

Inference of Robust Reachability Constraints

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Automatic Bug Detection

Programs have bugs

Bugs can be exploited → Vulnerabilities

```
void f() {  
    uint a, b = read();  
    if (a + b == 0)  
        /* bug */  
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Example: Symbolic Execution

- Explore the program paths
- Finds program input that exhibits the bug
- Sound: no false positives

Automatic Bug Detection

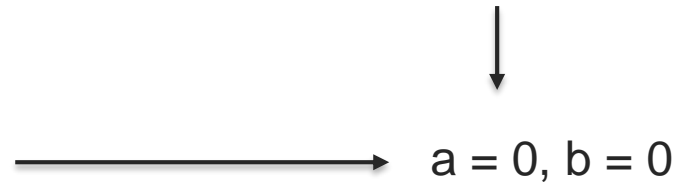
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False Positive in Practice

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False Positive in Practice

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- Depends on uncontrolled initial value (b)
- The formal result is not reliably reproducible

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Practical Causes of Unreliable Assignments

- Interaction with the environment
- Stack canaries
- Uninitialized memory/register dependency
- Choice of undefined behaviors

We need to characterize the replicability of bugs

Robust Reachability [Girol et. al., CAV 2021]

Idea

- Partition of the input space
 - What is controlled
 - What is uncontrolled

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controlled ↓ a uncontrolled ↓ b

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Focus: Reliable Bugs

- Controlled input that triggers the bug independently of the value of the uncontrolled inputs

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```

controlled \downarrow $\exists a$ uncontrolled \downarrow $\forall b$ error

Robust Reachability [Girol et. al., CAV 2021]

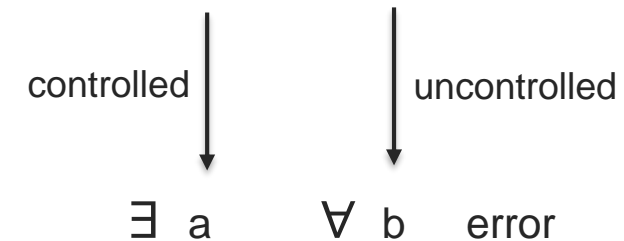
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Not Robustly Reachable

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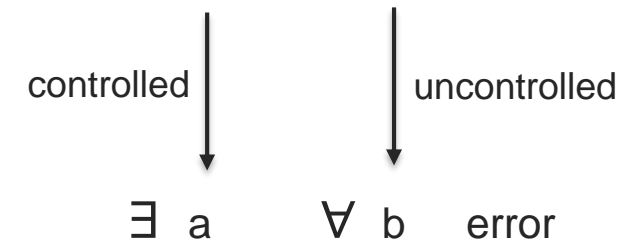
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Extension of Reachability and Symbolic Execution

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Not Robustly Reachable

The Remaining Problem

Example 3

- Memcopy with slow and fast path
- Fast path is buggy but slow path is not

```
typedef struct { unsigned char bytes[32]; } uint256_t;

void memcpy(void* dst, const void* src, size_t n) {
    if (((dst | src | n) & 0b11111))
        /* slow path */
        for (size_t i = 0; i < n; i += 1)
            dst[i] = src[i];
    else /* fast path */
        for (size_t i = 0; i <= (n >> 5); i += 1)
            (uint256_t*)dst[i] = (uint256_t*)src[i];
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buggy →

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- Reachability: Vulnerable
- Robust Reachability: Not reliably triggerable
 - Taking the fast path depends on uncontrolled initial values

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safe →

buggy →

$\exists *src, \forall src, dst, \text{ overflow?}$

Not Robustly Reachable

The bug is serious but not robustly reachable – The concept is too strong

Robust Reachability Constraints

Definition

- Predicate on program input sufficient to have Robust Reachability

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$\exists *src, \forall src, dst, \boxed{src \% 32 = 0 \wedge dst \% 32 = 0} \Rightarrow \text{overflow}$

(src and dst aligned on 32bits)

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- Part of the Robust Reachability framework
- Allows precise characterization

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How to Automatically Generate Such Constraints?

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Contributions

- **New program-level abduction algorithm for Robust Reachability Constraints Inference**
 - Extends and generalizes Robustness, made more practical
 - Adapts and generalizes theory-agnostic logical abduction algorithm
 - Efficient optimization strategies for solving practical problems
- **Implementation of a restriction to Reachability and Robust Reachability**
 - First evaluation of software verification and security benchmarks
 - Detailed vulnerability characterization analysis in a fault injection security scenario

Target: Computation of ϕ such that $\exists C$ *controlled value*, $\forall U$ *uncontrolled value*, $\phi(C, U) \Rightarrow reach(C, U)$

Abduction of Robust Reachability Constraints

Abductive Reasoning

[Josephson and Josephson, 1994]

- Find missing precondition of unexplained goal
- Compute ϕ_M in $\phi_H \wedge \phi_M \models \phi_G$

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Theory-Specific Abduction

[Bienvenu 2007, Tourret et. al. 2017]

- Handle a single theory

Specification Synthesis

[Albarghouthi et. al. 2016, Calcagno et. al. 2009, Zhou et. al. 2021]

- White-box program analysis

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Theory-Agnostic First-order Abduction

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- Efficient procedures
- Genericity

