

# Midterm Project Applied Analytics

Group 10

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# Outline

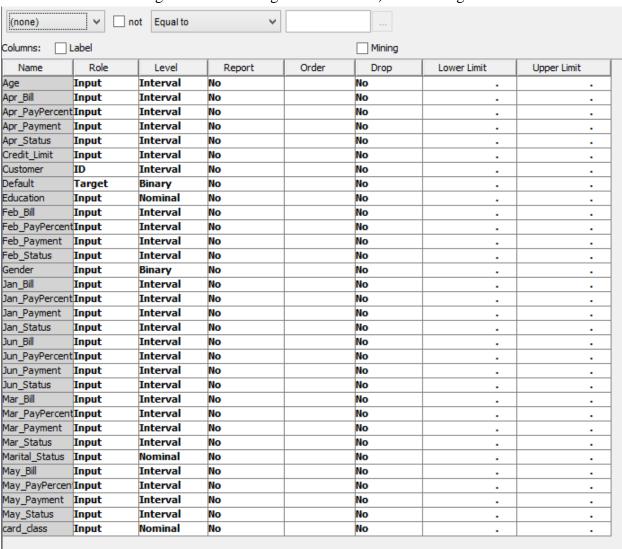
| 1. | Problem statement and Approach used |
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| 2. | Model fitting and assessment        |
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## **Problem Statement**

A data set consisting of 30,000 bank records of credit card customers was provided and the target is to predict whether the customer defaults on credit card balance or not based on the data related to the customer providing his/her education, age, monthly bill, marital status etc.

# **Data Preprocessing**

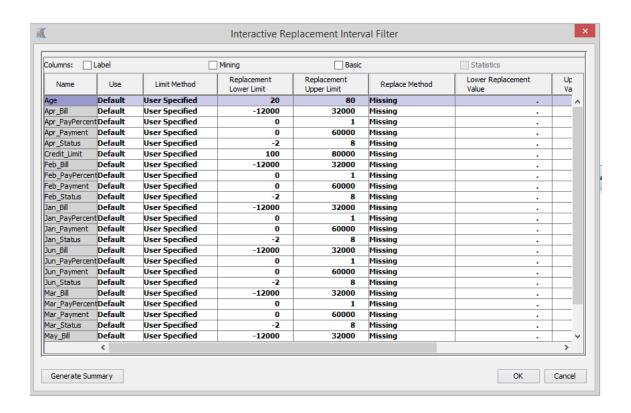
The dataset had 13607 values including NA, outlier (data dictionary was referred to set the limits for interval attributes and categories for the categorical attributes) and missing values.



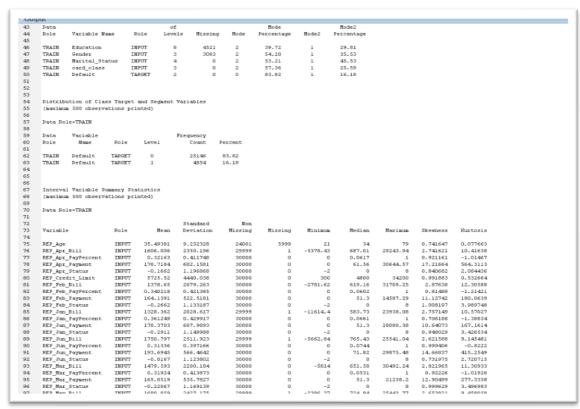
#### 

http://localhost:8888/notebooks/Midterm\_656.ipynb#

|      |   | Midterm_656                           |
|------|---|---------------------------------------|
| 4521 | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 5999 | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 1   |                                       |
| 0    | 1   |                                       |
| 0    | 1   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 1   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
| 0    | 0   |                                       |
|      | 0<br>0<br>0<br>5999<br>0<br>0<br>0<br>0<br>0<br>0<br>0<br>0<br>0<br>0<br>0<br>0 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 |

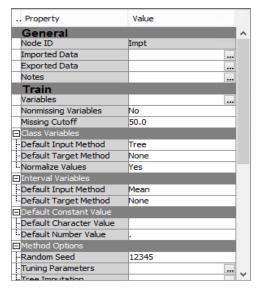


# Output after the replacement

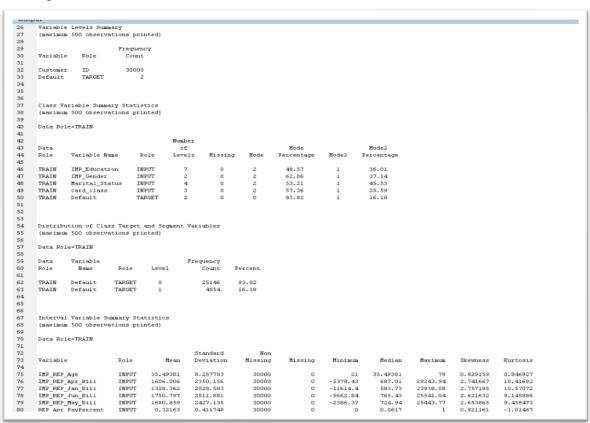


All of these were replaced with missing values and finally those missing values were imputed by the following method

In SAS EM, <u>tree imputation method</u> was used for class variables and <u>mean imputation method</u> Interval variables



# Imputation Output:



In Python, mean values were imputed for the interval attributes and mode values were imputed for the missing nominal attributes. After data cleaning and imputation, scaling of the interval attributes was done since the range of all the interval attributes are varying. This is done to make sure efficient running of Neural networks and to avoid any possible flaws in the feature selection techniques. Categorical attributes were encoded in Python by replacing each categorical value with <u>one hot encoding</u>.

