

## Summary of emulation comparisons (variance = $v_k$ )

- » Functions: borehole, OTL circuit, Wing weight, and piston
- » Number of locations: 25
- » Number of training parameters: 100
- »  $x$  are sampled uniformly in  $[0, 1]^{d_x}$
- »  $\theta$  are sampled from latin hypercube sampling in  $[0, 1]^{d_\theta}$
- » Test parameters are sampled uniformly in  $[0, 1]^{d_\theta}$

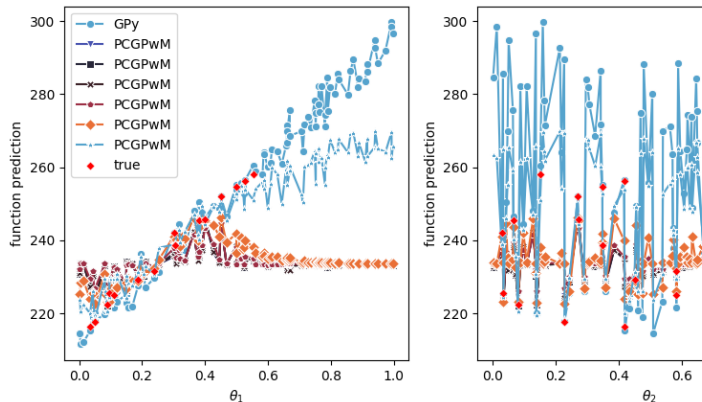
### Comparing between choices of variance constants $\beta_k$ 's

Main observation:

- » If a linear trend is present in one of the parameters, emulator prediction is better with very large  $\beta_k$ 's.
- » Often MLE does not work in such cases.

## Example: Wing weight function

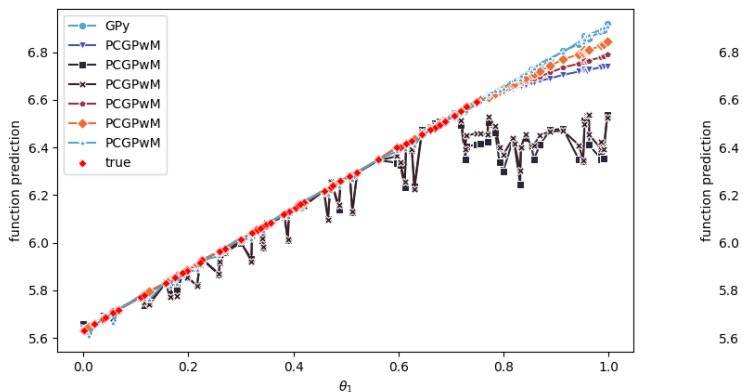
Failure mechanism: if  $\min(x) < 0.05$  and  $\max(\theta) > 0.8$



\*legend (top to bottom):  
GPy, PCGPwM (optimized,  $\log(\beta_k) = -6, -4, 0, 4, 20$ )

## Example: OTL circuit function

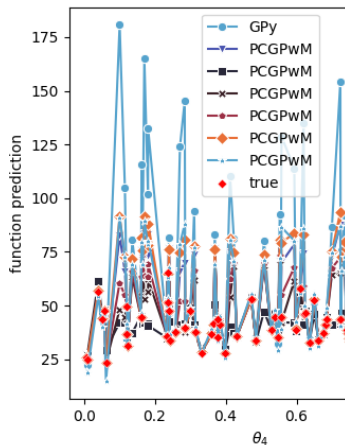
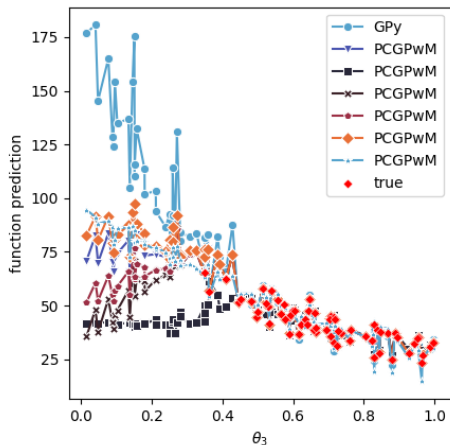
Failure mechanism: if  $\max(x) > 0.75$  and  $\max(\theta) > 0.6$



\*legend (top to bottom):  
GPy, PCGPwM (optimized,  $\log(\beta_k) = -6, -4, 0, 4, 20$ )

