Implementation of Network Data Model in ${\tt SECONDODBMS}$

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Last Update: June 23, 2010

Contents

1	Intr	duction	2
2	Imp	emented Data Types	2
	2.1	NetworkAlgebra	2
		2.1.1 <u>network</u>	2
		2.1.2 gpoint	3
		2.1.3 gpoints	3
		2.1.4 gline	3
	2.2	TemporalNetAlgebra	4
		2.2.1 mgpoint	4
		$2.2.2 \overline{\text{ugpoint}}$	5
		2.2.3 igpoint	5
		2.2.4 mgpsecunit	5
3	Imp	emented Operations	5
	3.1	Network Constructor	5
	3.2	Franslation from 2D Space into Network Data Model	6
		3.2.1 point2gpoint	7
		3.2.2 line 2 gline	7
		3.2.3 mpoint2mgpoint	7
	3.3	Translation from Network Data Model into 2D Space	8
		3.3.1 gpoint2point	8
		3.3.2 gline2line	9
		3.3.3 mgpoint2mpoint	9
	3.4	Extract Attributes	10
		3.4.1 trajectory	10
		3.4.2 deftime	11
		3.4.3 units	11
	3.5		11
		· ·	11
			12
	3.6	· · · · · · · · · · · · · · · · · · ·	12
	0.0		 13
			13
			13
		1	13
			14
	3.7	*	14
	0.1		14
			15
	3.8		$15 \\ 15$
	3.9	1 0	15 15
	5.9	. 0	-
			$\frac{15}{16}$
	9.10		16 16
	3.10	8 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	16 16
			16
		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\frac{16}{17}$
		5 10.5 a t	1 /

1 INTRODUCTION 2

Refere	nces	18
3.12	polygpoints	18
	$\operatorname{ugpoint2mgpoint}$	
	3.10.6 mpgsecunits, mgpsecunits2, and mgpsecunits3	17
	3.10.5 simplify	
	3.10.4 intersection	17

1 Introduction

The network data model was first presented in [7]. The network data model is restricted to represent objects which are constrained by a given network, e.g. cars on a street network. For this network constrained objects the network data model delivers a complete system of data types and operations.

In the next sections we describe our implementation of the network data model in the extensible Secondo DBMS [2,5,8]. Parts of this network implementation have been done by one of our students as final thesis [10].

The central idea of the network data model is that movements are restricted to given networks. Cars use street networks and trains railway networks. It is natural for us to speech about the position of a place relative to the street network, instead of giving its absolute position in coordinates. In the network data model all positions are given relatively to the routes of the network. The temporal element is represented by a time sliced representation of the spatio-temporal elements as described in [7,9].

The implementation of the network model in SECONDO is splitted into two algebra modules. One contains the spatial data types and operations (NetworkAlgebra), and the other one contains the spatio-temporal data types and operations (TemporalNetAlgebra).

We describe first the implemented data types of both algebra modules in Section 2 followed by the implemented operations on this data types in Section 3.

2 Implemented Data Types

All data types have a additional Boolean parameter, telling if the object of the data type is well defined or not. We will not mention this flag at every data type description.

2.1 NetworkAlgebra

The four implemented data types of the NetworkAlgebra-Module are: <u>network</u>, gpoint, gpoints, and gline.

2.1.1 network

The data type <u>network</u> is the central data type of the network data model. In the data model it consists of two relations routes and junctions describing the spatial structure of the (street) network.

The implementation of the <u>network</u> consists of three different relations (see tables 1 - 3); one contains the routes data (streets), one contains the junctions data (crossings), and one contains the sections (street parts between two crossings, or a crossing and the end of the street) of the network. Furthermore, the <u>network</u> consists of four B-Trees, indexing the route identifiers of the routes, junctions, and sections relation. A spatial R-Tree, indexing the ROUTE_CURVE attribute of the routes relation. A network identifier (<u>int</u>). And two sets connecting section identifiers of sections which are adjacent ¹.

¹Two sections are adjacent, iff they are connected by a junction, and the lanes of the streets are connected by the junction.

Attribute	Data Type	Explanation
JUNCTION_ROUTE1_ID	\underline{int}	Route identifier of the first ² route of the junction.
JUNCTION_ROUTE1_MEAS	<u>real</u>	Length of the route part between the start of the route and the junction.
JUNCTION_ROUTE2_ID	\underline{int}	Route identifier of the second route of the junction.
JUNCTION_ROUTE2_MEAS	<u>real</u>	Length of the route part between the start of the route and the junction.
JUNCTION_CC	\underline{int}	The connectivity code ³ tells us for which lanes of the streets an transition
		exists on the junction.
JUNCTION_POS	point	Representing the spatial position of the junction in the 2D space.
JUNCTION_ROUTE1_RC	TupleIdenitfier ⁴	Identifies the tuple of the first route of the junction in the routes relation.
JUNCTION_ROUTE2_RC	TupleIdenitfier	Identifies the tuple of the second route of the junction in the routes relation.
JUNCTION_SECTION_AUP_RC	TupleIdentifier	Identifies the tuple of the section upwards of the junction on the first route
		in the sections relation.
JUNCTION_SECTION_ADOWN_RC	TupleIdentifier	Identifies the tuple of the section downwards of the junction on the first
		route in the sections relation.
JUNCTION_SECTION_BUP_RC	TupleIdentifier	Identifies the tuple of the section upwards of the junction on the second
		route in the sections relation.
JUNCTION_SECTION_BDOWN_RC	TupleIdentifier	Identifies the tuple of the section downwards of the junction on the second
		route in the sections relation.

Table 1: The junctions relation of the data type <u>network</u>

Attribute	Data Type	Explanation
ROUTE_ID	\underline{int}	Route Identifier.
ROUTE_LENGTH	<u>real</u>	Length of the route.
ROUTE_CURVE	$\frac{sline}{}^{5}$	Spatial geometry data of the route.
ROUTE_DUAL	<u>bool</u>	TRUE means that the both lanes of the street are separated.
ROUTE_STARTSSMALLER	<u>bool</u>	TRUE means the route curve starts at the lexicographical smaller endpoint

Table 2: The routes relation of the data type <u>network</u>

Attribute	Data Type	Explanation
SECTION_RID	\underline{int}	Route identifier of the route the section belongs to.
SECTION_MEAS1	<u>real</u>	Length of the route part before the section start point from the begin of
		the route.
SECTION_MEAS2	<u>real</u>	Length of the route part before the section end point from the begin of
		the route.
SECTION_DUAL	<u>bool</u>	TRUE means that the both lanes of the section are separated.
SECTION_CURVE	sline	Spatial geometry of the section in the plane.
SECTION_CURVE_STARTS_SMALLER	<u>bool</u>	TRUE means the section curve starts at the lexicographical smaller end-
		point
SECTION_RRC	TupleIdentifier	Identifies the tuple of the route the section belongs to in the routes rela-
		tion.