| Re     | epiacea, im          | puted and End         | oded Data         |             |             |          |
|--------|----------------------|-----------------------|-------------------|-------------|-------------|----------|
|        | 100                  | Credit_Limit          | Jun_Status        | May_Status  | Apr_Status  | Mar_Sta  |
|        | B \                  | 1 121002              | 1 -04-64          | 00340       | 0 606663    | 0        |
| 599    |                      | -1.131883             | 1.794564          | 1.782348    | -0.696663   | -0.666   |
| 746    |                      | -0.366111             | -0.874991         | 1.782348    | 0.138865    | 0.188    |
| 2 -    | -0.180901            | -0.591338             | 0.014861          | 0.111736    | 0.138865    | 0.188    |
|        | 0.182399             | -0.906656             | 0.014861          | 0.111736    | 0.138865    | 0.188    |
|        | 2.604397             | -0.906656             | -0.874991         | 0.111736    | -0.696663   | 0.188    |
| 746    | 5                    |                       |                   |             |             |          |
| ,      | Feb_Status           | Jan_Status            | Jun_Bill M        | ay_Bill     | Ed          | ucationl |
| 0      | •                    | -1.486041             | -0.643742 -0      | .648829     |             | 0.0      |
| 1      | 0.234917             | 1.992316              | -0.660503 -0      | .668231     |             | 0.0      |
| 2      | 0.234917             | 0.253137              | -0.298915 -0      | .494888     |             | 0.0      |
| 3      | 0.234917             | 0.253137              | -0.057224 -0      | .012891     |             | 0.0      |
| 4      | 0.234917             | 0.253137              | -0.579693 -0      | .612646     |             | 0.0      |
|        |                      |                       |                   |             |             |          |
| 0      | Education2           | Education3<br>0.0     | Education4<br>0.0 | Education5  | Marital_Sta | 0.0      |
| p://lo | calhost 8888/noteboo | ks/Midterm_656.ipynb# |                   |             |             |          |
| _      |                      |                       |                   |             |             |          |
| 5/2018 | 8                    |                       |                   | Midterm_656 |             |          |
| 1      | 1.0                  | 0.0                   | 0.0               | 0.0         |             | 0.0      |
| 2      | 1.0                  |                       |                   | 0.0         |             | 0.0      |
| 3      | 1.0                  |                       | 0.0               | 0.0         |             | 0.0      |
| 4      | 1.0                  | 0.0                   | 0.0               | 0.0         |             | 0.0      |
|        | Marital_Sta          | atusl Marite          | al_Status2 c      | ard_class0  | card_class1 |          |
| 0      |                      | 1.0                   | 0.0               | 1.0         | 0.0         |          |
| 1      |                      | 0.0                   | 1.0               | 0.0         | 1.0         |          |
| 2      |                      | 0.0                   | 1.0               | 0.0         | 1.0         |          |
| 3      |                      | 1.0                   | 0.0               | 1.0         | 0.0         |          |
| 4      |                      | 1.0                   | 0.0               | 1.0         | 0.0         |          |

The cleaned, imputed, encoded and scaled data was then split for 10-fold cross validation which implies each time the model will be trained on 90% of the data and then the model will be assessed on the remaining 10% of the validation data or in other words, 90% of the data will be used for model fitting and remaining 10% data set will be held out for model assessment and this process will be carried out repeatedly until all the 10% held out test data has been utilized. The process for 10-fold cross validation is applied by running a loop. The screen shot of SAS code used is shown below:

```
Training Code
 data MYLIB.selection;
   call streaminit(12345);
   set dem import data;
   urand = rand('uniform');
 proc sort data=MYLIB.selection;
   by urand;
 data dem export train;
   drop fold size urand;
   set MYLIB.selection NOBS=nobs_;
   fold size = round(nobs / 10.0);
   if N <= fold size then fold='A';
   if N > fold size and N <= 2*fold size then fold='B';
   if _N_ > 2*fold_size and _N_ <= 3*fold_size then fold='C';
   if _N_ > 3*fold_size and _N_ <= 4*fold_size then fold='D';
   if N > 4*fold_size and N <= 5*fold_size then fold='E';
   if _N_ > 5*fold_size and _N_ <= 6*fold_size then fold='F';
   if N > 6*fold_size and N <= 7*fold_size then fold='G';
   if N > 7*fold size and N <= 8*fold size then fold='H';
   if N > 8*fold size and N <= 9*fold size then fold='I';
   if N > 9*fold size then fold='J';
   run;
```

```
raining Code
data MyLib.templ;
  retain cl c2 c3 c4 c5 c6 c7 c8 c9 c10 0;
   keep c1 c2 c3 c4 c5 c6 c7 c8 c9 c10;
   set &em_import_data end=eof;
   if fold='A' then cl=cl+1;
   if fold='B' then c2=c2+1;
   if fold='C' then c3=c3+1;
   if fold='D' then c4=c4+1;
   if fold='E' then c5=c5+1;
   if fold='F' then c6=c6+1;
   if fold='G' then c7=c7+1;
   if fold='H' then c8=c8+1;
   if fold='I' then c9=c9+1;
   if fold='J' then cl0=cl0+1;
   if eof then output;

☐ data &em_export_validate;

   drop cl c2 c3 c4 c5 c6 c7 c8 c9 c10 rfold;
   retain rfold '0';
   set MyLib.AllData_Train;
   if rfold='0' then do;
      set MyLib.templ;
      if cl=0 then rfold='A';
      if c2=0 then rfold='B';
      if c3=0 then rfold='C';
      if c4=0 then rfold='D';
      if c5=0 then rfold='E';
      if c6=0 then rfold='F';
      if c7=0 then rfold='G';
      if c8=0 then rfold='H';
      if c9=0 then rfold='I';
      if cl0=0 then rfold='J';
   end:
   if fold=rfold then output;
   run;
```

# **Model Fitting & Assessment**

Since this is a classification problem, the modelling techniques applied to classify the customer into the default/non-default category are as follows:

- 1. Logistic Regression
- 2. Decision Tree
- 3. Neural Networks
- 4. Random Forest.

The biggest challenge was to choose the best model amongst these and within each category, parameters such as depth of the tree, number of layers and perceptrons for neural network was varied to achieve the optimized model selection.

#### Selecting the most important model metrics

Since this data is from a bank, extra care would have been taken to particularly avoid incorrectly classifying a customer who will default, whereas incorrectly classifying a customer who will not default would be less problematic and would have less implications on the result. In other words, the value of False negatives has to be minimum and in order to achieve that, sensitivity/recall values have to optimized.

