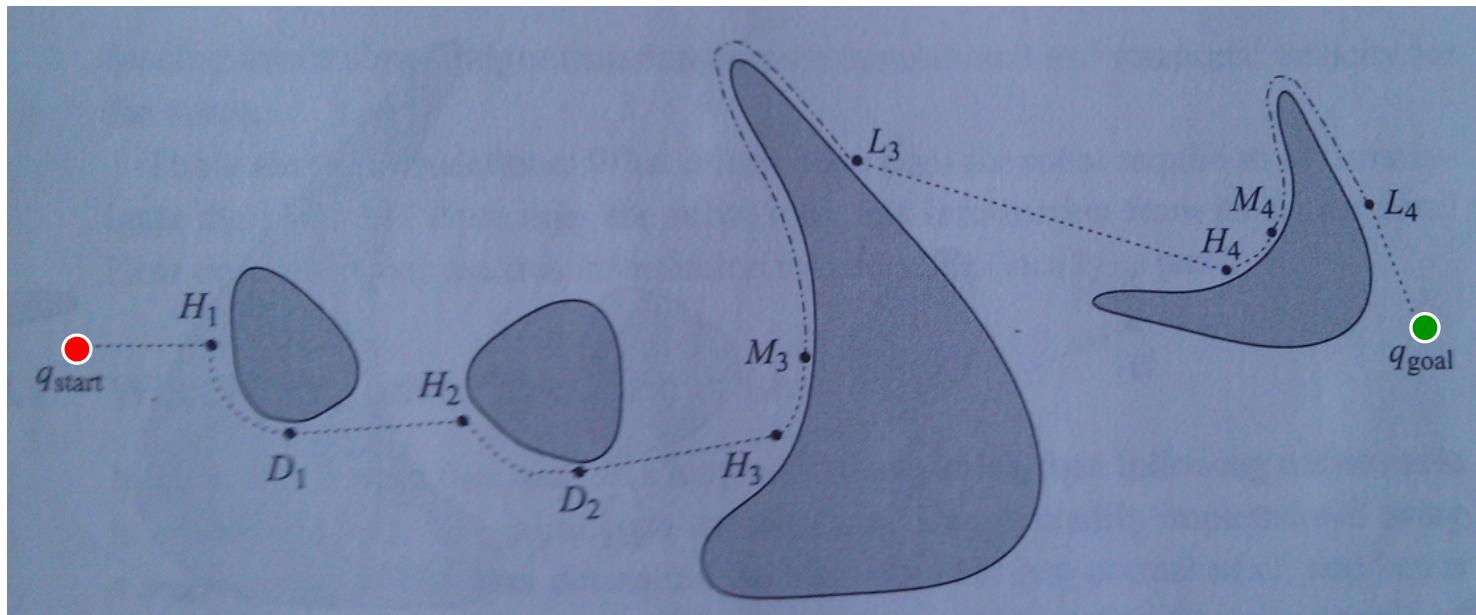
Example: range $R=\infty$



H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

Example: range $R=0$

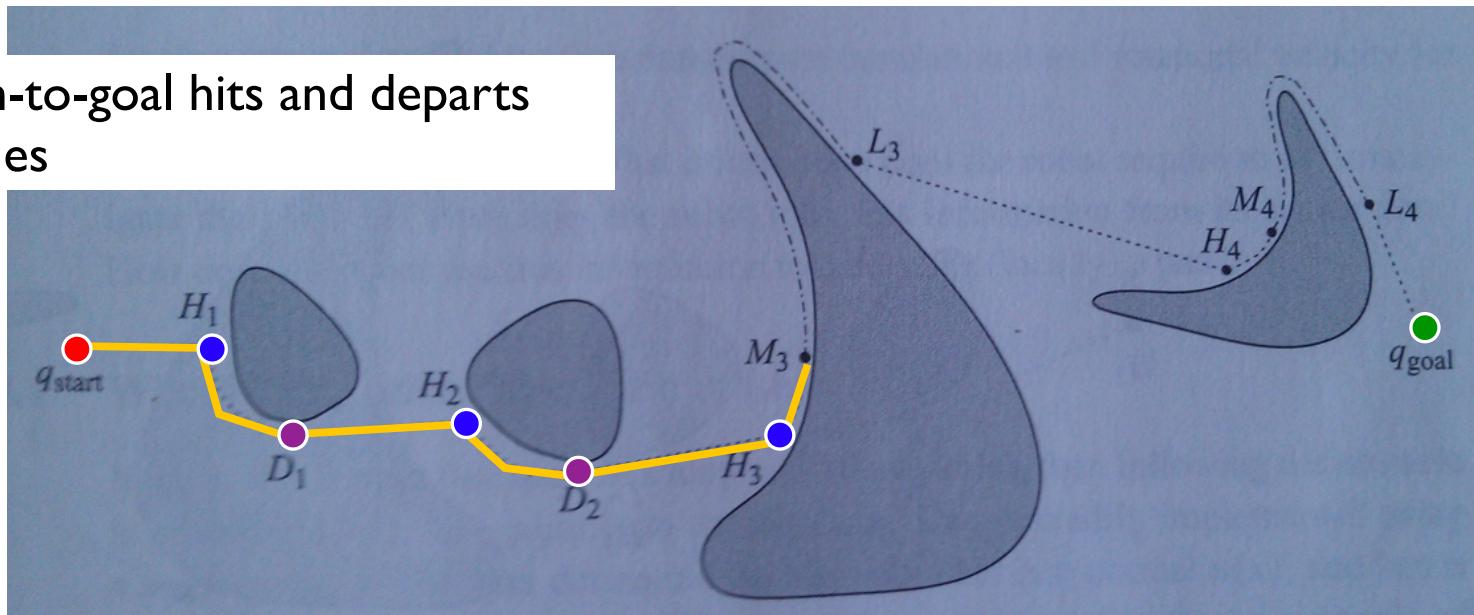