Table 3: The sections relation of the data type $\underline{network}$

2.1.2 gpoint

A <u>gpoint</u> describes a single position in the network. It consists of the network identifier (\underline{int}) , and the route location. The route location is given by the route identifier (\underline{int}) , the distance (\underline{real}) from the start of the route, and a parameter side (\underline{side}) .

<u>Side</u> has three possible values (Down, Up, None). Up(Down) means a position can only be reached from the up(down) side of a route. None means a position can be reached from both sides of the route. For example motorway service areas on German Highways can always be reached only from one side of the highway.

2.1.3 gpoints

gpoints is a set of gpoint. Implemented by Jianqiu Xu.

2.1.4 gline

A <u>gline</u> describes a part of the network. This part of the network might be a path between two <u>gpoint</u> or a district of a town. The data type <u>gline</u> consists of a network identifier (<u>int</u>), and a set of <u>route intervals</u>, the length of the gline (<u>real</u>), and a Boolean flag telling if the <u>route intervals</u> are stored sorted or not.

²The first route identifier of a junction will always be the lower route identifier of the two routes which cross in the junction.

³See [7] for detailed information about the meaning of the different connectivity code values.

⁴TupleIdentifier is a Secondo data type identifying tuples in other relations.

 $^{5\}overline{\underline{sline}}$ is a set of segments representing the curve of the route in the 2D plane.

Every <u>route interval</u> consists of a route identifier (<u>int</u>), and two position values (<u>real</u>), defining the start and the end position of the <u>route interval</u> on the route. The positions are given by the distance of the position from the start of the route.⁶.

The computation time of many algorithms on <u>gline</u> values can be reduced, if the set of <u>route intervals</u> is sorted. Sorted means that the set of <u>route intervals</u> fullfills the following conditions:

- All route intervals are disjoint.
- The route intervals are sorted by ascending route identifiers.
- If two route intervals have the same route identifier the route interval with the smaller start position is stored first.
- All start positions are less or equal to the end positions.

Unfortunately not all <u>gline</u> values can be stored sorted. If we describe an district or the parts of the network traversed by an <u>mgpoint</u> (See Section 2.2.1) we can store the <u>route intervals</u> sorted, because it is regardless in which sequence we read the <u>route intervals</u> describing the network part. But, if the <u>gline</u> represents a path between two <u>gpoint</u> a and b the <u>route intervals</u> must be stored in the sequence they are used in the path. And this will nearly never be a sorted sequence of <u>route intervals</u> as defined before. We introduced the Boolean flag sorted to solve this problem. Whenever a <u>gline</u> value can be stored sorted we do so and set the sorted flag to TRUE. Algorithms which can take profit from sorted sets of <u>route intervals</u> check the sorted flag and performs a binary scan for sorted and a linear scan for unsorted <u>gline</u> values. If r is the number of <u>route intervals</u> of a gline the computation time is reduced from O(r) for unsorted <u>gline</u> values to $O(\log r)$ for sorted <u>gline</u> values.

We pay for the advantage of reduced computation time for sorted <u>gline</u> values by the higher time complexity of algorithms which produce <u>gline</u> values. Sorting and compressing <u>route interval</u>s needs time. But we think, that this time is well invested, because sorting a <u>gline</u> is done once, whereas the sorted <u>gline</u> value can be used many times by other algorithms.

2.2 TemporalNetAlgebra

In the moment only the temporal version of the <u>gpoint</u> the so called <u>mgpoint</u> (short form from <u>moving(gpoint)</u>) is implemented in the TemporalNetAlgebra. This includes the implementation of the <u>unit(gpoint)</u> (short <u>ugpoint)</u> and the <u>intime(gpoint)</u> (short <u>igpoint)</u>. As explained in the following subsections.

Recently the TemporalNetAlgebra has been extended by a new data type <u>mgpsecunit</u> and operations mgpsecunits to create <u>streams</u> of this data type from <u>mgpoint</u> values. The new data type is expected to be usefull in the context of traffic estimation.

2.2.1 mgpoint

The main parameter of a <u>mgpoint</u> is a set of <u>ugpoints</u> (see Section 2.2.2) with disjoint time intervals. The time intervals of the <u>ugpoints</u> must be disjoint, because nothing can be at two different places at the same time. The <u>ugpoints</u> are stored in the <u>mgpoint</u> sorted by ascending time intervals. This allows us to perform a binary scan on the units of the <u>mgpoint</u> to find a given time instant within the definition time of the <u>mgpoint</u>. An <u>igpoint</u> (see Section 2.2.3), gives the position of the <u>mgpoint</u> at a given time instant.

In our experiments we extended the mgpoint from [7] with some additional parameters:

- length (<u>real</u>): The length parameter stores the distance driven by the mgpoint.
- trajectory (sorted set of <u>route intervals</u>)⁷: Represents all the places ever traversed by the mgpoint.
- trajectory_defined (<u>bool</u>): TRUE, if the trajectory parameter is well defined.
- bbox (<u>rect3</u> three dimensional rectangle): Spatio-temporal bounding box of the mgpoint.

The trajectory parameter reduces the time to decide if a $\underline{mgpoint}$ ever passed a given place (\underline{gpoint} or \underline{gline}) or not. Instead of an linear check of all m units of an $\underline{mgpoint}$ we can perform a binary scan on the much lower number r of route intervals of the trajectory parameter. Such that the time complexity is reduced from O(m) to $O(\log r)$ with $r \ll m$. The trajectory parameter is not maintenanced by every operation. The Boolean flag trajectory_defined tells us, if the trajectory parameter is actually well defined or if it has to be recomputed first.

In the network data model all spatial information is only stored in the central network object. Therefore it is very expensive to get spatial informations especially for mgpoints. Although the mgpoint stays on the

⁶ As you can see different from [7] the <u>side</u> value for <u>route intervals</u> is not implemented yet.

⁷This is a work around, caused by the fact that the SECONDO DBMS does not allow us to use a \underline{gline} value as parameter of an $\underline{mgpoint}$.

same route with the same speed the <u>mgpoint</u> might move in different spatial directions within a single unit. For example a car may drive downhill in serpentines. In this case it is not enough to look at the start and end position of the unit to compute the spatial part of the bounding box. The complete route part passed in this unit must be inherited in the computation of the spatial part of the bounding box. That makes the computation of the bounding box of the <u>mgpoint</u>, which is the union of all the unit bounding boxes very expensive. We introduced the bbox parameter to save our computational work. The bbox value is not maintenanced at every change of the <u>mgpoint</u> and it is only computed on demand using the trajectory of the <u>mgpoint</u> or stored if we could get it for free ⁸.

2.2.2 ugpoint

The <u>uppoint</u> consists of a time interval, an start, and an end <u>point</u>, whereby both <u>point</u> have the same network and <u>route identifiers</u>.

The time interval consists of an starting time instant, an end time instant, and two boolean flags, one for each of the both time instants, indicating if the time instant is part of the interval or not.

With help of this parameters we could compute the exact position of the <u>uppoint</u> at each time instant within the time interval. And, assumed the <u>uppoint</u> reaches the query <u>point</u> within the time interval, we can compute the time instant when a <u>uppoint</u> reaches a given <u>point</u>.