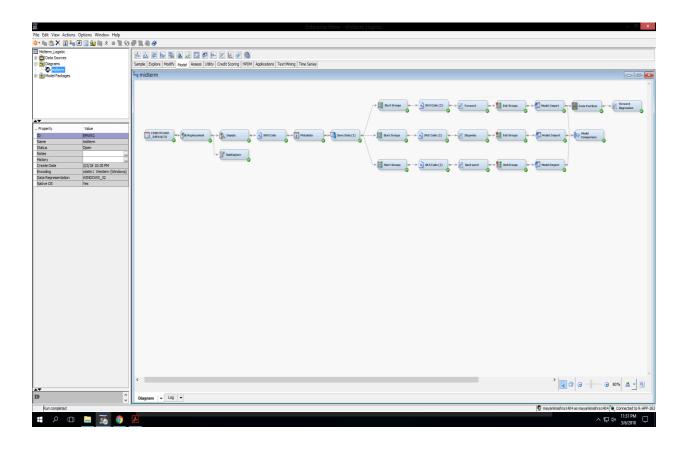
Now, for optimizing the values of sensitivity/recall, we used different methods for various classification models adopted.

For classifications models like Decision trees and Neural Networks, the parameters such as depth of the tree and layers of the neural network or the number of perceptrons in each layer of the neural networks were tuned. While optimizing the above-mentioned parameters of the respective classification model, the highest sensitivity/recall values were considered in selecting the best model while keeping in mind that the difference between training misclassification rate and the test misclassification rate should not be high enough to indicate overfitting of the model. This will in turn give poor results when the model will be used for a completely new data set in the future.

The dataset given presents us the problem of imbalanced classification since only 4584 out of 30000 customers are in default class which is 15.28% of the total number of customers. In such a scenario when one class outnumbers other class by large proportion, the machine learning algorithm doesn't get necessary information about the minority class so the TPR (True Positive Rate) values or the sensitivity/recall value would come out to be low until the case boosting of the minority class using the oversampling or any other method is carried out in order to eliminate the bias for the majority class ('not default' in this case).

# **Logistic Regression:**

This model classifies the customers into a default or non-default class by modelling the probability that the customer belongs to a particular category. In SAS EM, forward, backward and stepwise variable selection methods were carried out to find out the best logistics regression model.



|               | Logistic    | Logistic        | Logistic    |
|---------------|-------------|-----------------|-------------|
|               | Forward     | <b>Stepwise</b> | Backward    |
| MISC          | 0.136888889 | 0.136925926     | 0.138518519 |
| sensivity/TPR | 0.29532967  | 0.295100733     | 0.284340659 |
| specificity   | 0.972693531 | 0.972693531     | 0.972870272 |
| FPR           | 0.027306469 | 0.027306469     | 0.027129728 |
| Precision     | 0.676100629 | 0.675930781     | 0.669181034 |
| Accuracy      | 0.863111111 | 0.863074074     | 0.861481481 |
| <b>F1</b>     | 0.411089866 | 0.410836653     | 0.399100257 |

From the table, we observe that the **forward logistic regression is the best logistic regression model.** 

Python output for logistic regression:

```
****** Logistic Regression ******

Metric..... Mean Std. Dev.
accuracy..... 0.8616 0.0033

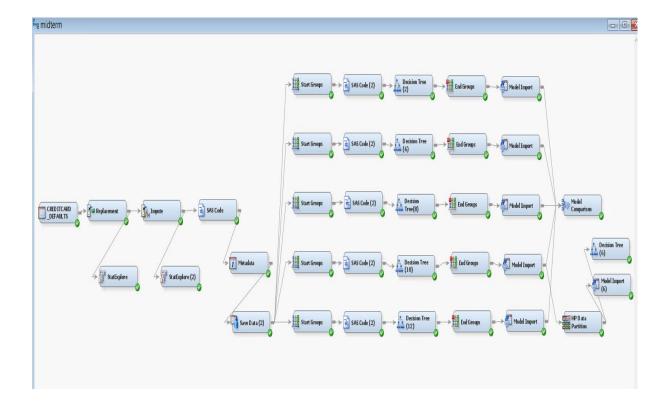
recall..... 0.2829 0.0233

precision.... 0.6750 0.0367

f1..... 0.3976 0.0204
```

#### **Decision Trees:**

In this model, the data is split into branch like segments to form an inverted tree with root node at the top of the tree. Decision trees of two branches and different depths were tested in order to get the best model. The SAS code taught during lecture sessions were adopted to cross validate the data. Below is the SAS diagram used.



The model metrics for the various Decision Tree classification model are as follows:

|                  | 2 Branch 3<br>depth | 2 Branch 6<br>depth | 2 Branch 8<br>depth | 2 Branch 10<br>depth | 2 Branch 12<br>depth |
|------------------|---------------------|---------------------|---------------------|----------------------|----------------------|
| MISC             | 0.125               | 0.120               | 0.117               | 0.113                | 0.111                |
| sensivity/Recall | 0.417               | 0.458               | 0.465               | 0.478                | 0.484                |
| specificity      | 0.96                | 0.960               | 0.962               | 0.964                | 0.966                |
| FPR              | 0.036               | 0.039               | 0.037               | 0.035                | 0.033                |
| Precision        | 0.686               | 0.693               | 0.707               | 0.723                | 0.736                |
| Accuracy         | 0.874               | 0.879               | 0.882               | 0.886                | 0.888                |
| Recall           | 0.417               | 0.458               | 0.465               | 0.478                | 0.484                |
| F1               | 0.519               | 0.551               | 0.561               | 0.576                | 0.584                |

From the model metrics, it is clear that the decision tree with 2 branches and depth=12 has the highest value of sensitivity/recall which is the most important parameter from the metrics. But when the misclassification error rate for the training data set and validation dataset were compared for the decision tree model of depth 12 are compared then it was observed that the model was overfitting the data. Therefore, **depth 10 was selected as the final best model for the decision tree in SAS EM**.

