

## \* Assignment 05 \*

Q.1.] Solution:

No. of RNN units = 2

$$W_x = [3, -4] ; b_h = 0$$

$$W_h = \begin{bmatrix} 4 & -5 \\ -3 & 2 \end{bmatrix} ; b_y = 10$$

$$h_0 = [0, 0]$$

$$W_y = \begin{bmatrix} -4 \\ 2 \end{bmatrix} ; x_1 = 1, x_2 = 2, x_3 = 3$$

$$h_t = \tanh(W_x \cdot x_t + W_h \cdot h_{t-1} + b_h)$$

$$h_1 = \tanh(1 \times [3 \ -4] + 0 + 0)$$

$$= [0.99505 \ -0.99932]$$

$$h_2 = \tanh(2 \times [3 \ -4] + [0.99505 \ -0.99932] \cdot \begin{bmatrix} 4 & -5 \\ -3 & 2 \end{bmatrix} + 0)$$

$$= [0.99999 \ -1]$$

$$h_3 = \tanh(3 \times [3 \ -4] + [0.99999 \ -1] \cdot \begin{bmatrix} 4 & -5 \\ -3 & 2 \end{bmatrix} + 0)$$

$$= \begin{bmatrix} 1 & -1 \end{bmatrix}$$

$$\hat{y}_t = W y \cdot h_t + b y$$

$$\hat{y}_t = W y \cdot h_3 + b y$$

$$= \begin{bmatrix} 1 & -1 \end{bmatrix} \begin{bmatrix} -4 \\ 2 \end{bmatrix} + 10$$

$$= -6 + 10$$

$$\hat{y}_t = 4$$

Q.2.] Solution :

$$\begin{array}{ccc} \text{(I) Embedding} & \longrightarrow & 72120 \\ 12020 & \times & 6 \end{array}$$

$$\left\{ \begin{array}{l} \text{input dim} \\ = \text{vocab len} \end{array} \right\} \quad \left\{ \begin{array}{l} \text{seq. output} \\ \text{dim} \end{array} \right\}$$

$$\text{(II) Simple RNN (1)} \longrightarrow 4544$$

$$(64 \times 64) + (64 \times 6) + 64$$

$$\left\{ \begin{array}{l} \text{Recurrent} \\ \text{weights} \end{array} \right\} \quad \left\{ \begin{array}{l} \text{No. of units} \times \\ \text{No. of feat} \\ \text{from embed} \end{array} \right\} \quad \left\{ \text{backprop} \right\}$$

$$\text{(III) Simple RNN (2)} \longrightarrow 3104$$

$$(32 \times 32) + (32 \times 64) + 32$$

$$\left\{ \begin{array}{l} \text{Recurrent} \\ \text{weights} \end{array} \right\} \quad \left\{ \begin{array}{l} \text{input} \\ \text{weights} \end{array} \right\} \quad \left\{ \text{backprop} \right\}$$

(IV) Simple RNN (3)  $\rightarrow$  784

$$(16 \times 16) + (16 \times 32) + 16$$

$\left\{ \begin{array}{l} \text{recurrent} \\ \text{weights} \end{array} \right\}$ 
 $\left\{ \begin{array}{l} \text{input} \\ \text{weights} \end{array} \right\}$ 
 $\left\{ \text{backprop} \right\}$

(V) Dense  $\rightarrow$  408

$$(24 \times 16) + 24$$

$\left\{ \begin{array}{l} \text{No. of units} \times \text{No. of} \\ \text{prev. RNN layer} \end{array} \right\}$ 
 $\left\{ \text{backprop} \right\}$

(VI) Dense (output layer)  $\rightarrow$  150

$$(6 \times 24) + 6$$

$\left\{ \begin{array}{l} \text{No. of o/p units} \times \text{No.} \\ \text{of prev hidden layer} \end{array} \right\}$ 
 $\left\{ \text{backprop} \right\}$