2.2.3 igpoint

The <u>igpoint</u> consists of a time instant and a <u>gpoint</u> representing the position of the <u>mgpoint</u> at the given time instant.

2.2.4 mgpsecunit

The data type <u>mgpsecunit</u> (see Section 2.2.4) was introduced in November 2009 to support better traffic estimation. It reduces the complex informations given in a <u>mgpoint</u> to the values which are useful for traffic estimation. Possibly this reduced information can be used to build a spatio-temporal index over <u>mgpoint</u> values in a later Secondo version.

secId	\underline{int}	Section identifier for a network section
partNo	\underline{int}	Partition number on this section ⁹ .
direct <u>int</u> Moving direction		Moving direction of the mgpoint within this section part. $(0 = Down, 1 =$
		Up)
avgSpeed	<u>real</u>	Average speed of the <u>mgpoint</u> within this section (part)
time	Interval;Instant;	Time interval the <u>mgpoint</u> moved within this section

Table 4: Description of data type mgpsecunit

3 Implemented Operations

In the next subsections we describe the implemented operations of the network data model. For every operator we present its signature, an example call and informations about the used algorithms and if interesting the time complexity of the algorithm.

3.1 Network Constructor

 $\underline{int} \times \underline{relation} \times \underline{relation} \to \underline{network}$ thenetwork(n, routes, junctions)

The operator **thenetwork** constructs the <u>network</u> object with the given identifier n^{10} from the two given relations by Algorithm 1. Therefore the two input relations should contain the following attributes:

 $^{^8}$ If we translate a \underline{mpoint} into an $\underline{mgpoint}$ we can copy the bounding box of the \underline{mpoint} without computational effort.

⁹For traffic estimation it might be useful to divide long sections into smaller parts. The operation **mgpsecunits** (see Section 3.10.6) which constructs the *mgpsecunits* from a set of *mgpoints* has a parameter which gives a maximum section length. Sections which are longer than this value will be divided up into several parts of this length. The partitioning starts at the smaller point of the section and the first part has the number 1. The length of the last part might be shorter than the given length value.

 $^{^{10}}$ If n is already used as network identifier in the database the next free integer value $i \ge n$ is used as network identifier instead of n.

- routes: route identifier (<u>int</u>), length of the route (<u>real</u>), geometry of the route curve (<u>sline</u>), and the two Boolean flags dual and startssmaller
- *junctions*: first route identifier (<u>int</u>), position on first route (<u>real</u>), second route identifier (<u>int</u>), position on the second route (<u>real</u>), and the connectivity code (<u>int</u>)

Algorithm 1 thenetwork (n, route, junctions)

Require: An integer $n \geq 0$, routes and junctions relation as described.

- 1: Create Network empty network object net with id n
- 2: Copy routes to routes relation of net
- 3: Construct B-Tree indexing route identifiers in routes relation
- 4: Construct R-Tree indexing route curves in routes relation
- 5: Copy junction to junctions relation of net and add route tuple identifiers from routes relation
- 6: Construct B-Trees indexing the first / second route identifiers in the junctions relation
- 7: for Each tuple in routes relation do
- 8: **for** Each junction on this route **do**
- 9: Compute the Up and Down sections
- 10: Add the sections to the sections relation
- 11: Add the section identifiers to the junctions relation
- 12: end for
- 13: end for
- 14: Construct B-Tree indexing route identifiers in the sections relation
- 15: for Each junction of the junctions relation do
- 16: Find pairs of adjacent sections and fill adjacency list
- 17: end for

Let r be the number of entries in *routes*, j the number of entries in *junctions*. and j_i the number of junctions on route r_i from the routes relation. The number of entries in the sections relation of net is $\sum_{i=1}^r j_i + 1 = r + \sum_{i=1}^r j_i$, The time complexities of the single steps of Algorithm 1 are:

- 1 O(1)
- 2 O(r)
- $3 + 4 \operatorname{O}(r \log r)$
 - 5 O(j)
 - 6 $O(j \log j)$

7 - 13
$$(r + \sum_{i=1}^{r} j_i)$$

14
$$O((r + \sum_{i=1}^{r} j_i) \log r + \sum_{i=1}^{r} j_i)$$

$$15 - 17 O(j)$$

For all steps together we get a time complexity of

$$O(1 + r + r \log r + j + j \log j + r + \sum_{i=1}^{r} j_i + (r + \sum_{i=1}^{r} j_i) \log(r + \sum_{i=1}^{r} j_i) + j) = O((r + \sum_{i=1}^{r} j_i) \log(r + \sum_{i=1}^{r} j_i))$$

, because $r, j \leq r + \sum_{i=1}^{r} j_i$.

3.2 Translation from 2D Space into Network Data Model

The next operations are used to translate spatial and spatio-temporal data types from the two dimensional plane data model [3,6,9] of the Secondo DBMS into the network data model representation. In [7] this operations are all called **in_network** with different signatures. All translations will only be successful if the values of the two dimensional data types are aligned to the given network otherwise the network representation of the object is not defined.

3.2.1 point2gpoint

The operation **point2gpoint** translates a <u>point</u> value into a <u>gpoint</u> value of the given network if possible. If r_r is the number of routes in the routes relation, and c_r the number of candidate routes the Algorithm 2 has a worst case complexity from $O(\log r_r + c_r)$.

Algorithm 2 point2gpoint(p)

```
Use R-Tree of routes relation to get the candidate routes close to the point found = false

while not found and not isEmpty(candidateRoutes) do

if Distance of point from route = 0 then

found = true

Compute position of point on route

end if
end while
return Gpoint
```

3.2.2 line2gline

The operation <u>line2gline</u> translates an <u>line</u> value into an sorted <u>gline</u> value. The algorithm takes every segment of the <u>line</u> value and tries to find the start and end of the segment on the same route using a variant of **point2gpoint**. The computed route intervals are sorted, merged and compressed with help of an <u>RITree</u>¹¹ before the resulting <u>gline</u> is returned.

If h is the number of segments of the <u>line</u> value, r_r and c_r are defined as in **point2gpoint**, and r is the number of resulting <u>route intervals</u> the time complexity is $O(h(\log r_r + c_r + \log r))$. The summand $h \log r$ is caused by merging and sorting the <u>route intervals</u> with the RITree. As mentioned before (see Section 2.1.4) we think that the many times reduced runtimes are bigger than the additional computation time invested at this point.

3.2.3 mpoint2mgpoint

The operation **mpoint2mgpoint** translates an <u>mpoint</u> value which is constrained by the network into an <u>mgpoint</u> value. The single steps of Algorithm 3

¹¹The RITree is a binary search tree for <u>route intervals</u>. It is implemented in the NetworkAlgebra of SECONDO. It sorts and compress <u>route intervals</u> in $O(r_{in} \log r_{out})$ time, if r_{in} is the number of inserted <u>route intervals</u> and r_{out} is the number of resulting <u>route intervals</u>.