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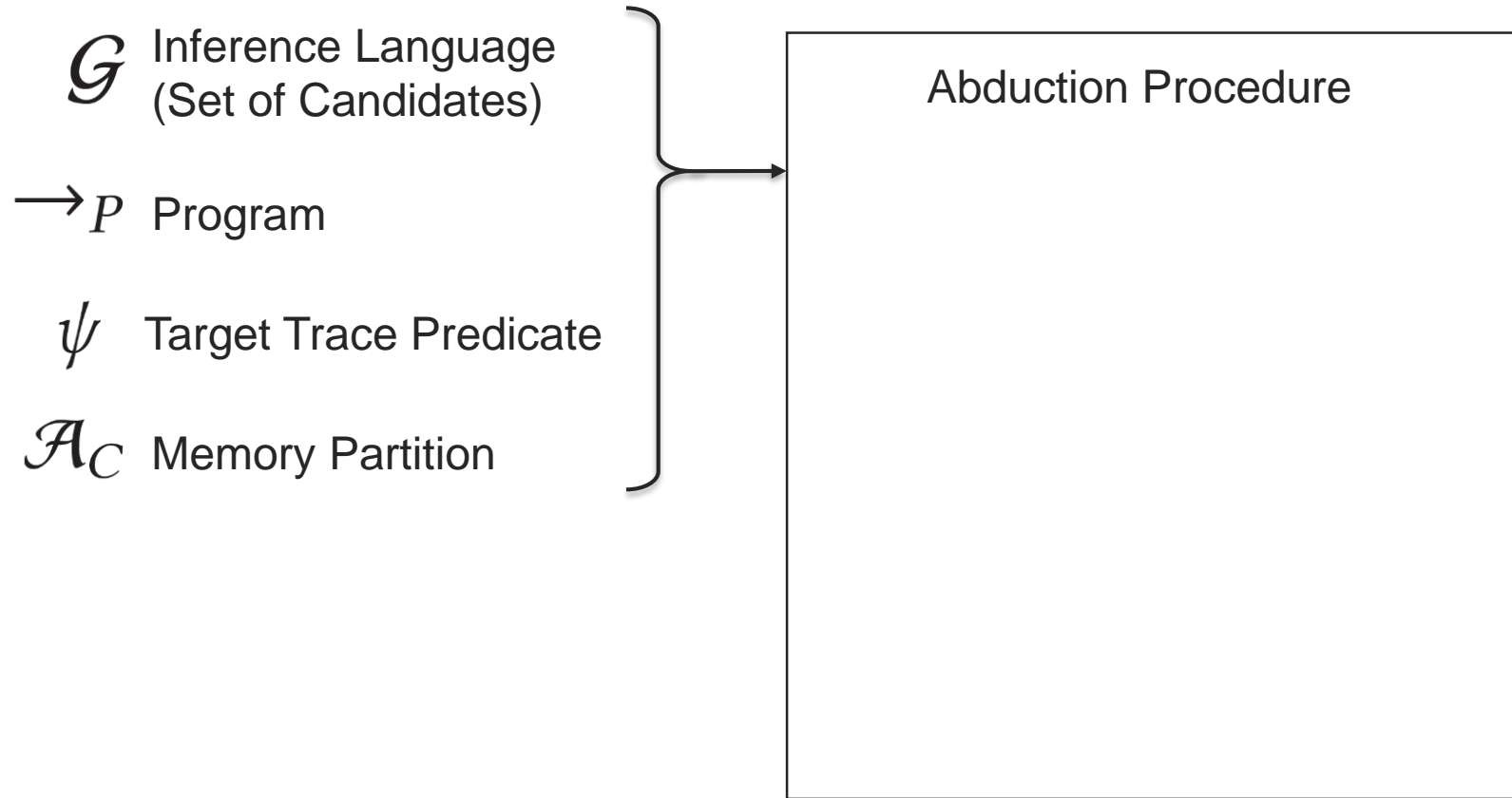
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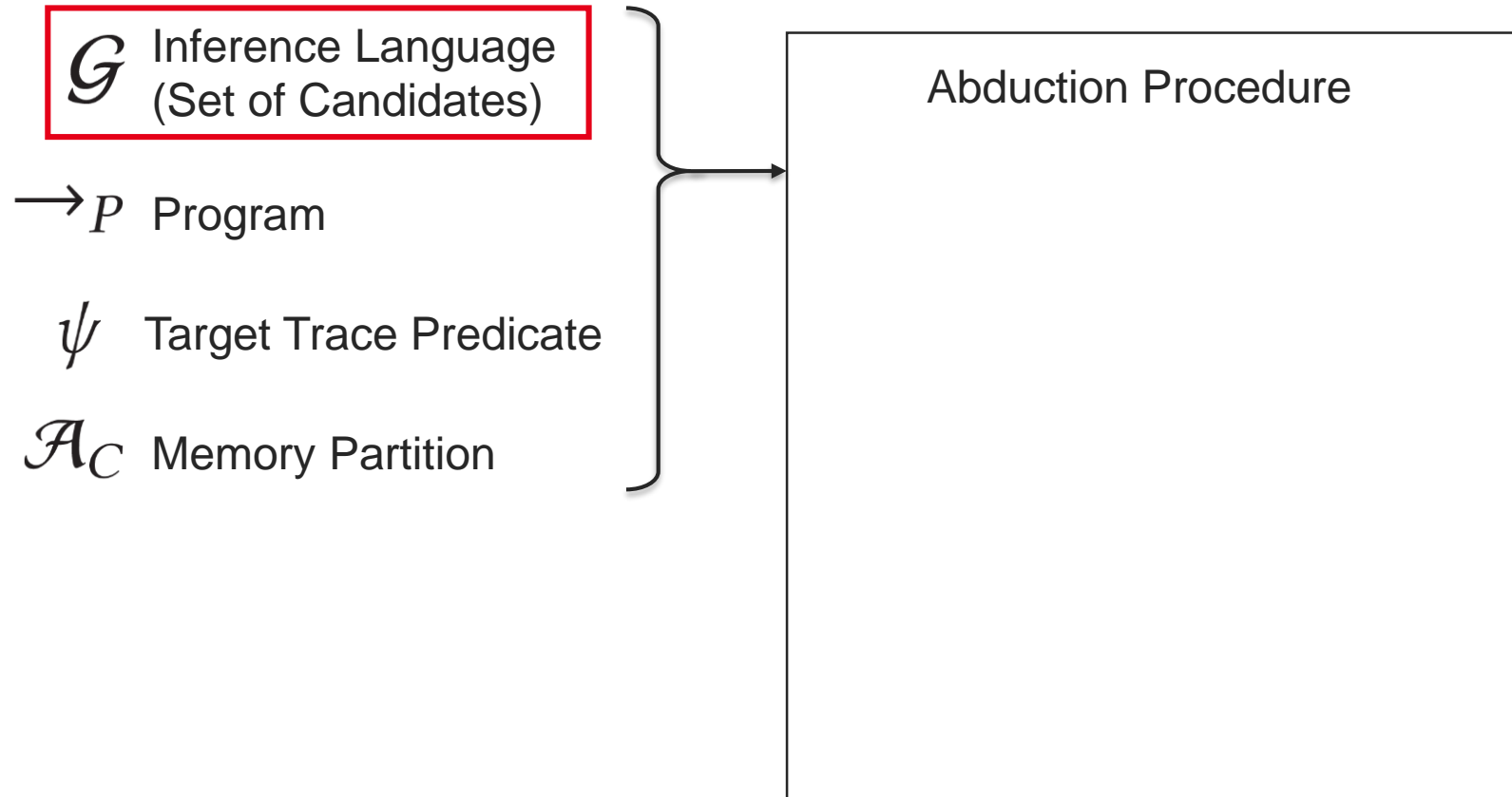
Our Proposal: Adapt Theory-Agnostic Abduction Algorithm to Compute Program-level Robust Reachability Constraints

