

IF5181 Pengenalan Pola

# Klasifikasi

Masayu Leylia Khodra

Referensi: Bab 8 dari Han, J., Pei, J., & Kamber, M. (2011). Data mining: concepts and techniques. Elsevier.

# Outline

- Klasifikasi: what, how
- Klasifikasi berbasis pengetahuan
- Klasifikasi berbasis pembelajaran mesin
  - Decision tree learning
  - Naive Bayes
  - IF-THEN rules
    - Ekstraksi dari Decision Tree
    - Rule Induction: Sequential Covering Method
  - Neural Network

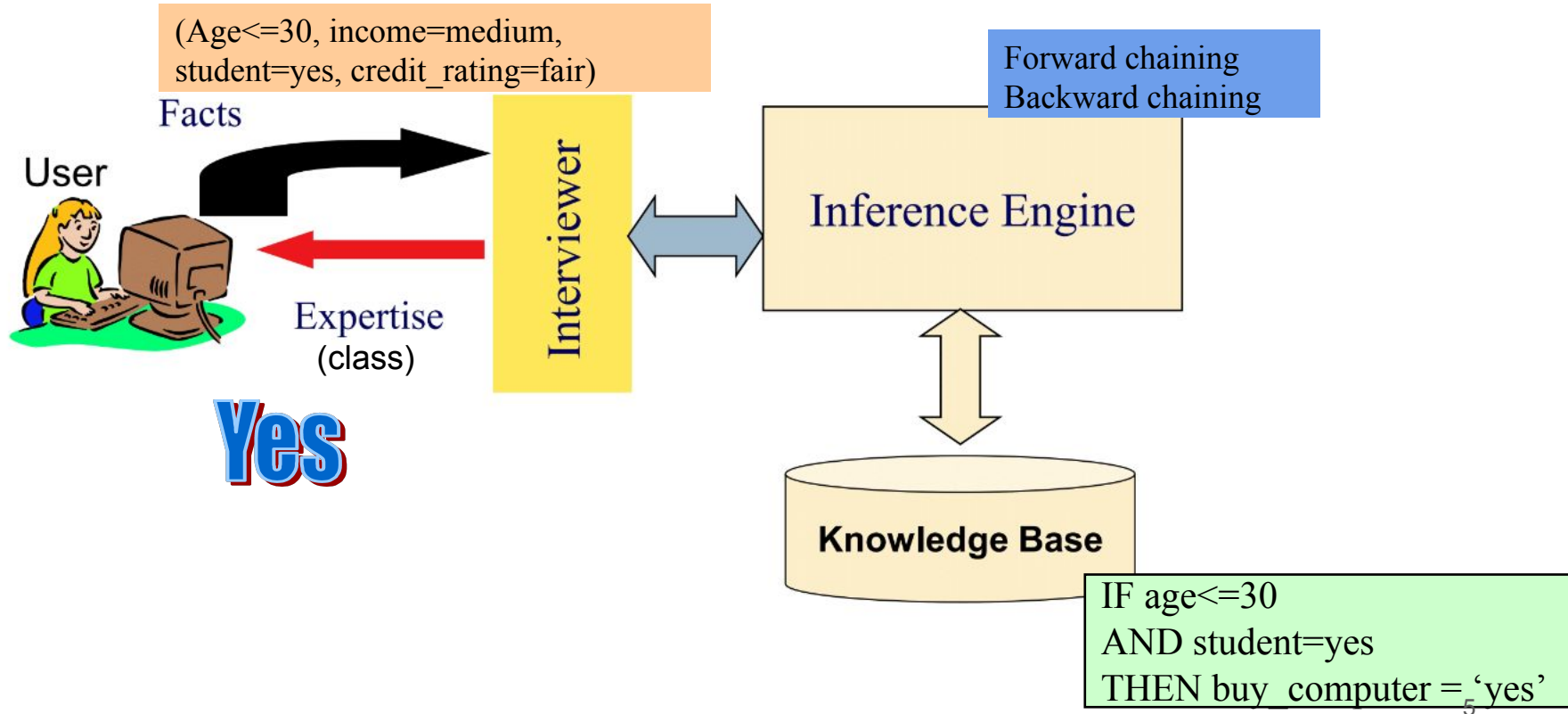
# Klasifikasi: Aplikasi

- Traffic sign recognition
- Kategorisasi aspek
- Klasifikasi sentimen
- Identifikasi kalimat majemuk
- Klasifikasi intent dari kalimat
- Spam filtering
- Klasifikasi citra hiu atau bukan
- POS Tagging
- Named-entity recognition
- Diagnosis penyakit
- Identifikasi pesawat tempur

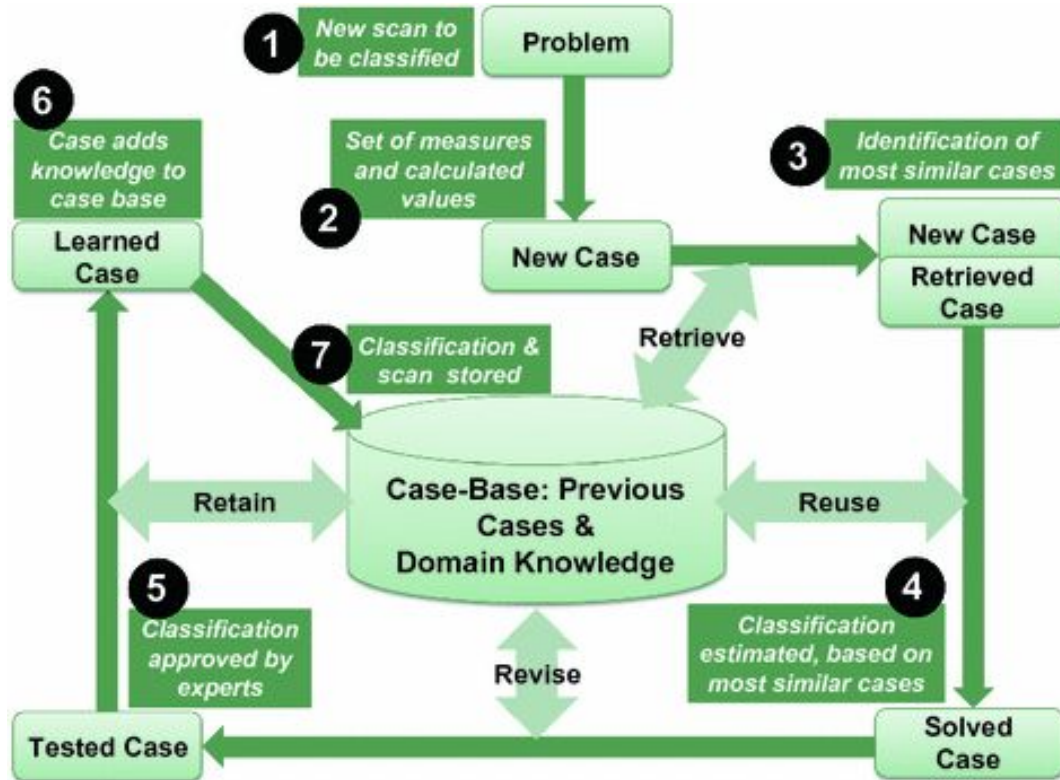
# Klasifikasi

- Klasifikasi: proses menentukan kategori yang diambil dari predefined-category set.
- Fungsi Klasifikasi:  $\text{data} \rightarrow \text{class} \in C$
- Pendekatan (Sebastiani, 2005; Aly, 2005):
  - Berbasis pengetahuan
  - Berbasis pembelajaran mesin: producing a learning model from a labeled training set

# Klasifikasi berbasis Pengetahuan



# Cased-based Classification

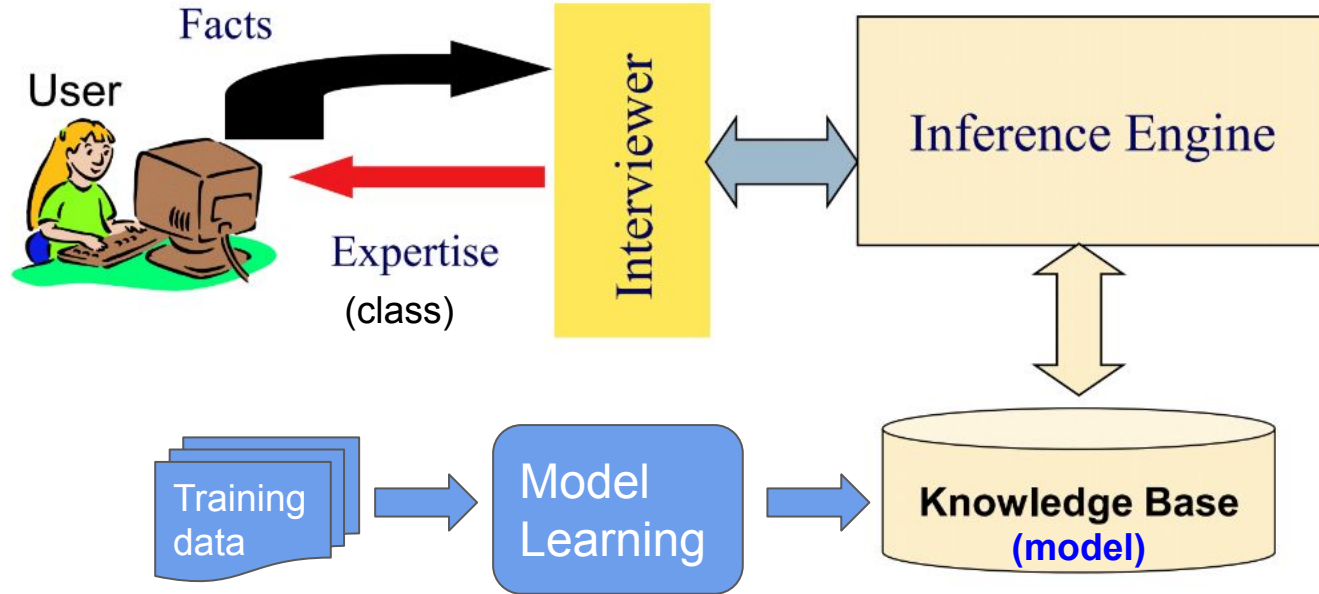


- Case-based reasoning:
  - Retrieve
  - Reuse
  - Revise
  - Retain

# Klasifikasi berbasis Pembelajaran Mesin

- **Konstruksi model:**
  - Training data: kumpulan data **berlabel** untuk konstruksi model.
  - Model direpresentasikan sebagai aturan klasifikasi, pohon keputusan, atau representasi pengetahuan lainnya.
- **Validasi dan Tes model:** estimasi kinerja model terhadap test data.
  - Test data harus independent dari training data.
  - Test data untuk memilih model disebut validation data.
- **Model deployment:** klasifikasi data baru

