BigTangle Whitepaper

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Abstract

BigTangle is a protocol for the internet of value. It is a cryptocurrency network extending existing directed acyclic graph architectures with MCMC as consensus algorithm. Through the use of industry-grade big data technology in conjunction with its parallelizable architecture, BigTangle is a successor to Bitcoin that can fulfill economically important key use-cases. Proof-of-Work mining and custom token self-issuances are supported. Key Features: Ease of Use, Completely Feeless, Real-Time Confirmation, Infinite Scalability, Permissionless, Trustless, Decentralized, Distributed Proof of Work and Quantum Security.

I. Introduction

Since the inception of Bitcoin in 2009 [1], new cryptocurrencies have been rising in popularity and are predicted to potentially rise to rival fiat currencies in the future. Transitioning to such a digital currency offers various advantages, of which the authors believe the infrastructure cost savings in the financial sector from revolutionizing highly complex and opaque traditional transaction systems of current banking and stock market technologies to be the most attractive.

To achieve this attractivity, two key properties are required: scalability and the absence of fees in general. Additionally, low transaction confirmation times, ease of use, security and anonymity are other baseline properties required for widespread adoption. Traditional Proof-of-Work-based blockchain approaches fail to meet these requirements [5], while Proof-of-Stake-based approaches [19] might face other problems such as voter politics, mining regulation etc.

In this paper we propose BigTangle, a scalable Proof-of-Work-based cryptocurrency as a protocol for the internet of value. The proposed solution's architecture is a directed acyclic graph (DAG) generalization of blockchains with MCMC as consensus algorithm [2] that is capable of scaling to infinite transactions per second while remaining feeless. The recently popularized DAG architectures [2][6][7] have the potential to scale beyond traditional blockchains and avoid problems of blockchains such as block forks [14] and scalability issues[5].

BigTangle supports all features supported by Bitcoin, including but not limited to escrow transactions, bonded contracts, third-party arbitration, multiparty signatures and its stack language Script in general. The Bitcoin blockchain is a special case in BigTangle's DAG architecture. Using the mining reward process detailed later, it is possible to change the BigTangle's parameters to return to a conventional blockchain.

In contrast to most recent high performance cryptocurrencies, BigTangle employs a Proof-of-Work-based mining process where in principle every transaction is rewarded and helps securing the network. This mining process incentivises users to run full nodes and secure the network, providing advantages such as inflationary currency models and value through economic coupling

to the real world. Full node operators and miners are therefore compensated with a time-normalized amount of new BigTangle tokens proportional to their mining contribution.

BigTangle is a successor to Bitcoin that focuses on a variety of economically important key use-cases: Beyond the decentralization of payment processing, the network can be used as a base service layer for the decentralization of markets in general, transfer and ownership management, authenticity proofs for assets of any kind or supply chains and ownership management as it has been described in as early as 1998 [24].

For this reason, the protocol includes various block types with different important use cases in mind. For example, the token issuance and virtual OS blocks are an extension of the DAG architecture that cover additional smart contract use cases.

In the authors' opinion, a transaction system capable of supporting the global transaction volume of banks and stock markets requires sufficiently performant computer clusters to work as full nodes. BigTangle will therefore employ established industrial grade big data technologies such as Apache Kafka, Spark and its GraphX API.

By utilizing local approximations to previously non-scalable graph computations of the asynchronous Tangle in addition to big data computation technologies, the proposed solution suffices the properties mentioned above.

Minimal end-user client requirements are a side effect, allowing end-users to participate and issue transactions without having to store and handle huge amounts of data but instead providing hashing power.

II. OVERVIEW

The protocol maintains a public ledger of transactions that are contained within blocks. In contrast to blockchain-based solutions, blocks reference and thereby approve two previous blocks and indirectly their predecessors to form a directed acyclic graph. A more detailed explanation of the base architecture and other important existing concepts can be found in [2].

As per protocol, a set of blocks is valid if all contained blocks are valid per se and no conflicts exist between any of the contained blocks. When issuing new blocks, it is to be made sure that the approved set of blocks is valid. Contributing blocks therefore helps securing and validating BigTangle by approving all referenced blocks and thereby increasing their confirmation level.