Algorithm 3 mpoint2mgpoint(mpoint,net)

```
1: Initialize bulkload with empty mgpoint
2: upoint = first unit mpoint
3: Initialize uppoint = net values of upoint)
4: for Each upoint in mpoint do
     if Endpoint of upoint is on same route than uppoint then
        if Direction and speed stay the same then
6:
7:
          Extend uppoint
        {f else}
8:
          Add uppoint to mapoint
9:
          Add route interval of uppoint to trajectory
10:
          Ugpoint = net values of upoint
11:
        end if
12:
     else
13:
14:
        Add uppoint to mappoint
        Add route interval of ugpoint to trajectory
15:
        Search upoint on adjacent sections
16:
17:
        Ugpoint = net values of upoint
     end if
18:
19: end for
20: Add uppoint to mapoint
21: Finish bulkload mgpoint
22: Copy bounding box of mpoint to mgpoint
23: return Mgpoint
```

have the following time complexities. The initialization in line 1 and 2 is done in O(1). The computation of the uppoint in line 3 needs a variant of the **point2gpoint**, such that $O(\log r_r + c_r)$ is needed. The for-loop in line 4 is executed m times if m is the number of units of the <u>mpoint</u> value. The for-loop knows three cases with different time complexities:

- 1. extend uppoint is done in O(1).
- 2. write uppoint and initialize new one on the same route is done in O(1) time
- 3. write uppoint and search adjacent route to initialize new one depends on the number of routes x_i connected by the crossing i. In the worst case the time complexity is $O(x_i(\log r_r + c_r))$.

In the worst case we get a total time complexity for the for-loop from $O(m(\log r_r + c_r)\sum_{i=1}^m (x_i))$. The last steps of the algorithm needs only O(1) time again, such that the time complexity of the for-loop dominates the algorithms run time and the worst case time complexity of the algorithm is $O(m(\log r_r + c_r)\sum_{i=1}^m (x_i))$. But this worst case takes only place if the car changes the route in each unit, all other cases need only O(1) time such that we will have a much smaller computation time in the average case.

3.3 Translation from Network Data Model into 2D Space

```
\begin{array}{ll} \underline{gpoint} \to \underline{point} & \mathbf{gpoint2point}(gpoint) \\ \underline{gline} \to \underline{line} & \mathbf{gline2line}(gline) \\ \underline{mgpoint} \to \underline{mpoint} & \mathbf{mgpoint2mpoint}(mgpoint) \end{array}
```

In [7] this operations are called **in_space**. The translation from network constrained data types into data types of the two dimensional plane is always possible.

3.3.1 gpoint2point

The operation <u>gpoint2point</u> translates a <u>gpoint</u> value into a <u>point</u> value. The algorithm uses the B-Tree of the routes relation to get the route curve of the route the <u>gpoint</u> is connected too. This takes $O(\log r_r + c_r)$ time if r_r is the number of routes in the routes relation and c_r the number of candidate routes. The spatial position of the <u>gpoint</u> on this route is computed by searching the O(h) segments of this route curve in O(h) time. Together we get a worst case time complexity of $O(h + \log r_r + c_r)$.

3.3.2 gline2line

The operation **gline2line** translates a <u>gline</u> value into an spatial <u>line</u> value. The algorithm uses the B-Tree index on the routes relation to get the corresponding route curve for every route interval of the r route intervals of the <u>gline</u> value. For each route interval the corresponding h_i segments of the route curve are computed and merged into the resulting <u>line</u> value.

Let r_r the number of routes in the routes relation of the network. For each route interval r_i we need $O(\log r_r)$ time to get the route curve and $O(h_i)$ time to get the segments of the route interval. The time complexity of the complete operation is $O(r \log r_r + \sum_{i=0}^r h_i)$

3.3.3 mgpoint2mpoint

The operation **mgpoint2mpoint** translates a <u>mgpoint</u> value into a corresponding <u>mpoint</u> value. See Algorithm 4 and sub Algorithm 5 for detailed description.

Algorithm 4 mgpoint2mpoint(mgpoint)

```
1: Use B-Tree of routes relation to get route curve for the first ugpoint
 2: Use variant of gpoint2point to compute the start and end point
 3: if start and end are not on the same segment then
      call splitugpoint
 4:
 5: else
      Add upoint to mpoint
 6:
 7: end if
 8: for Each uppoint do
     if Ugpoint stays on the same route then
 9:
        Use variant of gpoint2point to compute the position of the end point
10:
        if start and end are not on the same segment then
11:
          call splitugpoint
12:
13:
        else
          Add upoint to mpoint
14:
        end if
15:
      else
16:
        Use B-Tree Index to get new route curve for the uppoint
17:
        Use variant of gpoint2point to compute the start and end point
18:
        if start and end are not on the same segment then
19:
          call splitugpoint
20:
21:
22:
          Add upoint to mpoint
        end if
23:
      end if
24:
25: end for
26: return mpoint
```

Algorithm 5 splitugpoint (uppoint)

- 1: Depending on moving direction compute the time instant the uppoint reaches the start / end of the segment
- 2: Add upoint to mpoint
- 3: \mathbf{for} Each segment of the route curve passed completely in ugpoint \mathbf{do}
- 4: Compute time instant the uppoint reaches the start and end of the segment
- 5: Add corresponding upoint to mpoint
- 6: end for
- 7: Add last upoint (from section start / end to the end of uppoint to mpoint

The time complexity of the algorithm divideuppoint depends on the number of segments h_i of the route curve passed by the uppoint. It needs $O(h_i)$ time.

If r_r is the number of routes in the routes relation and m is the number of units of the $\underline{mgpoint}$ value. The steps of $\mathbf{mpoint2mgpoint}$ need the following times:

```
1 O(\log r_r)
```

```
2 \text{ O}(h_1)
3+4 \text{ O}(h_i)
3+6 \text{ O}(1)
8-24 \text{ The FOR-Loop is called O}(m) \text{ times}
9 \text{ O}(1)
10 \text{ O}(h_i)
11+12 \text{ O}(h_i)
11+14 \text{ O}(1)
16 \text{ O}(\log r_r)
17 \text{ O}(h_1)
18+19 \text{ O}(h_i)
18+21 \text{ O}(1)
25 \text{ O}(1)
```

For the whole operation we get in an worst case complexity of $O(\log r_r + h_i + m \log r_r + \sum_{i=1}^m h_i)$

3.4 Extract Attributes

The operators of Table 5 return the attributes from the different data types in O(1) time.