## Example: borehole function

Failure mechanism: if  $f(x, \theta) > f(x, [0.5]^{d_\theta})$



\*legend (top to bottom):

GPy, PCGPwM (optimized,  $\log(\beta_k) = -6, -4, 0, 4, 20$ )

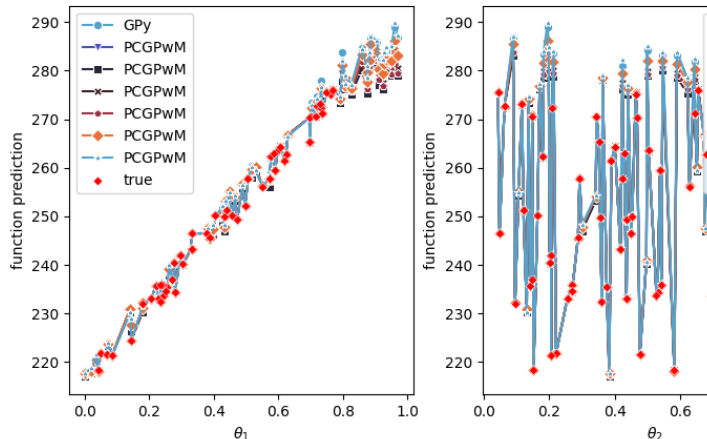
## Summary of emulation comparisons (variance = $v_k/(1 - v_k)$ )

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**Comparing between choices of variance constants  $\beta_k$ 's**

## Example: Wing weight function

Failure mechanism: if  $\min(x) < 0.05$  and  $\max(\theta) > 0.8$

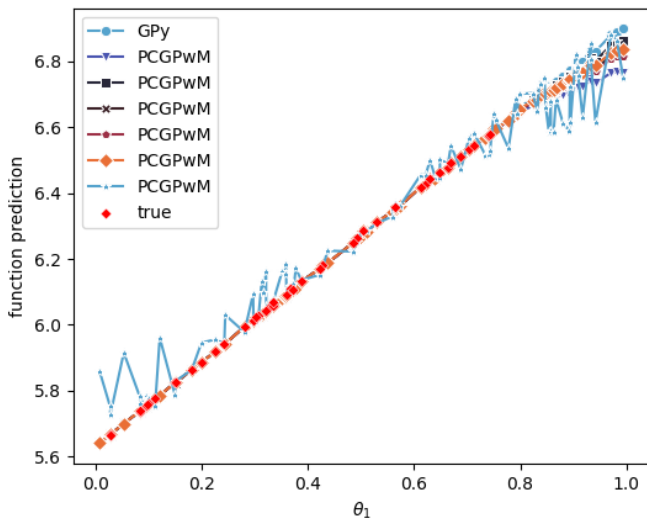


\*legend (top to bottom):

GPy, PCGPwM (optimized,  $\log(\beta_k) = -6, -4, 0, 4, 20$ )

## Example: OTL circuit function

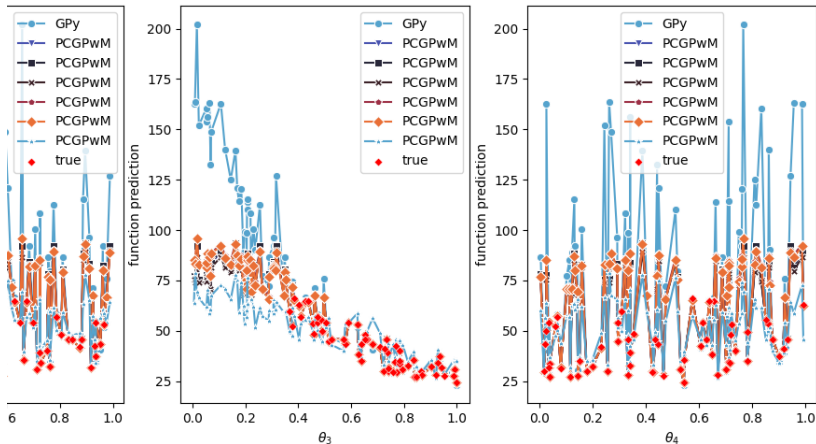
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\*legend (top to bottom):

## Example: borehole function

Failure mechanism: if  $f(x, \theta) > f(x, [0.5]^{d_\theta})$



\*legend (top to bottom):

GPy, PCGPwM (optimized,  $\log(\beta_k) = -6, -4, 0, 4, 20$ )