Tree-Structured Indexes

R & G Chapter 10

"If I had eight hours to chop down a tree, I'd spend six sharpening my ax."

Abraham Lincoln



Review: Files, Pages, Records

- Abstraction of stored data is "files" with "pages" of "records".
 - Records live on pages
 - Physical Record ID (RID) = <page#, slot#>
- Variable length data requires more sophisticated structures for records and pages. (why?)
 - Fields in Records: offset array in header
- Records on Pages: Slotted pages w/internal offsets & free space area
- Often best to be "lazy" about issues such as free space management, exact ordering, etc. (why?)
- Files can be unordered (heap), sorted, or kinda sorted (i.e., 'clustered") on a search key.
 - Tradeoffs are update/maintenance cost vs. speed of accesses via the search key.
 - Files can be clustered (sorted) at most one way.
- Indexes can be used to speed up many kinds of accesses. (i.e., "access paths")

Tree-Structured Indexes: Introduction

- Selections of form field <op> constant
- Equality selections (op is =)

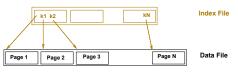
 Either "tree" or "hash" indexes help here.
- Range selections (op is one of <, >, <=, >=, BETWEEN)
 - "Hash" indexes don't work for these
- More complex selections (e.g. spatial containment)
 - There are fancier trees that can do this...
- Tree-structured indexing techniques support both range selections
- *ISAM*: static structure; early index technology.
- B+ tree: dynamic, adjusts gracefully under inserts and deletes.
- ISAM = Indexed Sequential Access Method

A Note of Caution

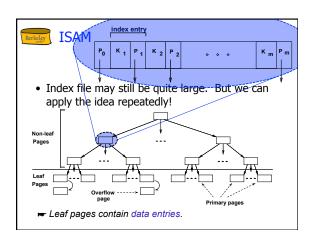
- · ISAM is an old-fashioned idea
 - B+-trees are usually better, as we'll see
 - Though not always
- But, it's a good place to start
 - Simpler than B+-tree, many of the same ideas
- Upshot
 - Don't brag about ISAM on your resume
 - **Do** understand ISAM, and tradeoffs with B+-trees

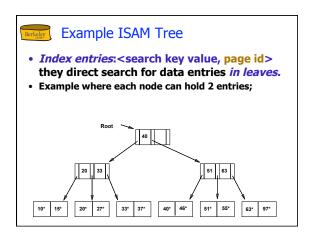
Range Searches

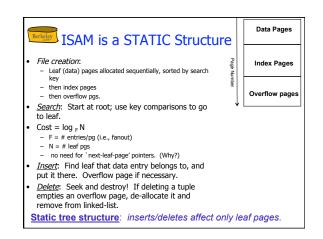
- ``Find all students with gpa > 3.0"
 - If data is in sorted file, do binary search to find first such student, then scan to find others.
 - Cost of binary search in a database can be quite high. Q: Why???
- Simple idea: Create an `index' file.

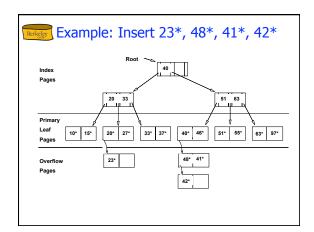


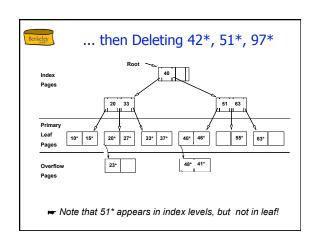
► Can do binary search on (smaller) index file!

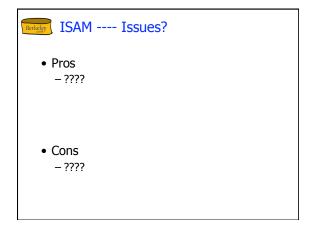


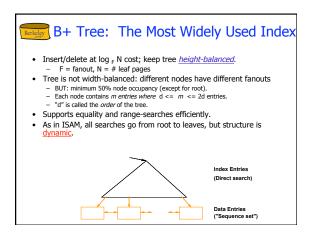






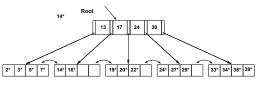






Example B+ Tree

- Search begins at root, and key comparisons direct it to a leaf (as in ISAM).
- Search for 5*, 15*, all data entries >= 24* ...



➡ Based on the search for 15*, we know it is not in the tree.

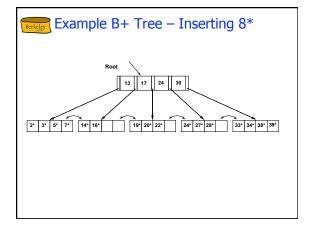
B+ Trees in Practice

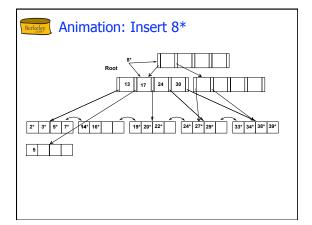
- Typical order: 100. Typical fill-factor: 67%.
 - average fanout = 133
- Typical capacities:
 - Height 2: $133^3 = 2,352,637$ entries
 - Height 3: $133^4 = 312,900,700$ entries
- Can often hold top levels in buffer pool:
 - Level 1 = 1 page = 8 Kbytes
 - Level 2 = 133 pages = 1 Mbyte
 - Level 3 = 17,689 pages = 133 MBytes

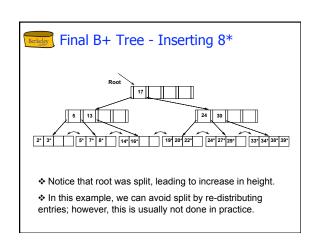


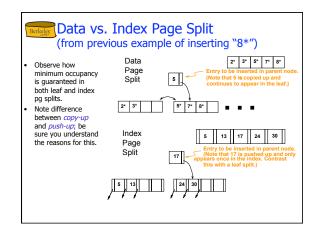
Inserting a Data Entry into a B+ Tree

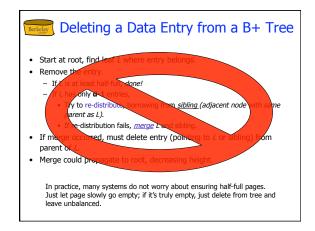
- Find correct leaf L.
- Put data entry onto L.
- If L has enough space, done!
 - Else, must <u>split</u> L (into L and a new node L2)
 - Redistribute entries evenly, copy up middle key.
 - Insert index entry pointing to L2 into parent of L.
- · This can happen recursively
 - To split index node, redistribute entries evenly, but <u>push up</u> middle key. (Contrast with leaf splits.)
- Splits "grow" tree; root split increases height.
 - Tree growth: gets <u>wider</u> or <u>one level taller at top.</u>

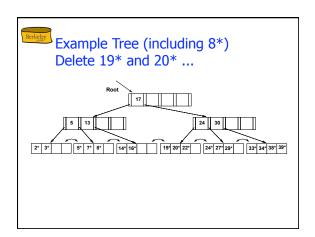


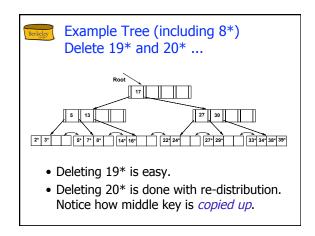


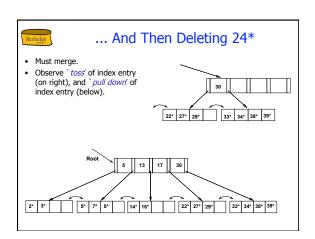


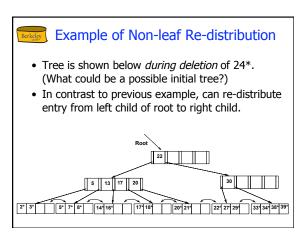








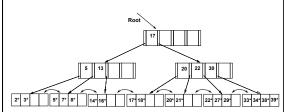






After Re-distribution

- Intuitively, entries are re-distributed by `pushing through' the splitting entry in the parent node.
- It suffices to re-distribute index entry with key 20; we've re-distributed 17 as well for illustration.





Prefix Key Compression

- Important to increase fan-out. (Why?)
- Key values in index entries just' direct traffic'; can often compress them.
 - E.g., If we have adjacent index entries with search key values Dannon Yogurt, David Smith and Devarakonda Murthy, we can abbreviate David Smith to Dav. (The other keys can be compressed too ...)
 - Is this correct? It depends on the leaves. What if there is a data entry Davey Jones? (Can only compress David Smith to Davi)
 - In general, while compressing, must leave each index entry greater than every key value (in any descendant leaf) to its left.
- Insert/delete must be suitably modified.



Suffix Key Compression

- If many index entries share a common prefix
 - E.g. MacDonald, MacEnroe, MacFeeley
 - Store the common prefix "Mac" at a well known location on the page, use suffixes as split keys
- Particularly useful for composite keys - Why?



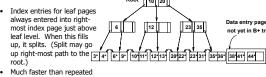
Bulk Loading of a B+ Tree

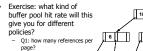
- Given: large collection of records
- Desire: B+ tree on some field
- Bad idea: repeatedly insert records
- Slow, and poor leaf space utilization . Why?
- **Bulk Loading** can be done much more efficiently.
- Initialization: Sort all data entries, insert pointer to first (leaf) page in a new (root) page

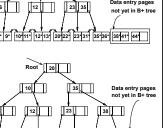




Bulk Loading (Contd.)







3* 4* 6* 9* 10*11* 12*13* 20*22* 23*31* 35*36* 38*41* 44*

Summary of Bulk Loading

- Option 1: multiple inserts.
 - Slow.
 - Does not give sequential storage of leaves.
- Option 2: Bulk Loading
 - Fewer I/Os during build.
 - Leaves will be stored sequentially (and linked, of course).
 - Can control "fill factor" on pages.



A Note on `Order'

- Order (d) makes little sense with variable-length entries
- Use a physical criterion in practice (`at least half-full').
 - Index pages often hold many more entries than leaf pages.
 - Variable sized records and search keys:
 - · different nodes have different numbers of entries.
- Even with fixed length fields, Alternative (3) gives variable length
- Many real systems are even sloppier than this --- only reclaim space when a page is *completely* empty.

Berkeley Summary

- Tree-structured indexes are ideal for range-searches, also good for equality searches.
- ISAM is a static structure.
 - Only leaf pages modified; overflow pages needed.
 - Overflow chains can degrade performance unless size of data set and data distribution stay constant.
- B+ tree is a dynamic structure.
 - Inserts/deletes leave tree height-balanced; log _F N cost.
 - High fanout (**F**) means depth rarely more than 3 or 4.
 - Almost always better than maintaining a sorted file.
 - Typically, 67% occupancy on average.
 - Usually preferable to ISAM; adjusts to growth gracefully.
 - If data entries are data records, splits can change rids!



Summary (Contd.)

- Key compression increases fanout, reduces height.
- Bulk loading can be much faster than repeated inserts for creating a B+ tree on a large data set.
- B+ tree widely used because of its versatility.
 - One of the most optimized components of a DBMS.