Operator	Signature	Explanation
routes	<u>network</u> → routes relation	Returns the routes relation of the <u>network</u> value
junctions	$\underline{network} \rightarrow junctions \ relation$	Returns the junctions relation of the <u>network</u> value
sections	$\underline{network} \rightarrow sections \ relation$	Returns the sections relation of the <u>network</u> value
no_components	$gline \rightarrow \underline{int}$	Returns the number of <u>route intervals</u> respectively units of the first argument.
	$mgpoint \rightarrow \underline{int}$	
isempty	gline → bool	Returns $TRUE$ if the first argument is not defined or no_components = 0.
	$\overline{mgpoint} \rightarrow \underline{bool}$	
length	$gline \rightarrow \underline{real}$	Returns the length of the gline value / driven distance of the mgpoint value
	$\overline{mgpoint} \rightarrow \underline{real}$	
initial	mgpoint→igpoint	Returns the first position and start time of the mgpoint value.
final	mgpoint→igpoint	Returns the last position and end time of the mgpoint value.
unitrid	$ugpoint \rightarrow \underline{real}$	Returns the route identifier of the uppoint value.
unitstartpos	$ugpoint \rightarrow \underline{real}$	Returns the start position of the uppoint value.
unitendpos	$ugpoint \rightarrow \underline{real}$	Returns the end position of the uppoint value.
unitstarttime	$ugpoint \rightarrow \underline{real}$	Returns the start time instant of the uppoint value as <u>real</u> value.
unitendtime	$ugpoint \rightarrow \underline{real}$	Returns the end time instant on the uppoint value as <u>real</u> value.
startunitinst	$ugpoint \rightarrow \underline{instant}$	Returns the start time instant of the uppoint value.
endunitinst	$ugpoint \rightarrow \underline{real}$	Returns the end time instant on the uppoint value.
val	igpoint → gpoint	Returns the gpoint of the igpoint value
inst	igpoint → instant	Returns the time instant of the igpoint value

Table 5: Operators returning simple attributes

The following operators return the more complex attributes of the network data types.

```
\begin{array}{ll} \underline{mgpoint} \rightarrow \underline{gline} & \mathbf{trajectory}(\underline{mgpoint}) \\ \underline{mgpoint} \rightarrow \underline{periods} & \mathbf{deftime}(\underline{mgpoint}) \\ \underline{ugpoint} \rightarrow \underline{periods} & \mathbf{deftime}(\underline{ugpoint}) \\ \underline{mgpoint} \rightarrow \underline{stream}(\underline{ugpoint}) & \mathbf{units}(\underline{mgpoint}) \end{array}
```

3.4.1 trajectory

The operation **trajectory** returns a sorted <u>gline</u> value representing all the places traversed by the <u>mgpoint</u>. If the trajectory parameter is defined the r route intervals are returned as a <u>gline</u> value immediately in O(r) time. Otherwise the trajectory parameter is computed by a linear scan of the <u>m</u> units of the <u>mgpoint</u> value in $O(m \log r_{out} + r_{out})$ time. The last time complexity value could be reduced to O(m) if we store the computed route intervals immediately to the resulting <u>gline</u> value without sorting and compressing. But, as mentioned in Section 2.1.4, we think that the overhead in computation time for sorting and compressing is well invested.

3.4.2 deftime

The operation **deftime** is defined for <u>mgpoint</u> and <u>ugpoint</u>. It returns the <u>periods</u> representing the definition times of the the <u>mgpoint</u> value respectively the <u>ugpoint</u> value.

This takes O(1) time for <u>uppoint</u> values and O(m) time for a <u>mappoint</u> values with m units, because every unit of the <u>mappoint</u> value must be read to merge the definition times.

3.4.3 units

The operation units returns the m units of a mgpoint value as <u>stream</u> of ugpoint in O(m) time.

3.5 Bounding Boxes

We know two different types of bounding boxes in our implementation of the network data model. On the one hand spatio-temporal bounding boxes analogous to the data model of [6]. And on the other hand network bounding boxes in which route identifiers and positions become coordinates, such that R-Trees can be abused to index non spatial network(-temporal) data.

3.5.1 Spatio-Temporal Bounding Boxes

The operations return the spatio-temporal bounding boxes of <u>uppoint</u> values respectively <u>mppoint</u> values as three dimensional rectangles with coordinates x_1, x_2, y_1, y_2, z_1 and z_2 of data type <u>real</u>.

unitboundingbox The spatial part of the unitbounding box, the x-,y-coordinates, are defined as the spatial bounding box of the <u>route interval</u> passed by the <u>uppoint</u> value. And the temporal part (z-coordinates) of the unitbounding box is given by the <u>real</u> values representing the start and the end time instant of the time interval of the <u>uppoint</u> value. More formal:

- $x_1 = \min(x \text{coordinate of the bounding box of the } \underline{route interval})$
- $x_2 = \max(x \text{coordinate of the bounding box of the } \underline{route interval})$
- $y_1 = \min(y \text{coordinate of the bounding box of the } \underline{route interval})$
- $y_2 = \max(y \text{coordinate of the bounding box of the route interval})$
- z_1 =start time instant as <u>real</u>
- $z_2 = \text{end time instant as } \underline{real}$

To compute the spatio temporal bounding box of an uppoint we need access to the h_i segments of the corresponding route curve. We use the B-Tree index of the routes relation to get the route curve in $O(\log r_r)$ time. In total get a worst case time complexity for **unitboundingbox** from $O(h_i + \log r_r)$.

mgpbbox The spatial-temporal bounding box of an <u>mgpoint</u> value is defined to be the union of the bounding boxes of its m units. The simple computation would take $O(m \log r_r + \sum_{i=1}^m h_i)$ time, which is very expensive.

We introduced the parameter bbox to the <u>mgpoint</u> to store the spatio-temporal bounding box of an <u>mgpoint</u> value, if it has been computed once, until the <u>mgpoint</u> value changes. Otherwise we use the trajectory parameter of the <u>mgpoint</u> value to get the same result in less time. The single steps of Algorithm 6 have a time complexity of:

```
1+2 O(1)

4+5 O(m \log r_{out} + r_{out})

6 O(\sum i = 1^{r_{out}} h_{ri})

7+8 O(1)
```

In the worst case we get a time complexity of $O(m \log r_{out} + \sum_i i = 1^{r_{out}} h_{ri})$, which is still better than the primitiv version, because $r_{out} \ll m$ and $r_{out} \ll r_r$.

Algorithm 6 mgpbbox(mgpoint)

```
1: if bbox exists then
```

2: **return** bbox

3: **else**

4: **if** Trajectory is not defined **then**

5: **trajectory**(mpoint)

6: end if

7: Compute union of bounding boxes of trajectories route intervals

8: Extend the resulting trajectory bounding box in the third dimension using real value of start and end time instant of the mappoint

9: **return** bbox

10: **end if**

3.5.2 Network Bounding Boxes

The following operators return network bounding boxes respectively <u>streams</u> of network bounding boxes.

```
\begin{array}{ll} \underline{gpoint} \rightarrow \underline{rect} & \underline{gpoint2rect}(gpoint) \\ \underline{gline} \rightarrow \underline{stream}(\underline{rect}) & \underline{routeintervals}(gline) \\ \underline{ugpoint} \rightarrow \underline{rect3} & \underline{unitbox}(ugpoint) \\ \underline{ugpoint} \rightarrow \underline{rect} & \underline{unitbox2d}(ugpoint) \end{array}
```

All network bounding boxes are two (network) respectively three (network-temporal) dimensional rectangles with coordinates (x_1, x_2, y_1, y_2) respectively $(x_1, x_2, y_1, y_2, z_1, z_2)$. For network bounding boxes the both x-coordinates are always identically and defined by the route identifier of the object. The z-coordinates are defined as <u>real</u> values representing the start (z_1) respectively the end time (z_2) instant of the time interval of the <u>uppoint</u>.

gpoint2rect The operator **gpoint2rect** computes the network box of a <u>gpoint</u> value in O(1) time. The y-coordinates are defined as $y_1 = position - 0.000001$ respectively $y_2 = position + 0.000001$. The small <u>real</u> value is used to avoid problems with the computational inaccuracy of <u>real</u> values.

routeintervals The operation **routeintervals** returns a stream of network boxes, one for each route interval of the <u>gline</u> value. The y-coordinates are defined to be $y_1 = \min(\text{start position}, \text{ end position})$ and $y_2 = \max(\text{start position}, \text{ end position})$.