Participants are connected in a standard peer-to-peer network via a gossip protocol as fall-back solution. In addition to that, BigTangle will employ Apache Kafka data streaming to achieve superior scalability and propagation speed. Network participants are split into two different archetypes: clients and network nodes. Generic end-users and small-time miners can participate as clients that issue transactions with the aid of a network node, using their hashing power to create blocks and solve the low-difficulty Proof-of-Work themselves, while network nodes maintain a copy of the graph and provide validated tip pairs to build upon.

The network nodes can derive account balances and transaction states from the graph and provide the maintained states to clients in exchange for e.g. hashing power. Furthermore, a network node operator might choose to also participate in the mining process himself. This consists of using available computational power to solve Proof-of-Works for new blocks.

The server-side validation as described in [2] can be effectively computed by utilizing approximations. The network nodes create their own local view of the Tangle by maintaining helper constructs such as locally confirmed block snapshots called milestones. Validation is then performed based on this snapshot. The consequence is that additional validity constraints are checked over the naive Tangle validity constraints, resulting in a stricter validity evaluation than without this approximation. Additional information can be found in chapter 3.

General properties provided by BigTangle are high hashing power and time-normalized inflation due to mining, infinite scalability, sufficiently fast transaction confirmation times, full decentralization, trustlessness and permissionlessness, feeless transactions and in-principle quantum security. To make use of these properties, BigTangle will natively support custom token issuances, smart contracts and decentralized token exchanges, in turn enabling economically important use cases.

Popular solutions to scalable cryptocurrencies include highly complex sharding, voting-based and capital-based Proof-of-Stake or workarounds [5] with the potential for exorbitant fees. Instead, we propose a fully permissionless solution that returns to the well-known Proof of Work approach of the original Bitcoin solution.

Mining rewards serve as a network maintenance incentive instead of fees. Since it is impossible to allow every device to participate as network nodes while achieving infinite scalability without attempting highly complex sharding solutions, it is intended that network nodes are deployed in sufficiently big computer clusters utilizing state-of-the-art big data technology. Instead of end-users hosting full network nodes and requiring significant computational resources, their clients cooperate with network nodes by e.g. providing mining revenue and building blocks.

The network stays permissionless and avoids centralized constructs. As long as nodes fulfill the minimum requirements for keeping up with the transaction volume, any node can effectively participate in network validation and mining.

Independent from the mining process, it is intended for many full nodes to exist regardless of mining rewards. For example, super market chains or banks can deploy their own full nodes to process their big transaction volume themselves.

By utilizing Proof-of-Work, we can avoid drawbacks of Proof-of-Stake-based models such as political apathy, regulations and lower financial stability due to missing mining hardware investments.

III. Technical Details

In the following, we briefly discuss technical key details and their realization. For further information on established concepts, please refer to existing literature.

i. Implementation

To achieve high scalability, the node implementation is built upon Bitcoin [1] and employs industry standard big data technologies, including but not limited to Apache Kafka [28] and Spark GraphX [27][26].

ii. Cryptographic Components

BigTangle currently relies on elliptic curve cryptography for multi-use signatures. The curve used is Bitcoin's Secp256k1. Similarly, the public key hashes are also Base-58 encoded, allowing Bitcoin users to reuse their addresses in BigTangle. The proposed Proof-of-Work hashing function is the currently ASIC-resistant Equihash algorithm [3]. The base architecture is quantum resistant as shown in [2].

iii. Transactions and Accounts

The accounting is based on Bitcoin's Unspent Transaction Output (UTXO) model. Users can issue valid transactions as long as they can provide a valid input script for the used UTXOs. The UTXOs use Bitcoins Turing-incomplete stack language allowing for the same set of functionality as found in Bitcoin.

iv. DAG Architecture

As found in [2], we provide a short reasoning on why the Tangle base architecture as mentioned before is qualitatively stable and leads to short confirmation times even for extremely high block volumes.

The following assumptions are made: There exists a valid Poisson point process model for the incoming blocks with constant rate λ, an average block issuance time h, a stationary number of tips L_0, an idealized network latency of h such that any blocks issued at time t become visible as new tips at time $t + h$ and a tip selection in form of a uniform probability distribution over all current tips.