# Konstruksi Model





# Konstruksi Model: Contoh

Training data



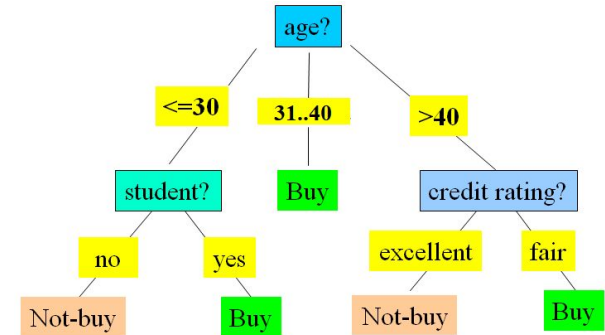
Model Learning



age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

Decision tree learning

Naive Bayes learning



$$P(\text{buys\_computer} = \text{"yes"}) = 9/14 = 0.643$$

$$P(\text{buys\_computer} = \text{"no"}) = 5/14 = 0.357$$

$$P(\text{age} = \text{"<=30"} | \text{buys\_computer} = \text{"yes"}) = 2/9 = 0.222$$

$$P(\text{age} = \text{"<= 30"} | \text{buys\_computer} = \text{"no"}) = 3/5 = 0.6$$

$$P(\text{income} = \text{"medium"} | \text{buys\_computer} = \text{"yes"}) = 4/9 = 0.444$$

$$P(\text{income} = \text{"medium"} | \text{buys\_computer} = \text{"no"}) = 2/5 = 0.4$$

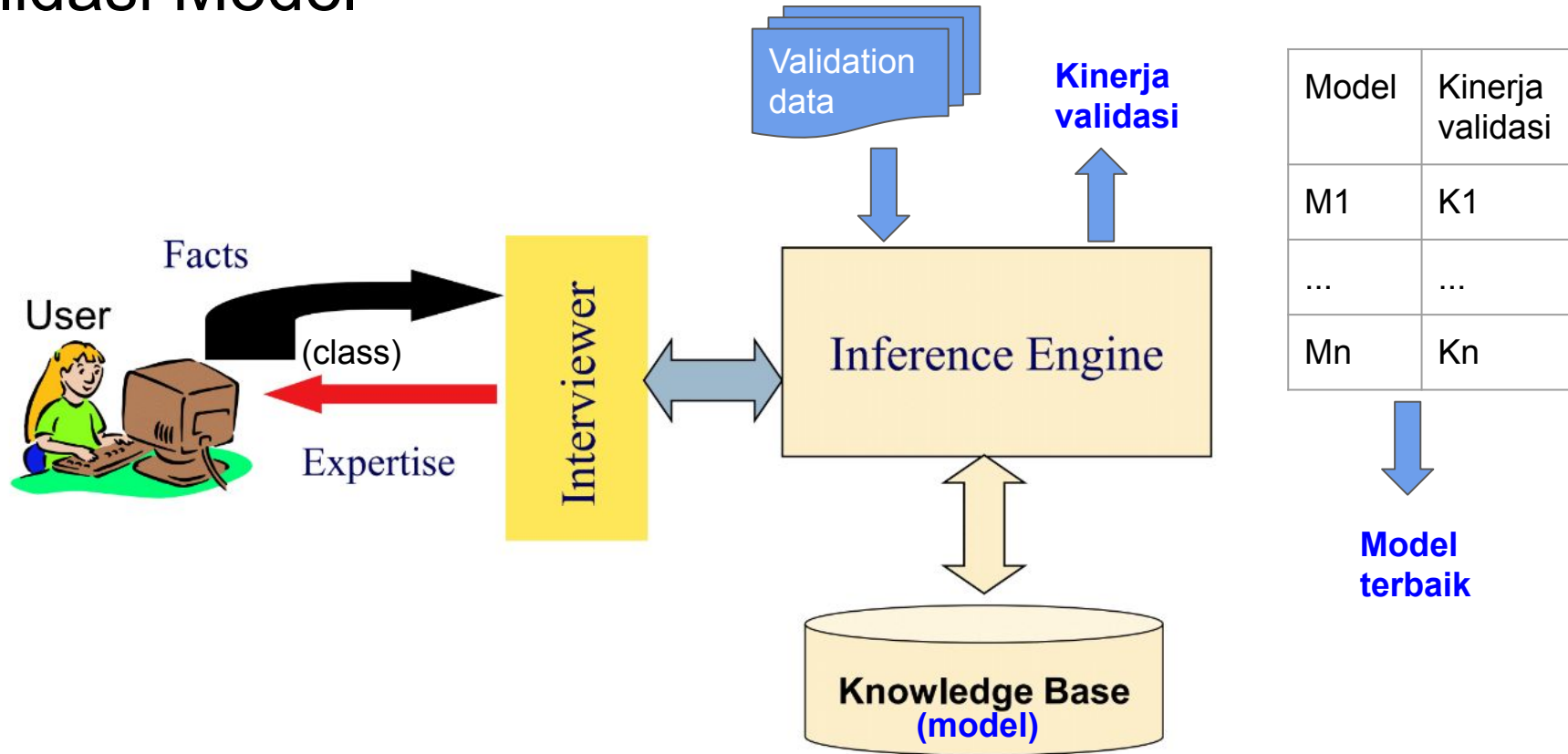
$$P(\text{student} = \text{"yes"} | \text{buys\_computer} = \text{"yes"}) = 6/9 = 0.667$$

$$P(\text{student} = \text{"yes"} | \text{buys\_computer} = \text{"no"}) = 1/5 = 0.2$$

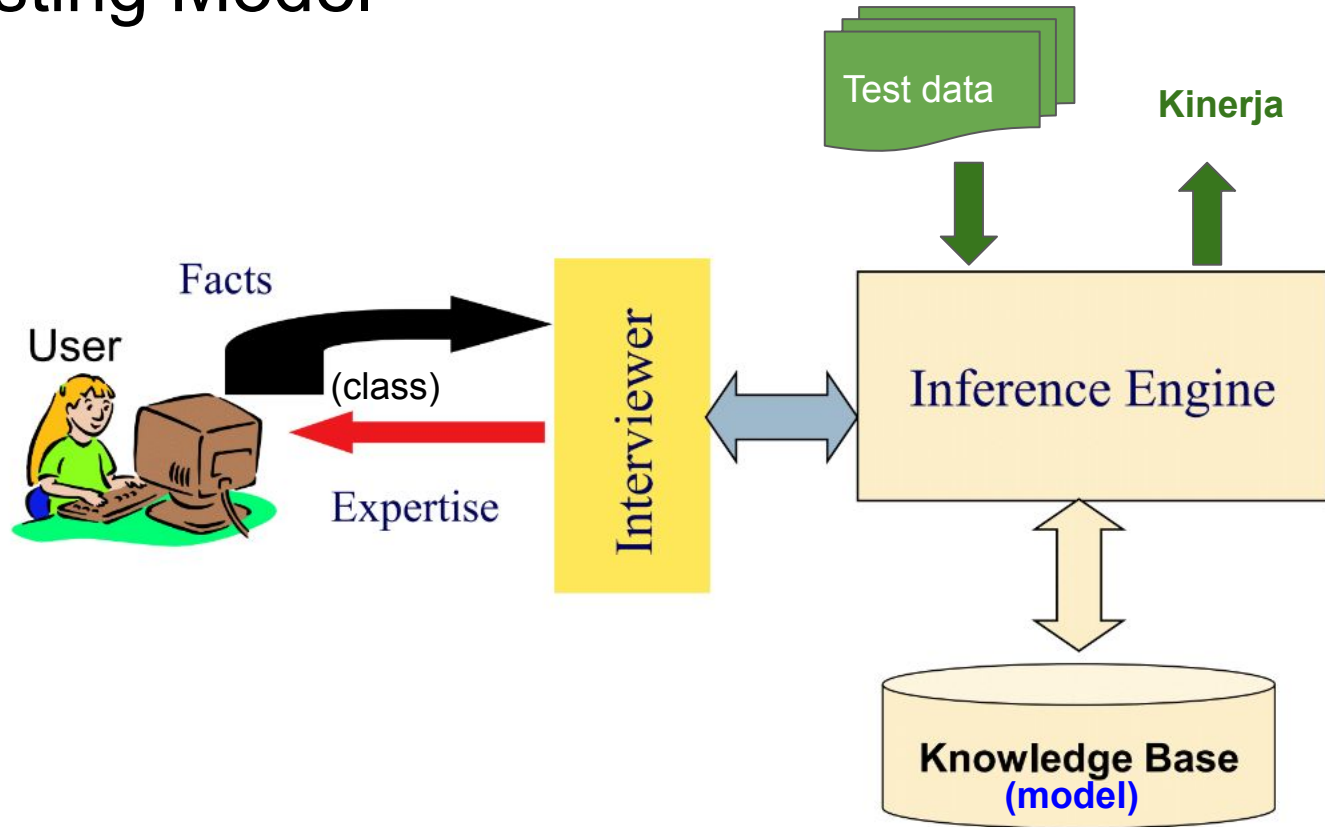
$$P(\text{credit\_rating} = \text{"fair"} | \text{buys\_computer} = \text{"yes"}) = 6/9 = 0.667$$

$$P(\text{credit\_rating} = \text{"fair"} | \text{buys\_computer} = \text{"no"}) = 2/5 = 0.4$$

# Validasi Model

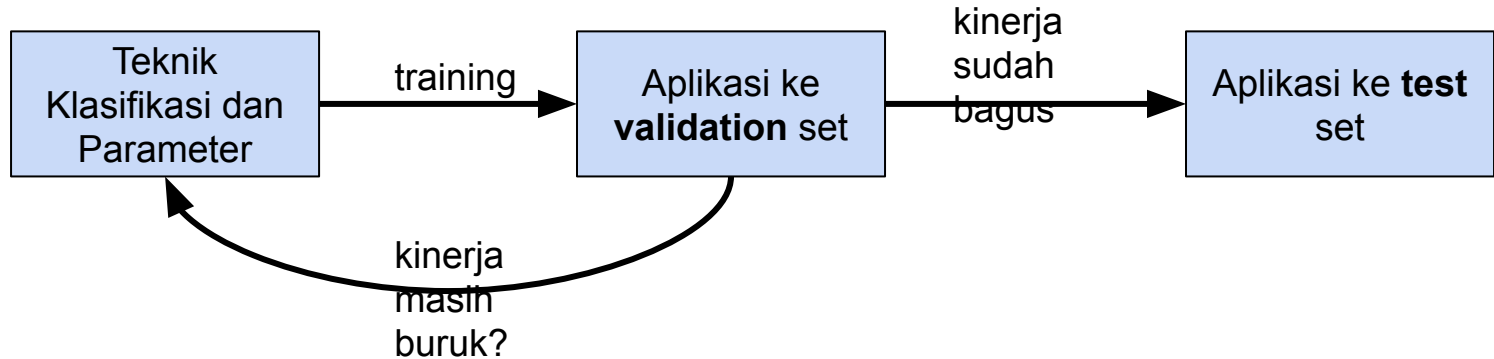


# Testing Model



# Validasi & Tes Model

- Idealnya ada tiga jenis dataset: training set, validation set, test set.
- Kinerja model = kinerja pada test-set.
- Test-set hanya digunakan satu kali.

