Practical 6: Mixed effects models

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We perform some classical linear modeling with a random grouping factor. Predictions etc can be computed with random effects, or fixed effects only. Model checks, model comparisons, hypotheses, etc are the same as with linear models.

```
rm(list=ls())
library("brms")
library("ggplot2")
library("performance")
library("ecostats")
library("cowplot")
try(dev.off())
```

Random interceps ANOVA

From Warton, D. (2022) Eco-Stats: Data Analysis in Ecology

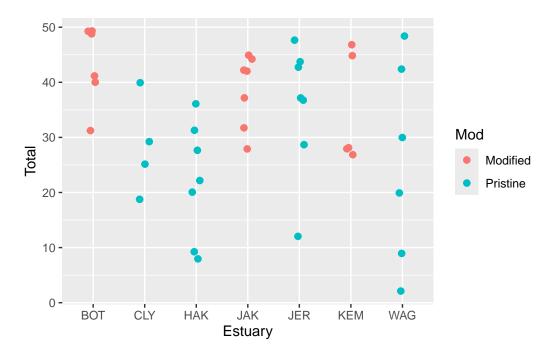
Counted number of invertebrate species in samples from different estuaries. Estuaries are either pristine or modified. Data are grouped, originate from 7 estuaries with multiple samples per estuary.

Question: Is there a difference in species richness between modified and pristine estuaries?

The random grouping factor Estuary is nested in Mod, because each Estuary is either modified or pristine. We could model this as (1|Mod/Estuary), but since Mod only has two levels, of which we are interested in species difference, we model Mod as fixed effect with random effects for Estuary.

```
data("estuaries")
table(estuaries$Mod, estuaries$Estuary)
```

ggplot(estuaries, aes(Estuary, Total, col=Mod)) + geom_jitter(width=0.1, size=2)



Remove NAs. brms automatically removes them in model fitting. But when different predictors have NAs for different observations, models that do not have the same predictors might end up with different datasets. In this case, model comparison would not be possible (requires identical datasets).

```
ID.complete = complete.cases(estuaries[, c("Total", "Mod", "Estuary", "Temperature")])
estuaries = estuaries[ID.complete, ]
```

```
 \begin{array}{ll} \text{Deterministic part:} & \mu_i = b(Mod_i) + \delta(Estuary_i) \\ \text{Stochastic part:} & Total_i \sim \text{Normal}(\mu_i, \sigma) \\ \text{Hierarchical part:} & \delta_j \sim \text{Normal}(0, \sigma_{Est}) \\ i = 1 \dots N, \ Mod = 1, 2, \ Estuary = 1 \dots 7 \\ \end{array}
```

```
default_prior(Total ~ Mod+(1|Estuary), data=estuaries)
```

```
group resp dpar nlpar lb ub
                 prior
                            class
                                          coef
                                                                                      source
                 (flat)
                                                                                     default
                 (flat)
                                b ModPristine
                                                                                (vectorized)
student_t(3, 32, 14.8) Intercept
                                                                                     default
student_t(3, 0, 14.8)
                                                                          0
                                                                                     default
student_t(3, 0, 14.8)
                                               Estuary
                                                                          0
                                                                                (vectorized)
                               sd
student_t(3, 0, 14.8)
                               sd
                                     Intercept Estuary
                                                                          0
                                                                                (vectorized)
student t(3, 0, 14.8)
                                                                          0
                                                                                     default
                            sigma
```

We only need to specify a prior for the fixed effect (which is dummy-coded), the random effects part is already taken care of by default.

Check convergence. There were divergent transitions, but just 2 which is no big deal.

Note that summary() and plot() do not display the actual random effects δ_j , only their sdev $\sigma_{Estuary} = sd(Intercept)$

```
summary(fit.est.1, prior=TRUE)
```

Warning: There were 2 divergent transitions after warmup. Increasing adapt_delta above 0.8 m

```
Family: gaussian
  Links: mu = identity; sigma = identity
Formula: Total ~ Mod + (1 | Estuary)
  Data: estuaries (Number of observations: 41)
  Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
  total post-warmup draws = 4000
```

Priors:

b ~ normal(0, 10)
Intercept ~ student_t(3, 32, 14.8)
<lower=0> sd ~ student_t(3, 0, 14.8)
<lower=0> sigma ~ student_t(3, 0, 14.8)

Multilevel Hyperparameters:

~Estuary (Number of levels: 7)