- Program-level
- Generic

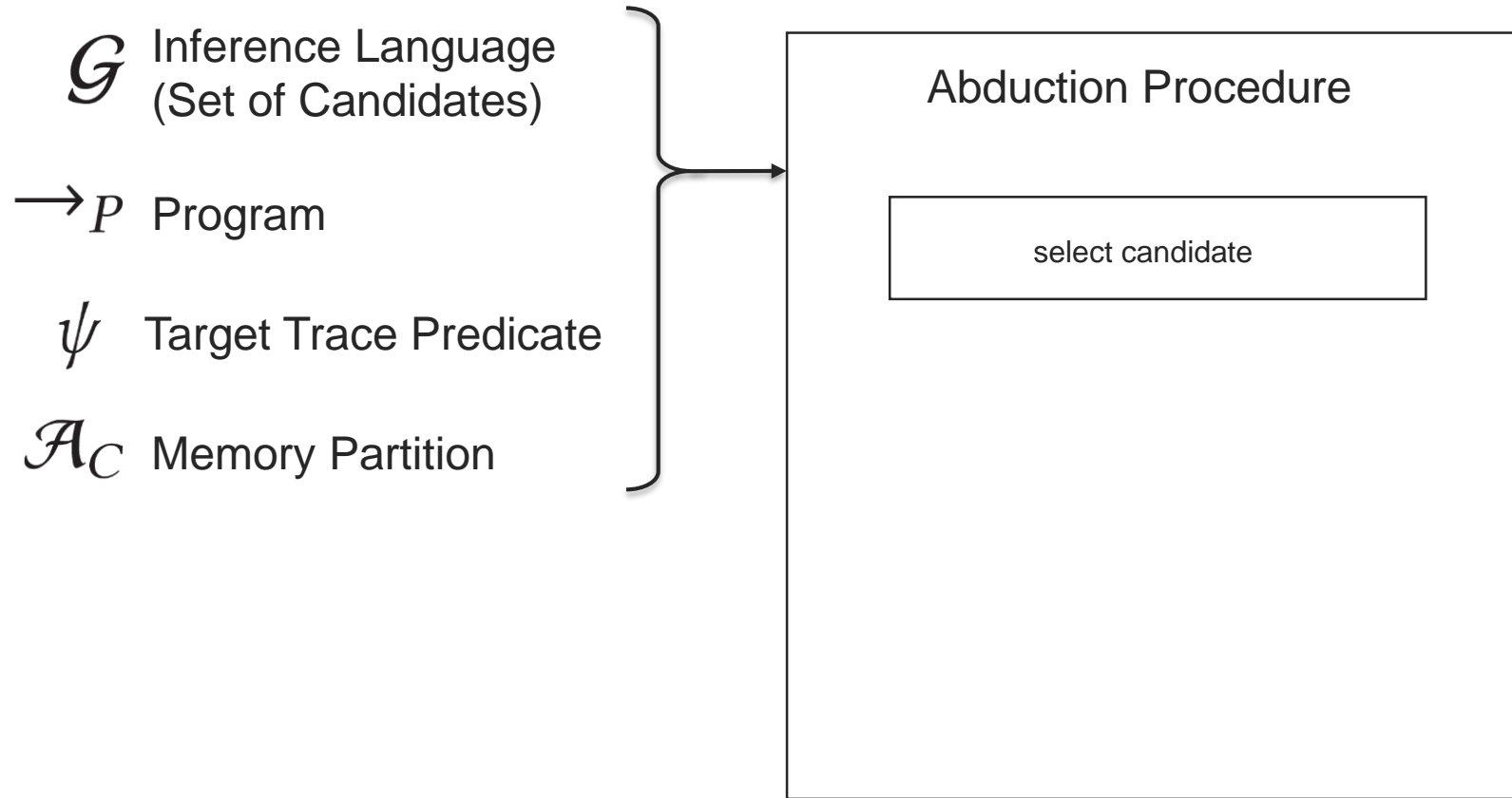
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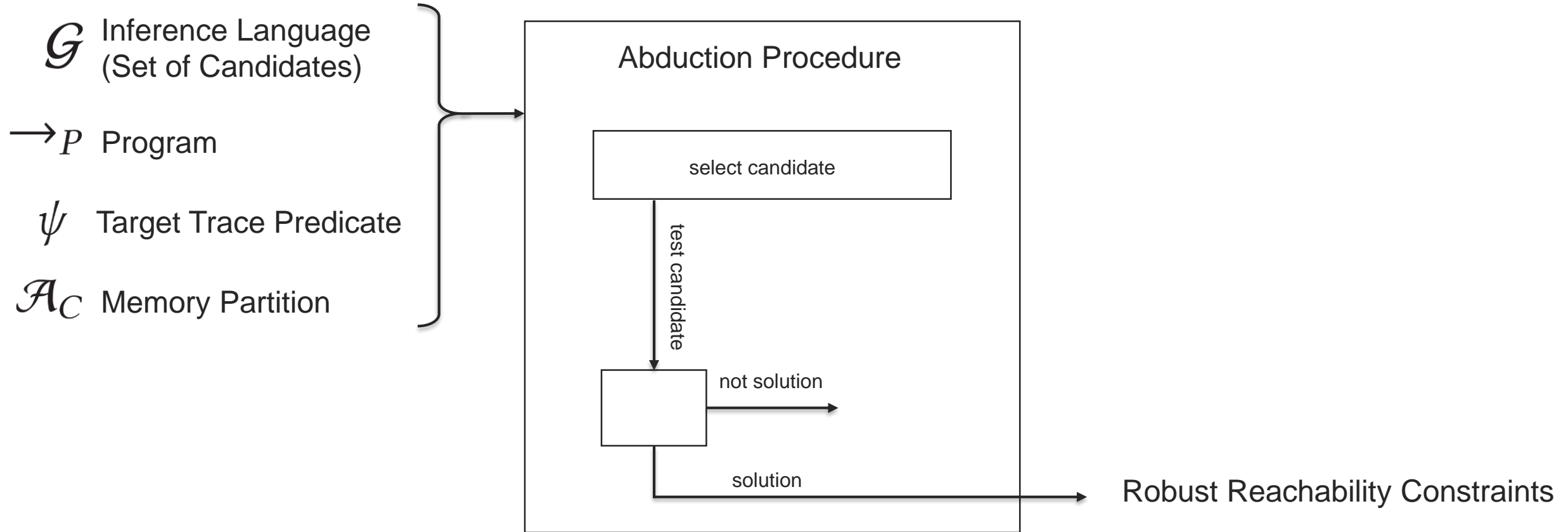
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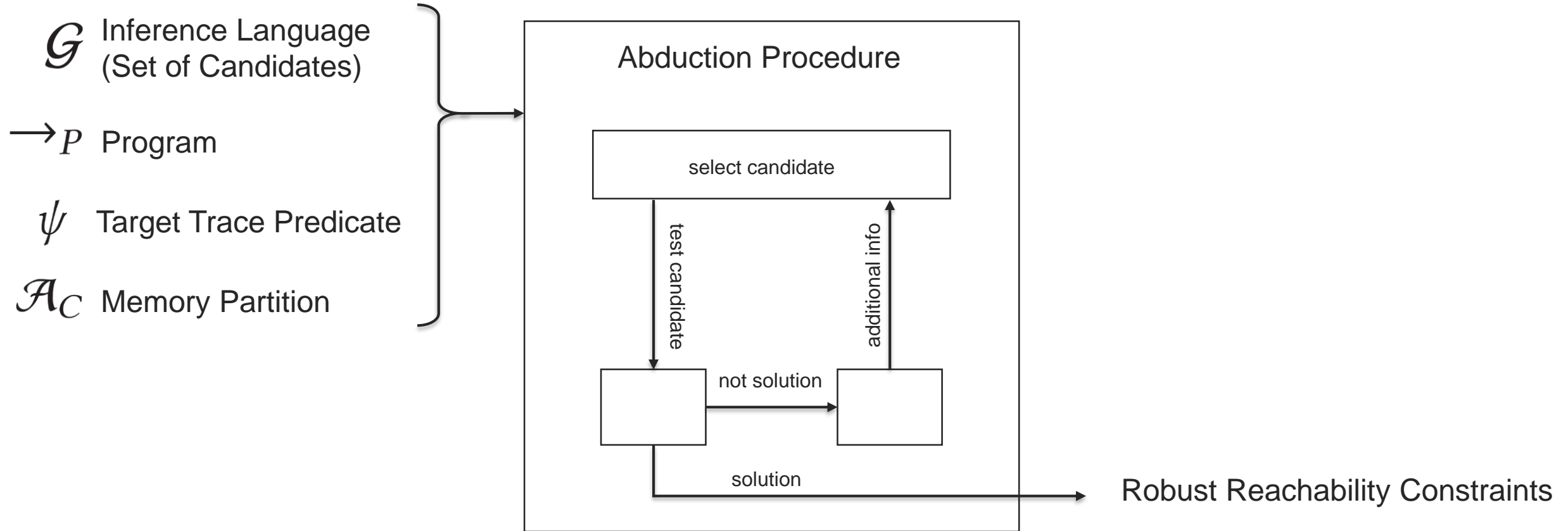
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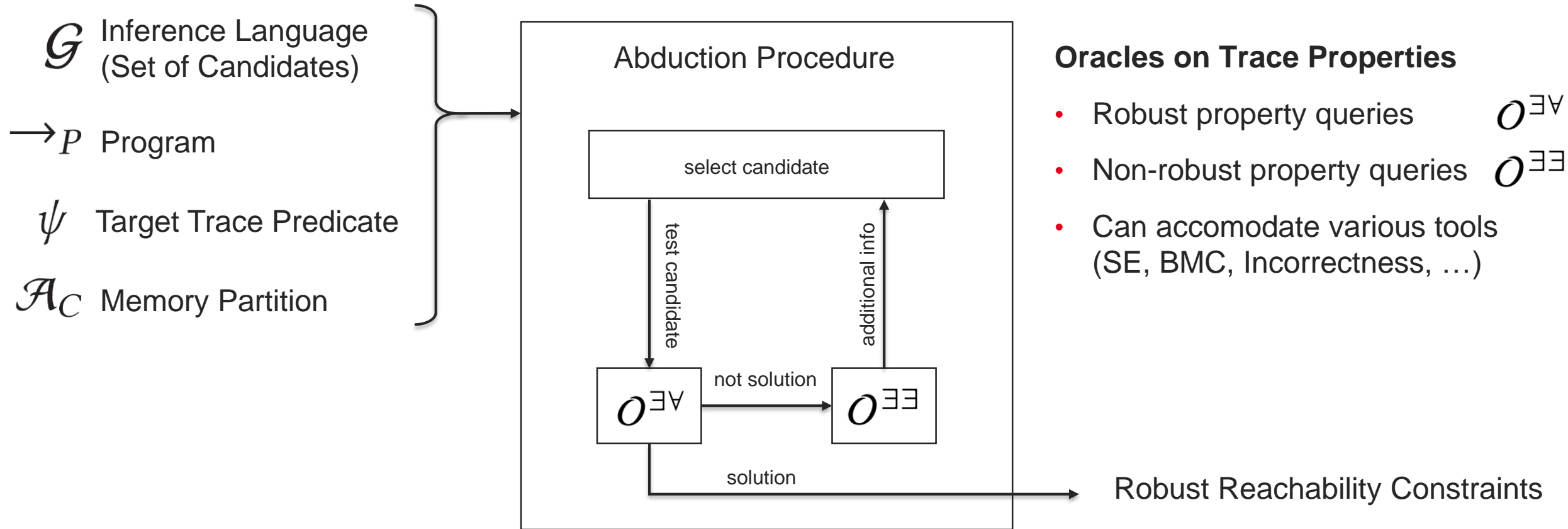
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Our Solution (Baseline Algorithm)

