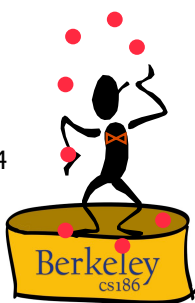


Implementation of Relational Operations (Part 2)

R&G - Chapters 12 and 14



An Alternative to Sorting: Hashing!

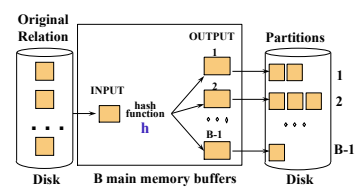
- Idea:
 - Many "sorting" tasks don't exploit the *order* of the sorted data
 - e.g.: removing duplicates in DISTINCT
 - e.g.: finding matches in JOIN
- Often good enough to match all tuples with equal values
- Hashing does this!
 - And may be cheaper than sorting! (Hmmm...!)
 - But how to do it for data sets bigger than memory??

General Idea

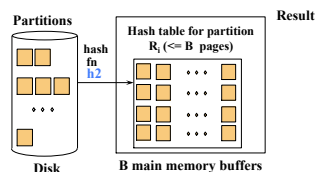
- Two phases:
 - Partition**: use hash function h to split tuples into disk *partitions*.
 - Key property: all matches live in the same partition.
 - ReHash**: for each disk partition, build a main-memory hash table using hash function h_2

Two Phases

Partition:

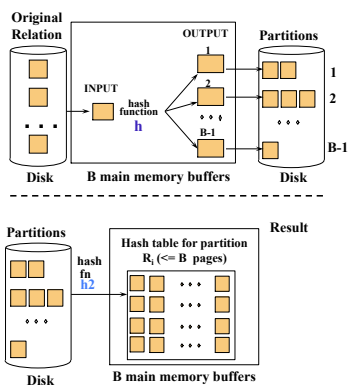


Rehash:

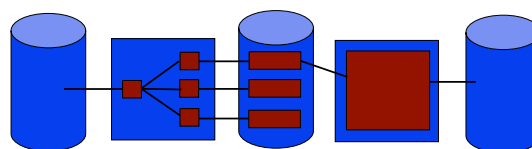


Duplicate Elimination using Hashing

- read one bucket at a time
- for each group of identical tuples, output one



Cost of External Hashing



$$\text{cost} = 4 * [R] \text{ IO's}$$



Memory Requirement

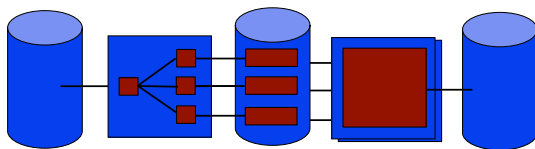
- How big of a table can we hash in two passes?
 - B-1 "partitions" result from Phase 0
 - Each should be no more than B pages in size
 - Answer: $B(B-1)$.
 - Said differently:*
We can hash a table of size N pages in about \sqrt{N} space
 - Note: assumes hash function distributes records evenly!*
- Have a bigger table? **Recursive partitioning!**



How does this compare with
external sorting?



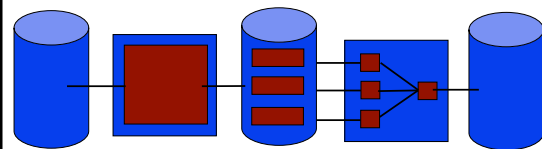
Cost of External Sorting



cost = $4*[R]$ IO's



Cost of External Sorting



cost = $4*[R]$ IO's



Memory Requirement for External Sorting

- How big of a table can we sort in two passes?
 - Each "sorted run" after Phase 0 is of size B
 - Can merge up to B-1 sorted runs in Phase 1
 - Answer: $B(B-1)$.
 - Said differently:*
We can sort a table of size N pages in about \sqrt{N} space
- Have a bigger table? **Additional merge passes!**