The operation needs O(r) time if r is the number of route intervals of the gline value.

unitbox2d Returns a two dimensional rectangle for the *ugpoint* in O(1) time. The y-coordinates are given by $y_1 = \min(\text{start position}, \text{ end position})$ and $y_2 = \max(\text{start position}, \text{ end position})$.

unitbox Returns a three dimensional rectangle for the ugpoint in O(1) time. The operation extends the two dimensional rectangle of **unitbox2d** with z-coordinates defined by the \underline{real} values of the start and end time instants of the ugpoint.

3.6 Boolean Operations

Boolean operations check if the arguments hold special characteristics or conditions and return *TRUE* if this is the case, *FALSE* elsewhere. A special case is the operation **inside** for <u>mgpoint</u>, because the argument and therefore the returned value are <u>moving</u> objects.

```
\begin{array}{lll} \underline{gpoint} \times \underline{gpoint} \to \underline{bool} & gpoint1 = gpoint2 \\ \underline{gline} \times \underline{gline} \to \underline{bool} & gline1 = gline2 \\ \underline{gline} \times \underline{gline} \to \underline{bool} & \mathbf{intersects}(gline1, gline2) \\ \underline{mgpoint} \times \underline{gpoint} \to \underline{bool} & mgpoint \ \mathbf{passes} \ gpoint \\ \underline{mgpoint} \times \underline{gline} \to \underline{bool} & mgpoint \ \mathbf{passes} \ gline \\ \underline{gpoint} \times \underline{gline} \to \underline{bool} & gpoint \ \mathbf{inside} \ gline \\ \underline{mgpoint} \times \underline{gline} \to \underline{bool} & mgpoint \ \mathbf{inside} \ gline \\ \underline{mgpoint} \times \underline{gline} \to \underline{mbool} & mgpoint \ \mathbf{inside} \ gline \\ \end{array}
```

```
\frac{\text{mgpoint}}{\text{mgpoint}} \times \frac{\text{instant}}{\text{periods}} \to \frac{\text{bool}}{\text{bool}} \qquad \text{mgpoint present instant}
\frac{\text{mgpoint}}{\text{mgpoint}} \times \frac{\text{periods}}{\text{periods}} \to \frac{\text{bool}}{\text{bool}} \qquad \text{mgpoint present periods}
```

3.6.1 =

The operator = compares the parameters of the arguments and returns TRUE if they are equal, FALSE elsewhere. For two <u>gline</u> values this can be done in O(1) time. For two <u>gline</u> values we have to compare all r <u>route intervals</u> of the both <u>gline</u> values this will take O(r) time if the both <u>gline</u> values are sorted. If the <u>gline</u> one of the values is sorted we need $O(r \log r)$ time. And if both are not sorted we need in the worst case $O(r^2)$ time. In all cases FALSE is returned immediately if a difference between the two gline values is detected.

3.6.2 intersects

The algorithm checks if there is a pair of <u>route interval</u>s (one from <u>gline1</u> and one from <u>gline2</u>) that intersects. Because sorted <u>gline</u> can reduce computation time the algorithm knows three cases:

- 1. If Both gline values are sorted, a parallel scan through the route intervals of both gline values is performed.
- 2. If only one <u>gline</u> value is sorted, a linear scan of the unsorted <u>gline</u> is performed. For each <u>route interval</u> of the unsorted <u>gline</u> a binary search for a overlapping route interval is performed on the sorted <u>gline</u>.
- 3. If both <u>gline</u> values are not sorted, a linear scan of the first <u>gline</u> value is performed. And for each <u>route interval</u> a linear scan for overlapping <u>route interval</u>s on the second gline value is performed.

In all three cases *TRUE* is returned and computation stops immediately if a intersecting pair of <u>route interval</u>s has been found.

If r is the number of <u>route interval</u>s of gline1 and s for gline2. We get the following time complexities for the three cases:

- 1. O(max(r,s))
- 2. $O(r \log s)$ respectively $O(s \log r)$, depending on which of the both gline is sorted.
- 3. O(rs)

3.6.3 passes

The operation **passes** checks if the *mgpoint* ever passes the given *gpoint* respectively *gline*. The algorithm uses the trajectory parameter of the *mgpoint*. If the trajectory is not defined the trajectory is first computed using **trajectory**(*mgpoint*). In this case we must add the time complexity **trajectory** to the time complexity of **passes**. In the following we assume that the trajectory is already defined.

gpoint A binary search of a route interval that contains the *gpoint* is performed on the trajectory parameter. This will take $O(\log r)$ time, if r is the number of route intervals in the trajectory parameter.

gline The algorithm is divided up into two cases:

- 1. If the *gline* is sorted a parallel scan of the route intervals of the *gline* and the route intervals of the trajectory parameter is performed to find a intersecting pair of route intervals.
- 2. If the *gline* is not sorted a linear scan of the route intervals of the *gline* is performed. And for every route interval a binary search of a intersecting route interval is performed on the trajectory parameter.

In both cases TRUE is returned immediately if a intersecting <u>route interval</u> has been found.

If r_m is the number of route intervals of the mgpoint, and r_g the number of route intervals of the gline we get for case 1 a time complexity of O(max(s,r)) and for case 2 a time complexity of $O(r_s \log r_m)$

3.6.4 inside

The operation checks if the gpoint respectively mgpoint is inside the gline.

gpoint In case of the gpoint the algorithm knows two different cases:

- 1. If the gline is sorted a binary search for a route interval containing the gpoint is performed on the r route intervals of the gline.
- 2. If the gline is not sorted a linear scan of the r route intervals of the gline is performed to find a route interval containing the gpoint.

The time complexity is $O(\log r)$ for a sorted gline values and O(r) for a unsorted gline values.

 $\underline{mgpoint}$ For a $\underline{mgpoint}$ a \underline{mbool}^{12} The \underline{mbool} is TRUE every time interval the mgpoint moves inside the gline and FALSE elsewhere. The algorithm checks for every unit m of the mgpoint if there is any intersection with the route intervals r of the gline. Based on this values the resulting mbool is computed. The search for intersecting route intervals is different for sorted and unsorted gline.

- If the gline is sorted a binary search on the route intervals is performed.
- If the gline is not sorted a linear scan on the route intervals is performed.

The operation takes $O(m \log r)$ time for sorted and O(mr) time for not sorted gline values.