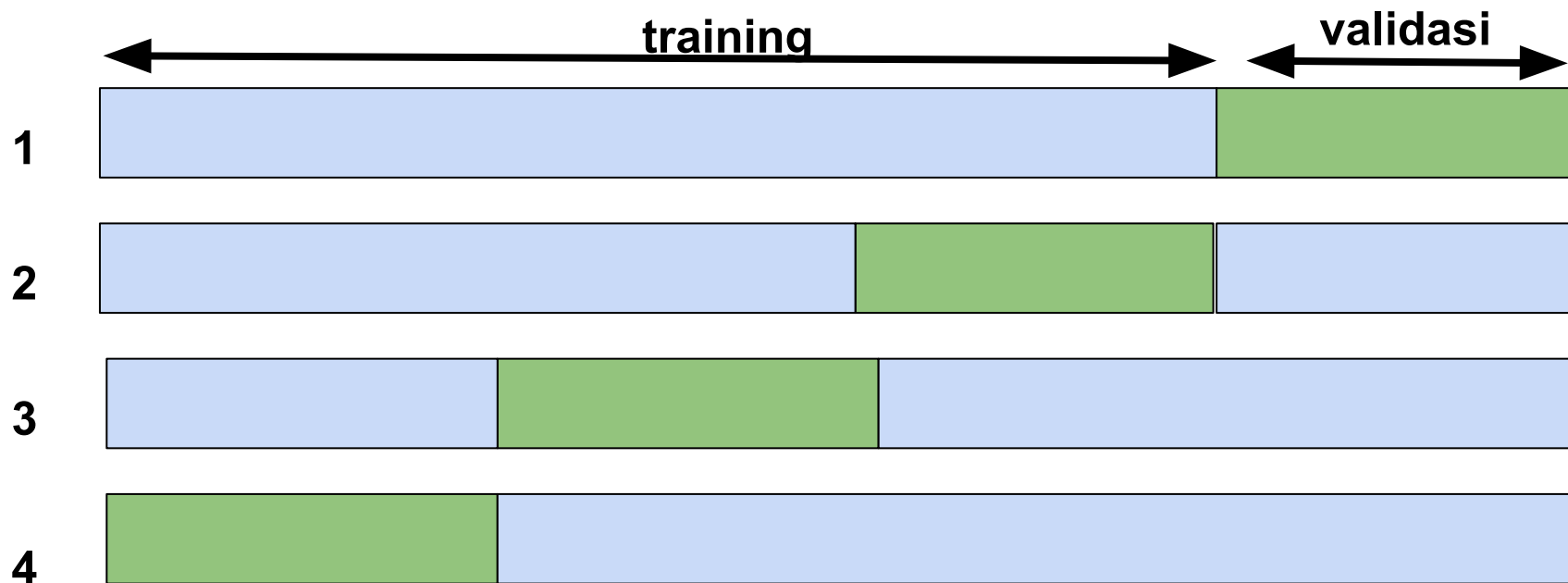


# Hold-out Validation

- Salah satu cara: pisahkan dataset menjadi training data dan validation data. Umumnya: 80% training, 20% validation data (atau 90:10)



# K-Fold Cross Validation



# Evaluasi: Confusion Matrix

n=165		Predicted: NO	Predicted: YES	
Actual: NO		TN = 50	FP = 10	60
Actual: YES		FN = 5	TP = 100	105
		55	110	

# Pengukuran

	Predicted class	
	+ve	-ve
Actual Class	+ve	True Positive(TP) False Negative(FN)
	-ve	False Positive(FP) True Negative(TN)

$$\text{Akurasi} = \frac{TP+TN}{TP+FP+TN+FN}$$



# F-Measure

Actual Class	Predicted class	
	+ve	-ve
	+ve True Positive(TP)	-ve False Negative(FN)
	-ve False Positive(FP)	True Negative(TN)

$$Precision = \frac{X}{Y} \text{ or } \frac{TP}{TP + FP}$$

$$Recall = \frac{Y}{Z} \text{ or } \frac{TP}{TP + FN}$$

Precision: % item yang dipilih yang benar.

Recall: % item benar yang diambil.

# F-Measure

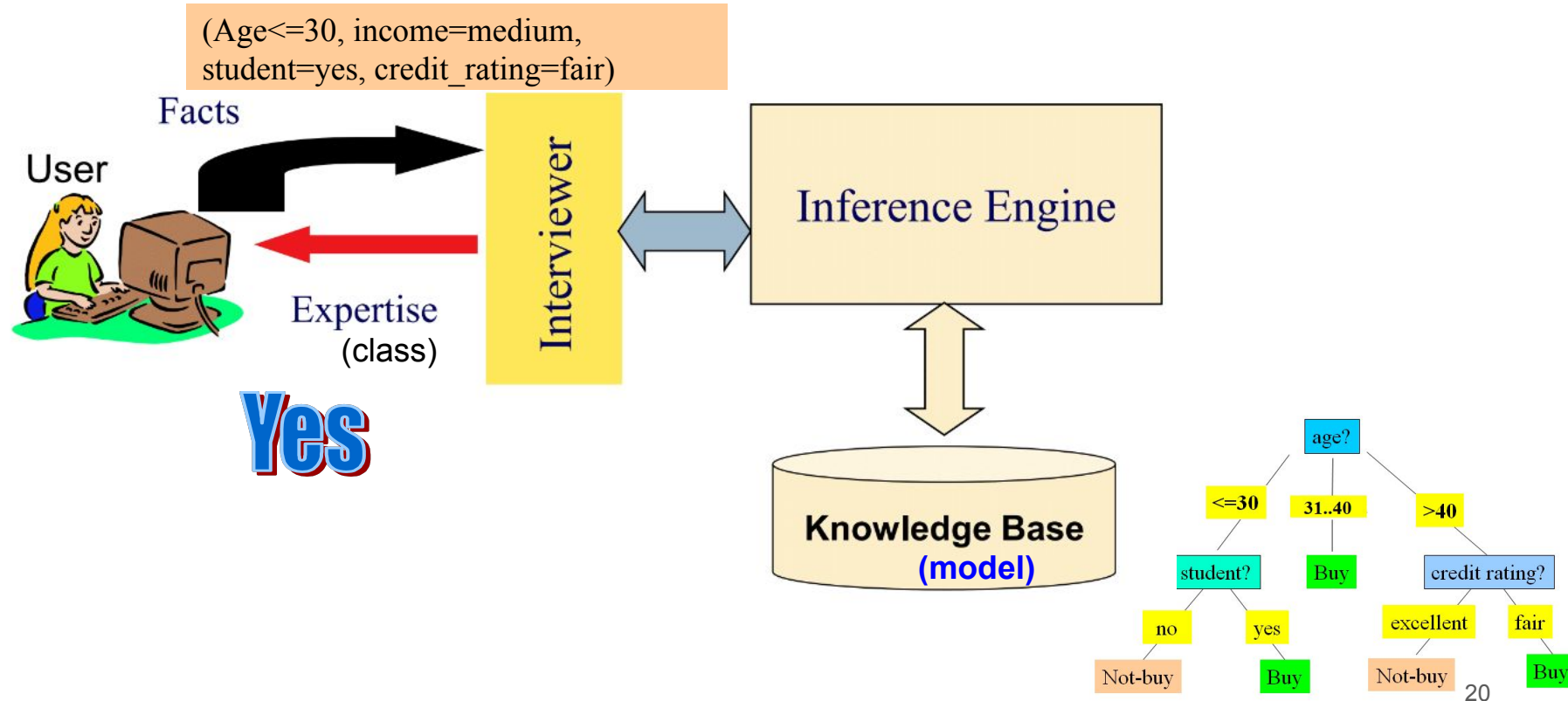
F-Measure: kombinasi antara nilai prec. dan recall

$$F - measure = \frac{2 \times Recall \times Precision}{Recall + Precision}$$

# Ukuran Kinerja Lain

- Kappa (Cohen's kappa):
  - akurasi dinormalisasi dengan imbalance dari class.
- ROC Curves
- Geometric mean of the true rates
- Dominance

# Model Deployment



# Review Tahapan Pembelajaran Mesin

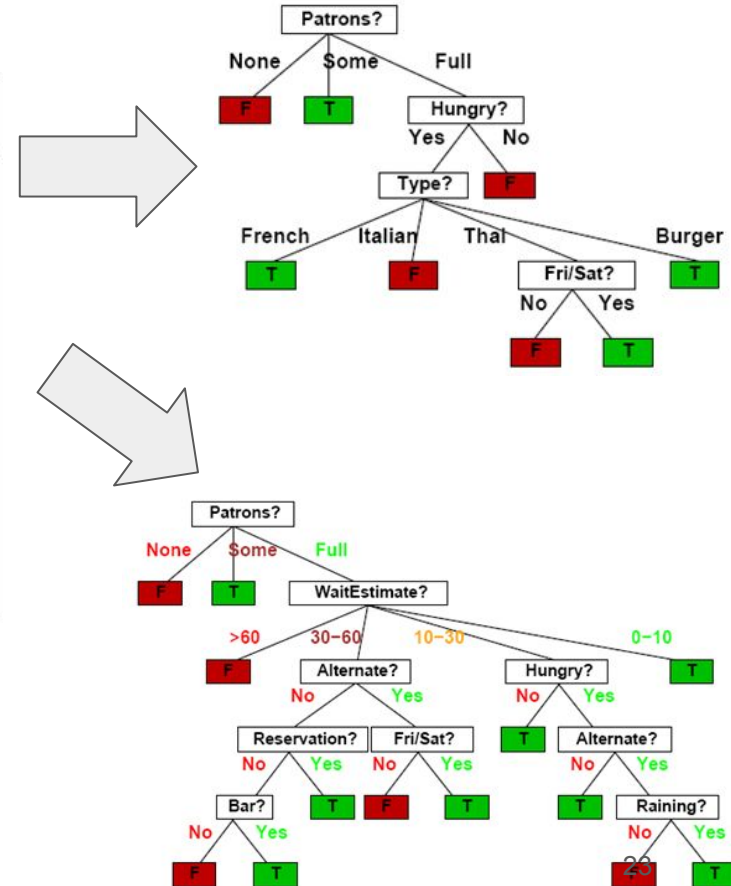
- Proses konstruksi model
  - Training data → Model Klasifikasi
- Proses validasi dan tes model
  - Validation data → model terbaik
  - Test data → kinerja model
- Proses klasifikasi (deployment)
  - Data yang tidak diketahui kelasnya → kelas data

# Algoritma Pembelajaran

- Decision tree learning
- Naive Bayes
- IF-THEN rules
  - Ekstraksi dari Decision Tree
  - Rule Induction: Sequential Covering Method
- Neural Network

# Decision Tree Learning

Example	Attributes										Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30-60	F
$X_3$	F	T	F	F	Some	\$	F	F	Burger	0-10	T
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10-30	T
$X_5$	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
$X_6$	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
$X_7$	F	T	F	F	None	\$	T	F	Burger	0-10	F
$X_8$	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0-10	F
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30-60	T



Russell, S. J., & Norvig, P. (2016). *Artificial intelligence: a modern approach*. Malaysia; Pearson Education Limited,.