The output of the various decision tree models in Python are as follows:

```
*********** Decision Trees **********
****** Decision Tree with Max Depth = 1 ******
Metric.....
            Mean
                    Std. Dev.
accuracy.... 0.8732
                     0.0076
recall..... 0.4306 0.0330
precision.... 0.6686
                    0.0401
f1..... 0.5232
                     0.0314
****** Decision Tree with Max Depth = 2 ******
                   Std. Dev.
Metric..... Mean
accuracy.... 0.8741
                    0.0065
recall..... 0.4081
                    0.0309
                   0.0386
precision.... 0.6881
f1..... 0.5116
                     0.0284
***** Decision Tree with Max Depth = 3 ******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8750
                    0.0068
recall..... 0.4156
                    0.0309
precision.... 0.6894 0.0402
f1..... 0.5178
                     0.0291
***** Decision Tree with Max Depth = 4 ******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8748
                    0.0077
recall..... 0.4565 0.0333
precision.... 0.6664
                    0.0408
f1..... 0.5410
                     0.0299
***** Decision Tree with Max Depth = 5 ******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8741
                    0.0071
recall..... 0.4479
                    0.0403
precision.... 0.6675
                    0.0449
f1..... 0.5344
                     0.0301
```

```
****** Decision Tree with Max Depth = 6 *******
                       Std. Dev.
 Metric....
               Mean
http://localhost:8888/notebooks/Midterm_656.ipynb#
3/6/2018
                                        Midterm_656
 accuracy.... 0.8751
                       0.0067
 recall..... 0.4516
                        0.0386
 precision.... 0.6708
                        0.0368
 f1..... 0.5386
                        0.0304
 ****** Decision Tree with Max_Depth = 7 ******
               Mean
                       Std. Dev.
 Metric....
 accuracy.... 0.8738
                       0.0068
 recall..... 0.4438
                        0.0355
 precision.... 0.6673
                        0.0384
                        0.0280
 f1..... 0.5318
 ****** Decision Tree with Max Depth = 8 ******
 Metric..... Mean
                      Std. Dev.
 accuracy.... 0.8723
                       0.0072
 recall..... 0.4425
                       0.0408
                     0.0382
 precision.... 0.6575
 f1..... 0.5278
                       0.0323
 ****** Decision Tree with Max Depth = 9 *******
                      Std. Dev.
 Metric....
               Mean
 accuracy.... 0.8712
                        0.0060
                        0.0296
 recall..... 0.4429
                       0.0337
 precision.... 0.6508
 f1..... 0.5263
                        0.0236
 ****** Decision Tree with Max Depth = 10
 Metric..... Mean
                      Std. Dev.
                       0.0084
 accuracy.... 0.8701
 recall..... 0.4444
                        0.0323
 precision.... 0.6453
                       0.0476
 f1..... 0.5252
                        0.0287
```

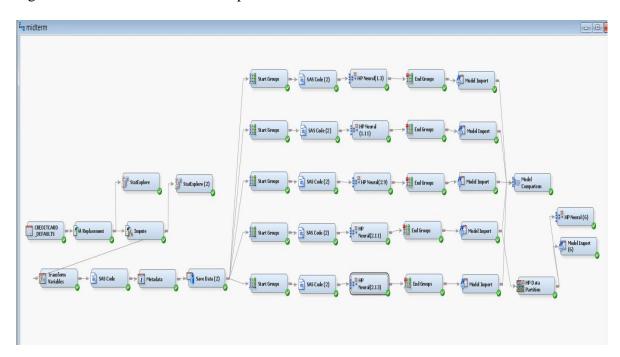
The decision tree with maximum depth=4 is the best model since it has the highest recall value.

#### **Neural Networks:**

These are a class of parametric models that accommodates a wider variety of nonlinear relationships between a set of predictors and a target variable. The network was defined with 3,5,7,9,11 perceptrons as instructed in the problem statement. The modeling was done using HP and non-HP nodes.

### HP Neural Network:

In non-HP method, maximum of 2 layers and 13 neurons were adopted to model the data. Below is the diagram that was used in SAS enterprise miner.



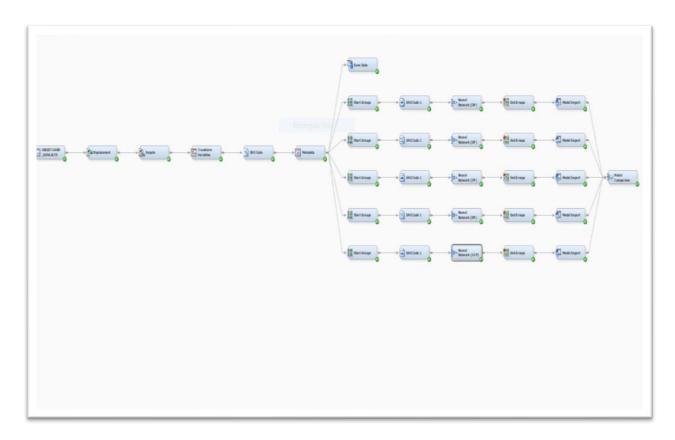
The model metrics for the various HP Neural Network classification model are shown below

|                  | 1 Layer 3 | 1 Layer 11 | 2 Layer 9 | 2 Layer 11 | 2 Layer 13 |
|------------------|-----------|------------|-----------|------------|------------|
|                  | Neurons   | Neurons    | Neurons   | Neurons    | Neurons    |
| MISC             | 0.136     | 0.135      | 0.135     | 0.136      | 0.138      |
| Sensivity/Recall | 0.414     | 0.393      | 0.436     | 0.441      | 0.427      |
| specificity      | 0.949     | 0.955      | 0.946     | 0.945      | 0.945      |
| FPR              | 0.050     | 0.044      | 0.053     | 0.054      | 0.054      |
| Precision        | 0.614     | 0.629      | 0.612     | 0.609      | 0.601      |
| Accuracy         | 0.863     | 0.864      | 0.864     | 0.863      | 0.861      |
| Recall           | 0.414     | 0.393      | 0.436     | 0.441      | 0.427      |
| <b>F1</b>        | 0.495     | 0.484      | 0.509     | 0.511      | 0.500      |

It is clear from the model metrics table that the sensitivity/recall, specificity, precision, accuracy, recall and F1 values are highest as well as FPR is the lowest for neural network with **2 layers and 11 neurons** therefore that neural network model is selected as the best neural network model in SAS EM.