Since approximately λh invisible tips exist due to latency, an equal amount of tips must no longer be tips anymore due to stationarity. This means that the probability of choosing new tips is $r/(r + \lambda h)$ with the current amount of visible tips r. This leads to the mean of $2r/(r + \lambda h)$ tips chosen by a new block. Again, due to stationarity the mean must be equal to 1 such that the new tips replace the old tips without changing the average number of tips. This leads to $r = \lambda h$ or $L_0 = 2\lambda h$. Assuming L_0 to be large henceforth, this leads to an expected time until first approval of $L_0/(2\lambda) = h$.

Going further, there exists an average time until almost all new blocks approve a block that can be calculated as follows. At that point of time, the block can be considered locally confirmed due to the fact that most new blocks will approve the block.

Let $K(t)$ be the expected amount of approving tips at time t. Since the probability of a tip not being a tip after time h is the tip substitution rate $L_0/(2\lambda h) = 1/2$, at time t one half of $K(t - h)$ tips remain unapproved, while the other half is approved at least once. Let $\mathcal{A}$ be the set of tips from time $t - h$ that remain unapproved at time t and $\mathcal{B}$ the set of tips from time $t - h$ that were already approved at time t. Analogously to previous results, the probability p_1 that a new block approves at least 1 block from $\mathcal{B}$ and none from $\mathcal{A}$ such that K increases equals to

$$p_1 = \frac{K(t-h)^2}{2L_0} + \frac{K(t-h)}{L_0}\left(1 - \frac{K(t-h)}{2L_0}\right) \quad (1)$$

and the probability p_2 that a new block approves $\mathcal{B}$ twice such that K decreases is

$$p_2 = \frac{K(t-h)^2}{2L_0} \quad (2)$$

The differential equation for $K(t)$ follows: [9]

$$\dot{K}(t) = \lambda \cdot (p_1 - p_2)$$
$$= \lambda \cdot \frac{K(t-h)}{L_0}\left(2 - \frac{K(t-h)}{L_0}\right) \quad (3)$$

For $K(t)$ up to $\epsilon L_0 \ll L_0$ the quadratic term is dropped and with $\lambda h/L_0 = 1/2$ equation (3) is simplified to

$$\dot{K}(t) = \frac{K(t-h)}{2h} \quad (4)$$

With $K(0) = 1$ and $K(t) = e^{\frac{c}{h}t}$ it follows that

$$K(t) = e^{W(\frac{1}{2})\frac{t}{h}} \approx e^{0.352\frac{t}{h}} \quad (5)$$

with $W(\cdot)$ denoting the Lambert W function. The time t_0 until ϵL_0 is reached then evaluates to

$$t_0 \approx \frac{h}{W(\frac{1}{2})}\ln\frac{L_0}{\epsilon} \leq 2.84 \cdot h \ln L_0 \quad (6)$$

The time between $K(t)$ reaching ϵL_0 and approximately L_0 is negligible and the resulting time until confirmation of a block is given by (6). Remembering $L_0 = \lambda h$, this result shows that the confirmation time of this architecture

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scales logarithmically with the block rate such that even very high block rates have a negligible effect on confirmation time.

Although this has only been formally shown under some simplifying assumptions such as uniform tip selection probability and idealized network latency, it can be argued that the above at least qualitatively holds for MCMC approval strategies and real networks. Simulations have shown that the confirmation time for MCMC approval strategies follows the results shown above [11].

v.   Blocks

A block consists of its header and transactions. In addition to fields existing in Bitcoin, the header contains an additional reference to a previous block, a miner address, a type field for the types as seen below and additional data depending on their type. We list all base block types and their use:

Transfer Blocks contain transactions intended to transfer value from one owner to another.

Mining Reward Blocks contain mining reward transactions that are computed in a deterministic fashion. More on this in the mining process detailed later.

Token Issuance Blocks are used to issue custom tokens. Tokens are identified by address plus sequence number and issuances are legitimized by the corresponding private key signatures. They contain at least one issuance transaction of the corresponding token.

Cross Chain Blocks are used for interconnectivity between other blockchains. This enables the connectivity of other blockchain systems with BigTangle as found in other recent blockchains [25], enabling BigTangle to be able to include other chains.

Storage Blocks are used to store user data. User data is identified by address and usage is legitimized by the corresponding private key signatures and the user data can be encrypted. User data is treated as a value object and can be transferred and traded. The BigTangle Mainnet limits the size of the storage. We thereby create an application layer storage network based on pay for use.