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima



Example: range $R=0$

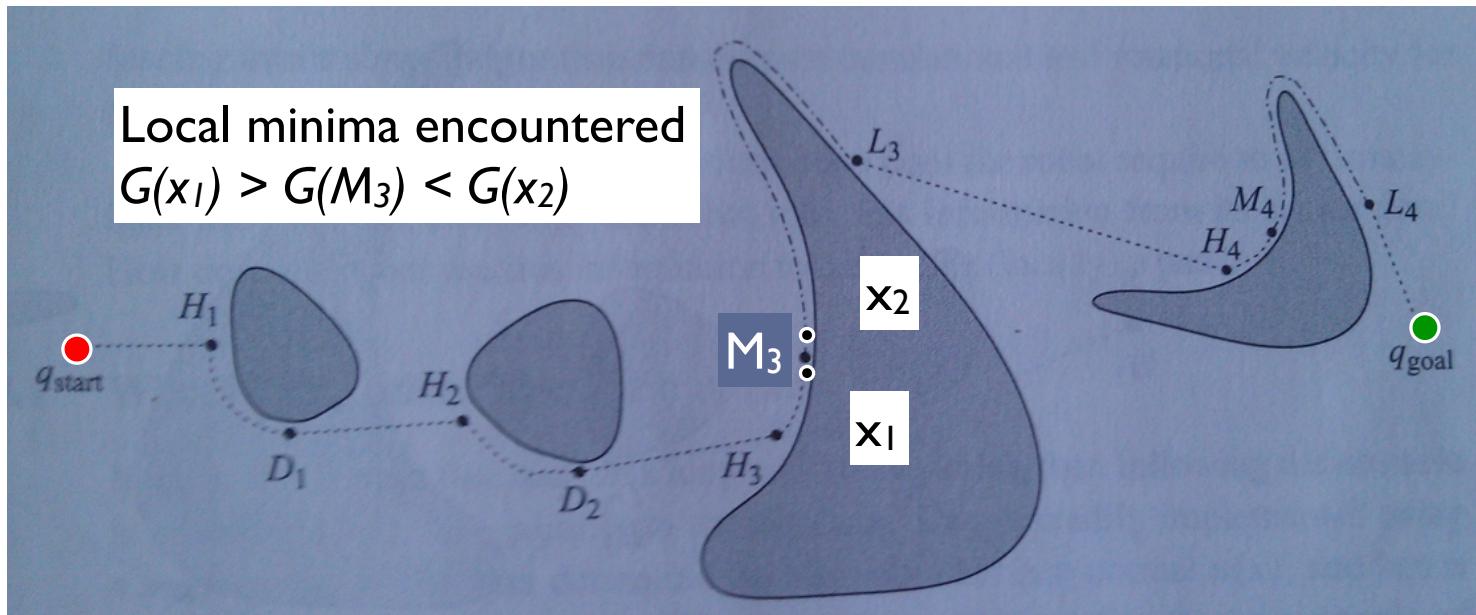
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