$\text{BASELINERCINFER}(\mathcal{G}, \rightarrow_P, \psi, \mathcal{A}_C)$

```
1 if  $\top, s \leftarrow O^{\exists\exists}(\rightarrow_P, \psi, \top)$  then
2    $R \leftarrow \{y = s\}$  if  $y = s \in \mathcal{G}$  else  $\emptyset$ ;
3   for  $\phi \in \mathcal{G}$  do
4     if  $O^{\exists\forall}(\rightarrow_P, \mathcal{A}_C, \psi, \phi)$  then
5        $R \leftarrow \Delta_{\min}(R \cup \{\phi\})$ ;
6       if  $\neg O^{\exists\exists}(\rightarrow_P, \psi, \neg(\bigvee_{\phi' \in R} \phi'))$  then
7         return  $R$ ;
8   return  $R$ ;
9 return  $\{\perp\}$ ;
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Theorem:

- **Termination** when the oracles terminate
- **Correction** at any step when the oracles are correct
- **Completeness** w.r.t. the inference language when the oracles are complete

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- Under correction and completeness of the oracles
 - **Minimality** w.r.t. the inference language
 - **Weakest** constraint generation when expressible

Making it Work



The Issue

- Exhaustive exploration of the inference language is inefficient

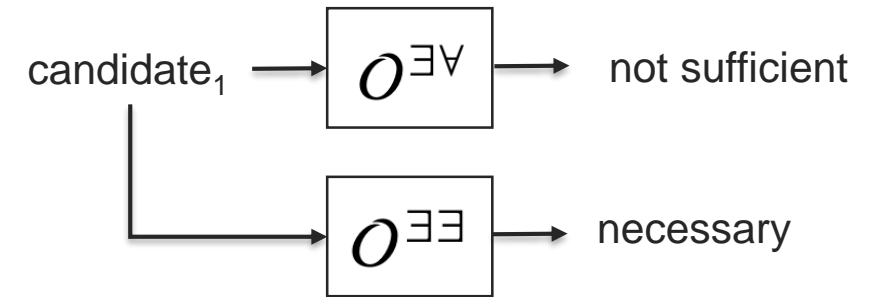
Key Strategies for Efficient Exploration

- Necessary constraints
- Counter-examples for Robust Reachability
- Ordering candidates

Making it Work: Necessary Constraints

The Idea

- Find and store Necessary Constraints



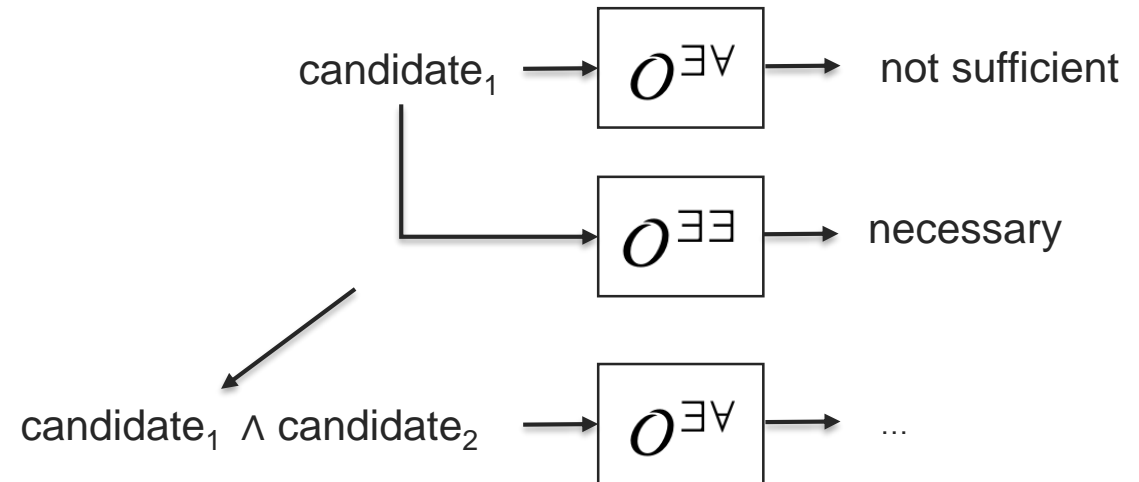
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Usage

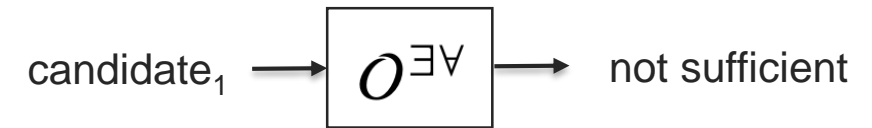
- Build a candidate solution faster
- Additional information on the bug
- Emulate unsat core usage in the context of oracles



Making it Work: Counter-Examples

The Idea

- Reuse information from failed candidate checks



The Issue

- Non Robustness ($\forall\exists$ quantification) does not give us counter-examples

Making it Work: Counter-Examples

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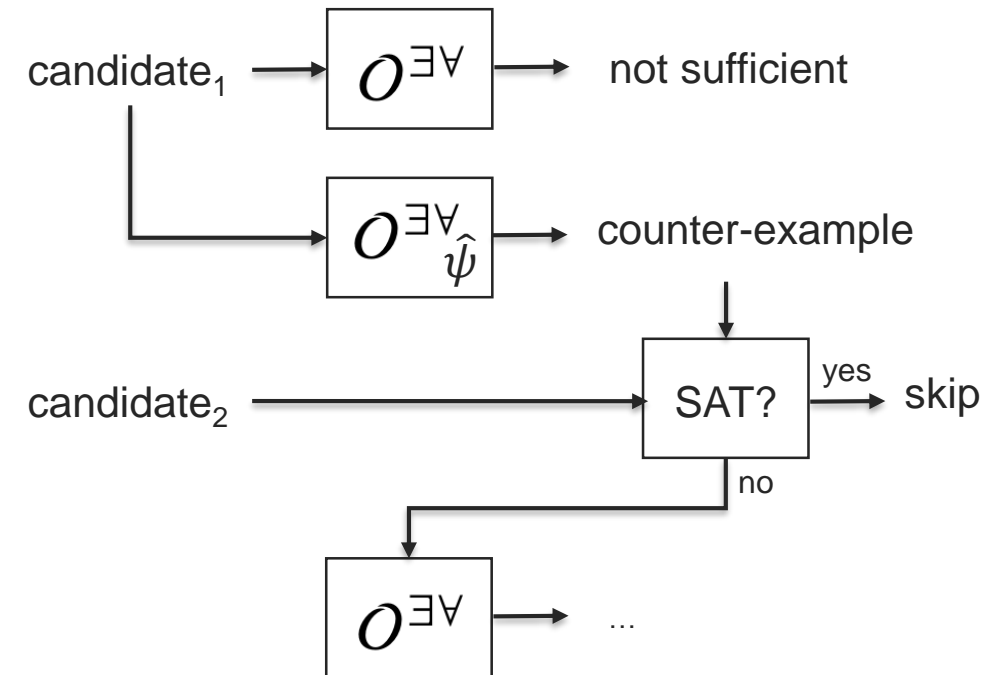
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Proposal

- Use a second trace property that ensures the bug does not arise
- Prune using these counter-examples



Experimental Evaluation

Implementation BINSEC

- (Robust) Reachability on binaries
- Tool: **BINSEC** [Djoudi and Bardin 2015]
- Tool: **BINSEC/RSE** [Girol at. al. 2020]

Prototype

- **PyAbd**, Python implementation of the procedure
- Candidates: Conjunctions of equalities and disequalities on memory bytes

Research Questions

- 1) Can we compute non-trivial constraints?
- 2) Can we compute weakest constraints?
- 3) What are the algorithmic performances?
- 4) Are the optimization effective?

Benchmarks

- Software verification (SVComp extract + compile)
- Security evaluation (FISSC, fault injection)

Results: Generating Constraints (RQ1, RQ2)

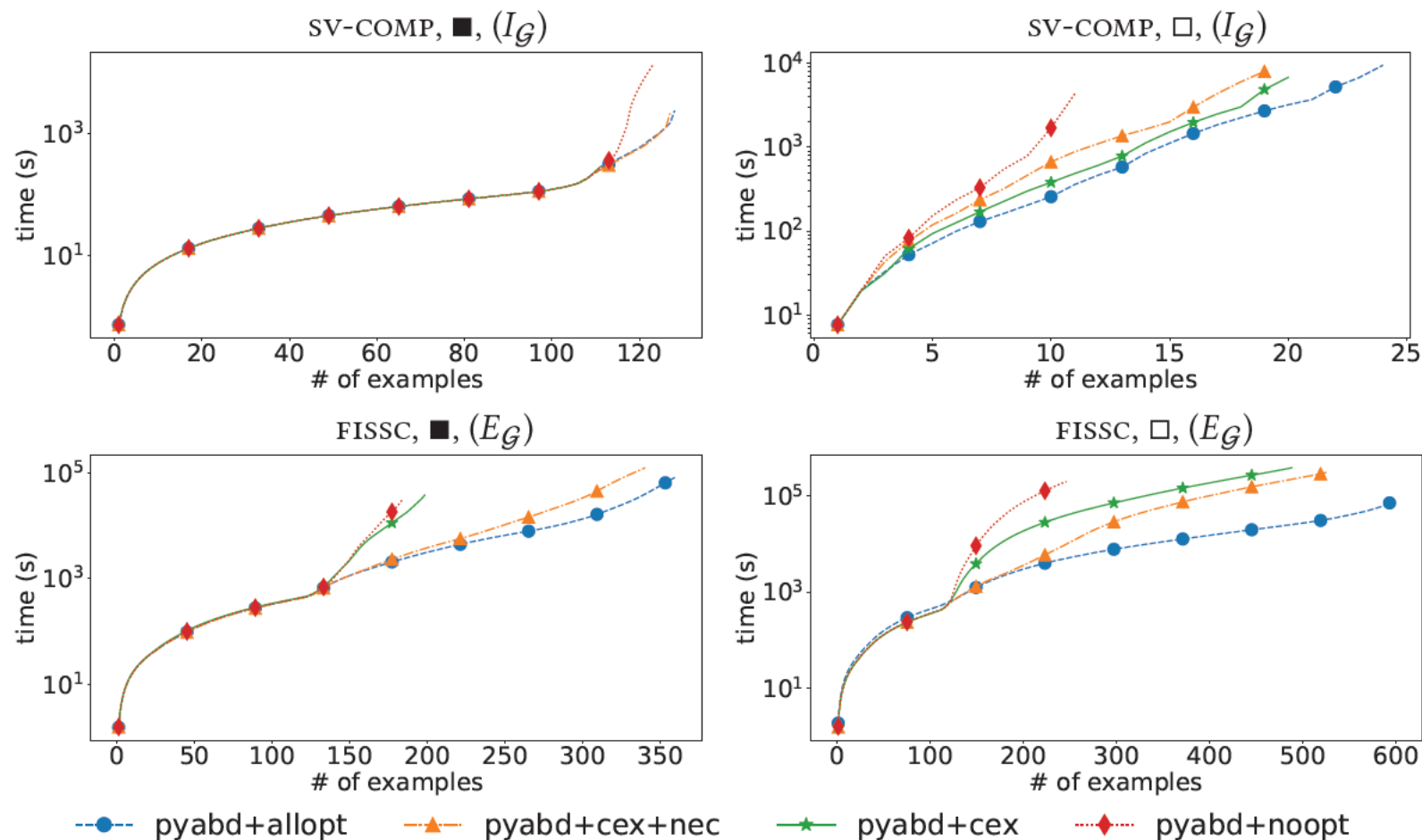
	SV-COMP ($E_{\mathcal{G}}$)		SV-COMP ($I_{\mathcal{G}}$)		FISSC ($E_{\mathcal{G}}$)		FISSC ($I_{\mathcal{G}}$)	
	■	□	■	□	■	□	■	□
# programs	147	64	147	64	719	719	719	719
# of robust cases	111	3	111	3	129	118	129	118
# of sufficient rrc	122	5	127	24	359	598	351	589
# of weakest rrc	111	3	120	4	262	526	261	518

Inference languages

- (dis-)Equality between memory bytes ($E_{\mathcal{G}}$)
- + Inequality between memory bytes ($I_{\mathcal{G}}$) → More expressivity but more candidates

We can find more reliable bugs than Robust Symbolic Execution

Results: Influence of the ‘Efficient Strategies’ (RQ4)



Significantly improves the capabilities of the method