# Decision Tree Learning

- Aim: find a small tree consistent with the training examples
- Idea: (recursively) choose "most significant" attribute as root of

```
function DTL(examples, attributes, default) returns a decision tree
  if examples is empty then return default
  else if all examples have the same classification then return the classification
  else if attributes is empty then return MODE(examples)
  else
    best ← CHOOSE-ATTRIBUTE(attributes, examples)
    tree ← a new decision tree with root test best
    for each value  $v_i$  of best do
       $examples_i \leftarrow \{\text{elements of } examples \text{ with } best = v_i\}$ 
      subtree ← DTL(examplesi, attributes – best, MODE(examples))
      add a branch to tree with label  $v_i$  and subtree subtree
  return tree
```

$$Info(D) = - \sum_{i=1}^m p_i \log_2(p_i)$$

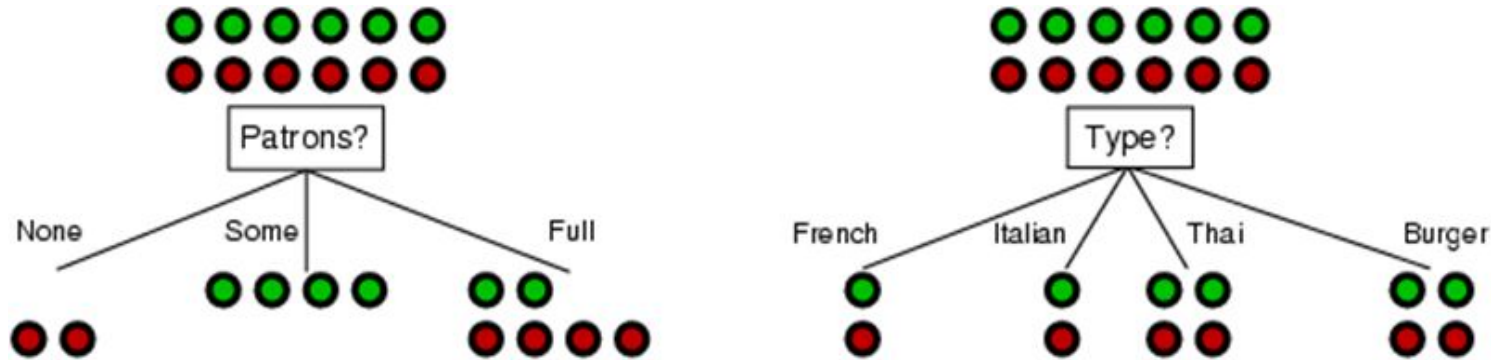
$$Info_A(D) = \sum_{j=1}^v \frac{|D_j|}{|D|} \times Info(D_j)$$

$$Gain(A) = Info(D) - Info_A(D)$$



# Choosing an attribute

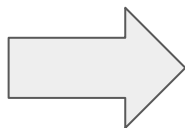
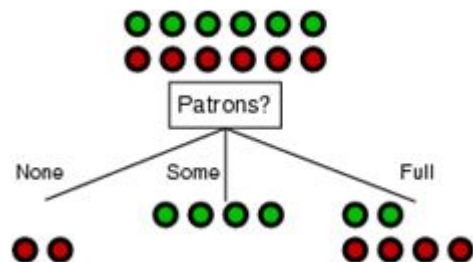
Idea: a good attribute splits the examples into subsets that are (ideally) "all positive" or "all negative"



$$IG(Patrons) = 1 - \left[ \frac{2}{12} I(0,1) + \frac{4}{12} I(1,0) + \frac{6}{12} I\left(\frac{2}{6}, \frac{4}{6}\right) \right] = 0.541 \text{ bits}$$

$$IG(Type) = 1 - \left[ \frac{2}{12} I\left(\frac{1}{2}, \frac{1}{2}\right) + \frac{2}{12} I\left(\frac{1}{2}, \frac{1}{2}\right) + \frac{4}{12} I\left(\frac{2}{4}, \frac{2}{4}\right) + \frac{4}{12} I\left(\frac{2}{4}, \frac{2}{4}\right) \right] = 0 \text{ bits}$$

# Patrons? = Full



Example	Input Attributes										Goal
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	<i>WillWait</i>
$x_2$	Yes	No	No	Yes	Full	\$	No	No	Thai	30-60	$y_2 = \text{No}$
$x_4$	Yes	No	Yes	Yes	Full	\$	Yes	No	Thai	10-30	$y_4 = \text{Yes}$
$x_5$	Yes	No	Yes	No	Full	\$\$\$	No	Yes	French	>60	$y_5 = \text{No}$
$x_9$	No	Yes	Yes	No	Full	\$	Yes	No	Burger	>60	$y_9 = \text{No}$
$x_{10}$	Yes	Yes	Yes	Yes	Full	\$\$\$	No	Yes	Italian	10-30	$y_{10} = \text{No}$
$x_{12}$	Yes	Yes	Yes	Yes	Full	\$	No	No	Burger	30-60	$y_{12} = \text{Yes}$

$$I(1/3, 2/3) = 0.92$$

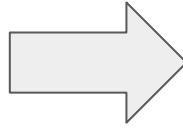
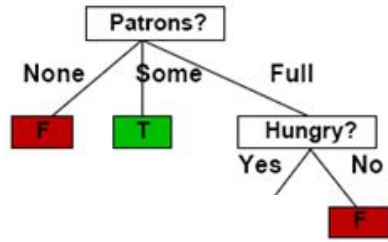
$$IG(\text{Alt}) = 0.92 - 5/6 * I(2/5, 3/5) - 1/6 * I(0, 1) = 0.11$$

...

$$IG(\text{Hun}) = 0.92 - 4/6 * I(1/2, 1/2) - 2/6 * I(0, 1) = 0.25$$

...

# Patrons? = Full and Hungry? = Yes



Example	Input Attributes										Goal
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
<b>x<sub>2</sub></b>	Yes	No	No	Yes	Full	\$	No	No	Thai	30–60	y <sub>2</sub> = No
<b>x<sub>4</sub></b>	Yes	No	Yes	Yes	Full	\$	Yes	No	Thai	10–30	y <sub>4</sub> = Yes
<b>x<sub>10</sub></b>	Yes	Yes	Yes	Yes	Full	\$\$\$	No	Yes	Italian	10–30	y <sub>10</sub> = No
<b>x<sub>12</sub></b>	Yes	Yes	Yes	Yes	Full	\$	No	No	Burger	30–60	y <sub>12</sub> = Yes

$$I(1/2, 1/2) = 1$$

$$IG(Alt) = 1 - 4/4 * I(1/2, 1/2) = 0$$

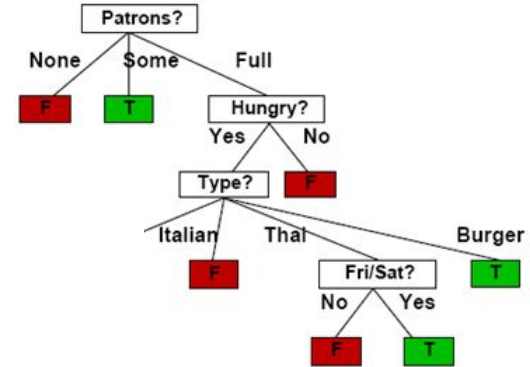
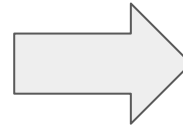
$$IG(Bar) = 1 - 1/2 * I(1/2, 1/2) - 1/2 * I(1/2, 1/2) = 0$$

$$IG(Fri) = 1 - 1/4 * I(0, 1) - 3/4 * I(2/3, 1/3) = 0.39$$

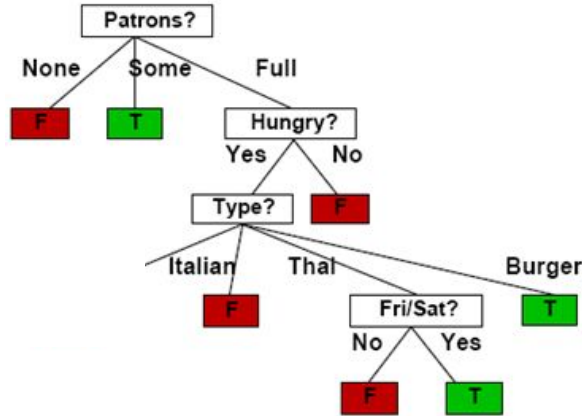
...

$$IG(Type) = 1 - 1/2 * I(1/2, 1/2) - 1/4 * I(0, 1) - 1/4 * I(1, 0) = 0.5$$

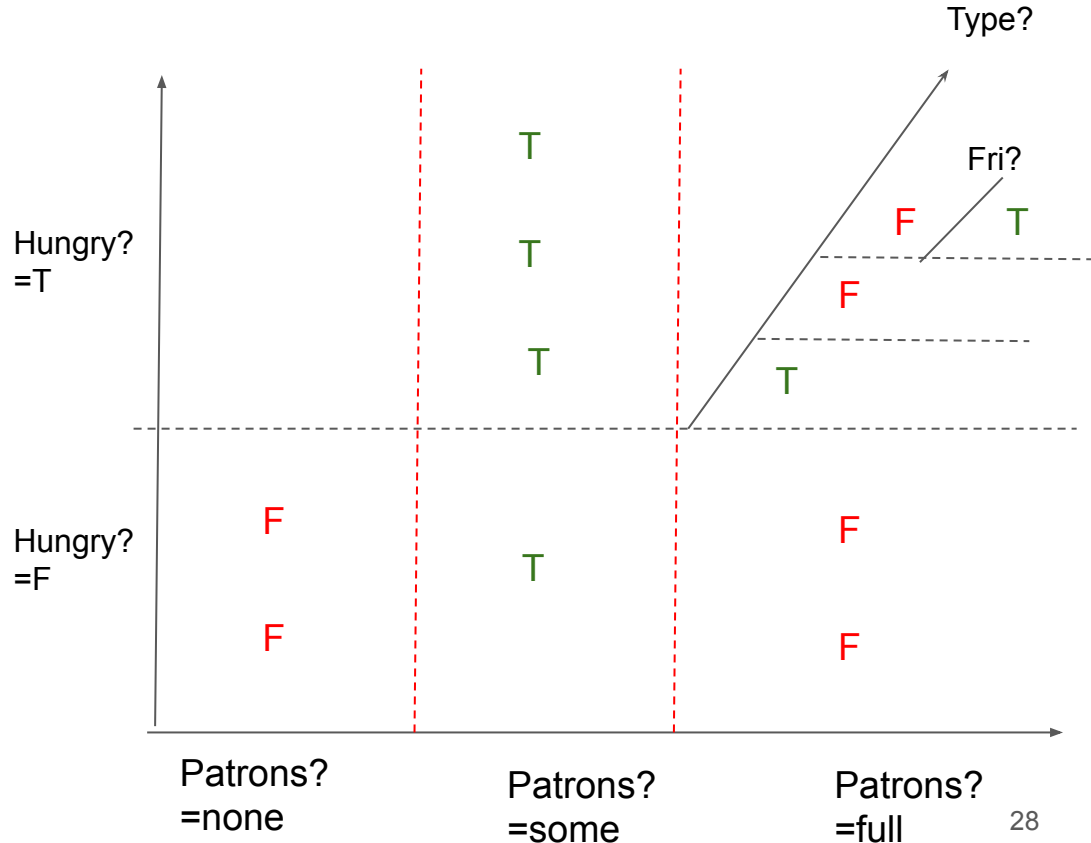
...



