



- Query has the form:  $\{T \mid p(T)\}$ 
  - **p(T)** is a **formula** containing **T**
- Answer = tuples T for which p(T) = true.



• Atomic formulae:

 $T \in Relation$ 

T.a op T.b

T.a op constant

... *op* is one of <,>,=,≤,≥,≠

- A formula can be:
  - an atomic formula
  - $\neg p, p \land q, p \lor q, p \Rightarrow q$
  - $-\exists R(p(R))$
  - $\forall R(p(R))$



- Quantifiers: ∃ and ∀
- Use of  $\exists X$  or  $\forall X$  binds X.
  - A variable that is not bound is free.
- Recall our definition of a query:
  - $-\{T\mid p(T)\}$
- Important restriction:
  - -T must be the *only* free variable in p(T).
  - $-\,\mbox{all}$  other variables must be bound using a quantifier.

## Simple Queries

• Find all sailors with rating above 7

 $\{S \mid S \in Sailors \land S.rating > 7\}$ 

• Find names and ages of sailors with rating above 7.

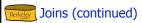
 $\{S \mid \exists S1 \in Sailors(S1.rating > 7 \land S.sname = S1.sname \land S.age = S1.age)\}$ 

– Note: S is a variable of 2 fields (i.e. S is a projection of Sailors)



Find sailors rated > 7 who've reserved boat #103

 $\{S \mid S \in Sailors \land S.rating > 7 \land \exists R(R \in Reserves \land R.sid = S.sid \land R.bid = 103) \}$ 



Find sailors rated > 7 who've reserved a red boat

```
\{S \mid S \in Sailors \land S.rating > 7 \land \exists R(R \in Reserves \land R.sid = S.sid \land \exists B(B \in Boats \land B.bid = R.bid \land B.color = 'red')) \}
```

 This may look cumbersome, but it's not so different from SQL!

```
Universal Quantification
```

Find sailors who've reserved all boats

```
{ S | S∈Sailors ∧
∀B∈Boats (∃R∈Reserves

(S.sid = R.sid
∧ B.bid = R.bid)) }
```



Find sailors who've reserved all Red boats

```
{S | S∈Sailors ∧

∀B ∈ Boats (B.color = 'red' ⇒

∃R(R∈Reserves ∧ S.sid = R.sid

∧ B.bid = R.bid)) }

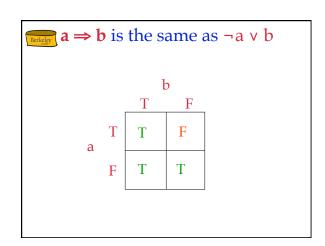
Alternatively...

{S | S∈Sailors ∧

∀B ∈ Boats (B.color ≠ 'red' ∨

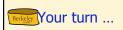
∃R(R∈Reserves ∧ S.sid = R.sid

∧ B.bid = R.bid)) }
```





- 3 syntactically correct calculus queries that have an infinite number of answers! *Unsafe* queries.
  - e.g.,  $|S| |S \in Sailors|$
  - Solution???? Don't do that!



w/thanks to Chris Olston, Yahoo Research former CS186 student and former CS186 instructor!

• Schema:

Movie(<u>title</u>, year, studioName) ActsIn(<u>movieTitle</u>, <u>starName</u>) Star(<u>name</u>, gender, birthdate, salary)

- Queries to write in Relational Calculus:
  - 1. Find all movies by Paramount studio
  - 2. ... movies whose stars are all women
  - 3. ... movies starring Kevin Bacon
  - 4. Find stars who have been in a film w/Kevin Bacon
  - 5. Stars within six degrees of Kevin Bacon\*
  - 6. Stars connected to K. Bacon via any number of films\*\*

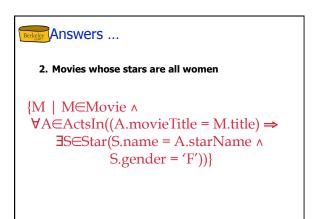
\* Try two degrees for starters

\* Good luck with this one!



1. Find all movies by Paramount studio

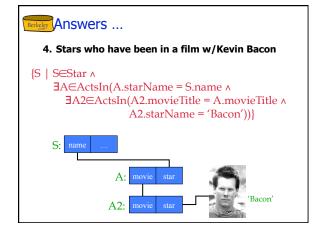
{M | M∈Movie ∧ M.studioName = 'Paramount'}

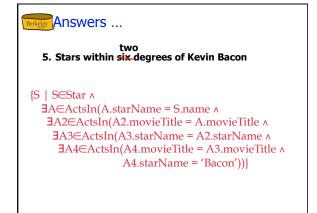


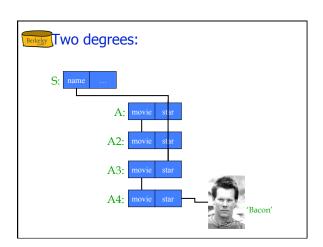
## Answers ...

3. Movies starring Kevin Bacon

 $\{M \mid M \subseteq Movie \land \\ \exists A \subseteq ActsIn(A.movie Title = M.title \land \\ A.starName = 'Bacon'))\}$ 









- 6. Stars connected to K. Bacon via <u>any number</u> of films
- Sorry ... that was a trick question
  - Not expressible in relational calculus!!
- What about in relational algebra?
  - We will be able to answer this question shortly ...

## Expressive Power

- Expressive Power (Theorem due to Codd):
  - Every query that can be expressed in relational algebra can be expressed as a safe query in relational calculus; the converse is also true.
- Relational Completeness:

Query language (e.g., SQL) can express every query that is expressible in relational algebra/calculus.

(actually, SQL is more powerful, as we will see...)



## Question:

- Can we express query #6 in relational algebra?
- A: If we could, then by Codd's theorem we could also express it in relational calculus.
   However, we know the latter is not possible, so the answer is no.

But it is expressible as a recursive query in Datalog ... or SQL!



- Formal query languages simple and powerful.
  - Relational algebra is operational
    - used as internal representation for query evaluation plans.
  - Relational calculus is "declarative"
    - query = "what you want", not "how to compute it"
  - Same expressive power
    - --> relational completeness.
- Several ways of expressing a given query
  - a *query optimizer* should choose the most efficient version.