Each strategy matters

Fig. 5. Cactus plot showing the influence of the strategies of Section 5 on the computation of the first sufficient k -reachability constraint with PyABD.

Results: Vulnerability Characterization on a Fault-Injection Benchmark

	PyABD	BINSEC/RSE	BINSEC
unknown	170	273	170
not vulnerable (0 input)	4414	4419	3921
vulnerable (≥ 1 input)	226	118	719
$\geq 0.0001\%$	226	118	—
$\geq 0.01\%$	209	118	—
$\geq 0.1\%$	173	118	—
$\geq 1.0\%$	167	118	—
$\geq 5.0\%$	166	118	—
$\geq 10.0\%$	118	118	—
$\geq 50.0\%$	118	118	—
100.0%	118	118	—

Our Solution:

- Finds and characterize vulnerabilities in-between Reachability and Robust Reachability

Conclusion

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- We propose a precondition inference technique to improve the capabilities of Robust Reachability
- We adapt theory-agnostic abduction algorithm to $\exists\forall$ formulas and apply it at program-level through oracles
- We demonstrates its capabilities on simple yet realistic vulnerability characterization scenarii



(hiring)



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Preconditions **explain** the vulnerability
Can be reused for understanding, counting, comparing



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Questions?



(hiring)

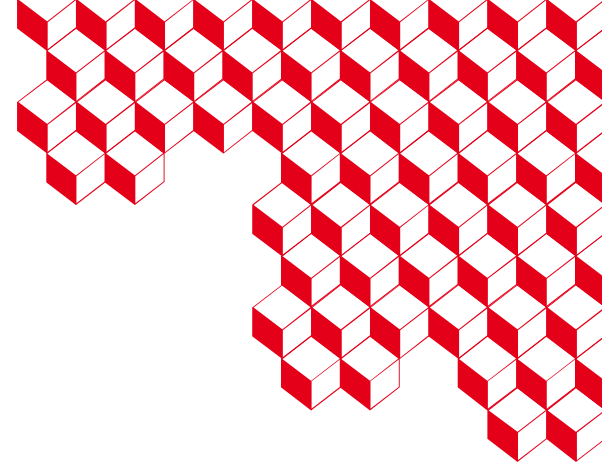


Questions



(hiring)





Results: Example of FISSC Constraints

- $\text{CardPIN}[0] == \text{UserPIN}[0] \ \&\& \ \text{UserPIN}[0] == 3$
Authentication when first digit is 3
- $\text{UserPIN}[0] == \text{UserPIN}[1] \ \&\& \ \text{UserPIN}[0] == \text{UserPIN}[2] \ \&\& \ \text{UserPIN}[0] == \text{UserPIN}[3] \ \&\& \ \text{UserPIN}[0] \neq 0$
Authentication when all digits are equal and non zero
- $\text{CardPIN}[2] \neq \text{UserPIN}[2] \ \&\& \ \text{CardPIN}[3] == \text{UserPIN}[3] \ \&\& \ \text{UserPIN}[1] == 5$
Authentication when we know the last digit, the 3rd is not correct and the 2nd is 5.
- $R0 == \text{UserPIN}[3] \ \&\& \ \text{UserPIN}[3] == \text{UserPIN}[2] \ \&\& \ \text{UserPIN}[3] == \text{UserPIN}[1] \ \&\& \ \text{UserPIN}[3] == \text{UserPIN}[0]$
Authentication with four time the initial value of R0
- $R2 = 0xaa \ \&\& \ R1 \neq 0x55 \ \&\& \ R1 \neq 0$
Authentication if R2=0xaa initially and R1 distinct from both 0x55 and 0x00 initially

Making it Work: Ordering Candidates



The Idea

- Some candidates are more likely to be solutions
- Try to guess which ones and try them first

What we already have

- Examples satisfying the goal
- Syntactic information on the candidates

Proposal

- Use an ordering heuristic on the candidates

$$\phi \mapsto (\text{count}(\wedge, \phi), -\text{CARD}(\{s \in V \mid \phi[s]\}))$$

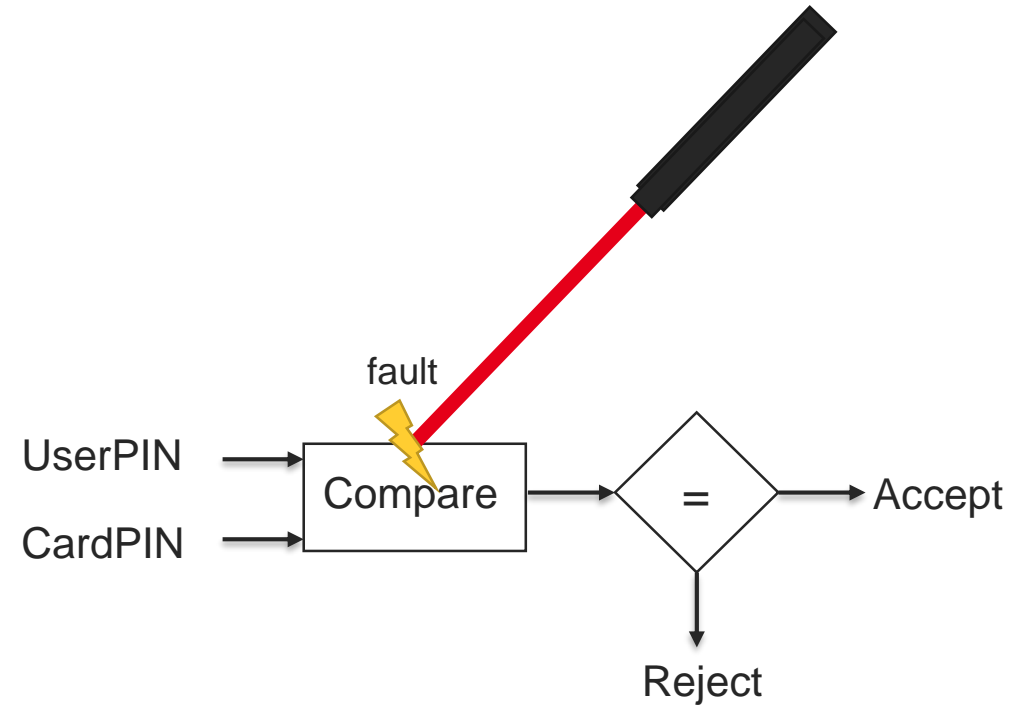
Benchmark: FISSC

Fault Injection Attacks

- Physical perturbation of the system executing the program
- Changes the program behavior
- Leverages new vulnerabilities
- Goal: Characterize these vulnerabilities

VerifyPINs

- 10 protected implementations
- 4800 faulted binary programs



Benchmark: SVComp

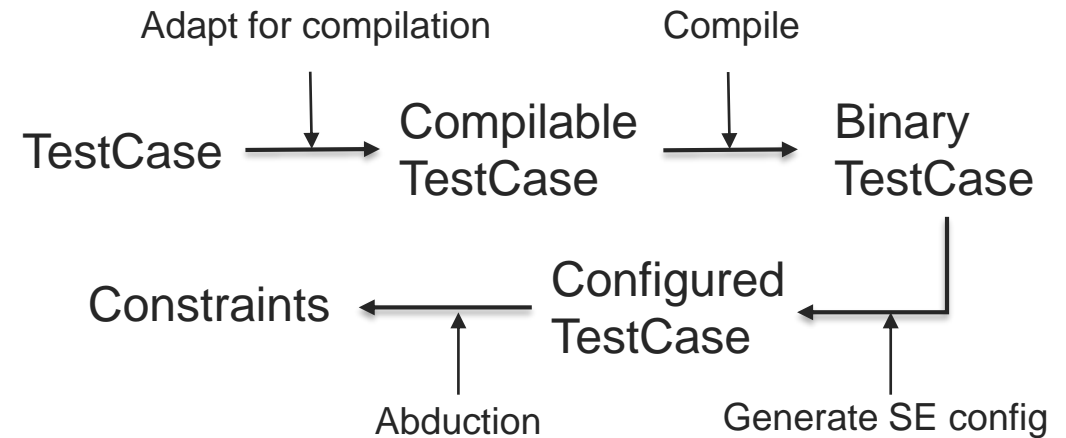
SVComp

- Collection of software verification tasks
- Evaluate the generative capabilities of our method
- Select 147 reachable reachability test cases for which BINSEC answers under 1 minute

Setup

- Use the target location of the benchmark
- Use the input variables as program input
- Abduce constraints on these variables to reach the target location

Process



Example