Motion-to-goal hits and departs obstacles



Example: range $R=0$

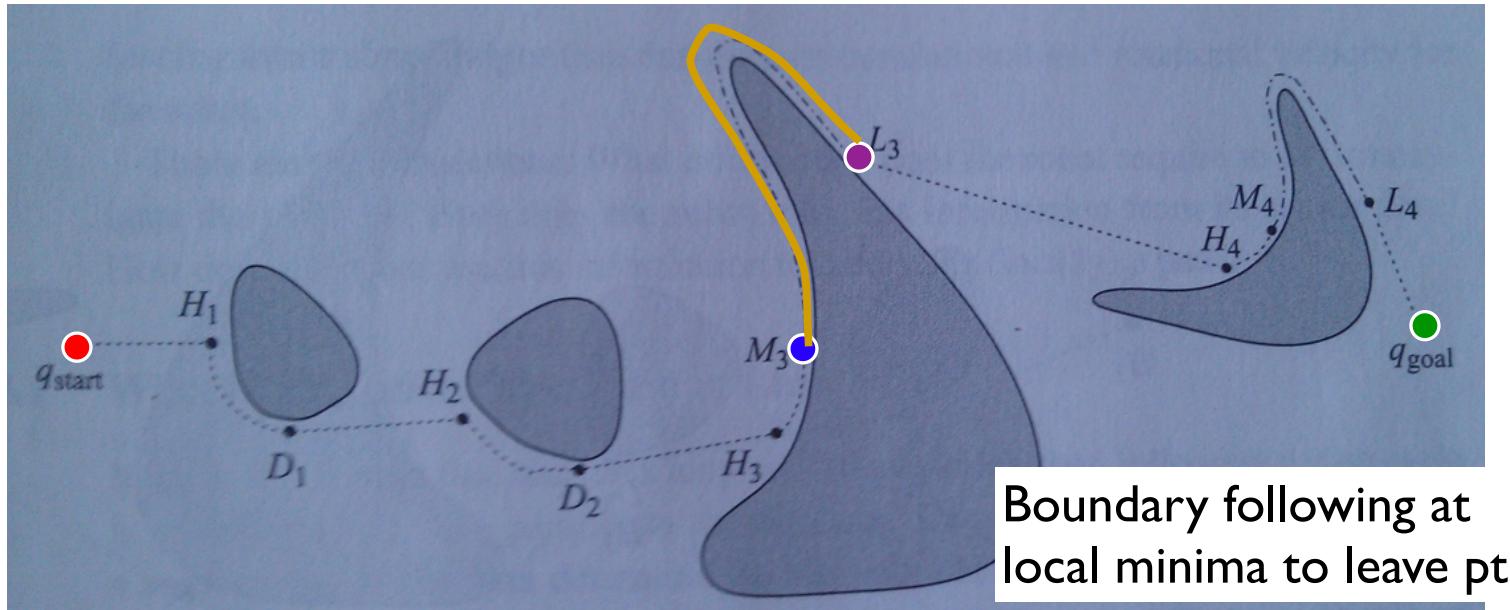
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima



Local minima at increase of $G(x) = d(x, O_i) + d(O_i, q_{goal})$

Example: range $R=0$

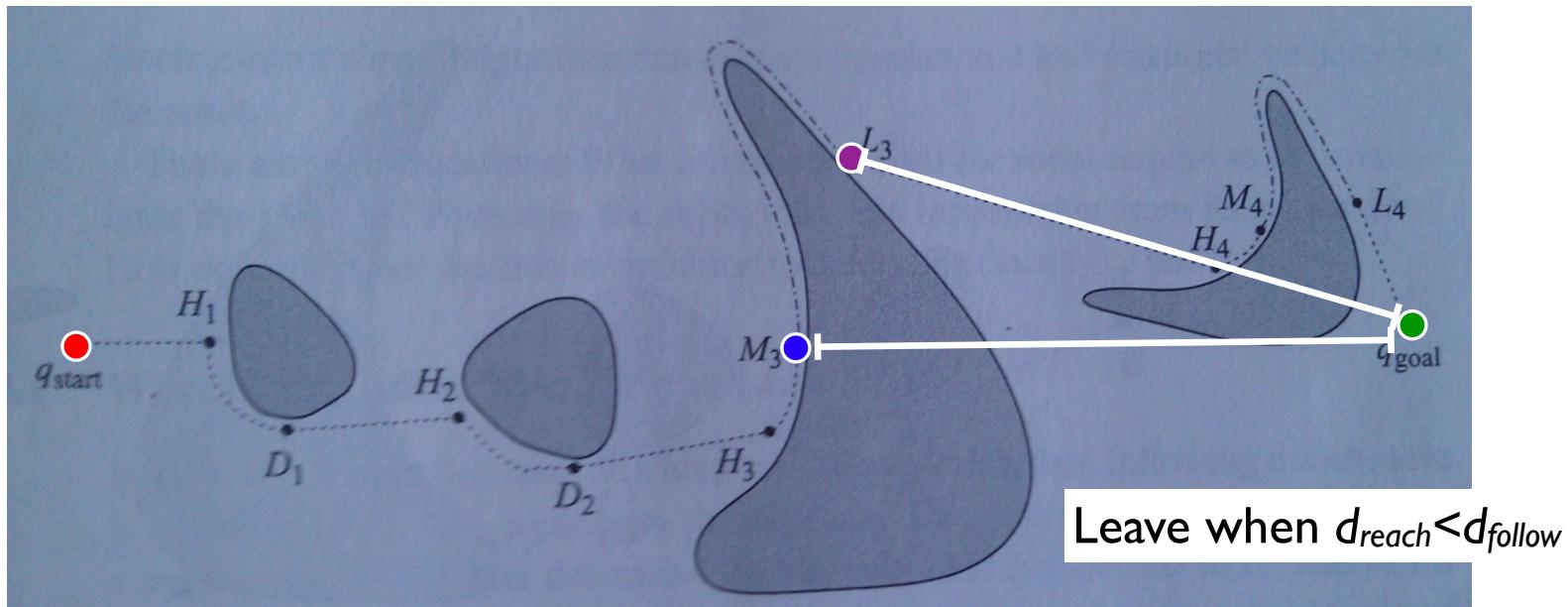
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima



Local minima at increase of $G(x) = d(x, O_i) + d(O_i, q_{goal})$

Example: range $R=0$

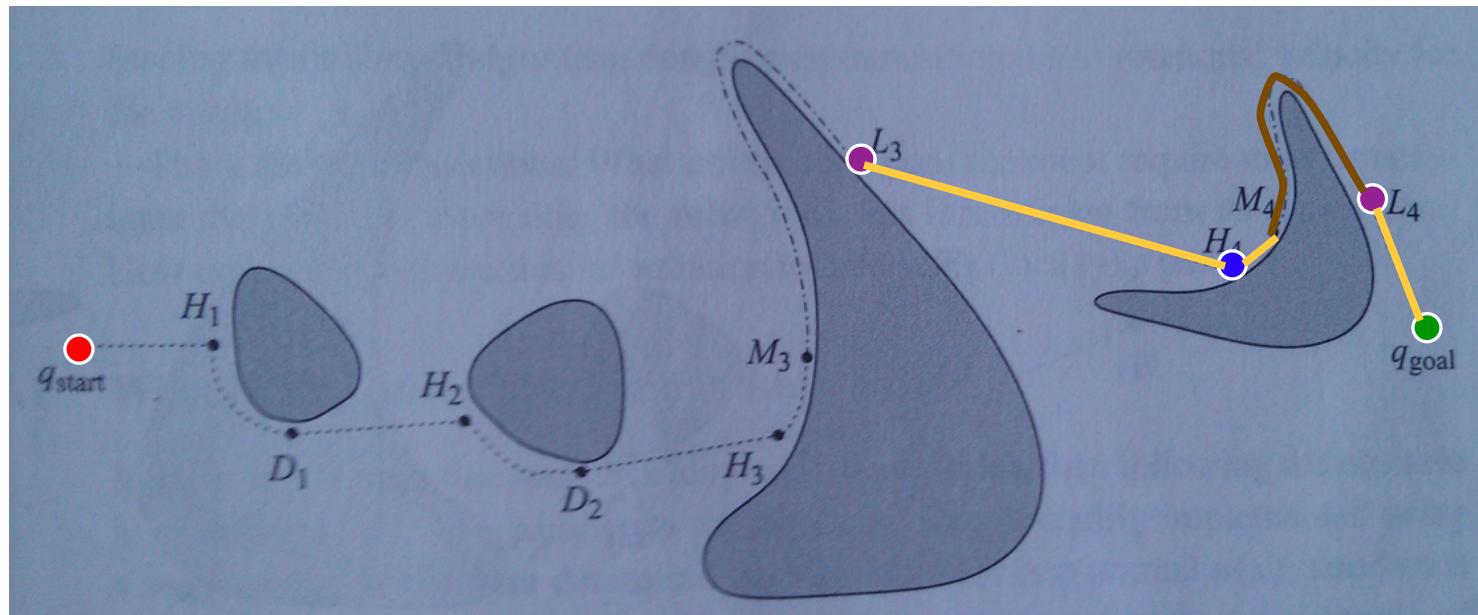
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima

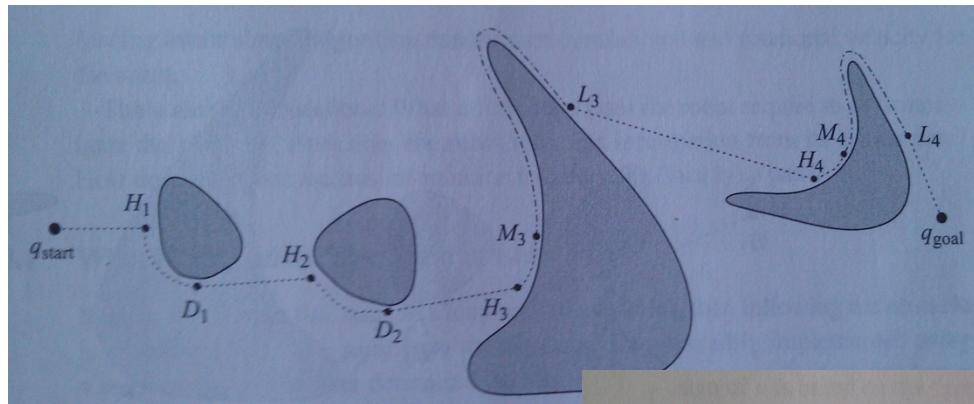


Local minima at increase of $G(x) = d(x, O_i) + d(O_i, q_{goal})$

Example: range $R=0$

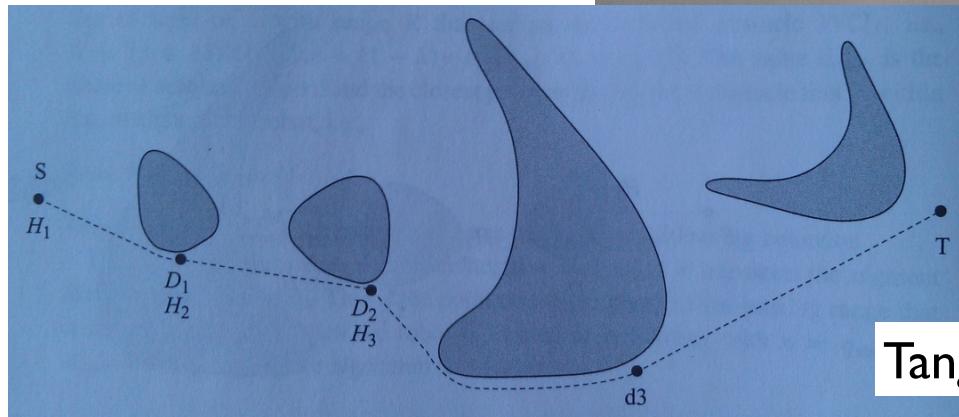
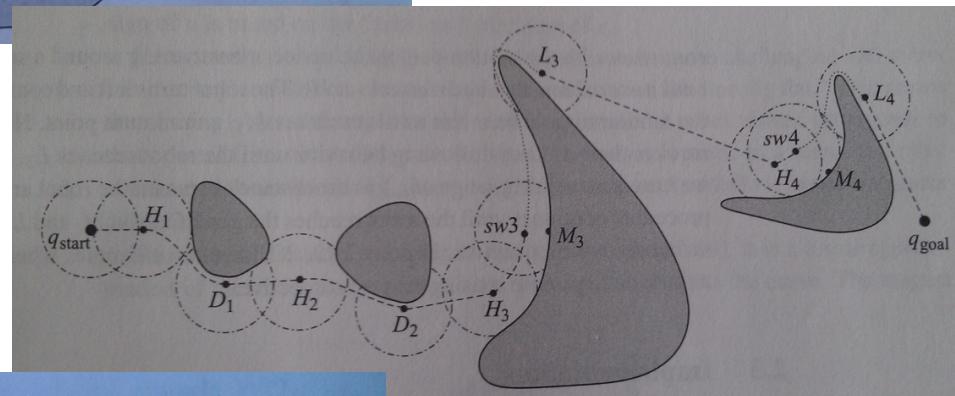
H_i : hit point
 D_i : Depart point
 L_i : Leave point
 M_i : local minima





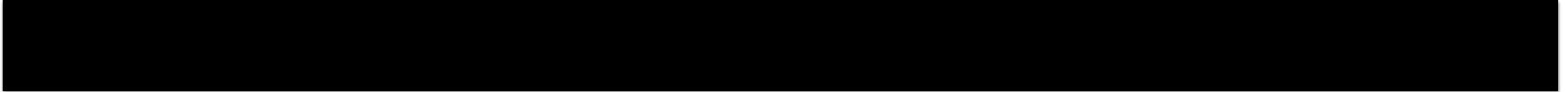
Tangent bug $R=0$

Tangent bug with limited radius



Tangent bug $R=\infty$

What does BugX assume that Random Walk does not?



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Localization: knowing the robot's location, at least wrt. distance to goal

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What do graph search algorithms assume that BugX does not?