Virtual OS Blocks (VOS) are used to create a virtual distributed Operation System for decentralized autonomous corporations, smart contracts and any other distributed applications similar to other alternative blockchains [21][22]. The distributed applications can be implemented in any modern language and are not limited to using specialized languages. The relevant code and state data is saved in the block as VM containers using technology such as Docker Composer [18] or Kubernetes Containers [15]. The execution of VOS blocks simply changes the state data and creates new blocks. As an example, the Mining Reward Process in BigTangle is implemented using this VOS and all nodes will execute the same computation for mining rewards based on the current data in BigTangle. As another example, the market exchange application is implemented in such a form that it requires only a single node for the execution. As the system provides the option to set n-m execution, there is a trade-off between trust, security and performance.

vi.   Participants

Participants can take on different roles in the network depending on their available resources and intentions. In the following, possible types of participation are ordered in descending requirements of bandwidth, space and computational power:

Full Nodes keep a copy of the full BigTangle. They can fully participate in the network and provide any requested blocks.

Pruned Nodes maintain a pruned version of BigTangle. Only the most recent blocks in terms of confirmation are kept in storage. The node can still fully participate in the mining process unless a highly unlikely reorganization event happens.

Clients do not keep a copy of BigTangle. They rely on the nodes to provide them with necessary information to create transactions and blocks. Clients solve proof of work for their issued blocks and can provide incentives for network nodes to assist them.

vii. Protocol Details

Node Maintenance
In the following, we briefly describe assorted technical details for preparing the Tangle base architecture to achieve scalable operation.

As mentioned before, the BigTangle node implementation locally maintains a snapshot called the milestone, a set of blocks it considers as locally confirmed and thereby in principle finalized. In addition, it maintains additional auxiliary information and block evaluations such as rating, cumulative weight, depth, height etc. as found in [2]. The milestone update process in simplified form consists of the following steps and is performed as often as possible:

1. Ingest new blocks such that an unbroken Tangle is obtained.

2. Update relevant block evaluations.

3. If needed, remove now unconfirmed blocks and dependents from milestone.

4. Find new locally confirmed blocks, resolve conflicts and add to milestone.

We consider as locally confirmed any block that has reached the upper confirmation threshold in terms of rating and is sufficiently deep. We also add a hysteresis to removing blocks to prevent unnecessary reorganizations due to the probabilistic nature of MCMC.

To ensure that the honest miners always find a consensus, we set the lower confirmation threshold to $t_{lower} = 2/3$ as shown in chapter 4. For stability purposes, we introduce a hysteresis by setting the upper confirmation threshold to $t_{upper} = 70\%$

Of particular note is the conflict resolution procedure. It should only find application in step 4 if malicious nodes approve conflicting block combinations such that conflicting blocks are considered locally confirmed. Nonetheless, this case must be handled correctly and the algorithm is also used in the tip selection algorithm. In short, we process conflicts in descending order of maximum rating occurring in the conflicts, eliminating all losing candidates by removing them and all their approvers or dependents from the milestone or candidate set.

Lastly, we may prune no longer relevant blocks and their evaluations to prevent Big-Tangle from growing indefinitely in terms of storage space. For example, blocks in the milestone and their conflicting counterparts could be pruned after reaching a combination of sufficient depth, age of confirmation etc.

Validation and Approval Selection
When generating a new block, we require two previous blocks to reference such that no conflict exists in the union of referenced blocks (such that they are valid). To find such conflict-free block pairs, we first apply an MCMC algorithm similar to the approach shown in [10] to find single tips. We then resolve conflicts according to the conflict resolution procedure detailed before and reverse on the path taken by MCMC until a block consistent with the milestone is found. Finally, we repeat an analogous conflict resolution procedure for a pair of obtained blocks, resulting in two blocks that are conflict free and consistent with the current local milestone.

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It is important to note that since we use the milestone as a shortcut to evaluating validity of new combinations of unconfirmed blocks, the validation overhead stays approximately constant over time under the assumption of constant transaction influx. This coupled with a suitable pruning strategy allows us to avoid increasingly long back-tracing to the genesis block and enables scalability.

A simple example is shown in figure 1. Consider the validation of the black block. Instead of taking the set of all directly or indirectly approved blocks and validating this set, we only take the difference to the milestone (in this example all cyan and black blocks) and then validate this small set against the current milestone. This results in a scalable validity computation.