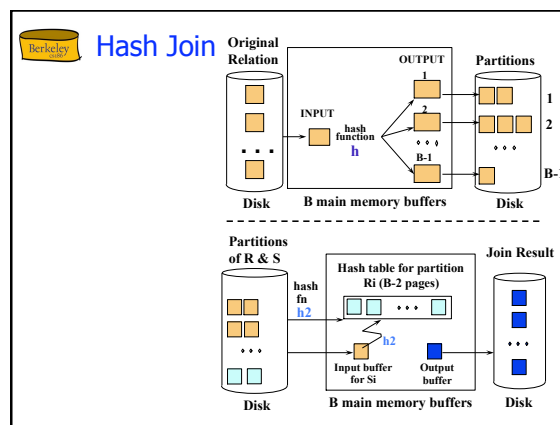
So which is better ??

- Based on our simple analysis:
 - Same memory requirement for 2 passes
 - Same IO cost
- Digging deeper ...
- Sorting pros:**
 - Great if input already sorted (or *almost* sorted)
 - Great if need output to be sorted anyway
 - Not sensitive to "data skew" or "bad" hash functions
- Hashing pros:**
 - For duplicate elimination/grouping, scales with # of values
 - Not # of tuples!
 - Can exploit extra memory to reduce # IOs (*stay tuned...*)

Berkeley

before we optimize hashing further ...

Q: Can we use hashing for JOIN ?



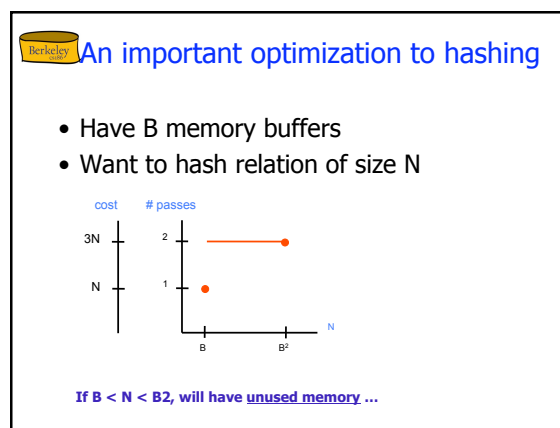
Berkeley **Cost of Hash Join**

- Partitioning phase:** read+write both relations
 $\Rightarrow 2([R] + [S])$ I/Os
- Matching phase:** read both relations, write output
 $\Rightarrow [R] + [S] + [\text{output}]$ I/Os
- Total cost of 2-pass hash join = $3([R] + [S]) + [\text{output}]$

Q: what is cost of 2-pass *sort join*?

Q: how much memory needed for 2-pass *sort join*?

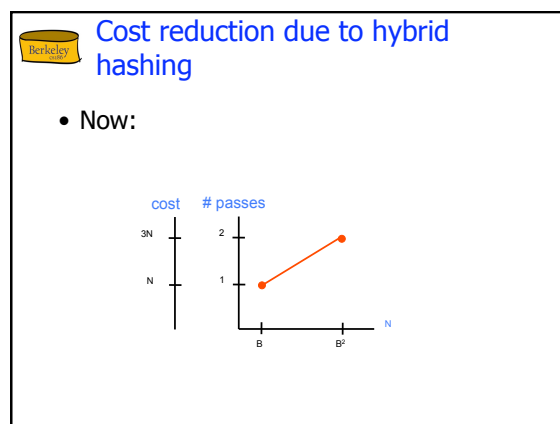
Q: how much memory needed for 2-pass *hash join*?



Berkeley **Hybrid Hashing**

- Idea:** keep one of the hash buckets in memory!

Q: how do we choose the value of k?





Summary: Hashing vs. Sorting

- Sorting pros:
 - Good if input already sorted, or need output sorted
 - Not sensitive to *data skew* or *bad hash functions*
- Hashing pros:
 - Often cheaper due to *hybrid hashing*
 - For join: # passes depends on size of *smaller* relation
 - For dup-elim/grouping, depends # of values, not #tuples