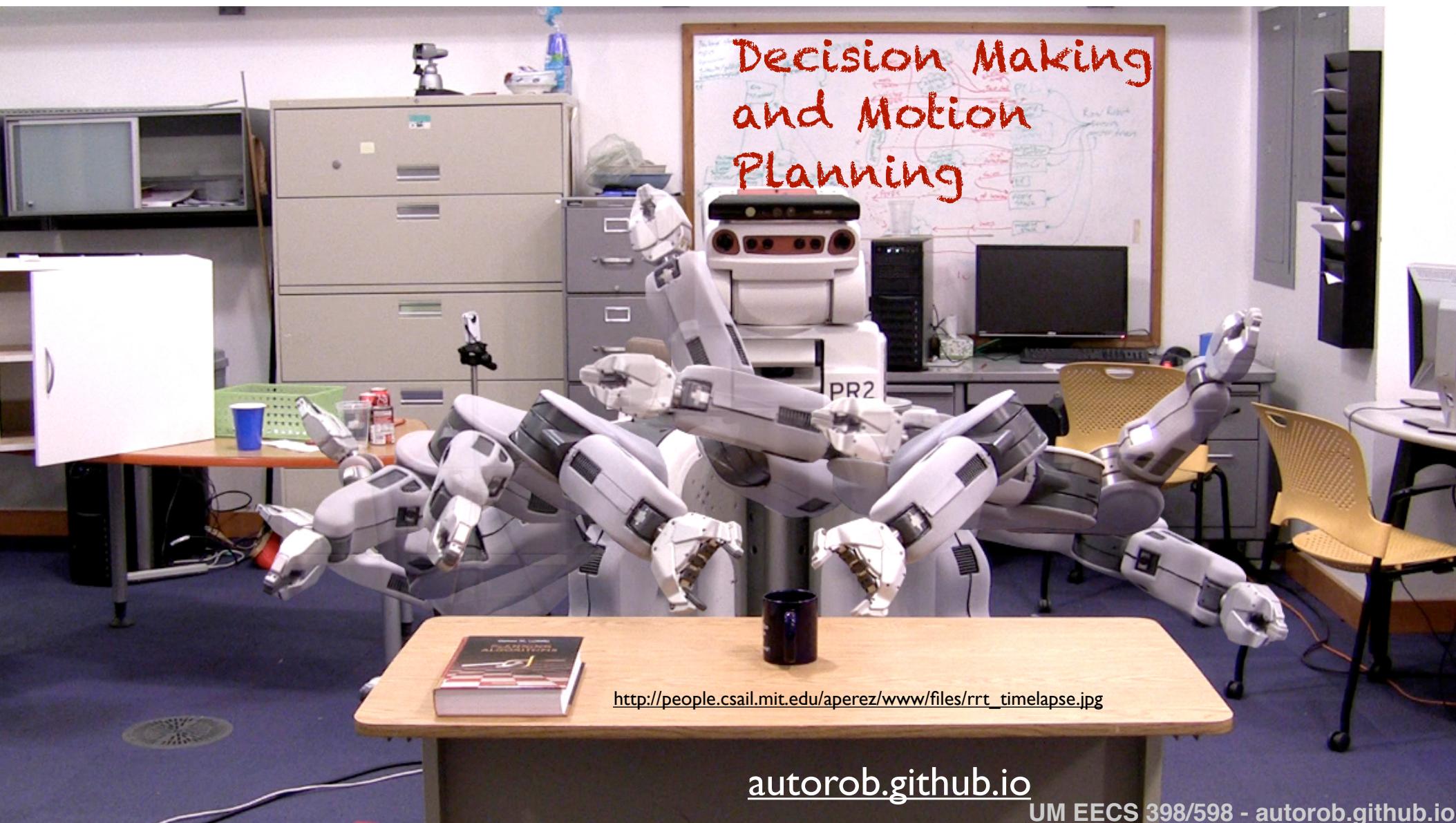
What does BugX assume that Random Walk does not?

Localization: knowing the robot's location, at least wrt. distance to goal

What do graph search algorithms assume that BugX does not?

A graph of valid locations that can be traversed

Suppose we have or can build such a graph...



http://people.csail.mit.edu/aperez/www/files/rrt_timelapse.jpg

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