3.6.5 present

The operation checks the temporal attribute of the mgpoint.

<u>instant</u> The algorithm performs a binary search on the m units of the mgpoint. It returns TRUE if a corresponding ugpoint is found. This takes $O(\log m)$ time.

<u>periods</u> The algorithm performs a parallel scan through the m units of the m units of

3.7 Merging Data Objects

union merges the two argument objects into one result object of the same data type, if possible.

3.7.1 gline

Algorithm 7 gline1 union gline2

```
if Both gline are sorted then

Perform parallel scan of both gline route intervals

if Current route intervals intersect then

Merge route Intervals

if Following route intervals intersect the resulting route interval then

extend merged route interval

end if

Add merged route interval to result and continue scan

else

Add smaller route interval to result and continue scan

end if

else

Fill route intervals of both gline in a common RITree

end if

return Resulting sorted and compressed gline
```

The operation returns a sorted gline which contains the union of the $\underline{route\ interval}$ s of the both gline. The steps of the Algorithm 7 have the following time complexities:

 $^{^{12}}$ Short form of $moving(\underline{bool})$ is returned. A \underline{mbool} changes its \underline{bool} value within time. See [6] for more details.

Let r_1 respectively r_2 be the number of <u>route intervals</u> of the both gline and r_{out} the number of route intervals in the resulting <u>gline</u>. If both gline are sorted the time complexity is O(r+s) in all other cases we get a time complexity of $O((r+s)\log k)$.

If we don't want to store the resulting <u>gline</u> sorted we could simply add every route interval of the both <u>gline</u> into the new <u>gline</u> in O(r + s) time. But, as mentioned before in Section 2.1.4, many algorithms take profit from sorted <u>gline</u> values. We think that the additional time is well invested at this place.

3.7.2 mgpoint

The operation merges two *mgpoint* if the time intervals of all units of the both *mgpoint* are disjoint or the units with the same time intervals have identical values.

The algorithm performs a parallel scan through the units of the both mgpoint and writes the units of the mgpoints in ascending order of their time intervals to the resulting mgpoint. If there are overlapping time intervals the algorithm checks if the both ugpoints are identically. If the ugpoints are identically one of them is written to the result and the other one ignored. If the ugpoints are not identically the computation is stopped and the result is undefined. This takes O(m+n) if m respectively n is the number of units of the first respectively second mgpoint.

3.8 Path Computing

```
gpoint \times gpoint \rightarrow gline shortest\_path(gpoint1, gpoint2)
```

The operation computes the shortest path in the network between gpoint1 and gpoint2 using Dijkstras Algorithm of shortest paths [4]. In the worst case this takes $O(s + j \log j)$ time if j is the number of junctions and s the number of sections in the network.

3.9 Distance Computing

There is a big difference between the Euclidean Distance and the Network Distance between two places a and b. The Euclidean Distance is given by the length of the beeline between the two places regardless from existing paths in the network between the two locations. Contrary to this the Network Distance is given by the length of the shortest path between a and b in the network. According to this, and contrary to the Euclidean Distance, the Network Distance from a to b might be another than the Network Distance from b to a. Because there might be one way routes in the shortest path from a to b, which cannot be used in the shortest path from b to a.

3.9.1 Euclidean Distances

```
\begin{array}{ll} \underline{gpoint} \times \underline{gpoint} \to \underline{real} & \mathbf{distance}(gpoint1, \, gpoint2) \\ \underline{gline} \times \underline{gline} \to \underline{real} & \mathbf{distance}(gline1, \, gline2) \\ \underline{mgpoint} \times \underline{mgpoint} \to \underline{mreal}^{13} & \mathbf{distance}(mgpoint1, \, mgpoint2) \end{array}
```

Although Euclidean Distances don't make much sense in a network environment we implemented the **distance** operation which computes the Euclidean Distance of two <u>gpoint</u>, <u>gline</u>, or <u>mgpoint</u> for network objects for convenience. All following algorithms for Euclidean Distance computing do first a translation of the network data types into equivalent two dimensional data types using the operators of Section 3.3 before they use the existing distance operation of this equivalent two dimensional data types to compute the Euclidean Distance between the network data types. The time complexity is therefore always given by the sum of the translation time and the time for the distance computation. We get the following time complexities:

- <u>gpoint</u>: **distance** (**gpoint2point**(gpoint1), **gpoint2point**(gpoint2) The time complexity is dominated by **gpoint2point**, therefore the time complexity is $O(h + \log r_r + c_r)$.
- <u>gline</u>: **distance**(**gline2line**(gline1), **gline2line**(gline2)) Again the **gline2line** dominates the algorithm and the time complexity is $O(r \log r_r + \sum_{i=0}^r h_i)$
- <u>mgpoint</u>: **distance** (mgpoint2mpoint(mpoint1),(mpoint2)) Once more the computation time is dominated by the translation time. We get a time complexity of $O(\log r_r + h_i + m \log r_r + \sum_{i=1}^m h_i)$

 $^{^{13}}$ We have moving data types so the result is also a moving data type. See [6] for detailed explanation of <u>mreal</u>.

3.9.2 Network Distances

As mentioned before the Network Distance is given by the length of the shortest path between the arguments. In the simple case of two gpoint we use **length** (shortest_path (gpoint1, gpoint2)) and get a time complexity of $O(s + j \log j)^{14}$.

For two <u>gline</u> values we use Algorithm 8 to compute the minimum Network distance between a gpoint from <u>gline</u>1 and a gpoint from <u>gline</u>2.

Algorithm 8 netdistance(gline1,gline2)

```
BGP1 = Bounding GPoints<sup>15</sup> of gline1
BGP2 = Bounding GPoints of gline2
minDist = ∞
for Each pair of Elements from BGP1 and BGP2 do
  if gp1 is inside gline2 or gp2 is inside gl1 then
    return 0.0
else
    actDist = length(shortestpath(gp1,gp2))
    if actDist ; minDist then
        minDist = actDist
    end if
end if
end for
return minDist
```

Let o be the number of sections covered by the route intervals of gline1 and p the number of sections covered by route intervals of gline2. The computation of the bounding gpoints of both glines will take O(o+p) time. Let u respectively v be the number of bounding gpoints of the both gline. The Network distance computation between this points will take $O(uv(s+j\log j))$ time. We get a total worst case time complexity of $O(o+p+uv(s+j\log j))$ for the **netdistance** operation between two gline values.

3.10 Restricting and Reducing

The following operations restrict a $\underline{mgpoint}$ to given times or places or reduce the number of units of the mgpoint.

```
\begin{array}{ll} \underline{mgpoint} \times \underline{instant} \to \underline{igpoint} & mgpoint \ atinstant \ periods \\ \underline{mgpoint} \times \underline{periods} \to \underline{mgpoint} & mgpoint \ atperiods \ periods \\ \underline{mgpoint} \times \underline{gpoint} \to \underline{mgpoint} & mgpoint \ at(gpoint) \\ \underline{mgpoint} \times \underline{gline} \to \underline{mgpoint} & mgpoint \ at(gline) \\ \underline{mgpoint} \times \underline{mgpoint} \to \underline{mgpoint} & \underline{mtersection}(mgpoint1, mgpoint2) \\ \underline{mgpoint} \times \underline{real} \to mgpoint & \underline{simplify}(mgpoint,real) \\ \end{array}
```

3.10.1 atinstant

Restricts the mgpoint to the given time instant. Therefore a binary scan of the units of the mgpoint is performed to find the unit containing the given time instant. If a corresponding unit is found the resulting $\underline{igpoint}$ is returned. The time complexity depends on the number m of units of the mgpoint and is $O(\log m)$.