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS sd(Intercept) 5.11 3.35 0.35 13.39 1.00 928 1367

Regression Coefficients:

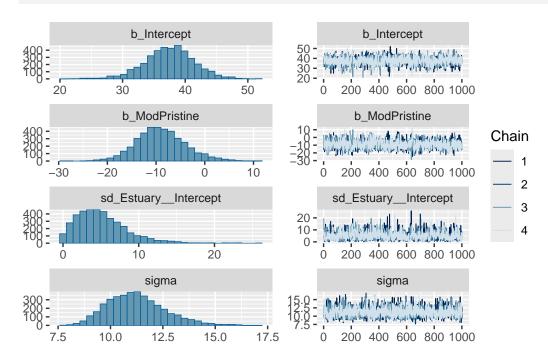
Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS Intercept 37.45 4.00 28.90 45.02 1.00 1485 1511 ModPristine -8.96 5.11 -18.45 1.91 1.00 1475 1761

Further Distributional Parameters:

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS sigma 11.24 1.39 8.90 14.29 1.00 2437 2535

Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

plot(fit.est.1)



If needed, fixed and random effects can be extracted with these functions:

```
fixef(fit.est.1)
```

```
Estimate Est.Error Q2.5 Q97.5 Intercept 37.44954 4.003155 28.89980 45.022357 ModPristine -8.96339 5.108531 -18.45213 1.912913
```

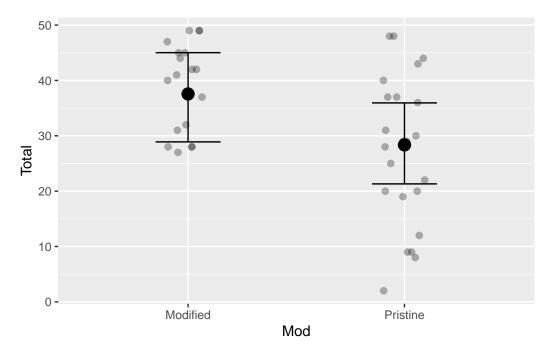
```
ranef(fit.est.1)
```

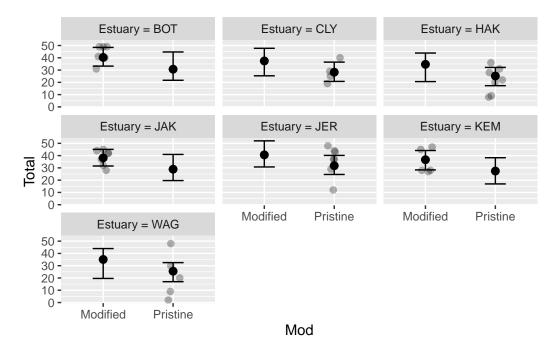
\$Estuary

, , Intercept

```
Estimate Est.Error Q2.5 Q97.5
BOT 2.9199439 4.401671 -4.001824 13.455701
CLY -0.1883263 4.088938 -8.995330 7.894171
HAK -3.4409207 4.343956 -13.633125 3.606532
JAK 0.7751533 4.044399 -7.270259 9.503657
JER 3.4372259 4.163375 -3.426794 13.033421
KEM -0.9766246 4.088095 -9.849672 7.344053
WAG -3.1842804 4.438557 -13.908306 3.926569
```

Conditional effects plots of fixed effects only (default, "population-level"), but by specifying re_formula=NULL and conditions, we can plot on group-level, too. We even get predictions (on group-level) of what would happen if we applied the modification to the estuary instead of keeping it pristine.





When computing predictions with fitted (deterministic part) or predict (deterministic & stochastic part), we can choose to include random effects (default), or fixed effects only with re_formula=NA.

In general, re_formula=NULL enforces random effects, re_formula=NA omits random effects.

```
fitted(fit.est.1) |> head()

Estimate Est.Error Q2.5 Q97.5
[1,] 38.22469 3.459319 31.5402 45.08605
[2,] 38.22469 3.459319 31.5402 45.08605
[3,] 38.22469 3.459319 31.5402 45.08605
[4,] 38.22469 3.459319 31.5402 45.08605
[5,] 38.22469 3.459319 31.5402 45.08605
[6,] 38.22469 3.459319 31.5402 45.08605
[6,] 38.22469 3.459319 31.5402 45.08605

fitted(fit.est.1, re_formula=NA) |> head()
```

```
Estimate Est.Error Q2.5 Q97.5 [1,] 37.44954 4.003155 28.8998 45.02236 [2,] 37.44954 4.003155 28.8998 45.02236 [3,] 37.44954 4.003155 28.8998 45.02236 [4,] 37.44954 4.003155 28.8998 45.02236 [5,] 37.44954 4.003155 28.8998 45.02236 [6,] 37.44954 4.003155 28.8998 45.02236
```

