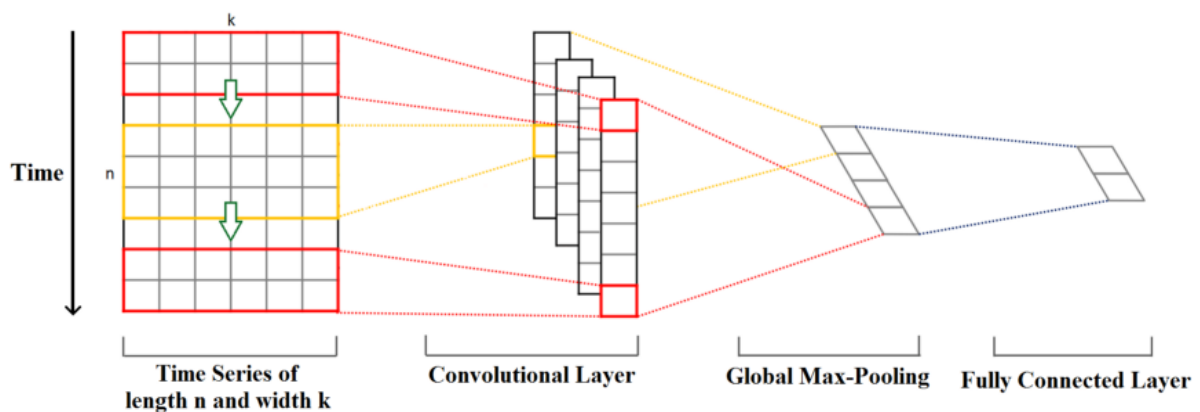


## 1-D Convolution for Time Series

Imagine a time series of length  $n$  and width  $k$ . The length is the number of timesteps, and the width is the number of variables in a multivariate time series. For example, for electroencephalography it is the number of channels (nodes on the head of a person), and for a weather time series it can be such variables as temperature, pressure, humidity etc.

The convolution kernels always have the same width as the time series, while their length can be varied. This way, the kernel moves in one direction from the beginning of a time series towards its end, performing convolution. It does not move to the left or to the right as it does when the usual 2-D convolution is applied to images.



1-D Convolution for Time Series.

The elements of the kernel get multiplied by the corresponding elements of the time series that they cover at a given point. Then the results of the multiplication are added together and a nonlinear activation function is applied to the value. The resulting value

becomes an element of a new “filtered” univariate time series, and then the kernel moves forward along the time series to produce the next value. The number of new “filtered” time series is the same as the number of convolution kernels. Depending on the length of the kernel, different aspects, properties, “features” of the initial time series get captured in each of the new filtered series.

The next step is to apply max-pooling to each of the filtered time series vectors: the largest value is taken from each vector. A new vector is formed from these values, and this vector of maximums is the final feature vector that can be used as an input to a regular fully connected layer. This whole process is illustrated in the picture above.