# Klasifikasi dengan Hyperplane Decision Tree



Example	Attributes										Target WillWait
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	
X <sub>1</sub>	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
X <sub>2</sub>	T	F	F	T	Full	\$	F	F	Thai	30-60	F
X <sub>3</sub>	F	T	F	F	Some	\$	F	F	Burger	0-10	T
X <sub>4</sub>	T	F	T	T	Full	\$	F	F	Thai	10-30	T
X <sub>5</sub>	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
X <sub>6</sub>	F	T	F	T	Some	\$	T	T	Italian	0-10	T
X <sub>7</sub>	F	T	F	F	None	\$	T	F	Burger	0-10	F
X <sub>8</sub>	F	F	F	T	Some	\$	T	T	Thai	0-10	T
X <sub>9</sub>	F	T	T	F	Full	\$	T	F	Burger	>60	F
X <sub>10</sub>	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
X <sub>11</sub>	F	F	F	F	None	\$	F	F	Thai	0-10	F
X <sub>12</sub>	T	T	T	T	Full	\$	F	F	Burger	30-60	T

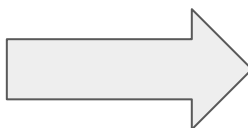


# Decision Tree Learning: Why Popular

- Relatively fast learning speed
- Convertible to simple and easy to understand classification rules
- Easy to be adapted to database system implementations (e.g., using SQL)
- Comparable classification accuracy with other methods

# Naive Bayes Classifier

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no



$$P(\text{buys\_computer} = \text{"yes"}) = 9/14 = 0.643$$

$$P(\text{buys\_computer} = \text{"no"}) = 5/14 = 0.357$$

$$P(\text{age} = \text{"<=30"} \mid \text{buys\_computer} = \text{"yes"}) = 2/9 = 0.222$$

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$$P(\text{income} = \text{"medium"} \mid \text{buys\_computer} = \text{"yes"}) = 4/9 = 0.444$$

$$P(\text{income} = \text{"medium"} \mid \text{buys\_computer} = \text{"no"}) = 2/5 = 0.4$$

$$P(\text{student} = \text{"yes"} \mid \text{buys\_computer} = \text{"yes"}) = 6/9 = 0.667$$

$$P(\text{student} = \text{"yes"} \mid \text{buys\_computer} = \text{"no"}) = 1/5 = 0.2$$

$$P(\text{credit\_rating} = \text{"fair"} \mid \text{buys\_computer} = \text{"yes"}) = 6/9 = 0.667$$

$$P(\text{credit\_rating} = \text{"fair"} \mid \text{buys\_computer} = \text{"no"}) = 2/5 = 0.4$$

# Naive Bayes: Learning

$$P(\text{age} = "<=30" \mid \text{buys\_computer} = \text{"yes"}) \\ = 2/9 = 0.222$$

$$P(\text{age} = "<= 30" \mid \text{buys\_computer} = \text{"no"}) \\ = 3/5 = 0.6$$

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$$v_{NB} = \arg \max_{v_j \in \{yes, no\}} P(v_j) \prod_i P(a_i \mid v_j)$$

$P(v_j)$ : probabilitas kelas  $v_j$

$P(a_i \mid v_j)$ : probabilitas atribut  $a_i$  pada  $v_j$

$$P(a_i \mid v_j) = (v_j \cap a_i) / |v_j|$$

# Naive Bayes: Klasifikasi

$$v_{NB} = \arg \max_{v_j \in \{yes, no\}} P(v_j) \prod_i P(a_i | v_j)$$

$$P(\text{buys\_computer} = \text{"yes"}) = 9/14 = 0.643$$

$$P(\text{buys\_computer} = \text{"no"}) = 5/14 = 0.357$$

$$P(\text{age} = \text{"<=30"} | \text{buys\_computer} = \text{"yes"}) = 2/9 = 0.222$$

$$P(\text{age} = \text{"<= 30"} | \text{buys\_computer} = \text{"no"}) = 3/5 = 0.6$$

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$$P(\text{credit\_rating} = \text{"fair"} | \text{buys\_computer} = \text{"yes"}) = 6/9 = 0.667$$

$$P(\text{credit\_rating} = \text{"fair"} | \text{buys\_computer} = \text{"no"}) = 2/5 = 0.4$$

**X = (age <= 30 , income = medium,  
student = yes, credit\_rating = fair)**

$$P(X | \text{buys\_computer} = \text{"yes"}) = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044$$

$$P(X | \text{buys\_computer} = \text{"yes"}) *$$

$$P(\text{buys\_computer} = \text{"yes"}) = 0.028$$

$$P(X | \text{buys\_computer} = \text{"no"}) = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$$

$$P(X | \text{buys\_computer} = \text{"no"}) *$$

$$P(\text{buys\_computer} = \text{"no"}) = 0.007$$



# Naive Bayes: Keuntungan vs Kerugian

- Keuntungan
  - Mudah untuk dibuat
  - Hasil bagus
  - Incremental learning
- Kerugian
  - Asumsi independence antar atribut

# Klasifikasi dengan IF-THEN rules

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no



IF age = young AND student = no THEN  
buys\_computer = no

IF age = young AND student = yes THEN  
buys\_computer = yes

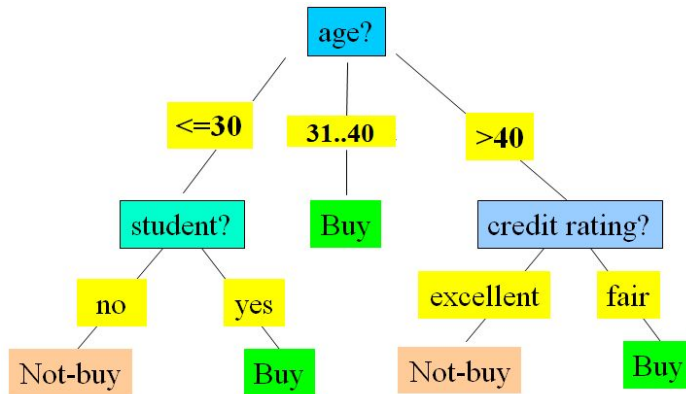
IF age = mid-age THEN buys\_computer = yes

IF age = old AND credit\_rating = excellent  
THEN buys\_computer = no

IF age = old AND credit\_rating = fair THEN  
buys\_computer = yes

# Klasifikasi dengan IF-THEN rules (2)

- Represent the knowledge in the form of IF-THEN rules  
Format: IF rule-precondition THEN rule-consequent  
Contoh: IF age = youth AND student = yes THEN buys\_computer = yes
- Ekstraksi rule dari decision trees karena lebih mudah dimengerti daripada trees.



IF age = young AND student = no THEN  
buys\_computer = no

IF age = young AND student = yes THEN  
buys\_computer = yes

IF age = mid-age THEN buys\_computer = yes

IF age = old AND credit\_rating = excellent THEN  
buys\_computer = no

IF age = old AND credit\_rating = fair THEN  
buys\_computer = yes

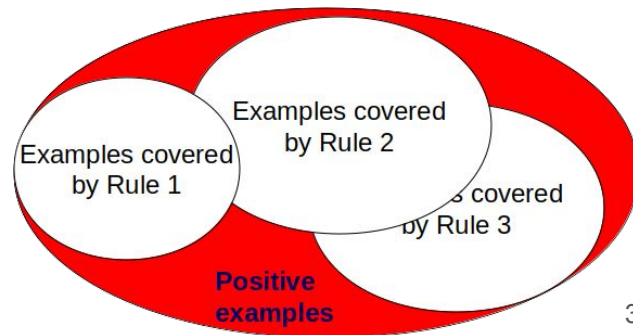
# Rule Induction: Sequential Covering Algorithm

- Sequential covering algorithm: Extracts rules directly from training data
- Rules are learned sequentially, each for a given class  $C_i$  will cover many tuples of  $C_i$  but none (or few) of the tuples of other classes

while (enough target tuples left)

    generate a rule

    remove positive target tuples satisfying this rule



# Sequential Covering Algorithm

$\text{COVER}(\text{Target\_attr}, \text{Attrs}, \text{Examples}, \text{Threshold})$

- $\text{Learned\_rules} \leftarrow \{\}$
- $\text{Rule} \leftarrow \text{LEARN-ONE-RULE}(\text{Target\_attr}, \text{Attrs}, \text{Examples})$
- **WHILE**  $\text{PERFORMANCE}(\text{Rule}, \text{Examples}) > \text{Threshold}$ , **DO**
  - $\text{Learned\_rules} \leftarrow \text{Learned\_rules} + \text{Rule}$
  - $\text{Examples} \leftarrow \text{Examples} - \{\text{EXAMPLES CORRECTLY CLASSIFIED BY Rule}\}$
  - $\text{Rule} \leftarrow \text{LEARN-ONE-RULE}(\text{Target\_attr}, \text{Attrs}, \text{Examples})$
- $\text{Learned\_rules} \leftarrow \text{SORT } \text{Learned\_rules} \text{ ACCORD TO PERFORMANCE OVER } \text{Examples}$
- **RETURN**  $\text{Learned\_rules}$

- Algoritma covering: bangkitkan rules yang meng-cover kelas spesifik
- Steps:
  - Generate rule R on training data
  - Remove training data covered by R
  - Repeat the process

# Learn-One-Rule

LEARN-ONE-RULE(*Target\_attr*, *Attrs*, *Examples*)

- $Pos \leftarrow$  positive *Examples*;  $Neg \leftarrow$  negative *Examples*
- If  $Pos$

$NewRule \leftarrow$  most general rule possible;  $NewRuleNeg \leftarrow Neg$

While  $NewRuleNeg$

1.  $Candidate\_literals(CLs) \leftarrow$  generate candidates
  2.  $Best\_literal \leftarrow \operatorname{argmax}_{L \in CLs} PERFORMANCE(Specialize(NewRule, L))$
  3. add  $Best\_literal$  to  $NewRule$  preconditions
  4.  $NewRuleNeg \leftarrow$  subset of  $NewRuleNeg$  that satisfies  $NewRule$  preconditions
- Return  $NewRule$

T: attributes

C: classes

For all A in T do:

For all possible value  $v_i$  in A do:

For all  $C_j$  in C do:

find count( $C_j$ )

$C_{max}$ =class with largest count

$RA = RA \cup (A=v \Rightarrow C_{max})$

$ErrA$ =number of incorrectly classified by RA

$R = RA$  where  $ErrA$  is minimum

# Learn-One-Rule: Contoh

Day	Outlook	Temperature	Humidity	Wind	Ski?
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Attribute	Rules	Error	Total
Outlook	outlook=Sunny⇒No	2/5	4/14
	outlook=Overcast⇒Yes	0/4	
	outlook=Rain⇒Yes	2/5	
Temp	Temp=Hot⇒No	2/4	5/14
	Temp=Mild⇒Yes	2/6	
	Temp=Cool⇒Yes	1/4	
Humidity	Humidity=High⇒No	3/7	4/14
	Humidity=Normal⇒Yes	1/7	
Windy	Windy=Weak⇒Yes	2/8	5/14
	Windy=Strong⇒No	3/6	