R2 0.2695999 0.104506 0.06138227 0.4586746

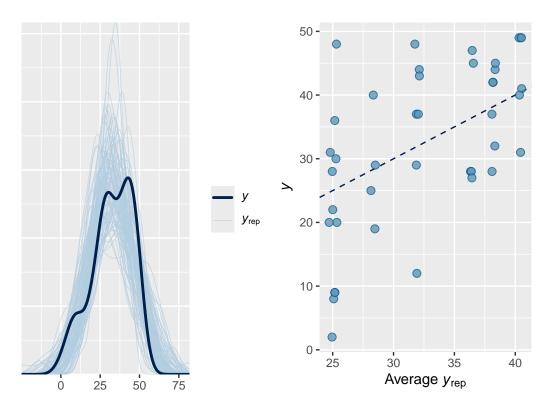
Finally, we check the model fit. Again, we can choose to use predictions with random effects (default) and compute the **conditional R2**, while without random effects (re_formula=NA) we compute the **marginal R2**.

```
bayes_R2(fit.est.1, re_formula=NA) # marginal
```

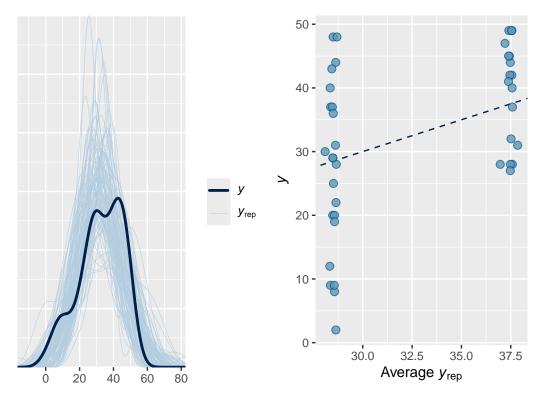
```
Estimate Est.Error Q2.5 Q97.5
R2 0.1543518 0.1097426 0.0007859223 0.3845651
```

Model checks use random effects per default, but can also be done with fixed effects only if required.

```
p1 = pp_check(fit.est.1, ndraws=100)
p2 = pp_check(fit.est.1, type="scatter_avg")
plot_grid(p1,p2)
```

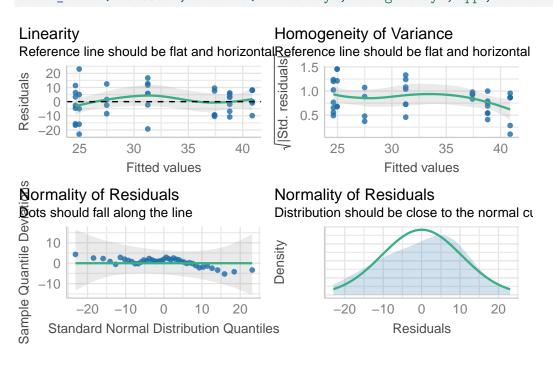


```
p1 = pp_check(fit.est.1, ndraws=100, re_formula=NA)
p2 = pp_check(fit.est.1, type="scatter_avg", re_formula=NA)
plot_grid(p1,p2)
```



Since this is a linear model, we can assess model assumptions with check_model()

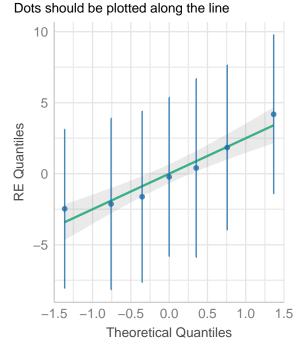
check_model(fit.est.1, check=c("linearity", "homogeneity", "qq", "normality"))



It also provides an additional check for normality of random effects

```
check_model(fit.est.1, check=c("reqq"))
```

Normality of Random Effects (Estuary)



The summary table already tells us that the difference between pristine and modified estuaries ModPristine is -8.96, 95% CI [-18.45,1.91]. Or we use the hypothesis function. Note that here we get 90% CIs. But Post.Prob is the quantity of interest here

hypothesis(fit.est.1, "ModPristine<0")</pre>

Hypothesis Tests for class b:

Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio Post.Prob Star 1 (ModPristine) < 0 -8.96 5.11 -16.83 -0.15 20.28 0.95 *

'CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

'*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI. Posterior probabilities of point hypotheses assume equal prior probabilities.