3.10.2 atperiods

Restricts the *mgpoint* to the given *periods*. Therefore a parallel scan of *periods* and the units of the *mgpoint* is performed. And the (parts) of units which are inside the *periods* value are written to the resulting *mgpoint*.

¹⁴See Section 3.8 for information about **shortest_path** respectively Section 3.4 for information about **length**(gline)

¹⁵Bounding GPoints means at least a set of <u>gpoints</u>. Where each <u>gpoint</u> of the set must be passed by everyone who wants to reach the inside of the <u>gline</u> from the outside of the <u>gline</u> and vice versa. This bounding gpoints are the interesting <u>gpoints</u> for Network Distance computing between two <u>gline</u>, because every other place inside a <u>gline</u> can only be reached by passing one of these bounding gpoints.

The time complexity is O(m+p) if m is the number of units of the mgpoint and p is the number of time intervals of the periods.

3.10.3 at

Restricts the mgpoint to the times and places it passes a given gpoint respectively gline.

gpoint The algorithm performs a linear scan on the m units of the mgpoint and checks for every unit if the mgpoint passes the gpoint. If this is the case a gpoint for the time the gpoint was at the gpoint is computed and added to the resulting gpoint. The computation takes O(m) time.

<u>gline</u> The algorithm performs a linear scan on the m units of the mgpoint. If the gline is sorted a binary search on the r route intervals of the gline is performed for each unit of the mgpoint. If the gline is not sorted a linear scan of the route intervals is performed for each unit of the mgpoint. In both cases it is checked if the actual $\underline{ugpoint}$ passes any route interval of the gline. If this is the case the times and places of passing are computed as $\underline{ugpoint}$ and added to the resulting $\underline{mgpoint}$.

The time complexity for the operation is $O(m \log r)$ for sorted and O(mr) for unsorted gline.

3.10.4 intersection

Returns a $\underline{mgpoint}$ value representing the times and places where both mgpoints have been at the same time. The algorithm first computes the refinement partitions of the both mgpoint. Then it performs a parallel scan through the refinement partitions of the both mgpoint and checks for every pair of units if the positions intersect. If this is the case a $\underline{ugpoint}$ with the intersection value is computed and written to the resulting mgpoint.

Let \overline{m} respectively n is the number of units of the both mgpoint and r the number of units of the refinement partitions. The time complexity of the algorithm is O(m+n+r).

3.10.5 simplify

The operation reduces the number of units of the mgpoint, by merging the units, where the mgpoint moves on the same route, in the same direction, and the speed difference is smaller as the given real. To do this a linear scan on the m units of the mgpoint is performed and the condition is checked for every unit. This will take O(m) time. Detailed information about the simplification can be found in [10].

3.10.6 mpgsecunits, mgpsecunits2, and mgpsecunits3

mgpsecunits: $\underline{rel}(tuple((a_1 \ x_1)(a_2 \ x_2)...(a_2 \ x_2))) \times a_i \times \underline{network} \times \underline{real} \rightarrow \underline{stream}(mgpsecunit)$

mgpsecunits2: $mgpoint \times \underline{real} \rightarrow \underline{stream}(mgpsecunit)$

 $\underline{mgpsecunits3}: \underline{\underline{stream}(\underline{mgpoint}) \times \underline{real} \rightarrow \underline{stream}(\underline{mgpsecunit})}$

We implemented three different versions of the **mgpsecunits**. They all get different input values. Whereas the second operation **mgpsecunits2** is provided to support later on a new spatio-temporal network index for <u>mgpoint</u> values. The first (**mgpsecunits**) and the last (**mgpsecunits3**) should support traffic estimation operations. This traffic estimation operations will be part of another new Secondo algebra module called TrafficAlgebra.

The algorithm is for all three versions of the **mgpsecunits** operation almost the same. The input is a set of <u>mgpoint</u> or in case of **mgpsecunits2** a single <u>mgpoint</u> and the output a stream of <u>mgpsecunits</u> containing all the information's given by the input <u>mgpoints</u>. The algorithm computes for all units of every <u>mgpoint</u> a corresponding set of <u>mgpsecunits</u>. The resulting <u>mgpsecunits</u> for a single <u>mgpoint</u> are merged as far as possible. Merging means here that as long as the <u>mgpoint</u> moves in the same section part in the same direction the different <u>mgpsecunits</u> are merged into one <u>mgpsecunits</u>. At last the result is returned as <u>stream</u> of <u>mgpsecunits</u>.

3.11 ugpoint2mgpoint

 $\underline{ugpoint} \rightarrow \underline{mgpoint} \qquad \qquad \underline{ugpoint2mgpoint(\underline{ugpoint})}$

The operation constructs a mgpoint from a single uppoint in O(1) time.

¹⁶Refinement partition means that the units of both *mgpoint* are parted, so that in the end the units of both *mgpoint* have the same time intervals for the times they both exist.

REFERENCES 18

3.12 polygpoints

 $gpoint \rightarrow \underline{stream}(gpoint)$ **polygpoints**(gpoint)

A problem of the network data model is that junctions belong to more than one route. Therefore they are represented by more than one <u>gpoint</u>. Operators like **passes** or **inside** do not check if the query <u>gpoint</u> is a junction and probably has more than one representation, because the interpretation of passing a network junction in [7] is slightly different from passing a <u>point</u> in the two dimensional space. So if, for example, a <u>mgpoint</u> passes a junction on the one route and the <u>gpoint</u> representing the junction is given related to another route we get <u>FALSE</u> as result. This is correct in the network data model but doesn't correspond to the **passes** interpretation of the data model of free movement in two dimensional space.

We introduced the operation **polygpoints** to bypass this problem in the BerlinMOD Benchmark [1]. This operation returns for every given *gpoint* a <u>stream</u> of <u>gpoint</u>. This stream contains only the *gpoint* itself if the *gpoint* is not a junction, and the *gpoint* itself and all the alias <u>gpoints</u> representing the same place if the *gpoint* is a junction.

The algorithm **polygpoints** first copies the argument gpoint to the output stream in O(1) time. Then it checks if the gpoint represents a junction by selecting all junctions from the junctions relation which are on the route with the route identifier of the gpoint with help of the junctions relation B-Tree in $O(c + \log j)$ time. This c junctions are checked if they are identified by the gpoint. In the worst case this takes O(c). If this is the case all other gpoint values identifying the same junction on other routes are returned in the output stream. The complete algorithm has a worst case complexity of $O(c + \log j)$.

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