

$$I = (1 - p)I + p\sigma^X \otimes \sigma^X$$