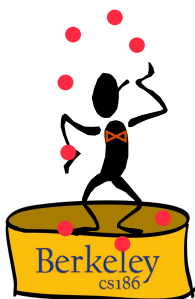


Implementation of Relational Operations

R&G - Chapters 12 and 14



Introduction

- Next topic: QUERY PROCESSING
- Some database operations are EXPENSIVE
- Huge performance gainst by being "smart"
 - We'll see 1,000,000x over naive approach
- Main weapons are:
 - clever implementation techniques for operators
 - exploiting relational algebra "equivalences"
 - using statistics and cost models to choose



Simple SQL Refresher

```
· SELECT <list-of-fields>
  FROM <list-of-tables>
  WHERE <condition>
```

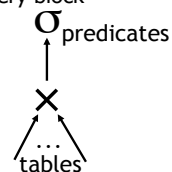
```
SELECT S.name, E.cid
FROM Students S, Enrolled E
WHERE S.sid=E.sid AND E.grade='A'
```



A Really Bad Query Optimizer

- For each Select-From-Where query block

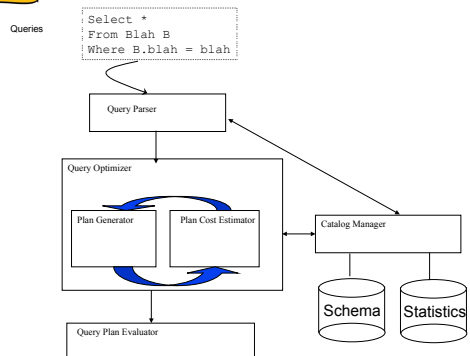
- Create a plan that:
 - Forms the cross product of the FROM clause
 - Applies the WHERE clause



- (Then, as needed:
 - Apply the GROUP BY clause
 - Apply the HAVING clause
 - Apply any projections and output expressions
 - Apply duplicate elimination and/or ORDER BY)



Cost-based Query Sub-System



The Query Optimization Game

- Goal is to pick a "good" plan
 - Good = low expected cost, under *cost model*
 - Degrees of freedom:
 - [access methods](#)
 - [physical operators](#)
 - [operator orders](#)
- Roadmap for this topic:
 - *First*: implementing individual operators
 - *Then*: optimizing multiple operators

Relational Operations

- We will consider how to implement:
 - Selection (σ) Select a subset of rows.
 - Projection (π) Remove unwanted columns.
 - Join (\bowtie) Combine two relations.
 - Set-difference ($-$) Tuples in reln. 1, but not in reln. 2.
 - Union (\cup) Tuples in reln. 1 and in reln. 2.
- Q: What about Intersection?

Schema for Examples

Sailors (sid: integer, sname: string, rating: integer, age: real)
 Reserves (sid: integer, bid: integer, day: dates, rname: string)

- Sailors:
 - Each tuple is 50 bytes long, 80 tuples per page, 500 pages.
 - $[S]=500, p_S=80$.
- Reserves:
 - Each tuple is 40 bytes, 100 tuples per page, 1000 pages.
 - $[R]=1000, p_R=100$.

Simple Selections

```
SELECT *
FROM Reserves R
WHERE R.rname < 'C%'
```

$$\sigma_{R.attr op value}(R)$$

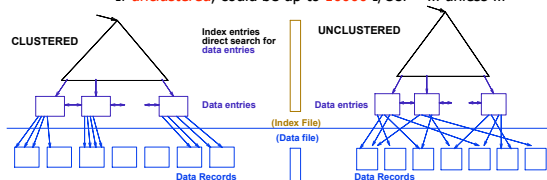
- How best to perform? Depends on:
 - what indexes are available
 - expected size of result
- Size of result approximated as
 - $(size\ of\ R) * selectivity$
 - $selectivity$ estimated via statistics – we will discuss shortly.

Our options ...

- If no appropriate index exists:
 Must scan the whole relation
 $cost = [R]$. For "reserves" = 1000 I/Os.

Our options ...

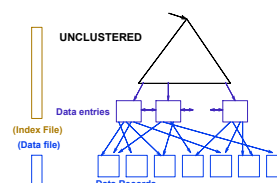
- With index on selection attribute:
 - Use index to find qualifying data entries
 - Retrieve corresponding data records
- Total cost = cost of step 1 + cost of step 2
- For "reserves", if selectivity = 10% (100 pages, 10000 tuples):
 - If **clustered** index, cost is a little over 100 I/Os;
 - If **unclustered**, could be up to 10000 I/Os! ... unless ...



Refinement for unclustered indexes

- Find qualifying data entries.
- Sort the rid's of the data records to be retrieved.
- Fetch rids in order.

Each data page is looked at just once (though # of such pages likely to be higher than with clustering).