## Non-HP Neural Network:

In non-HP model, 3,5,7,9,11 perceptrons were adopted and the model was trained with 20 iterations and 30 runs with maximum run time for each node set to 1 hour.



The model metrics for the various non-HP Neural Network classification model are as shown below:

|                  | 3 Neurons | 5 Neurons | 7 Neurons | 9 Neurons | 11 Neurons |
|------------------|-----------|-----------|-----------|-----------|------------|
| MISC             | 0.130     | 0.127     | 0.129     | 0.130     | 0.129      |
| sensivity/Recall | 0.388     | 0.415     | 0.398     | 0.380     | 0.388      |
| specificity      | 0.963     | 0.961     | 0.963     | 0.964     | 0.964      |
| Precision        | 0.666     | 0.672     | 0.674     | 0.672     | 0.673      |
| Accuracy         | 0.870     | 0.873     | 0.872     | 0.870     | 0.871      |
| <b>F</b> 1       | 0.491     | 0.513     | 0.500     | 0.486     | 0.492      |
| FPR              | 0.612     | 0.585     | 0.602     | 0.620     | 0.612      |

Comparing both the metric table, it is clearly evident that the HP neural network outperforms the non-HP neural network so we do not consider non-HP neural network while considering the final best model.

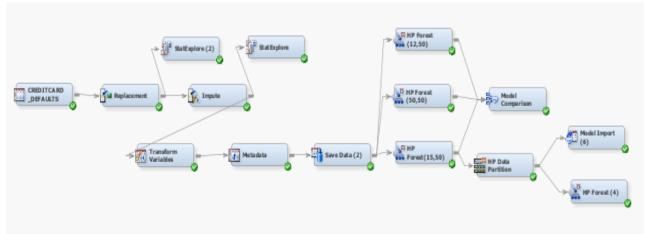
Output of different neural networks in python are as follows:-

```
*********** Neural Networks ********
****** NEURAL NETWORK; 1 hidden layer with 3 perceptrons******
Metric..... Mean Std. Dev.
                    0.0061
accuracy.... 0.8720
recall..... 0.4155
                      0.0346
precision.... 0.6707 0.0397
f1..... 0.5118
                      0.0270
****** NEURAL NETWORK; 1 hidden layer with 11 perceptrons******
Metric..... Mean Std. Dev.
accuracy.... 0.8708
                    0.0075
recall..... 0.4429
                    0.0386
precision.... 0.6487
                      0.0388
f1..... 0.5253
                     0.0311
****** NEURAL NETWORK; 2 hidden layer with 5 & 4 perceptrons******
Metric..... Mean Std. Dev.
                    0.0069
accuracy.... 0.8719
recall..... 0.4473
                      0.0326
precision.... 0.6553
                      0.0447
f1..... 0.5302
                      0.0238
****** NEURAL NETWORK; 2 hidden layer with 6 & 5 perceptrons******
Metric..... Mean
                     Std. Dev.
accuracy.... 0.8731
                      0.0063
p://localhost:8888/notebooks/Midterm_656.ipynb#
/2018
                                      Midterm 656
recall..... 0.4627
                      0.0397
precision.... 0.6539
                      0.0363
f1..... 0.5405
                      0.0279
****** NEURAL NETWORK; 2 hidden layer with 7 & 6 perceptrons*******
Metric..... Mean
                     Std. Dev.
accuracy.... 0.8702
                    0.0064
recall..... 0.4524
                      0.0340
precision.... 0.6421
                      0.0361
f1..... 0.5295
                      0.0247
```

The best neural network model from python is the one with 2 hidden layers and 6&5 perceptrons.

#### **Random Forest**

Various Random Forest models were built by changing the number of depth and maximum number of trees.



Following are the model metrics-

| <b>Model Metrics</b> | 12Trees 50Depth | 50Trees 50Depths | 15Trees 50Depths |
|----------------------|-----------------|------------------|------------------|
| MISC                 | 0.130           | 0.162            | 0.129            |
| Sensivity/Recall     | 0.368           | 0.204            | 0.369            |
| specificity          | 0.966           | 0.932            | 0.967            |
| FPR                  | 0.033           | 0.067            | 0.032            |
| Precision            | 0.676           | 0.310            | 0.686            |
| Accuracy             | 0.869           | 0.837            | 0.870            |
| Recall               | 0.368           | 0.204            | 0.369            |
| <b>F1</b>            | 0.476           | 0.246            | 0.480            |

From the metrics table it is observed that the Random Forest model with depth=50 and maximum number of trees=15 is the best model in SAS EM since the sensitivity/recall, specificity, precision, accuracy, recall and F1 values are the highest while the misclassification error rate and FPR values are the lowest.

