

Assignment 5.1.

Given:-

$$w_x = [3, -4]$$

$$b_h = 0$$

$$b_y = 10$$

$$w_h = \begin{bmatrix} 4 & -5 \\ -3 & 2 \end{bmatrix}$$

$$h_0 = [0, 0]$$

$$x = [1, 2, 3]$$

$$w_y = \begin{bmatrix} -4 \\ 2 \end{bmatrix}$$

No. of RNN units = 2

$$h_t = \tanh(w_x \cdot x_t + w_h \cdot h_{t-1} + b_h)$$

$$h_1 = \tanh(1 \times [3 \ -4] + 0 + 0)$$

$$\cancel{= \tanh} = [0.99505 \quad -0.99932]$$

$$h_2 = \tanh(2 \times [3 \ -4] + [0.99505 \quad -0.99932] \begin{bmatrix} 4 & -5 \\ -3 & 2 \end{bmatrix})$$

$$= \tanh([6 \ -8] + [6.97816 \quad -6.97389])$$

$$= \tanh([12.97816 \quad -14.97389])$$

$$= [0.99999 \quad -1]$$

$$\begin{aligned}
 h_3 &= \tanh \left(3 \times \begin{bmatrix} 3 & -4 \end{bmatrix} + \begin{bmatrix} 0.99999 & -1 \end{bmatrix} \begin{bmatrix} 4 & -5 \\ -3 & 2 \end{bmatrix} + 0 \right) \\
 &= \tanh \left(\begin{bmatrix} 9 & -12 \end{bmatrix} + \begin{bmatrix} 6.99996 & -6.99995 \end{bmatrix} \right) \\
 &= \tanh \left(\begin{bmatrix} 15.99996 & -18.99995 \end{bmatrix} \right) \\
 &= \begin{bmatrix} 1 & -1 \end{bmatrix}
 \end{aligned}$$

$$\hat{y}_t = w_y \cdot h_t + b_y$$

$$= w_y \cdot h_3 + b_y$$

$$= \begin{bmatrix} 1 & -1 \end{bmatrix} \begin{bmatrix} -4 \\ 2 \end{bmatrix} + 10$$

$$= -4 - 2 + 10$$

$$= -6 + 10$$

$$= 4$$

$$\boxed{\hat{y}_t = 4}$$

Assignment 5.2

Ques 10-)

★ Embedding layer.

$$= \text{vocab length} \times \text{Required output dim}$$

$$= 12020 \times 6$$

$$= 72120$$

★ Simple RNN layer (first).

$$= (\text{Recurrent weights}) + (\text{no. of units} \times \text{no. of features from embedding}) + (\text{backpropagation})$$

$$= (64 \times 64) + (64 \times 6) + 64$$

$$= 4544$$

★ Simple RNN layer (second)

$$= (\text{Recurrent weights}) + (\text{No. of units} \times \text{no. of units of previous layer}) + (\text{backpropagation})$$

$$= (32 \times 32) + (32 \times 64) + 32$$

$$= 3104$$

★ Simple RNN layer (third)

$$= (16 \times 16) + (16 \times 32) + 16$$

$$= 784$$

★ Dense layer

$$= (\text{No. of units} \times \text{no. of units of previous RNN layer}) + (\text{backpropagation})$$

$$= (24 \times 16) + 24$$

$$= 408$$

$$\begin{aligned}
 & \star \text{ Dense (output layer)} \\
 & = (\text{No. of O/P units} \times \text{no. of units of previous hidden layer}) + (\text{backpropagation}) \\
 & = (6 \times 24) + 6 \\
 & = 150
 \end{aligned}$$

$$\begin{aligned}
 & \text{Total trainable parameters} \\
 & = 72120 + 4544 + 3104 + 784 + 408 + 150 \\
 & = 81110
 \end{aligned}$$