# Sequential Covering Algorithm: Contoh

Day	Outlook	Temperature	Humidity	Wind	Ski?
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Threshold=0.5

LearnedRules={}

Rule R1: { outlook=Sunny⇒No;  
outlook=overcast⇒Yes;  
outlook=Rain⇒Yes}

RelativeFreq(R1,Examples)=10/14 > threshold

LearnedRules={R1}

Examples= {D6,D9,D11,D14}

**Relative Frequency:**

$$\frac{n_c}{n}$$

$n$  = # examples the rule matches

$n_c$  = # examples the rule matches and classifies correctly



# Sequential Covering Algorithm: Contoh (lanj)

Day	Outlook	Temperature	Humidity	Wind	Ski?
D6	Rain	Cool	Normal	Strong	No
D9	Sunny	Cool	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D14	Rain	Mild	High	Strong	No

Rule R2: { outlook=Sunny $\Rightarrow$ Yes;  
outlook=Rain $\Rightarrow$ No}

RelativeFreq(R2,Examples)=4/4 > threshold

LearnedRules={R1,R2}

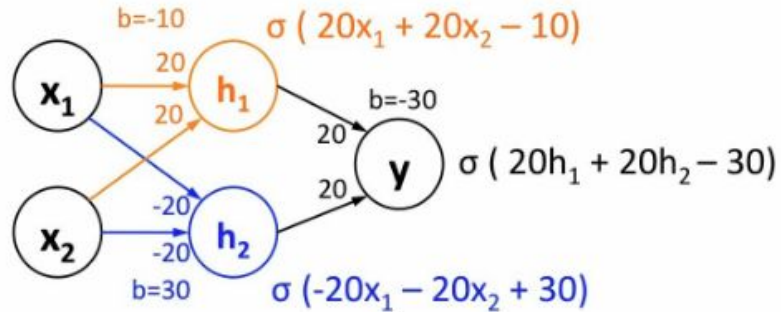
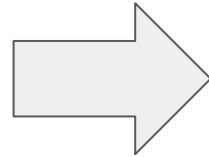
Examples= {}

Sorted LearnedRules: {R2,R1}

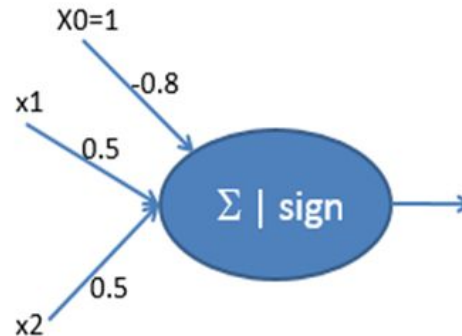
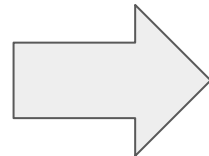
Attribute	Rules	Error	Total
Outlook	outlook=Sunny $\Rightarrow$ Yes	0/2	0/4
	outlook=Rain $\Rightarrow$ No	0/2	
Temp	Temp=Mild $\Rightarrow$ Yes	1/2	2/4
	Temp=Cool $\Rightarrow$ Yes	1/2	
Humidity	Humidity=High $\Rightarrow$ No	0/1	1/4
	Humidity=Normal $\Rightarrow$ Yes	1/3	
Windy	Windy=Weak $\Rightarrow$ Yes	0/1	1/4
	Windy=Strong $\Rightarrow$ No	1/3	

# Klasifikasi dengan Artificial Neural Network (FFNN)

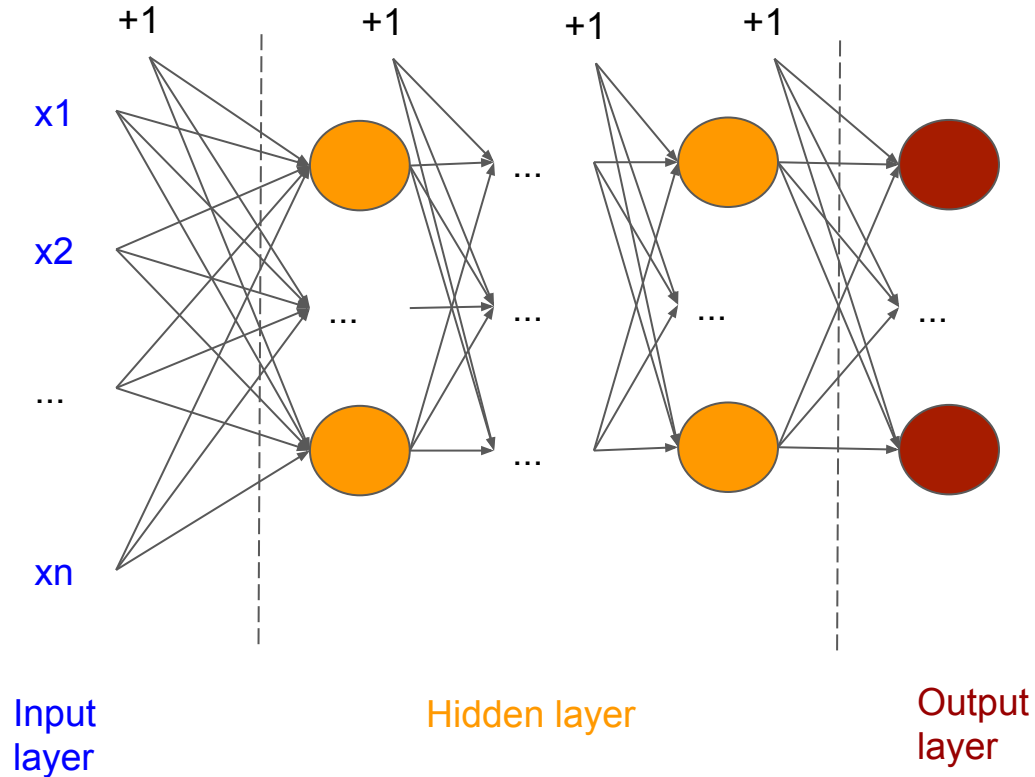
x1	x2	f
0	0	0
0	1	1
1	0	1
1	1	0



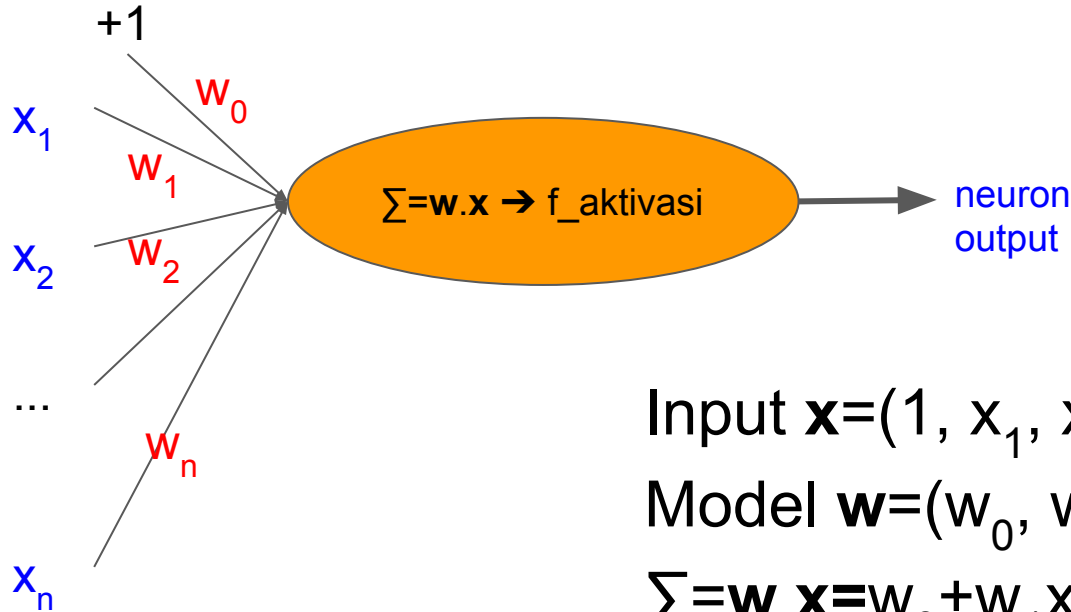
x1	x2	f
1	1	1
1	-1	-1
-1	1	-1
-1	-1	-1



# Artificial Neural Network (Jaringan Syaraf Tiruan)



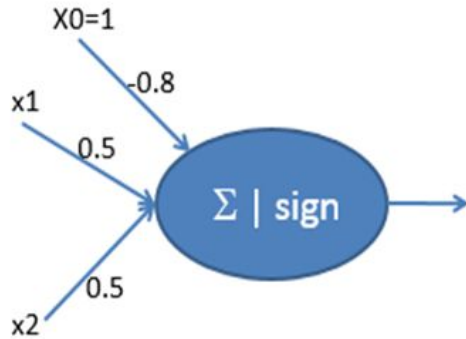
# Artificial Neuron



Input: real-valued vector  
 $x_0=1$  (bias)

$$\begin{aligned}\text{Input } \mathbf{x} &= (1, x_1, x_2, \dots, x_n) \\ \text{Model } \mathbf{w} &= (w_0, w_1, w_2, \dots, w_n) \\ \Sigma &= \mathbf{w} \cdot \mathbf{x} = w_0 + w_1 x_1 + \dots + w_n x_n \\ \text{Output} &= f(\Sigma)\end{aligned}$$

# Perceptron AND



$$\Sigma = -0.8 \cdot x_0 + 0.5 \cdot x_1 + 0.5 \cdot x_2$$
$$f = \text{sign}(\Sigma)$$

$x_1$	$x_2$	$\Sigma$	$\text{sign}(\Sigma)$	$f$
1	1	$-0.8 \cdot 1 + 0.5 \cdot 1 + 0.5 \cdot 1 = 0.2$	+1	1
1	-1	$-0.8 \cdot 1 + 0.5 \cdot 1 + 0.5 \cdot -1 = -0.8$	-1	-1
-1	1	$-0.8 \cdot 1 + 0.5 \cdot -1 + 0.5 \cdot 1 = -0.8$	-1	-1
-1	-1	$-0.8 \cdot 1 + 0.5 \cdot -1 + 0.5 \cdot -1 = -1.8$	-1	-1

