

Assignment 3 + Compression

(SNLP Tutorial 4)

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Assignment 3

- Exercise 1: Entropy Intuition
- Exercise 2: Uncertainty of events
- Exercise 3: KL Divergence
- Bonus: KL Divergence calculation

Compression

- Prefix Codes: No whole code word is a prefix of any other code word
- Uniquely decodable codes: Each word maps to one and only one code word

Prefix codes are a subset of uniquely decodable codes!

Optimal length of code words

$$l_i = -\log_D p(w_i)$$

Kraft's Inequality

$$\sum_{i=1}^m D^{-l_i} \leq 1$$

What does the sum < 1 imply?

What does the sum $= 1$ imply?

What does the sum > 1 imply?

What does this tell us about uniquely decodable and prefix codes?

Exercise: Test Kraft's Inequality on Morse Code

(Hint: What is the encoding alphabet?)

ASCII/UTF{8,16,32}/Unicode

Encoding from characters to binary alphabet:

ASCII: 7 bits (byte was standardized to 8 bits later!)

- Q: How many values?
- Q: It has to be aligned to 8 bits nowadays (modern CPU requirement).
What do we with the eight bit?

Windows-1252, Windows-1250

- Full 8 bits, map lower 128 to ASCII
- Individual differences, different encoding for í

UTF

- Encoding over Unicode (character alphabet)
- UTF8 - Start with 8 bits, extend to 16 or 32; UTF32 - Always 32 bits
- Compositionality: i with little tail and acute accent U+0301U+0328U+0069
- Valid misuse: snowman U+0301U+0328U+2603

Encoding

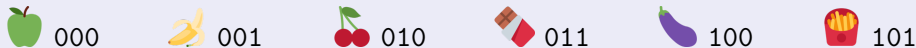
Task

Create encoding (binary) for the following recipe:

apple apple banana cherries apple dark_chocolate eggplant banana cherries banana ...



Fixed-width encoding









Length = $14 \times 3 = 42$

Issues?

- Encoding for  and ?
- What do 110 and 111 mean?

Encoding - Huffman

4×  A 4×  B 2×  C 2×  E 1×  D 1×  F

Huffman Bonus

- When will the Huffman tree be balanced?
- How do we store the tree? Does the efficiency of this matter?
- Are there undefined sequences of bits when using Huffman encoding?
- Does the result of Huffman encoding depend on the text ordering?

E.g. 🍏 🍌 🍌 🍫 vs. 🍌 🍫 🍏 🍌

- Can there be two equally good Huffman encodings?
- Can Huffman result in assigning an element code of length 1?

Long Range Dependencies

- Correlation
- Conditional entropy

Assignment 4

- Exercise 1: Encodings (ASCII, UTF, Huffman)
- Exercise 2: Conditional Entropy on DNA
- Bonus: Huffman Encoding alphabet

Resources

- 1 Twitter emojis
- 2 <https://www.ics.uci.edu/~dan/pubs/DC-Sec1.html>
- 3 https://en.wikipedia.org/wiki/Shannon%27s_source_coding_theorem
- 4 https://en.wikipedia.org/wiki/Huffman_coding
- 5 <http://www.mss.cbi.fau.de/content/uploads/epnat.pdf>
- 6 <https://arxiv.org/pdf/adap-org/9507007.pdf>