If we had fitted the model **without random intercepts** (complete pooling), the model would be overly confident in the Modified-Pristine difference (uncertainty is smaller here):

```
Estimate Est.Error Q2.5 Q97.5 Intercept 38.27533 2.653983 33.15225 43.339139 ModPristine -10.46960 3.453143 -17.11447 -3.830119
```

```
fixef(fit.est.1)
```

```
Estimate Est.Error Q2.5 Q97.5 Intercept 37.44954 4.003155 28.89980 45.022357 ModPristine -8.96339 5.108531 -18.45213 1.912913
```

Random intercepts ANCOVA

i = 1 ... N, Mod = 1, 2, Estuary = 1 ... 7

Now we add the continuous predictor Temperature.

Question: Is there still a difference between modified and pristine estuaries when controlling for temperature?

```
\begin{array}{ll} \text{Deterministic part:} & \mu_i = b(Mod_i) + c \cdot Temp + \delta(Estuary_i) \\ \text{Stochastic part:} & Total_i \sim \text{Normal}(\mu_i, \sigma) \\ \text{Hierarchical part:} & \delta_j \sim \text{Normal}(0, \sigma_{Est}) \end{array}
```

```
class
                  prior
                                                        group resp dpar nlpar lb ub
                                                 coef
                                                                                              sourc
                 (flat)
                                 b
                                                                                             defaul'
                 (flat)
                                 b
                                         ModPristine
                                                                                       (vectorized
                 (flat)
                                 b scaleTemperature
                                                                                       (vectorized
student_t(3, 32, 14.8) Intercept
                                                                                            defaul
 student_t(3, 0, 14.8)
                                                                                 0
                                                                                            defaul'
                                sd
 student_t(3, 0, 14.8)
                                                                                 0
                                                                                       (vectorized
                                sd
                                                      Estuary
 student_t(3, 0, 14.8)
                                                                                       (vectorized
                                sd
                                           Intercept Estuary
                                                                                 0
 student_t(3, 0, 14.8)
                                                                                 0
                                                                                             defaul<sup>-</sup>
                             sigma
```

We only need to specify a prior for the fixed effects, the effect of Modified and slope in Temperature (scaled). We choose a very weak prior for both.

Check convergence.

```
summary(fit.est.2)
```

Warning: There were 4 divergent transitions after warmup. Increasing adapt_delta above 0.8 m

```
Family: gaussian
```

Links: mu = identity; sigma = identity

Formula: Total ~ Mod + scale(Temperature) + (1 | Estuary)

Data: estuaries (Number of observations: 41)

Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;

total post-warmup draws = 4000

Multilevel Hyperparameters:

~Estuary (Number of levels: 7)

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS sd(Intercept) 3.35 2.79 0.15 10.27 1.00 931 1010

Regression Coefficients:

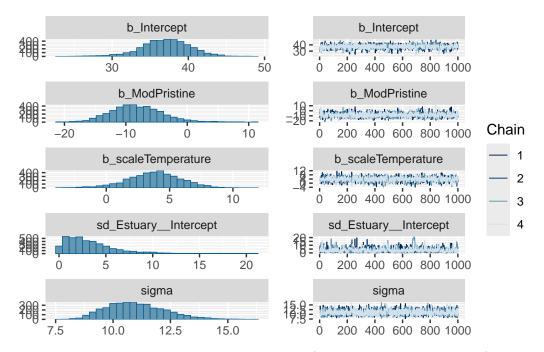
	Estimate	Est.Error	1-95% CI	u-95% C	Rhat	Bulk_ESS	Tail_ESS
Intercept	37.04	3.27	30.08	43.12	2 1.00	1527	1099
ModPristine	-8.21	4.24	-15.73	0.9	5 1.00	1442	892
scaleTemperature	3.79	2.12	-0.69	7.8	1.00	2209	1576

Further Distributional Parameters:

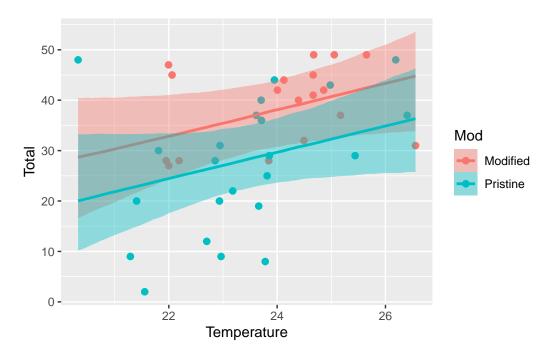
```
Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS sigma 11.00 1.28 8.88 13.80 1.00 3408 2981
```

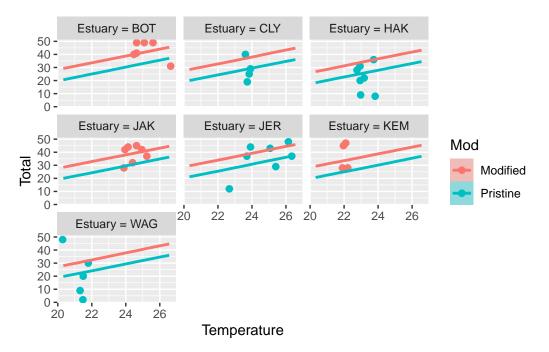
Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

plot(fit.est.2)



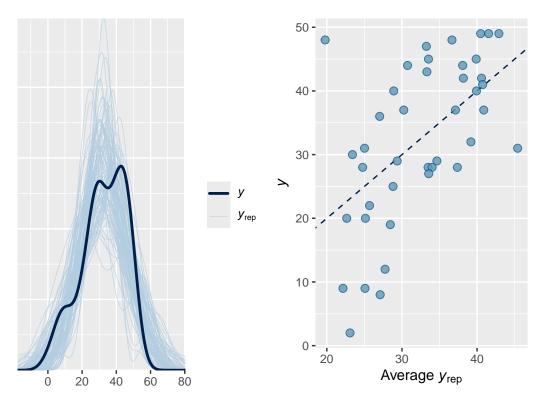
Conditional effects plots of fixed effects only (default, "population-level"), but by specifying re_formula and conditions, we can plot on group-level, too





Finally, we check the model fit

```
p1 = pp_check(fit.est.2, ndraws=100)
p2 = pp_check(fit.est.2, type="scatter_avg")
plot_grid(p1,p2)
```



There is only very weak support for the temperature model. Both models come to similar conclusions regarding Mod-Pristine difference in species richness.

L00(fit.est.1, fit.est.2)

elpd_diff se_diff

fit.est.2 0.0 0.0 fit.est.1 -0.5 2.3

hypothesis(fit.est.1, "ModPristine<0")</pre>

Hypothesis Tests for class b:

Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio Post.Prob Star 1 (ModPristine) < 0 -8.96 5.11 -16.83 -0.15 20.28 0.95 *

^{&#}x27;CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

^{&#}x27;*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI. Posterior probabilities of point hypotheses assume equal prior probabilities.

hypothesis(fit.est.2, "ModPristine<0")</pre>

Hypothesis Tests for class b:

```
Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio Post.Prob Star 1 (ModPristine) < 0 -8.21 4.24 -14.75 -1 28.2 0.97 *
```

Exercise

Also from Warton, D. (2022) Eco-Stats: Data Analysis in Ecology

Test the additional effect of outer vs inner (Zone) in this new dataset. Does the effect still hold when accounting for temperature?

```
data("estuaryZone")
table(estuaryZone$Estuary, estuaryZone$Mod, estuaryZone$Zone)
```

, , = Inner

	${\tt Modified}$	Pristine
BOT	6	0
\mathtt{CLY}	0	4
HAK	0	7
JAK	7	0
JER	0	7
KEM	5	0
WAG	0	6

, , = Outer

	Modified	Pristine
BOT	6	0
\mathtt{CLY}	0	5
HAK	0	7

^{&#}x27;CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

^{&#}x27;*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI. Posterior probabilities of point hypotheses assume equal prior probabilities.

```
JAK 4 0
JER 0 5
KEM 6 0
WAG 0 2
```

```
ID.complete = complete.cases(estuaryZone[, c("Total", "Mod", "Estuary", "Temperature", "Zone")])
estuaryZone = estuaryZone[ID.complete, ]
```