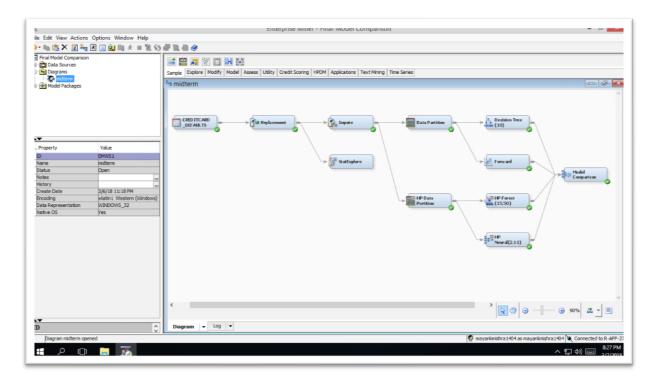
The corresponding output of various random forest models in python are as follows:

```
********** Random Forests *********
                                              *****
*******Number of Trees: 10 Max features:
                                        auto
                   Std. Dev.
Metric..... Mean
accuracy.... 0.8715
                    0.0045
recall..... 0.3943
                     0.0323
precision.... 0.6787
                     0.0309
f1..... 0.4977
                     0.0244
*******Number of Trees: 10 Max features: 0.3 *******
Metric..... Mean
                   Std. Dev.
accuracy.... 0.8739
                    0.0070
                     0.0331
recall..... 0.4028
precision... 0.6906
                     0.0441
f1..... 0.5078
                     0.0296
*******Number of Trees:
                       10 Max_features: 0.5 ******
Metric..... Mean
                   Std. Dev.
accuracy.... 0.8776
                    0.0051
recall..... 0.4269
                     0.0316
precision.... 0.7017
                     0.0343
f1..... 0.5297
                     0.0235
*******Number of Trees:
                      10 Max_features: 0.7 ******
Metric..... Mean
                   Std. Dev.
accuracy.... 0.8761
                    0.0058
                     0.0377
recall..... 0.4209
precision.... 0.6943
                     0.0344
f1..... 0.5229
                     0.0294
*******Number of Trees: 15 Max features:
                                       auto ******
Metric..... Mean
                   Std. Dev.
accuracy.... 0.8746
                     0.0051
recall..... 0.4425
                     0.0414
precision.... 0.6722
                     0.0297
f1..... 0.5321
                     0.0284
*******Number of Trees:
                      15 Max features: 0.3 ******
Metric..... Mean
                   Std. Dev.
accuracy.... 0.8766
                    0.0059
recall..... 0.4551
                     0.0331
                     0.0359
precision.... 0.6785
f1..... 0.5437
                     0.0238
```

```
********Number of Trees: 15 Max features: 0.5 *******
Metric.... Mean
                     Std. Dev.
accuracy.... 0.8800
                     0.0064
ttp://localhost:8888/notebooks/Midterm_656.ipynb#
/6/2018
                                      Midterm_656
recall..... 0.4724
                     0.0345
precision.... 0.6911
                      0.0402
fl..... 0.5598
                     0.0242
 ********Number of Trees: 15 Max features: 0.7 *******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8777
                      0.0063
recall..... 0.4679
                     0.0318
precision.... 0.6781
                     0.0358
fl..... 0.5528
                     0.0243
 ********Number of Trees: 20 Max features: auto *******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8770
                     0.0057
                     0.0337
recall..... 0.4244
precision.... 0.6990
                     0.0374
fl..... 0.5270
                      0.0263
 ********Number of Trees: 20 Max features: 0.3 *******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8789
                     0.0061
recall..... 0.4364
                     0.0357
precision.... 0.7044
                      0.0361
f1..... 0.5378
                      0.0290
********Number of Trees: 20 Max features: 0.5 *******
Metric..... Mean
                    Std. Dev.
accuracy.... 0.8810
                     0.0061
recall..... 0.4485
                     0.0345
precision.... 0.7112
                      0.0393
fl..... 0.5489
                      0.0265
********Number of Trees: 20 Max features: 0.7 *******
Metric.... Mean
                    Std. Dev.
accuracy.... 0.8800
                     0.0060
recall..... 0.4510
                      0.0295
                     0.0336
precision... 0.7020
fl..... 0.5485
                      0.0254
```

The best model from the above metric values appears to be the random forest model with maximum number of trees=15 and max number of features=0.7.

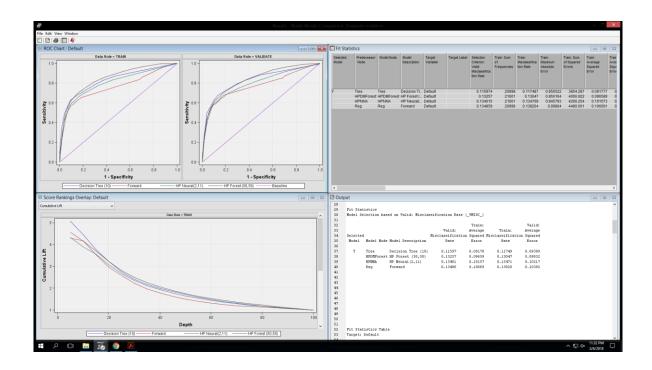
# **Model Comparison:**



Comparing the various classification model from the SAS EM, we get the following table:-

| <b>Model Metrics</b> | Decision Tree(2<br>branch, depth=10) | Neural Network(2<br>Layer 11 Neurons) | Random<br>Forest(15 Tree<br>depth=50) |
|----------------------|--------------------------------------|---------------------------------------|---------------------------------------|
| MISC                 | 0.113                                | 0.136                                 | 0.129                                 |
| sensivity/Recall     | 0.478                                | 0.441                                 | 0.369                                 |
| specificity          | 0.964                                | 0.945                                 | 0.967                                 |
| FPR                  | 0.035                                | 0.054                                 | 0.032                                 |
| Precision            | 0.723                                | 0.609                                 | 0.686                                 |
| Accuracy             | 0.886                                | 0.863                                 | 0.870                                 |
| F1                   | 0.576                                | 0.511                                 | 0.480                                 |

Therefore, Decision Tree with 2 branch and depth=10 comes out to be the winner amongst all the SAS EM models.



Comparing the model output in Python we get,

| <b>Model Metrics</b> | Logistic<br>Regression | Decision<br>Tree(depth=4) | Neural<br>Network(2 Layer<br>11 Neurons) | Random Forest(15<br>Tree<br>max_features=0.7) |
|----------------------|------------------------|---------------------------|--|---|
| Accuracy             | 0.8616                 | 0.8478                    | 0.8731                                   | 0.8777  |
| sensivity/Recall     | 0.2829                 | 0.4565                    | 0.4627                                   | 0.4679  |
| Precision            | 0.6750                 | 0.6664                    | 0.6539                                   | 0.6781  |
| F1                   | 0.3976                 | 0.5410                    | 0.5405                                   | 0.5528  |