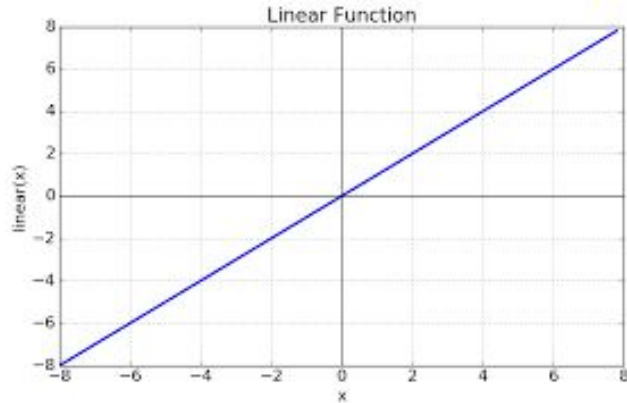
**sign** (net): +1 jika net > 0, dan -1 sebaliknya

# Fungsi Aktivasi

## Linear / identity

$$f(\text{net}) = \text{net}$$

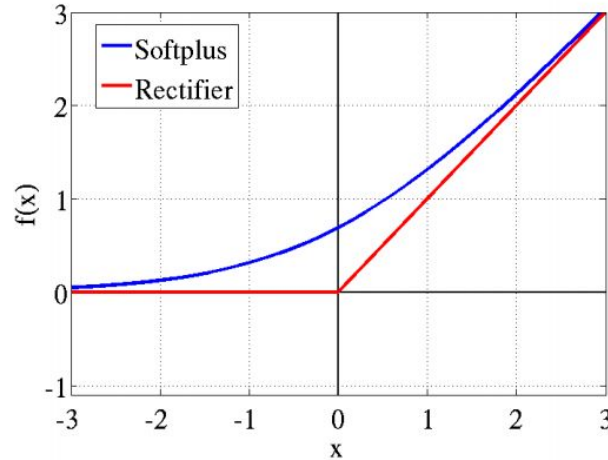
$$f'(\text{net}) = 1$$



## Relu (rectified linear unit)

$$f(\text{net}) = \max(0, \text{net})$$

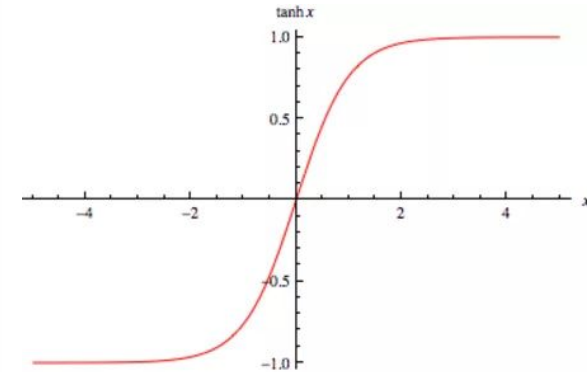
$$f'(\text{net}) = \max(0, 1)$$



## tanh

$$f(\text{net}) = (e^{\text{net}} - e^{-\text{net}}) / (e^{\text{net}} + e^{-\text{net}})$$

$$f'(\text{net}) = 1 - (f(\text{net}))^2$$

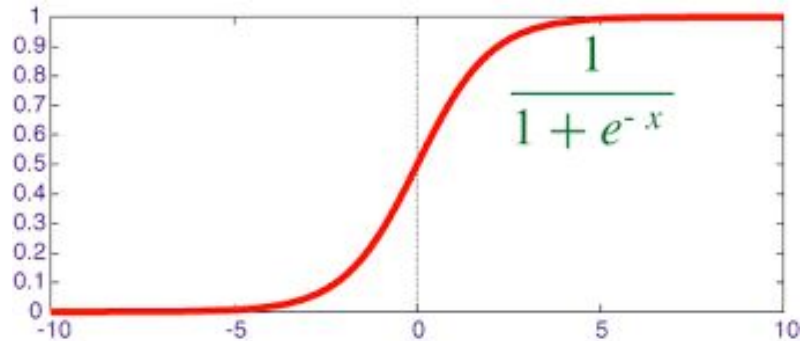


# Fungsi Aktivasi (lanjutan)

Sigmoid / logistik / soft step

$$f(\text{net}) = 1 / (1 + e^{-\text{net}})$$

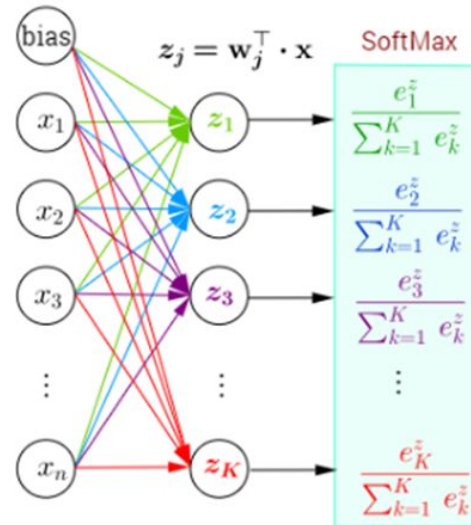
$$f'(\text{net}) = f(\text{net})(1 - f(\text{net}))$$



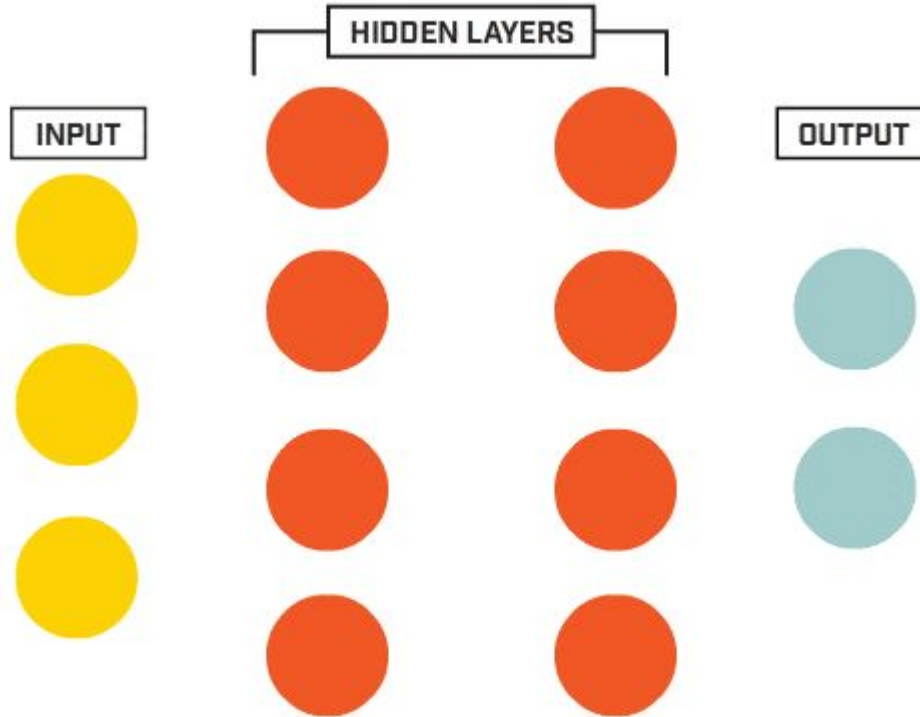
Softmax

$$f(\text{net}_i) = e^{\text{net}_i} / \sum e^{\text{net}_j}$$

$$f'(\text{net}_i) = f(\text{net}_i)(1 - f(\text{net}_i))$$



# Feed Forward ANN

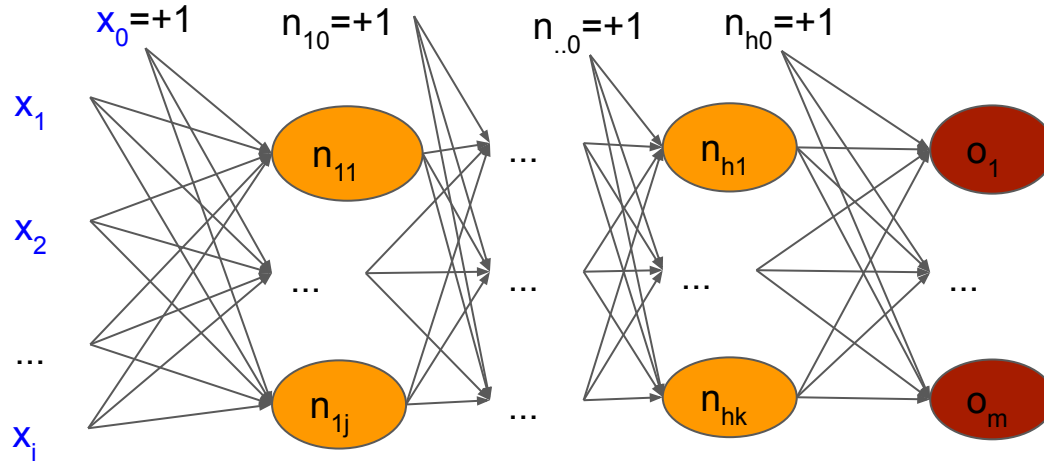


Struktur jaringan tanpa backward link

Informasi mengalir maju  
input → hidden layers → output



# Feed Forward ANN: Topologi

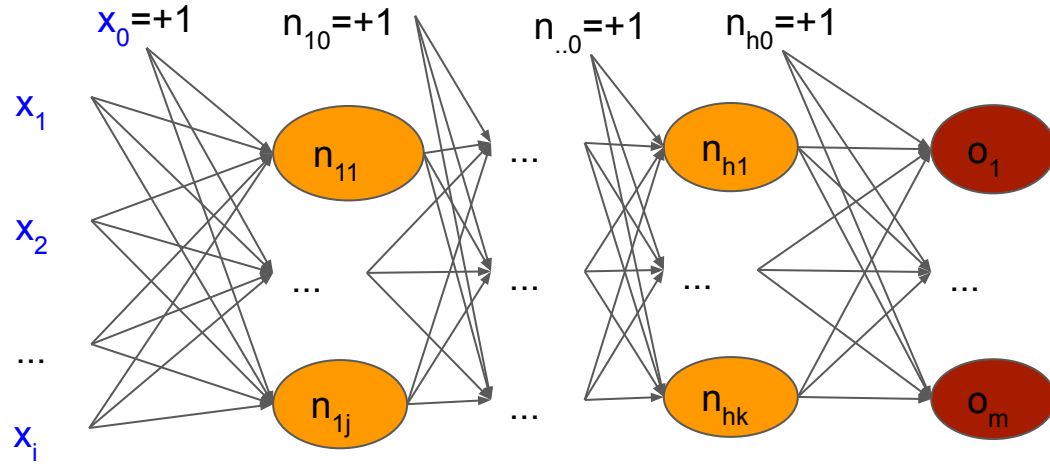


Input layer  
berukuran  $i$  fitur

$H$  hidden layer  
Hidden layer 1:  $j$  neuron  
Hidden layer  $h$ :  $k$  neuron