General Selection Conditions

- $(day < 8/9/94 \text{ AND } rname = 'Paul') \text{ OR } bid = 5 \text{ OR } sid = 3$
- First, convert to conjunctive normal form (CNF):
 - $(day < 8/9/94 \text{ OR } bid = 5 \text{ OR } sid = 3) \text{ AND } (rname = 'Paul' \text{ OR } bid = 5 \text{ OR } sid = 3)$
- We only discuss the case with no ORs
- Terminology:
 - A **B-tree** index matches terms that involve only attributes in a prefix of the search key. e.g.:
 - Index on $\langle a, b, c \rangle$ matches $a=5 \text{ AND } b=3$, but not $b=3$.



2 Approaches to General Selections

Approach I:

1. Find the cheapest access path
 2. retrieve tuples using it
 3. Apply any remaining terms that don't match the index
- Cheapest access path: An index or file scan that we estimate will require the fewest page I/Os.



Cheapest Access Path - Example

query: $day < 8/9/94 \text{ AND } bid = 5 \text{ AND } sid = 3$

some options:

*B+tree index on day; check bid=5 and sid=3 afterward.
hash index on <bid, sid>; check day<8/9/94 afterward.*

- How about a B+tree on $\langle rname, day \rangle$?
- How about a B+tree on $\langle day, rname \rangle$?
- How about a Hash index on $\langle day, rname \rangle$?



2 Approaches to General Selections

Approach II: use 2 or more matching indexes.

1. From each index, get set of rids
2. Compute intersection of rid sets
3. Retrieve records for rids in intersection
4. Apply any remaining terms

EXAMPLE: $day < 8/9/94 \text{ AND } bid = 5 \text{ AND } sid = 3$

Suppose we have an index on *day*, and another index on *sid*.

- Get rids of records satisfying $day < 8/9/94$.
- Also get rids of records satisfying $sid = 3$.
- Find intersection, then retrieve records, then check $bid = 5$.



Projection

```
SELECT DISTINCT
      R.sid, R.bid
FROM   Reserves R
```

- Issue is removing duplicates.
- Use sorting!!
 1. Scan R, extract only the needed attributes
 2. Sort the resulting set
 3. Remove adjacent duplicates

Cost:

Ramakrishnan/Gehrke writes to temp table at each step!

Reserves with size ratio 0.25 = 250 pages.

With 20 buffer pages can sort in 2 passes, so:

$$1000 + 250 + 2 * 2 * 250 + 250 = 2500 \text{ I/Os}$$



Projection -- improved

- Avoid the temp files, work on the fly:
 - Modify Pass 0 of sort to eliminate unwanted fields.
 - Modify Passes 1+ to eliminate duplicates.

Cost:

Reserves with size ratio 0.25 = 250 pages.

With 20 buffer pages can sort in 2 passes, so:

1. Read 1000 pages
2. Write 250 (in runs of 40 pages each) = 7 runs
3. Read and merge runs (20 buffers, so 1 merge pass!)

$$\text{Total cost} = 1000 + 250 + 250 = 1500.$$



Other Projection Tricks

If an index search key contains all wanted attrs:

- Do *index-only* scan
 - Apply projection techniques to data entries (*much smaller!*)

If a B+Tree index search key *prefix* has all wanted attrs:

- Do *in-order index-only* scan
 - Compare adjacent tuples on the fly (*no sorting required!!*)



Joins

```
SELECT *
FROM   Reserves R1, Sailors S1
WHERE  R1.sid=S1.sid
```

- Joins are very common.
- $R \times S$ is large; so, $R \times S$ followed by a selection is inefficient.
- Many approaches to reduce join cost.
- Join techniques we will cover today:
 - Nested-loops join
 - Index-nested loops join
 - Sort-merge join



Simple Nested Loops Join

```
R ⋈ S:  foreach tuple r in R do
        foreach tuple s in S do
            if r_i == s_j then add <r, s> to result
```

Cost = $(p_R * [R]) * [S] + [R] = 100 * 1000 * 500 + 1000$ IOs
 – At 10ms/IO, Total time: ???

- What if smaller relation (S) was “outer”?
- What assumptions are being made here?
- What is cost if one relation can fit entirely in memory?



Page-Oriented Nested Loops Join

```
R ⋈ S:  foreach page b_R in R do
        foreach page b_S in S do
            foreach tuple r in b_R do
                foreach tuple s in b_S do
                    if r_i == s_j then add <r, s> to result
```

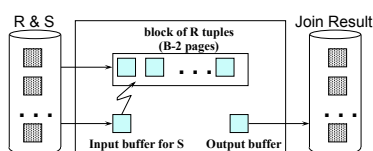
Cost = $[R] * [S] + [R] = 1000 * 500 + 1000$

- If smaller relation (S) is outer, cost = $500 * 1000 + 500$
- Much better than naïve per-tuple approach!