Note that the milestone block marked with an 'x' is not in the set of directly or indirectly approved blocks but is now also being validated against, meaning that this validation scheme approximates the naive Tangle validity definition by adding additional validation constraints. However, these additional constraints do not affect the validation in a negative way, since any milestone blocks are considered locally confirmed and conflicting blocks should not be approved by any new blocks and thus should not be selected.

In the case of other blocks conflicting with a current milestone block achieving higher rating than the milestone blocks, they and, if applicable, their approvers would simply be included instead of the previous milestone blocks.

Mining Process
To incentivise node operation and network maintenance, we introduce a mining process quite similar to the Bitcoin mining process. Since the BigTangle is an asynchronous network and every node sees a different version of the BigTangle, we cannot simply reward what is seen locally since we require an ap-
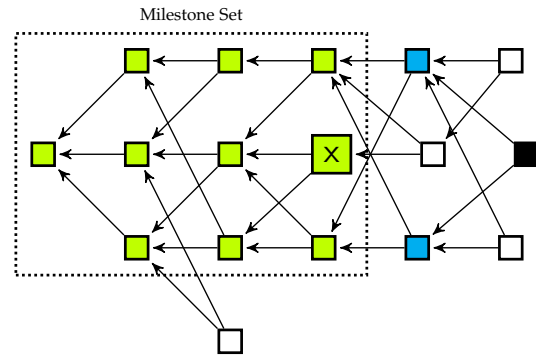

Figure 1: *Example for Validation
(black block: block to validate,
lime blocks: milestone blocks,
white blocks: irrelevant unconfirmed blocks,
cyan blocks: to validate vs. milestone,
x: additionally confirmed over naive scheme)*

proximately fixed inflation rate. Instead, we introduce a fix point such that every node can calculate the same rewards in a deterministic manner.

We divide blocks by height intervals and issue mining reward blocks to reward intervals. All blocks referenced by the mining reward blocks in the respective interval are considered for compensation and the mining reward block must therefore be in conflict with other such blocks of the same reward height interval.

Using only the blocks approved by the mining reward block, we can compute consistent rewards in a deterministic fashion since we know the referenced subgraph to be unbroken in order for the mining reward block to be considered for confirmation. The calculation of rewards is then done locally. As an example, refer to figure 2 where the red dotted box contains potential reward candidates.

A key problem is deciding on a method to approve mining reward blocks that are consistent and fair according to the nodes local BigTangle state. The solution is to use
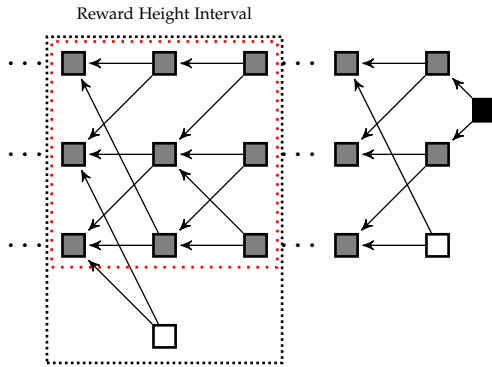
Reward Height Interval

Figure 2: *Example for Mining Process
(black block: considered reward block,
gray blocks: used in reward calculation,
white blocks: not used in calculation,
red outline: reward candidates)*

the following validity constraints for mining reward blocks: All of the approved blocks in the specified height interval must be in the milestone and most of the milestone blocks in the specified height interval must be referenced at the time of reward block reception. To prevent deadlocks due to local inconsistencies however, we must also allow this constraint to be overridden by e.g. sufficient rating and age, as in that case the rest of the network has accepted the block as valid.

Additionally, we must include counter-measures against non-validating miners' attacks. We punish the blocks with the lowest cumulative weight of their specific height as seen from the reward block's point view, since attackers will pursue a suboptimal tip selection algorithm to avoid validating new blocks and gain less cumulative weight. In the example from figure 2, this amounts to calculating cumulative weights for the candidates based on the mining reward block's (black) approved blocks (gray).

Finally, a per-transaction reward for the next interval is calculated analogously to Bitcoin's difficulty adjustment: By enforcing a monotonous increase of block timestamps and limiting the validity of timestamps from

the future, the per-transaction reward is adjusted according to the current transaction rate to enforce an approximately constant coin emission rate.