Output layer  
berukuran  $m$  neuron

# Feed Forward ANN: Representasi Model (Bobot)

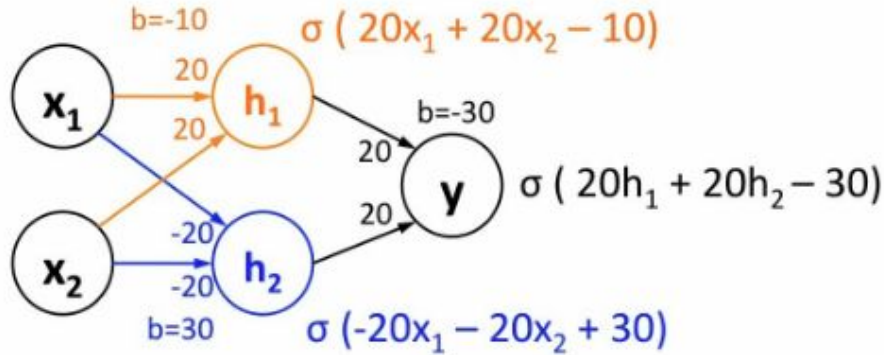


	$n_{11}$	$n_{12}$	...	$n_{1j}$
$x_0 = +1$	$w_{0\_11}$	$w_{0\_12}$	...	$w_{0\_1j}$
$x_1$	$w_{1\_11}$	$w_{1\_12}$	...	$w_{1\_1j}$
$x_2$	$w_{2\_11}$	$w_{2\_12}$	...	$w_{2\_1j}$
...	...	...	...	...
$x_i$	$w_{i\_11}$	$w_{i\_12}$	...	$w_{i\_1j}$

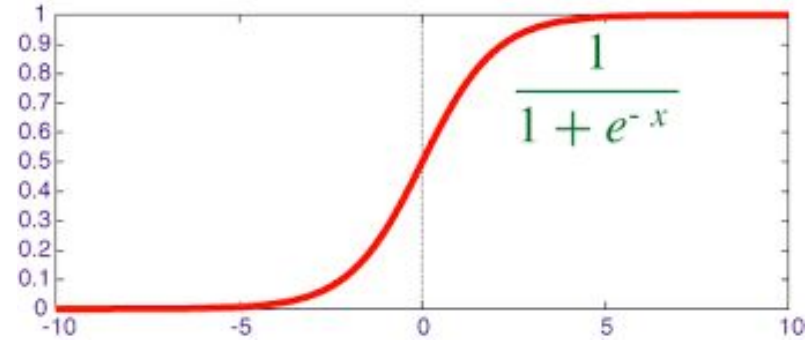
	$n_{21}$	$n_{22}$	...
$n_{10} = +1$	$w_{10\_21}$	$w_{10\_22}$	...
$n_{11}$	$w_{11\_21}$	$w_{11\_22}$	...
$n_{12}$	$w_{12\_21}$	$w_{12\_22}$	...
...	...	...	...
$n_{1j}$	$w_{1j\_21}$	$w_{1j\_22}$	...

	$o_1$	...	$o_m$
$n_{h0} = +1$	$w_{h0\_1}$	...	$w_{h0\_m}$
$n_{h1}$	$w_{h1\_1}$	...	$w_{h1\_m}$
$n_{h2}$	$w_{h2\_1}$	...	$w_{h2\_m}$
...	...	...	...
$n_{hk}$	$w_{hk\_1}$	...	$w_{hk\_m}$

# Feed Forward ANN: Contoh Klasifikasi



Sigmoid / logistik / soft step  
 $f(\text{net}) = 1/(1 + e^{-\text{net}})$



x1	x2	f
0	0	0
0	1	1
1	0	1
1	1	0

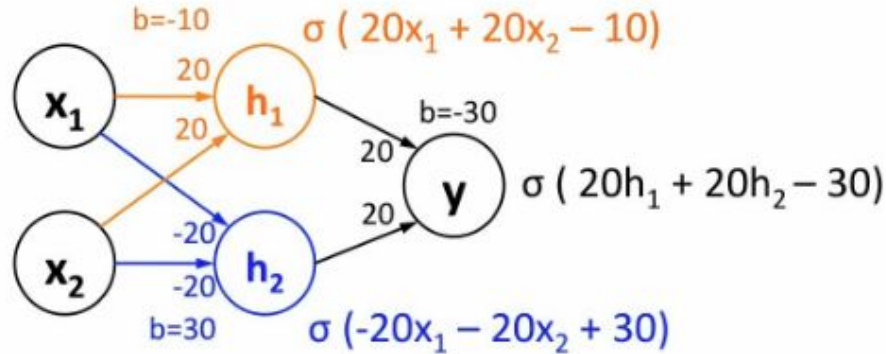
**x1=1; x2=0:**

$$h1 = \sigma(20x1 + 20x2 - 10) = \sigma(20 \cdot 1 + 20 \cdot 0 - 10) = \sigma(10) \approx 1$$

$$h2 = \sigma(-20x1 - 20x2 + 30) = \sigma(-20 \cdot 1 - 20 \cdot 0 + 30) = \sigma(10) \approx 1$$

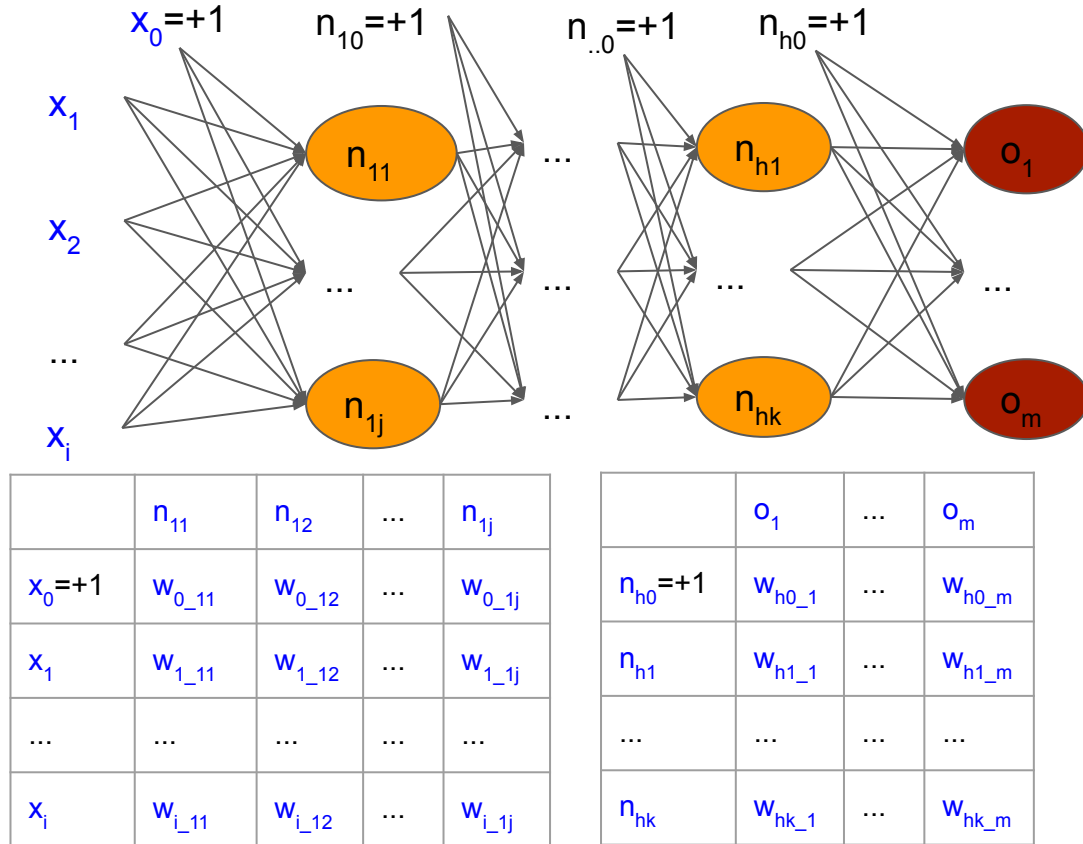
$$y = \sigma(20h1 + 20h2 - 30) = \sigma(20 \cdot 1 + 20 \cdot 1 - 30) = \sigma(10) \approx 1$$

# Feed Forward ANN: Contoh Klasifikasi



x0	x1	x2	f	$\Sigma h_1$	h1	$\Sigma h_2$	h2	$\Sigma y$	y
1	0	0	0	-10	0.00	30	1.00	-10.00	0.00
1	0	1	1	10	1.00	10	1.00	10.00	1.00
1	1	0	1	10	1.00	10	1.00	10.00	1.00
1	1	1	0	30	1.00	-10	0.00	-10.00	0.00

# Feed Forward ANN: Perhitungan Output



Input  $\mathbf{x}=(1, x_1, x_2, \dots, x_i)$

$$n_{11} = f((w_{0\_11}, \dots, w_{i\_11}).(1, x_1, \dots, x_i))$$

...

$$n_{1j} = f((w_{0\_1j}, \dots, w_{i\_1j}).(1, x_1, \dots, x_i))$$

$$n_{21} = f((w_{10\_21}, \dots, w_{1j\_21}).(1, n_{11}, \dots, n_{1j}))$$

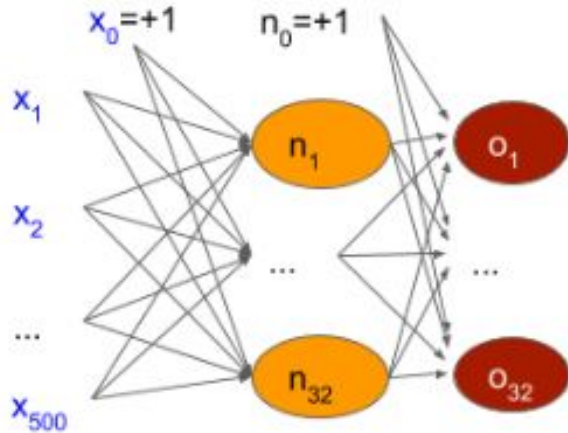
...

$$o_1 = f((w_{h0\_1}, \dots, w_{hk\_1}).(1, n_{h1}, \dots, n_{hk}))$$

...

$$o_m = f((w_{h0\_m}, \dots, w_{hk\_m}).(1, n_{h1}, \dots, n_{hk}))$$

# Feed Forward ANN pada Keras



```
from keras import models
from keras import layers
```

```
#definisikan model sebagai urutan layer
model = models.Sequential()
#model menerima input dengan jumlah fitur 500 dan output 32
#jumlah instance tidak perlu dituliskan dalam input_shape
model.add(layers.Dense(32, input_shape=(500,)))
#input layer ini otomatis 32 (output layer sebelumnya)
model.add(layers.Dense(32))
```

# Tugas 1

- Pilihlah dataset dari <https://archive.ics.uci.edu/ml/datasets.php>
- Tools: Jupyter Notebook dengan python. Gunakan scikit-learn untuk konstruksi model klasifikasi (training data)
- Skenario:
  - split dataset menjadi 90:10 (train:test)
  - Lakukanlah holdout validation dengan split training data menjadi 90:10 (train:validasi)
    - Gunakanlah validation data untuk memilih model klasifikasi terbaik dari berbagai algoritma pembelajaran dengan variasi nilai parameter berbeda.
  - Lakukanlah 5-fold cross validation untuk training data.
    - Pilih model klasifikasi terbaik dari berbagai algoritma pembelajaran dengan variasi nilai parameter berbeda.
  - Gunakanlah test data untuk mendapatkan kinerja dari setiap skenario.
- Lakukanlah analisis di proses validasi dan testing