Block Nested Loops Join

- Page-oriented NL doesn't exploit extra buffers :(
- Idea to use memory efficiently:

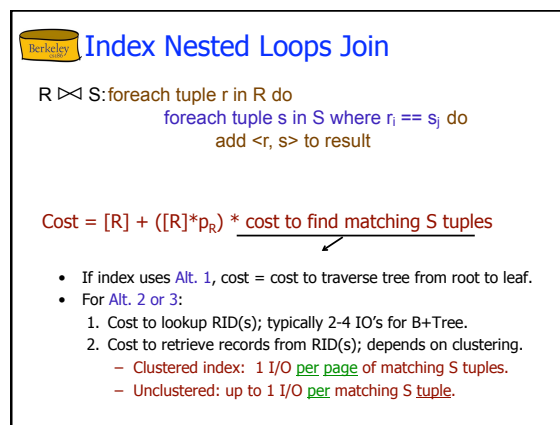
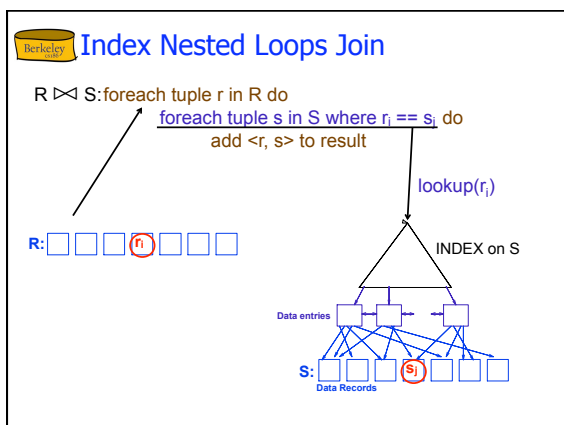


Cost: Scan outer + (#outer blocks * scan inner)
 $\#outer\ blocks = \lceil \#of\ pages\ of\ outer / blocksize \rceil$



Examples of Block Nested Loops Join

- Say we have $B = 100 + 2$ memory buffers
- Join cost = [outer] + (#outer blocks * [inner])
 $\#outer\ blocks = [outer] / 100$
- With R as outer ($[R] = 1000$):
 - Scanning R costs 1000 IO's (*done in 10 blocks*)
 - Per block of R, we scan S; costs $10 * 500$ IO's
 - Total = $1000 + 10 * 500$.
- With S as outer ($[S] = 500$):
 - Scanning S costs 500 IO's (*done in 5 blocks*)
 - Per block of S, we scan R; costs $5 * 1000$ IO's
 - Total = $500 + 5 * 1000$.



Reminder: Schema for Examples

Sailors (sid: integer, sname: string, rating: integer, age: real)
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Sort-Merge Join

- Sort R on join attr(s)
- Sort S on join attr(s)
- Scan sorted- R and sorted- S in tandem, to find matches

Example:

```
SELECT *
FROM   Reserves R1, Sailors S1
WHERE  R1.sid=S1.sid
```

sid	sname	rating	age	sid	bid	day	rname
28	dustin	7	45.0	28	103	12/4/96	guppy
28	yuppy	9	35.0	28	103	11/3/96	yuppy
31	lubber	8	55.5	31	101	10/10/96	dustin
44	guppy	5	35.0	31	102	10/12/96	lubber
58	rusty	10	35.0	31	101	10/11/96	lubber
				58	103	11/12/96	dustin

Cost of Sort-Merge Join

- Cost: Sort R + Sort S + $([R]+[S])$
 - But in worst case, last term could be $[R]*[S]$ (very unlikely!)
 - Q: what is worst case?

Suppose $B = 35$ buffer pages:

- Both R and S can be sorted in 2 passes
- Total join cost = $4*1000 + 4*500 + (1000 + 500) = 7500$

Suppose $B = 300$ buffer pages:

- Again, both R and S sorted in 2 passes
- Total join cost = 7500

Block-Nested-Loop cost = 2500 ... 15,000

Other Considerations ...

- An important refinement:

Do the join during the final merging pass of sort!

 - If have enough memory, can do:
 - Read R and write out sorted runs
 - Read S and write out sorted runs
 - Merge R -runs and S -runs, while finding $R \bowtie S$ matches

Cost = $3*[R] + 3*[S]$

Q: how much memory is "enough" (will answer next time ...)
- Sort-merge join an especially good choice if:
 - one or both inputs are already sorted on join attribute(s)
 - output is required to be sorted on join attributes(s)

Q: how to take these savings into account? (stay tuned ...)



Summary

- A virtue of relational DBMSs:
 - queries are composed of a few basic operators
 - The implementation of these operators can be carefully tuned
- Many alternative implementation techniques for each operator
 - No universally superior technique for most operators.
- Must consider available alternatives
 - Called "Query optimization" -- we will study this topic soon!