Token Issuance Process
The token issuance process enables a variety of important use cases for the internet of value and supports features as proposed in [23]. We legitimize a new token issuance block by signing their transactions with the token's corresponding multiple private keys. A token is identified by its ID in form of a public key hash and sequence number.

The issuances can be configured to e.g. disallow further issuances and enforce other custom token rules. Any issuances following another issuance must adhere to the previous issuance's defined rules, e.g. multi-signature checks: the created tokens must be signed by the given number of keys to spent the tokens. The tokens can then be used analogous to BigTangle's system currency.

IV. Attack Mitigation

In the following, we examine a few new attack vectors due to the milestone process. For generic Tangle attack vectors such as double spends, please refer to [2]. We assume that at least two-thirds of the blocks are made by honest miners and validate correctly. For up to one-third of malicious hashing power, we assume that while hashing power does not directly correlate with hijacked rating tips, less than one-third of the rating is hijacked by the attackers for most of the relevant blocks since only one-third of the cumulative weight can be hijacked. Further mitigation can be provided by using low-pass filters during rating calculation.

- In case percentage p of rating tips maliciously approve double spends, we must ensure that no reorganization occurs, meaning that the lower confirmation threshold must be below $(1 - p)$.

• In case percentage p of rating tips maliciously approve a conflict, we must ensure that no network split occurs, meaning that the lower confirmation threshold must be above $(\frac{1-p}{2} + p)$ to prevent the network from having conflicting blocks between their milestones due to a network split where up to 50% of honest miners plus malicious miners would not come to the same consensus as the other honest miners.

The maximum percentage for which such a lower confirmation threshold exists is $p = 1/3$. The corresponding lower confirmation threshold that follows from the equations is therefore $t_{lower} = 2/3$.

Other attacks include parallelizing Proof-of-Work to accumulate the highest cumulative weight and in turn gaining more rewards, which is mitigated by the probabilistic nature of MCMC as well as network latency and milestone update rate in general being slower than Proof-of-Work computations.

Not validating any transactions runs the risk of building invalid blocks, while building your own subgraph by approving your own blocks only will lead to high orphaning risk due to introducing more than the optimal amount of transitions on your approved blocks.

Trying to relink a pre-built subgraph of higher height to circumvent gaining less cumulative weight is mitigated by heavily penalizing high height difference transition probabilities.

V. PRACTICAL USE CASES

As mentioned before, projected practical use cases that the token derives its value from include the substitution of various currently costly and trust-based technical processes. In the following, the use cases are briefly explored.

i. Payment

A simple and important use case is payment processing. By providing scalable infrastructure, BigTangle enables the global transaction volume to be processed in one network. Most importantly, this offers infrastructural cost advantages by eliminating complex and costly processes of traditional payment processing for banks, companies and the general populace.

Note that the network hashing power is approximately proportional to the BigTangle internal token market cap and is therefore decoupled from actual transaction volumes, theoretically resulting in downwards unbounded energy upkeep at the cost of increased confirmation times for constant economic risk. Adequate confirmation times at a global scale can be achieved [2].

ii. Fiat Money

The token issuance protocol can be used to issue bank-backed tokens denoting conventional fiat money. Since the issuance and usage requires no participation in the network, BigTangle is a low cost solution for all parties. Fiat money transactions can then feasibly be processed within seconds on a global scale.

iii. Stock Markets

Markets for stocks, bonds etc. can easily be realized by creating new token equivalents. Companies can publish stocks and use the BigTangle network, essentially substituting costly stock exchange processes by the feeless BigTangle processing network.

Examples for the largest segments that will be affected: Bonds, Swaps, Derivatives, Commodities, Unregistered/Registered securities, Over-the-counter markets, Collateral management, Syndicated loans, Warehouse receipts, Repurchase markets etc.

iv. Micro Transactions

Service fees can now be charged in microdollar range or alternatively via seconds of hashing power due to the departure from winner-takes-it-all, allowing for new business models, e.g. online newspapers with alternatives to commercial advertisement.

v. Supply Chain

Assuming suppliers issuing authenticity tokens, it is trivial to track product authenticity via token transfers. This use case extends into classic supply chain management, allowing the trustless tracking of inventories in supply chains.

VI. Future Investigations

i. Privacy

There are a multitude of arguments for and against private transactions. Regardless, private transactions are an interesting extension to BigTangle and will be investigated after release.

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