Clearly, the winner amongst the python model is the Random Forest model with 15 tree and maximum features=0.7

|   | accuracy_mean | accuracy std | recall mean | recall |  |
|---|---------------|--------------|-------------|--------|--|
| std \                                     |               |              |             |        |  |
| Logistic regression<br>252                |               |              | 0.282865    |        |  |
| DT_Max_Depth_1<br>007                     | 0.873202      | 0.007624     | 0.430596    | 0.033  |  |
| DT_Max_Depth_2<br>860                     | 0.874135      | 0.006458     | 0.408136    | 0.030  |  |
| DT_Max_Depth_3<br>882                     | 0.874968      | 0.006826     | 0.415555    | 0.030  |  |
| DT_Max_Depth_4<br>350                     | 0.874835      | 0.007739     | 0.456550    | 0.033  |  |
| DT_Max_Depth_5<br>262                     | 0.874068      | 0.007116     | 0.447891    | 0.040  |  |
| DT_Max_Depth_6<br>587                     | 0.875135      | 0.006730     | 0.451605    | 0.038  |  |
| DT_Max_Depth_7<br>521                     | 0.873835      | 0.006753     | 0.443765    | 0.035  |  |
| DT_Max_Depth_8<br>824                     | 0.872268      | 0.007167     | 0.442534    | 0.040  |  |
| DT_Max_Depth_9<br>625                     | 0.871168      | 0.006009     | 0.442946    | 0.029  |  |
| DT_Max_Depth_10                           | 0.870102      | 0.008368     | 0.444391    | 0.032  |  |
| http://localhost:8888/notebooks/Midterm_0 | 556 ipynb#    |              |             |        |  |
|   |               |              |             |        |  |
| 3/6/2018                                  |               | Midterm_656  |             |        |  |
| 319<br>NN 1L 3P                           | 0.872035      | 0.006059     | 0.415544    | 0.034  |  |
| 600<br>NN 1L 11P                          | 0.870768      | 0.007493     |             |        |  |
| 604                                       |               |              |             |        |  |
| NN_2L_5P_4P<br>622                        | 0.871935      | 0.006865     |             |        |  |
| NN_2L_6P_5P<br>735                        | 0.873068      | 0.006316     | 0.462731    | 0.039  |  |
| NN_2L_7P_6P<br>040                        | 0.870168      | 0.006354     | 0.452411    | 0.034  |  |
| RF_10T_autoF<br>310                       | 0.871534      | 0.004451     | 0.394331    | 0.032  |  |
| RF_10T_0.3F<br>059                        | 0.873868      | 0.006997     | 0.402779    | 0.033  |  |
| RF_10T_0.5F<br>594                        | 0.877601      | 0.005080     | 0.426882    | 0.031  |  |
| RF_10T_0.7F<br>696                        | 0.876102      | 0.005831     | 0.420910    | 0.037  |  |
| RF_15T_autoF<br>359                       | 0.874568      | 0.005076     | 0.442541    | 0.041  |  |
| RF_15T_0.3F<br>065                        | 0.876602      | 0.005939     | 0.455108    | 0.033  |  |
| RF_15T_0.5F<br>539                        | 0.880001      | 0.006400     | 0.472407    | 0.034  |  |
| RF_15T_0.7F<br>757                        | 0.877668      | 0.006299     | 0.467876    | 0.031  |  |
| RF_20T_autoF<br>707                       | 0.877001      | 0.005727     | 0.424409    | 0.033  |  |
| RF_20T_0.3F                               | 0.878935      | 0.006149     | 0.436359    | 0.035  |  |
| 670<br>RF_20T_0.5F                        | 0.880968      | 0.006073     | 0.448510    | 0.034  |  |
| 469                                       | 0.000024      | 0.00000      | 0.450003    | 0.020  |  |