Without temperature

```
default_prior(Total ~ Mod+Zone+(1|Estuary), data=estuaryZone)
```

```
prior
                            class
                                         coef
                                                 group resp dpar nlpar lb ub
                                                                                     source
                (flat)
                                                                                    default
                                b
                (flat)
                                                                               (vectorized)
                                b ModPristine
                                                                               (vectorized)
                (flat)
                                    ZoneOuter
student_t(3, 37, 14.1) Intercept
                                                                                   default
student_t(3, 0, 14.1)
                                                                         0
                                                                                   default
student_t(3, 0, 14.1)
                                               Estuary
                                                                         0
                                                                              (vectorized)
                               sd
student_t(3, 0, 14.1)
                               sd
                                    Intercept Estuary
                                                                         0
                                                                               (vectorized)
student_t(3, 0, 14.1)
                                                                                    default
                            sigma
```

Check convergence

```
summary(fit.zone.1)
```

Warning: There were 5 divergent transitions after warmup. Increasing adapt_delta above 0.8 m

```
Family: gaussian
  Links: mu = identity; sigma = identity
Formula: Total ~ Mod + Zone + (1 | Estuary)
   Data: estuaryZone (Number of observations: 76)
Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
   total post-warmup draws = 4000
```

Multilevel Hyperparameters:

~Estuary (Number of levels: 7)

	Estimate	Est.Error	1-95% CI	u-95% C	I Rhat	Bulk_ESS	Tail_ESS
sd(Intercept)	2.40	1.92	0.09	7.4	3 1.00	1293	1393

Regression Coefficients:

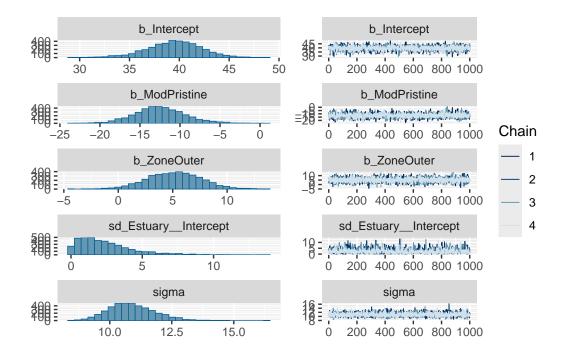
	Estimate	Est.Error	1-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
Intercept	39.47	2.76	33.52	44.67	1.00	1723	1390
${ t ModPristine}$	-12.47	3.28	-18.63	-5.51	1.00	1512	1237
ZoneOuter	5.15	2.50	0.21	10.11	1.00	3563	2572

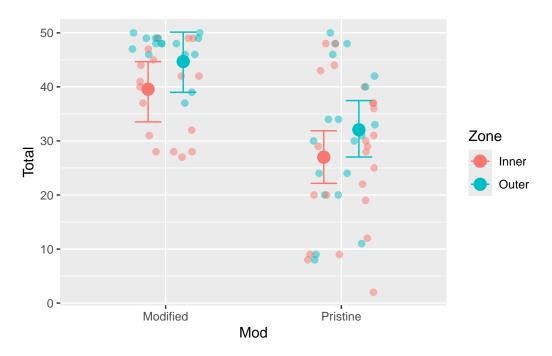
Further Distributional Parameters:

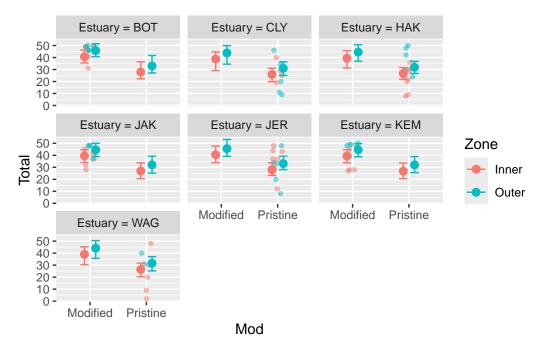
	Estimate	Est.Error	1-95% CI	u-95% (CI	Rhat	Bulk_ESS	Tail_ESS
sigma	10.88	0.93	9.25	12.8	83	1.00	3217	2467

Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

plot(fit.zone.1)







From the summary table we already have the information that there are on average +5.15 species more in the outer zone, but you can also check the hypothesis function.

Hypothesis Tests for class b:

Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio Post.Prob Star 1 (ZoneOuter) > 0 5.15 2.50 1.09 9.17 47.78 0.98 2 (ModPristine) < 0 -12.473.28 -17.69-6.89 799.00 1.00 *

With temperature

^{&#}x27;CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

^{&#}x27;*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI. Posterior probabilities of point hypotheses assume equal prior probabilities.

```
prior
                            class
                                                coef
                                                       group resp dpar nlpar lb ub
                                                                                           sourc
                 (flat)
                                b
                                                                                          defaul'
                 (flat)
                                b
                                        ModPristine
                                                                                     (vectorized
                                b scaleTemperature
                                                                                     (vectorized
                 (flat)
                 (flat)
                                b
                                          ZoneOuter
                                                                                     (vectorized
student_t(3, 37, 14.1) Intercept
                                                                                          defaul'
student_t(3, 0, 14.1)
                                                                               0
                                                                                          defaul:
student_t(3, 0, 14.1)
                               sd
                                                     Estuary
                                                                                     (vectorized
                                                                               0
                                                                                     (vectorized
student_t(3, 0, 14.1)
                               sd
                                          Intercept Estuary
student_t(3, 0, 14.1)
                            sigma
                                                                               0
                                                                                          defaul'
```

Here we got 19 divergent transitions while fitting, so it's time to increase MCMC accuracy with adapt_delta=0.9. Then, everything is fine:

Check convergence

```
summary(fit.zone.2)
 Family: gaussian
  Links: mu = identity; sigma = identity
Formula: Total ~ Mod + Zone + scale(Temperature) + (1 | Estuary)
   Data: estuaryZone (Number of observations: 76)
  Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
         total post-warmup draws = 4000
Multilevel Hyperparameters:
~Estuary (Number of levels: 7)
              Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
sd(Intercept)
                  2.09
                            1.81
                                      0.08
                                               6.53 1.00
                                                             1134
                                                                       1724
Regression Coefficients:
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
Intercept
                    36.04
                                2.99
                                        29.98
                                                 41.96 1.00
                                                                 2631
                                                                          2438
ModPristine
                   -10.76
                                3.16
                                       -16.90
                                                 -4.38 1.00
                                                                 2692
                                                                          1986
ZoneOuter
                    10.61
                                3.43
                                         3.66
                                                 17.27 1.00
                                                                 2983
                                                                          2300
```

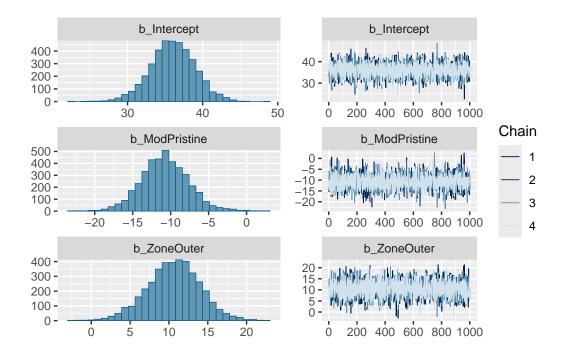
scaleTemperature 4.23 1.84 0.58 7.81 1.00 2878 2733

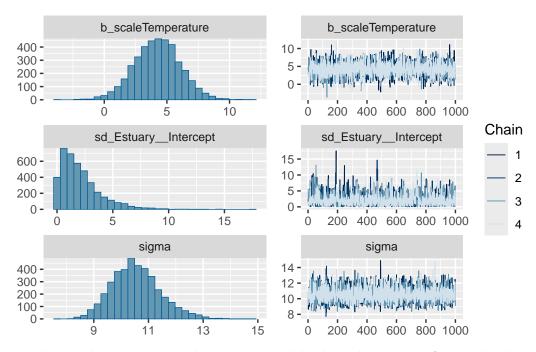
Further Distributional Parameters:

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS sigma 10.55 0.89 8.96 12.50 1.00 4920 3028

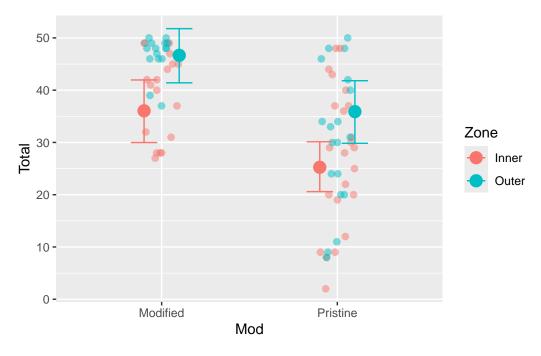
Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

plot(fit.zone.2)

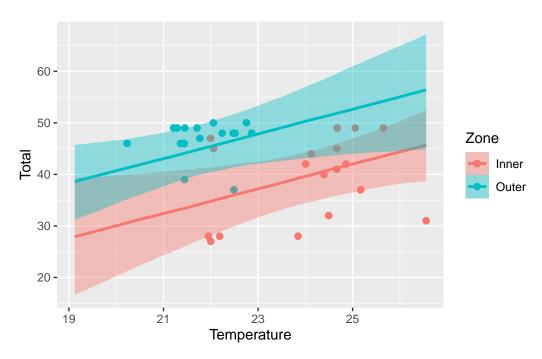




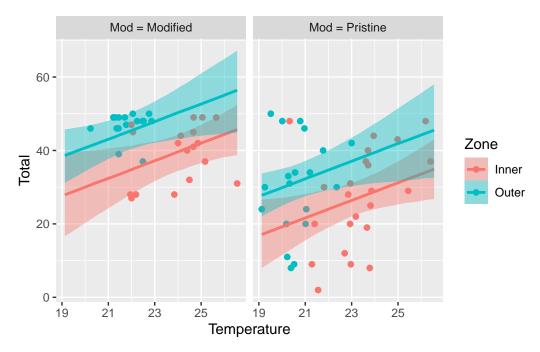
With 3 predictors, we can plot against 2 while the 3rd is at its reference level







Or we can plot against all 3



There is only very weak support for including temperature regarding predictive accuracy, but temperature effect is positive

LOO(fit.zone.1, fit.zone.2)

```
elpd_diff se_diff
fit.zone.2 0.0 0.0
fit.zone.1 -2.1 3.0
```

The direct effect of Zone is now 2x stronger when controlling for temperature! There are ~ 10 species more in the outer zone than in an inner zone of the same temperature. How can that happen??

```
fixef(fit.zone.1)
```

```
Estimate Est.Error Q2.5 Q97.5 Intercept 39.470272 2.757911 33.5211542 44.668288
```

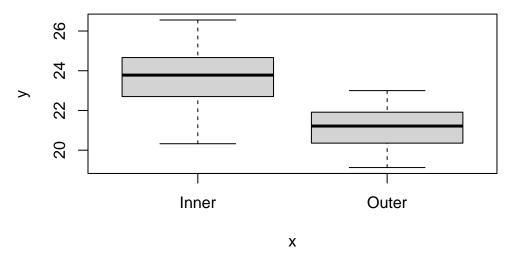
```
ModPristine -12.473993 3.275475 -18.6265579 -5.514716
ZoneOuter 5.151376 2.499280 0.2089617 10.108564
```

fixef(fit.zone.2)

```
Estimate Est.Error Q2.5 Q97.5 Intercept 36.04123 2.986821 29.9818478 41.958176 ModPristine -10.75982 3.156734 -16.8988015 -4.380493 ZoneOuter 10.60718 3.433391 3.6634936 17.270785 scaleTemperature 4.23131 1.838677 0.5823119 7.806587
```

However, inner zones are usually warmer, so this difference is a rather pointless prediction!

plot(estuaryZone\$Zone, estuaryZone\$Temperature)



If interested in a meaningful difference, compare predictions between inner & outer zone at their typical temperatures.

Hypothesis Tests for class :

```
Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio Post.Prob Star 1 (Inner)-(Outer) < 0 -5.85 2.41 -9.78 -1.88 94.24 0.99 *
```

'CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

'*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI. Posterior probabilities of point hypotheses assume equal prior probabilities.

This is much closer to the model without temperature, which actually would be sufficient here.

Hypothesis Tests for class b:

```
Hypothesis Estimate Est.Error CI.Lower CI.Upper Evid.Ratio Post.Prob Star
                                                       9.17
    (ZoneOuter) > 0
                         5.15
                                   2.50
                                             1.09
                                                                 47.78
                                                                             0.98
1
                                   3.28
                                                      -6.89
2 (ModPristine) < 0
                       -12.47
                                           -17.69
                                                                799.00
                                                                             1.00
```

'CI': 90%-CI for one-sided and 95%-CI for two-sided hypotheses.

'*': For one-sided hypotheses, the posterior probability exceeds 95%; for two-sided hypotheses, the value tested against lies outside the 95%-CI. Posterior probabilities of point hypotheses assume equal prior probabilities.

Be careful if predictors are correlated. Parameters only describe direct effect, meaning other predictors are held constant. Just looking at effect size, you might compare predictions which are very unlikely to occur in the data (Inner and Outer zone with same temperature).