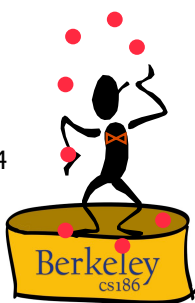


## Implementation of Relational Operations (Part 2)

R&G - Chapters 12 and 14



## An Alternative to Sorting: Hashing!

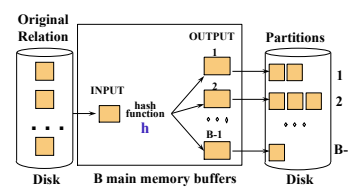
- Idea:
  - Many "sorting" tasks don't exploit the *order* of the sorted data
  - e.g.: removing duplicates in DISTINCT
  - e.g.: finding matches in JOIN
- Often good enough to match all tuples with equal values
- Hashing does this!
  - And may be cheaper than sorting! (Hmmm...!)
  - But how to do it for data sets bigger than memory??

## General Idea

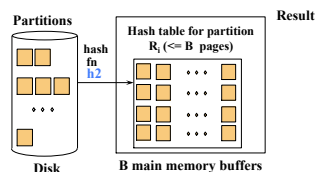
- Two phases (divide & conquer):
  - Partition:** use hash function  $h$  to split tuples into disk *partitions*.
    - Key property: all matches live in the same partition.
  - ReHash:** for each disk partition, build a main-memory hash table using hash function  $h_2$

## Two Phases

### Partition:

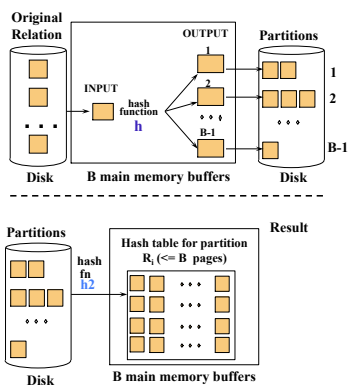


### Rehash:

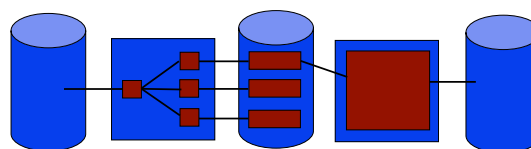


## Duplicate Elimination using Hashing

- read one bucket at a time
- for each group of identical tuples, output one



## Cost of External Hashing



$$\text{cost} = 4 \cdot [R] \text{ IO's}$$



## Memory Requirement

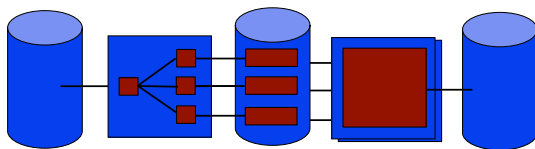
- How big of a table can we hash in two passes?
  - B-1 "partitions" result from Phase 0
  - Each should be no more than B pages in size
  - Answer:  $B(B-1)$ .
  - Said differently:*  
We can hash a table of size N pages in about  $\sqrt{N}$  space
  - Note: assumes hash function distributes records evenly!*
- Have a bigger table? **Recursive partitioning!**



How does this compare with  
external sorting?



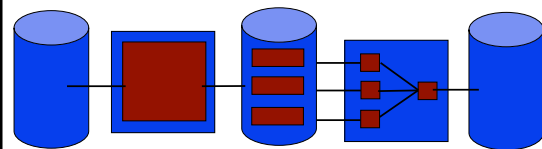
## Cost of External Sorting



cost =  $4 * [R]$  IO's



## Cost of External Hashing



cost =  $4 * [R]$  IO's



## Memory Requirement for External Sorting

- How big of a table can we sort in two passes?
  - Each "sorted run" after Phase 0 is of size B
  - Can merge up to B-1 sorted runs in Phase 1
  - Answer:  $B(B-1)$ .
  - Said differently:*  
We can sort a table of size N pages in about  $\sqrt{N}$  space
- Have a bigger table? **Additional merge passes!**



## So which is better ??

- Based on our simple analysis:
  - Same memory requirement for 2 passes
  - Same IO cost
- Digging deeper ...
- Sorting pros:**
  - Great if input already sorted (or *almost* sorted)
  - Great if need output to be sorted anyway
  - Not sensitive to "data skew" or "bad" hash functions
- Hashing pros:**
  - For duplicate elimination/grouping, scales with # of values
    - Not # of tuples!
  - Can exploit extra memory to reduce # IOs (*stay tuned...*)

Berkeley

before we optimize hashing further ...

**Q: Can we use hashing for JOIN ?**

Berkeley

### Hash Join

Do this for R.  
Then do it for S.

Build an R H.T.  
Stream S & probe.

Berkeley

### Cost of Hash Join

- Partitioning phase:** read+write both relations  
 $\Rightarrow 2([R]+[S])$  I/Os
- Matching phase:** read both relations, write output  
 $\Rightarrow [R]+[S] + [output]$  I/Os
- Total cost of 2-pass hash join =  $3([R]+[S])+[output]$

**Q: what is cost of 2-pass *sort-merge join*?**

**Q: how much memory needed for 2-pass *sort-merge join*?**

**Q: how much memory needed for 2-pass *hash join*?**

Berkeley

### An important optimization to hashing

- Have B memory buffers
- Want to hash relation of size N

If  $B < N < B^2$ , will have unused memory ...

Berkeley

### Hybrid Hashing

- Idea:** keep one of the hash buckets in memory!

**Q: how do we choose the value of k?**

Berkeley

### Cost reduction due to hybrid hashing

- Now:



## Summary: Hashing vs. Sorting

- Sorting pros:
  - Good if input already sorted, or need output sorted
  - Not sensitive to *data skew* or *bad hash functions*
- Hashing pros:
  - Often cheaper due to *hybrid hashing*
  - For join: # passes depends on size of *smaller* relation
  - For dup-elim/grouping, depends # of values, not #tuples