|  |  | ·  |  |  |
|--|--|--|--|--|
| Logistic regression  | 0.674993   | 0.036698   | 0.397554   | 0.020424   |
| DT_Max_Depth_1   | 0.668596   | 0.040104   | 0.523210   | 0.031426   |
| DT_Max_Depth_2   | 0.688117   | 0.038631   | 0.511633   | 0.028421   |
| DT_Max_Depth_3   | 0.689393   | 0.040202   | 0.517834   | 0.029109   |
| DT_Max_Depth_4   | 0.666419   | 0.040791   | 0.541039   | 0.029913   |
| DT_Max_Depth_5   | 0.667509   | 0.044878   | 0.534378   | 0.030089   |
| DT_Max_Depth_6   | 0.670811   | 0.036808   | 0.538575   | 0.030402   |
| DT_Max_Depth_7   | 0.667265   | 0.038383   | 0.531785   | 0.027998   |
| DT_Max_Depth_8   | 0.657498   | 0.038156   | 0.527823   | 0.032266   |
| DT_Max_Depth_9   | 0.650849   | 0.033704   | 0.526327   | 0.023551   |
| DT_Max_Depth_10  | 0.645271   | 0.047575   | 0.525212   | 0.028696   |
| NN_1L_3P   | 0.670669   | 0.039727   | 0.511788   | 0.027022   |
| http://localhost:8888/notebooks/Midterm_6  | 56 ipynb#  |  |  |  |
|  |  |  |  |  |
| 3/6/2018   |  | Midterm_656  |  |  |
|  |  |  |  |  |
| NN_1L_11P  | 0.648689   | 0.038787   | 0.525281   | 0.031061   |
| NN_1L_11P<br>NN_2L_5P_4P   | 0.648689<br>0.655312   | 0.038787<br>0.044721   |  |  |
|  |  |  | 0.530217   | 0.023778   |
| NN_2L_5P_4P  | 0.655312   | 0.044721<br>0.036262   | 0.530217   | 0.023778   |
| NN_2L_5P_4P<br>NN_2L_6P_5P   | 0.655312<br>0.653860   | 0.044721<br>0.036262   | 0.530217<br>0.540513<br>0.529507   | 0.023778<br>0.027915<br>0.024688   |
| NN_2L_5P_4P NN_2L_6P_5P NN_2L_7P_6P  | 0.655312<br>0.653860<br>0.642102   | 0.044721<br>0.036262<br>0.036107   | 0.530217<br>0.540513<br>0.529507<br>0.497670   | 0.023778<br>0.027915<br>0.024688<br>0.024417   |
| NN_2L_5P_4P NN_2L_6P_5P NN_2L_7P_6P RF_10T_autoF   | 0.655312<br>0.653860<br>0.642102<br>0.678669   | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135   | 0.530217<br>0.540513<br>0.529507<br>0.497670   | 0.023778<br>0.027915<br>0.024688<br>0.024417<br>0.029581   |
| NN_2L_5P_4P NN_2L_6P_5P NN_2L_7P_6P RF_10T_autoF RF_10T_0.3F   | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578   | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258   | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753   | 0.023778<br>0.027915<br>0.024688<br>0.024417<br>0.029581<br>0.023515   |
| NN_2L_5P_4P NN_2L_6P_5P NN_2L_7P_6P RF_10T_autoF RF_10T_0.3F RF_10T_0.5F   | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685   | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258   | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700   | 0.023778<br>0.027915<br>0.024688<br>0.024417<br>0.029581<br>0.023515<br>0.029407   |
| NN_2L_5P_4P NN_2L_6P_5P NN_2L_7P_6P RF_10T_autoF RF_10T_0.3F RF_10T_0.5F   | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317   | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679   | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910   | 0.023778<br>0.027915<br>0.024688<br>0.024417<br>0.029581<br>0.023515<br>0.029407<br>0.028449                                   |
| NN_2L_5P_4P  NN_2L_6P_5P  NN_2L_7P_6P  RF_10T_autoF  RF_10T_0.3F  RF_10T_0.5F  RF_10T_0.7F   | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317   | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679<br>0.035902   | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910<br>0.532125   | 0.023778<br>0.027915<br>0.024688<br>0.024417<br>0.029581<br>0.023515<br>0.029407<br>0.028449                                   |
| NN_2L_5P_4P NN_2L_6P_5P NN_2L_7P_6P RF_10T_autoF RF_10T_0.3F RF_10T_0.5F RF_15T_autoF  | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317<br>0.672159<br>0.678518   | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679<br>0.035902<br>0.040197   | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910<br>0.532125<br>0.543672   | 0.023778 0.027915 0.024688 0.024417 0.029581 0.023515 0.029407 0.028449 0.023816 0.024174                                      |
| NN_2L_5P_4P  NN_2L_6P_5P  NN_2L_7P_6P  RF_10T_autoF  RF_10T_0.3F  RF_10T_0.5F  RF_15T_autoF  RF_15T_autoF  | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317<br>0.672159<br>0.678518<br>0.691078                                     | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679<br>0.035902<br>0.040197<br>0.035791                                     | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910<br>0.532125<br>0.543672<br>0.559817                                     | 0.023778 0.027915 0.024688 0.024417 0.029581 0.023515 0.029407 0.028449 0.023816 0.024174 0.024319                             |
| NN_2L_5P_4P  NN_2L_6P_5P  NN_2L_7P_6P  RF_10T_autoF  RF_10T_0.3F  RF_10T_0.5F  RF_15T_autoF  RF_15T_autoF  RF_15T_0.3F                                       | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317<br>0.672159<br>0.678518<br>0.691078<br>0.678069                         | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679<br>0.035902<br>0.040197<br>0.035791<br>0.037374                         | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910<br>0.532125<br>0.543672<br>0.559817<br>0.552766                         | 0.023778 0.027915 0.024688 0.024417 0.029581 0.023515 0.029407 0.028449 0.023816 0.024174 0.024319 0.026349                    |
| NN_2L_5P_4P  NN_2L_6P_5P  NN_2L_7P_6P  RF_10T_autoF  RF_10T_0.3F  RF_10T_0.5F  RF_15T_autoF  RF_15T_o.3F  RF_15T_0.7F  RF_15T_0.7F                           | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317<br>0.672159<br>0.678518<br>0.691078<br>0.678069<br>0.699006             | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679<br>0.035902<br>0.040197<br>0.035791<br>0.037374<br>0.036116             | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910<br>0.532125<br>0.543672<br>0.559817<br>0.552766<br>0.526987<br>0.537778 | 0.023778 0.027915 0.024688 0.024417 0.029581 0.023515 0.029407 0.028449 0.023816 0.024174 0.024319 0.026349 0.028981           |
| NN_2L_5P_4P  NN_2L_6P_5P  NN_2L_7P_6P  RF_10T_autoF  RF_10T_0.3F  RF_10T_0.5F  RF_15T_autoF  RF_15T_0.3F  RF_15T_0.3F  RF_15T_0.3F  RF_15T_0.5F  RF_15T_0.5F | 0.655312<br>0.653860<br>0.642102<br>0.678669<br>0.690578<br>0.701685<br>0.694317<br>0.672159<br>0.678518<br>0.691078<br>0.678069<br>0.699006<br>0.704398 | 0.044721<br>0.036262<br>0.036107<br>0.030947<br>0.044135<br>0.034258<br>0.034401<br>0.029679<br>0.035902<br>0.040197<br>0.035791<br>0.037374<br>0.036116<br>0.039282 | 0.530217<br>0.540513<br>0.529507<br>0.497670<br>0.507753<br>0.529700<br>0.522910<br>0.532125<br>0.543672<br>0.559817<br>0.552766<br>0.526987<br>0.537778 | 0.023778 0.027915 0.024688 0.024417 0.029581 0.023515 0.029407 0.028449 0.023816 0.024174 0.024319 0.026349 0.0268981 0.026461 |

# **Conclusion:**

Comparison between the best SAS EM Model and best Python model:

| Model Metrics    | Decision Tree(2<br>branch, depth=10) | Random Forest(15 Tree max_features=0.7) |
|------------------|--------------------------------------|---|
| Accuracy         | 0.886                                | 0.878                                   |
| sensivity/Recall | 0.479                                | 0.468                                   |
| Precision        | 0.723                                | 0.678                                   |
| <b>F1</b>        | 0.576                                | 0.553                                   |

From the following table, we can conclude that the Decision Tree model of SAS EM with 2 branches and depth=10 is by far the best model with highest Sensitivity/recall, Accuracy, Precision and F1 values.

The Sensitivity/recall value of the best model is 0.4785 which implies that the model correctly predicts whether a customer is going to default 47.8% of the time when the customer actually defaults. The best model has an accuracy of 88.60% which depicts that the true events are correctly classified 88.60% of the time.

# Best Model Output shown in SAS EM:



