

# Removal of Left Recursion

- 1  $program \rightarrow \text{program id ( identifier\_list ) ; declarations subprogram\_declarations compound\_statement .}$ 
  - 2.1.1  $identifier\_list \rightarrow \text{id identifier\_list'}$
  - 2.2.1  $identifier\_list' \rightarrow \text{, id identifier\_list'}$
  - 2.2.2  $identifier\_list' \rightarrow \epsilon$
  - 3.1.1  $declarations \rightarrow \text{var id : type ; declarations}$
  - 3.2.1  $declarations \rightarrow \epsilon$
  - 4.1  $type \rightarrow \text{standard\_type}$
  - 4.2  $type \rightarrow \text{array [ num .. num ] of standard\_type}$
  - 5.1  $standard\_type \rightarrow \text{integer}$
  - 5.2  $standard\_type \rightarrow \text{real}$
  - 6.1.1  $subprogram\_declarations \rightarrow \text{subprogram\_declaration ; subprogram\_declarations}$
  - 6.2.1  $subprogram\_declarations \rightarrow \epsilon$
- 7  $subprogram\_declaration \rightarrow \text{subprogram\_head declarations subprogram\_declarations compound\_statement}$
- 8  $subprogram\_head \rightarrow \text{function id arguments : standard\_type ;}$ 
  - 9.1  $arguments \rightarrow \text{( parameter\_list )}$
  - 9.2  $arguments \rightarrow \epsilon$
  - 10.1.1  $parameter\_list \rightarrow \text{id : type parameter\_list'}$
  - 10.2.1  $parameter\_list' \rightarrow \text{; id : type parameter\_list'}$
  - 10.2.2  $parameter\_list' \rightarrow \epsilon$
- 11  $compound\_statement \rightarrow \text{begin optional\_statements end}$ 
  - 12.1  $optional\_statements \rightarrow \text{statement\_list}$
  - 12.2  $optional\_statements \rightarrow \epsilon$
  - 13.1.1  $statement\_list \rightarrow \text{statement statement\_list'}$
  - 13.2.1  $statement\_list' \rightarrow \text{; statement statement\_list'}$
  - 13.2.2  $statement\_list' \rightarrow \epsilon$
  - 14.1  $statement \rightarrow \text{variable assignop expression}$
  - 14.2  $statement \rightarrow \text{compound\_statement}$
  - 14.3  $statement \rightarrow \text{if expression then statement}$
  - 14.4  $statement \rightarrow \text{if expression then statement else statement}$
  - 14.5  $statement \rightarrow \text{while expression do statement}$
  - 15.1  $variable \rightarrow \text{id}$
  - 15.2  $variable \rightarrow \text{id [ expression ]}$
  - 16.1.1  $expression\_list \rightarrow \text{expression expression\_list'}$
  - 16.2.1  $expression\_list' \rightarrow \text{, expression expression\_list'}$
  - 16.2.2  $expression\_list' \rightarrow \epsilon$
  - 17.1  $expression \rightarrow \text{simple\_expression}$
  - 17.2  $expression \rightarrow \text{simple\_expression relop simple\_expression}$
  - 18.1.1  $simple\_expression \rightarrow \text{term simple\_expression'}$
  - 18.2.1  $simple\_expression \rightarrow \text{sign term simple\_expression'}$
  - 18.3.1  $simple\_expression' \rightarrow \text{addop term simple\_expression'}$
  - 18.3.2  $simple\_expression' \rightarrow \epsilon$
  - 19.1.1  $term \rightarrow \text{factor term'}$
  - 19.2.1  $term' \rightarrow \text{mulop factor term'}$
  - 19.2.2  $term' \rightarrow \epsilon$
  - 20.1  $factor \rightarrow \text{id}$
  - 20.2  $factor \rightarrow \text{id [ expression ]}$
  - 20.3  $factor \rightarrow \text{id ( expression\_list )}$
  - 20.4  $factor \rightarrow \text{num}$
  - 20.5  $factor \rightarrow \text{( expression )}$
  - 20.6  $factor \rightarrow \text{not factor}$
  - 21.1  $sign \rightarrow \text{+}$
  - 21.2  $sign \rightarrow \text{-}$