```
void init (int* x)
{
    for (int i = 0; i < 4; i++)
        x[i] = __VERIFIER_nondet_int();
}

int verify(int * x)
{
    int stuff[4] = { 1, 2, 3, 4 };
    for (int i = 0; i < 4; i++)
        if (x[i] != stuff[i])
            return 1;
    return 0;
}
```

```
int main ()
{
    int x[4];

    init(x);
    assert(verify(x) != 0);

    return 0;
}
```

Inference Languages

Program Variables

$$\Sigma \mathcal{A}_8, \Sigma \mathcal{A}_{32}, \Sigma \mathcal{V}_8, \Sigma \mathcal{V}_{32}$$

Equalities

$$*a_8 = *a'_8 \quad *a_{32} = *a'_{32}$$

$$*a_8 = v_8 \quad *a_{32} = v_{32}$$

Register-Memory Bytes Equalities

$$*a_{32} = 0x000000:(*a_8)$$

$$*a_{32} = 0x000000:v_8$$

Inequalities, Negation, Conjunction

$$*a_8 \leq *a'_8 \quad \neg \langle nliteral \rangle$$

$$*a_{32} \leq *a'_{32}$$

$$*a_8 \leq v_8 \quad \langle constraint \rangle \wedge \langle constraint \rangle$$

Two Inference Languages

- One with equalities and disequalities ($E_{\mathcal{G}}$)
- One with added inequalities ($I_{\mathcal{G}}$)

Controlled Variables

- Recovered from the Symbolic Execution Queries
- One setup with controlled variables ☒
- One setup without ☐

Final Algorithm

Algorithm 2: ARCINFER($\mathcal{G}, \rightarrow_P, \psi, \hat{\psi}, \mathcal{A}_C, \text{prunef}$)

Input: \mathcal{G} : inference language, \rightarrow_P : program, ψ : prop, $\hat{\psi}$: prop breaking ψ , \mathcal{A}_C : controlled variables, prunef: strategy flags
Output: R : sufficient constraints, N : necessary constraints, U : breaking constraints
Note: O^{33} : trace property oracle, O^{3V} : robust trace property oracle

```

1 if  $\mathcal{T}, s \leftarrow O^{33}(\rightarrow_P, \psi, \mathcal{T})$  then // ensure  $\psi$  satisfiable
2    $V \leftarrow \{s\};$  // init satisfying memory states examples
3    $R, N, U \leftarrow \{y = s\} \text{ if } y = s \in \mathcal{G} \text{ else } \emptyset, \{\mathcal{T}\}, \{\perp\};$  // init result sets
4   while  $\phi_K, \phi, \delta_N, \delta_R \leftarrow \text{NEXTRC}(\mathcal{G}, \rightarrow_P, \psi, \hat{\psi}, \mathcal{A}_C, V, R, N, U, \text{prunef})$  do // explore
5     if  $\delta_R$  and  $\mathcal{T}, s \leftarrow O^{33}(\rightarrow_P, \psi, \phi)$  then // ensure  $\psi$  satisfiable under  $\phi$ 
6        $V \leftarrow V \cup \{s\};$  // new trace example
7       if  $O^{3V}(\rightarrow_P, \mathcal{A}_C, \psi, \phi)$  then // check candidate  $\phi$ 
8          $R \leftarrow \Delta_{\min}(R \cup \{\phi\});$  // update and minimize  $R$ 
9         if  $\neg O^{33}(\rightarrow_P, \psi, \neg(\bigvee_{\phi \in R} \phi))$  then // check weakest
10           return  $(R, \bigvee_{\phi \in R} \phi', U);$ 
11       else
12          $U \leftarrow U \cup \{\phi\};$  // new breaking constraint
13     else if  $\delta_R$  then
14        $N \leftarrow N \cup \{\neg\phi\};$  // new necessary constraint
15     if  $\delta_N$  and  $\neg O^{33}(\rightarrow_P, \psi, \neg\phi_K)$  then
16        $N \leftarrow N \cup \{\phi_K\};$  // new necessary constraint
17   return  $(R, N, U);$ 
18 return  $(\{\perp\}, \{\perp\}, \{\perp\});$ 

```

Algorithm 3: NEXTRC($\mathcal{G}, \rightarrow_P, \psi, \hat{\psi}, \mathcal{A}_C, V, R, N, U, \text{prunef}$)

Input: \mathcal{G} : inference language, \rightarrow_P : program, ψ : prop, $\hat{\psi}$: prop breaking ψ , \mathcal{A}_C : controlled variables, V : examples of input states of \rightarrow_P satisfying ψ , R : known sufficient constraints, N : known necessary constraints, U : known breaking constraints, prunef: strategy flags
Output: ϕ_K : core candidate, ϕ : candidate, δ_N : check for necessary flag, δ_R : check for sufficient flag
Note: O^{33} : oracle for trace property satisfaction, O^{3V} : oracle for robust trace property satisfaction

```

1  $\bar{V} \leftarrow \emptyset;$  // init. counter-examples
2 for  $\phi_K \in \text{browse}(\mathcal{G}, V)$  if prunef.browse else  $\mathcal{G}$  do // get candidate from  $\mathcal{G}$ 
3    $\phi \leftarrow \phi_K \wedge \bigwedge_{\phi' \in \text{max}(\phi_K, \mathcal{G}, N)} \phi';$  if prunef.nec else  $\phi_K;$  // add nec. constraints
4   if  $\phi$  is unsatisfiable then
5     continue; // skip: inconsistent
6   if prunef.cex and  $\exists m, X \in \bar{V}, \phi \wedge y|x = m$  is satisfiable then
7     continue; // skip: sat. by counter-example
8   if  $\exists \phi_s \in R, \phi \models \phi_s$  then
9     continue; // skip: stronger than known suff. constraint
10  if prunef.nec and  $\exists \phi_u \in U, \phi_u \models \phi$  then
11    continue; // skip: weaker than known break. constraint
12  if prunef.nec and  $(\bigwedge_{\phi_n \in N} \phi_n) \models \phi$  then
13    continue; // skip: weaker than known nec. constraint
14  if prunef.cex and  $\mathcal{T}, \text{cex} \leftarrow O^{3V}(\rightarrow_P, X, \hat{\psi}, \phi)$  for  $X \subseteq \mathcal{A} \setminus \mathcal{A}_C$  then
15     $\bar{V} \leftarrow \bar{V} \cup \{\text{cex}\}, X;$  // new counter-example
16    yield  $\phi_K, \phi, \text{prunef.nec}, \perp;$  // forward for nec. check
17  else
18    yield  $\phi_K, \phi, \text{prunef.nec}, \mathcal{T};$  // forward for nec. and suff. checks

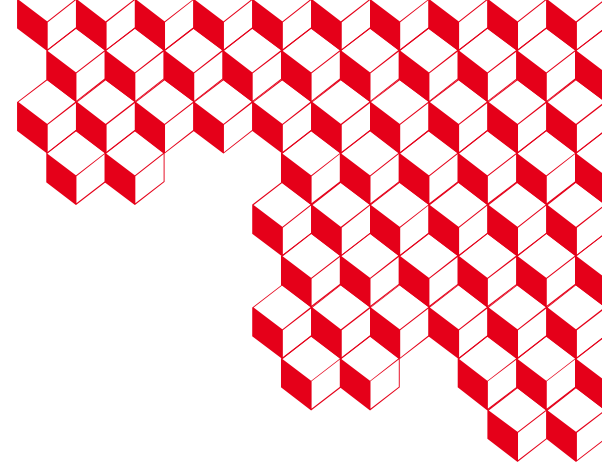
```

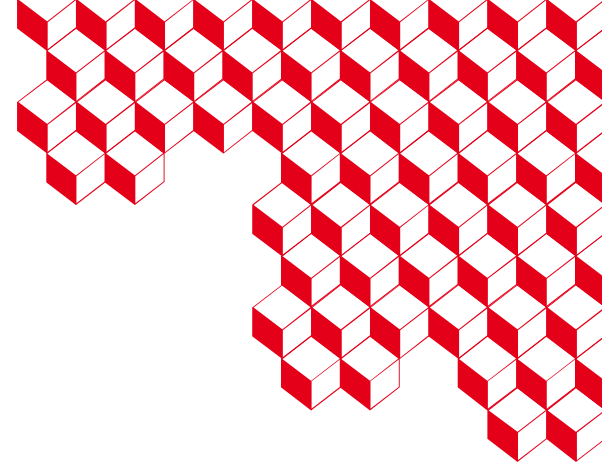
Theorem

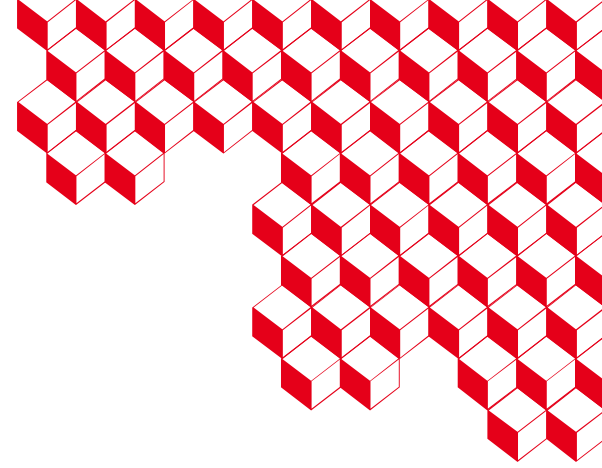
- Termination, Correction, Completeness are preserved
- Correction for necessary constraints at any step
- Minimality is preserved modulo equivalence between formulas
- Weakest constraints generation on given return is preserved

Remarks

- Generic procedure definition with oracle queries abstraction
- The previously described strategies can be activated/deactivated
- Can be applied to a larger range of program properties (reachability, safety, hypersafety)
- If SMT-Solvers are used as oracles, can be used an $\exists\forall$ abduction solver







Robust Reachability Examples

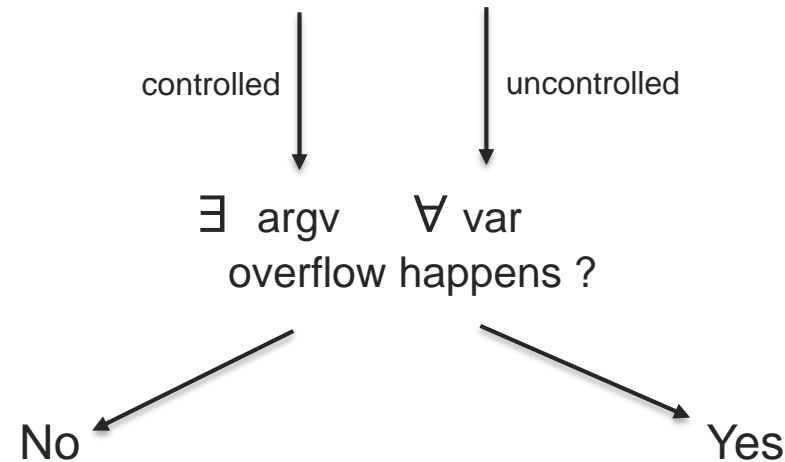
Example 1

```
void memcpy1(char* dst, const char* src, size_t n) {  
    for (size_t i = 0; i < n; i += 1)  
        dst[i] = src[i];  
}
```

Example 2

```
void memcpy2(char* dst, const char* src, size_t n) {  
    for (size_t i = 0; i <= (n >> 3); i += 1)  
        (uint64_t*)dst[i] = (uint64_t*)src[i];  
}
```

```
void main(const char* argv) {  
    char buf[64];  
    char var = random();  
    memcpy(buf, argv, 64);  
    assert(var != 0xee);  
    return 0;  
}
```



Motivation (1)

```
void f(const char* input) {
    char buf[64] = {0};
    memcpy(buf, input, 64);
    buf[63] = 0;
    return
}

void g() { puts("hijacked"); }

void memcpy1(void* dst, const void* src, size_t n) {
    /* assume src[n - 1] == 0 */
    size_t i = 0;
    while (*((uint8_t*) src + i) != 0)
        *((uint8_t*) dst + i) = *((uint8_t*) src + i++);
}
```

Automatic Detection and Characterization of Bugs

Example: Buffer Overflow

- Overwriting the return address by copying too much data

Automatic Detection: Symbolic Execution

- Look for paths reaching g()
- Express paths as logical predicates
- Use an SMT-Solver to evaluate the feasibility of the path
- Conclusion: memcpy1 is buggy

Motivation (2)

```
void memcpy2(void* dst, const void* src, size_t n) {
    uint32_t canary = 0xdeadbeef;
    size_t i = 0;
    while (*((uint8_t*) src + i) != 0)
        *((uint8_t*) dst + i) = *((uint8_t*) src + i++);
    if (canary != 0xdeadbeef) exit(-2);
}
```

Possible counter-measure: Canary Implementation

- Unless the attacker knows the canary (or is lucky), prevents branching to g()

Symbolic Execution Evaluation

- memcpy2 is buggy
- No difference between memcpy1 and memcpy2

Robust Symbolic Execution [Girol et. al. 2020]

- Partition the input space: what an attacker controls x what an attacker doesn't control
- Build reaching controlled inputs that do not depend on the value of the uncontrolled memory
- $\exists c, controlled, \forall u, uncontrolled, reach_g(c, u)$
- Conclusion:
 - memcpy1 is buggy
 - memcpy2 is not

Motivation (3)

```
typedef struct { unsigned char bytes[32]; } uint256_t;

void memcpy3(void* dst, const void* src, size_t n) {
    if (((intptr_t) dst | (intptr_t) src | n) & 0b11111)
        /* slow path */
        for (size_t i = 0; i < n; i += 1)
            *((uint8_t*) dst + i) = *((uint8_t*) src + i);
    else /* fast path */
        for (size_t i = 0; i <= (n >> 5); i += 1)
            *((uint256_t*) dst + i) = *((uint256_t*) src + i);
}
```

Only one path is buggy (fast path)

- Overflow is only possible if both dst and src are aligned on 32bits
- This is not an unrealistic precondition

Problem with Robust Symbolic Execution

- memcpy3 is not buggy

We need a more precise bug characterization method to distinguish between such cases

- Our proposal: use assumptions on top of robust reachability
- $\exists c, \forall u, \text{assumption}(c, u) \Rightarrow \text{reach}_g(c, u)$
- Example: $\text{dst} \% 32 = 0 \wedge \text{src} \% 32 = 0$
- Helps express that memcpy3 is more vulnerable than memcpy2

Contributions

1. Abduction Procedure for Robust Assumptions of Program Trace Properties

- A. Preliminaries
- B. Framework
- C. Baseline Algorithm

2. Efficient Strategies for Abduction under Robustness

- A. Necessary Constraints
- B. Counter-Examples
- C. Ordering Heuristic

3. Experimental Evaluation and Application to Realistic Security Evaluation Scenarios

- A. Implementation, Benchmark and Setup
- B. Generation Capabilities
- C. Influence of the Strategies
- D. Vulnerability Characterization



Abduction Procedure for Robust Assumptions of Program Trace Properties

1 ■

Abduction of Robust Assumptions

Abductive Reasoning [Josephson and Josephson, 1994]

- Search for missing precondition to entail an unexplained goal
- Compute ϕ_M in $\phi_H \wedge \phi_M \models \phi_G$
- Efficient procedures exist for computation of theory-agnostic first-order solutions [Echenim et al. 2018, Reynolds et al. 2020]

Program-level Abduction

- Goal: Predicate on program traces ψ
- Search for a predicate on program inputs that entails ψ for the given program

Trace Predicate Oracles

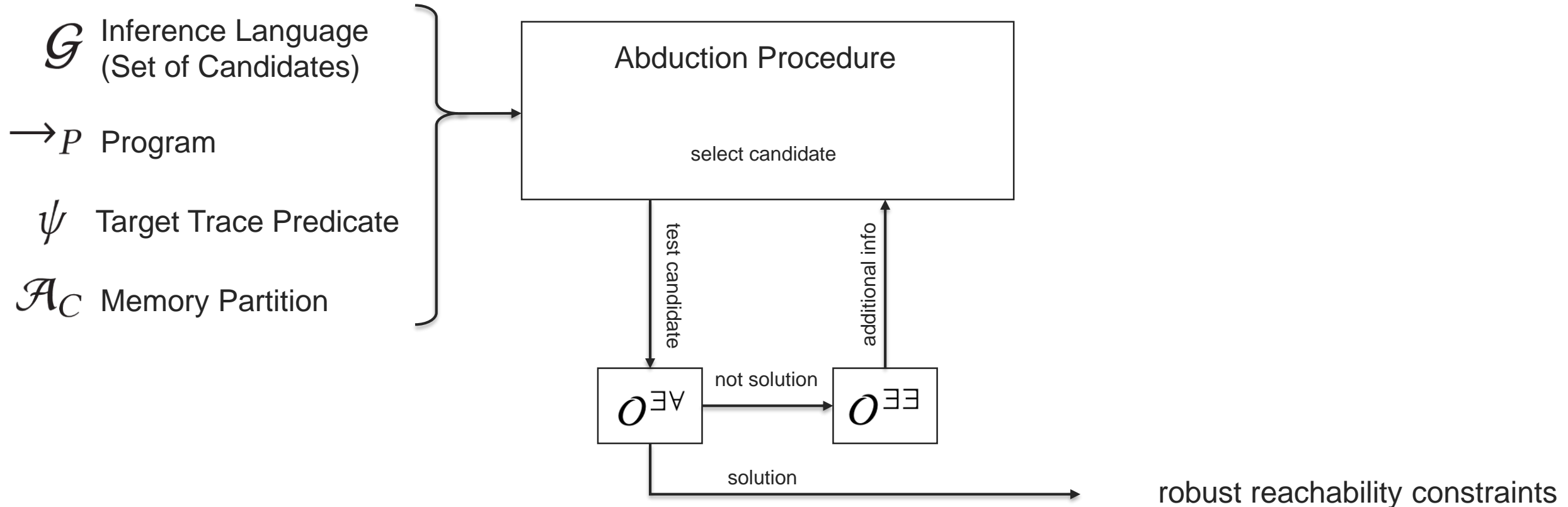
- We assume the existence of oracles (tools)
- Checking whether a trace predicate is satisfiable for a program under an assumption

$$O^{\exists\exists}(\rightarrow_P, \psi, \phi)$$

- Checking whether a trace predicate is robustly satisfiable for a program under an assumption and a given controlled/uncontrolled input partition

$$O^{\exists\forall}(\rightarrow_P, \mathcal{A}_C, \psi, \phi)$$

Framework



Baseline Algorithm

$\text{BASELINERCINFER}(\mathcal{G}, \rightarrow_P, \psi, \mathcal{A}_C)$

```
1 if  $\top, s \leftarrow O^{\exists\exists}(\rightarrow_P, \psi, \top)$  then
2    $R \leftarrow \{y = s\}$  if  $y = s \in \mathcal{G}$  else  $\emptyset$ ;
3   for  $\phi \in \mathcal{G}$  do
4     if  $O^{\exists\forall}(\rightarrow_P, \mathcal{A}_C, \psi, \phi)$  then
5        $R \leftarrow \Delta_{\min}(R \cup \{\phi\})$ ;
6       if  $\neg O^{\exists\exists}(\rightarrow_P, \psi, \neg(\bigvee_{\phi' \in R} \phi'))$  then
7         return  $R$ ;
8   return  $R$ ;
9 return  $\{\perp\}$ ;
```

Theorem:

- Termination when the oracles terminate
- Correction at any step when the oracles are correct
- Completeness w.r.t. the inference language when the oracles are complete
- Under correction and completeness of the oracles
 - Minimality w.r.t. the inference language
 - Weakest constraint generation when returning from line 7



2. Efficient Strategies for Abduction under Robustness

Reusing Necessary Constraints

The Idea

- At each step, we can also check if the candidate is necessary for the satisfaction on the target property
- We can exploit such constraints to build a solution faster by constraining the search space
 - We can skip candidates that are consequences of these necessary constraints
 - We can add to the candidates we test the conjunction of these necessary constraints

How it is done

- Additional $O^{\exists\exists}$ query at each step
- For a candidate ϕ_K , try instead its conjunction with the maximal subset of necessary constraints that remain in the inference language, that is

$$\max_{\mathcal{G}} : \phi_K, \mathcal{G}, N \mapsto \max_{\succsim} (\{N_{\phi_K} \subset N \mid \phi_K \wedge \bigwedge_{\phi \in N_{\phi_K}} \phi \in \mathcal{G}\})$$

$$\succsim : N_1, N_2 \mapsto \text{CARD}(N_1) < \text{CARD}(N_2) \vee (\text{CARD}(N_1) = \text{CARD}(N_2) \wedge \bigwedge_{\phi \in N_1} \phi < \bigwedge_{\phi \in N_2} \phi)$$

Counter-Examples for Robustness



The Idea

- Similarly to what is done in the non-robust case, use counter-examples of the target property to prune the search space of candidates

The Issue

- Robustness ($\exists\forall$ quantification) prevents us from obtaining these examples from the verification oracle queries

Proposal

- Consider a second trace property, $\hat{\psi}$, the satisfaction of which ensuring that our target property ψ is not satisfied
- Additional $O^{\exists\exists}$ query for this second property to obtain counter-examples
- Prune candidates that are satisfiable when they are evaluated to one of these counter-examples on the uncontrolled memory

Ordering Candidates with Heuristics

The Idea

- Some candidates are more likely to be solutions than others
- Reuse information obtained during the computation to make informed guesses on which candidates are better

What we already have

- Examples satisfying the constraint
- Syntactic information on the candidates

Proposal

- Use an ordering heuristic on the candidates

$$\phi \mapsto (\text{count}(\wedge, \phi), -\text{CARD}(\{s \in V \mid \phi[s]\}))$$

- A few examples can be recovered at the beginning of the execution
- Resorting may be applied during the execution to take into account newly obtained examples



3 ■ Experimental Evaluation and Application to Realistic Security Evaluation Scenarios

Implementation



Restriction

- Restriction to bounded reachability and robust reachability
- Use of Symbolic Execution and Robust Symbolic Execution as Oracles
 - BINSEC [Djoudi and Bardin 2015]
 - Symbolic execution at binary level
- Use of SMT-Solver for formula handling and evaluation (z3, cvc5)

Prototype

- PyAbd, Python implementation of the abduction procedure
- Takes as input the binary program and the target reachability target as a BINSEC configuration
- Outputs the robust reachability constraints it found

Benchmark: SVComp

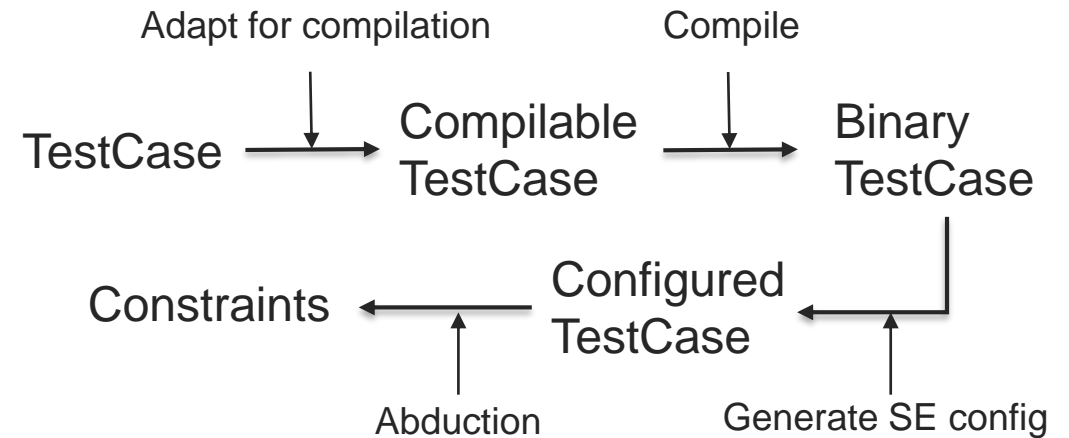
SVComp

- Collection of software verification tasks
- Evaluate the generative capabilities of our method
- Select 147 reachable reachability test cases for which BINSEC answers under 1 minute

Setup

- Use the target location of the benchmark
- Use the input variables as program input
- Abduce constraints on these variables to reach the target location

Process



Example

```
void init (int* x)
{
    for (int i = 0; i < 4; i++)
        x[i] = __VERIFIER_nondet_int();
}

int verify(int * x)
{
    int stuff[4] = { 1, 2, 3, 4 };
    for (int i = 0; i < 4; i++)
        if (x[i] != stuff[i])
            return 1;
    return 0;
}
```

```
int main ()
{
    int x[4];

    init(x);
    assert(verify(x) != 0);

    return 0;
}
```

Benchmark: FISSC

FISSC VerifyPINs

- Collection of verifyPIN C implementations, protected against fault-injection attack
- Reachability: location of incorrect auth

Setup

- Compile source to initial binary
- Simulate 1 instruction skip fault injection by program mutation
- Select 719 reachable mutant programs
- Look for constraints on PIN inputs that lead to an authentication with a wrong PIN

Example

```
#ifndef LAZART
inline BOOL byteArrayCompare(UBYTE* a1, UBYTE* a2) __attribute__((always_inline))
#else
BOOL NOINLINE_BAC byteArrayCompare(UBYTE* a1, UBYTE* a2)
#endif
{
    int i = 0;
    BOOL status = BOOL_FALSE;
    BOOL diff = BOOL_FALSE;
    for(i = 0; i < PIN_SIZE; i++)
        if(a1[i] != a2[i]) diff = BOOL_TRUE;
    if((i == PIN_SIZE) && (diff == BOOL_FALSE)){
        //__begin_secure__("stepCounter");
        status = BOOL_TRUE;
        //__end_secure__("stepCounter");
    }
    return status;
}

void verifyPIN_A()
{
    g_authenticated = BOOL_FALSE;

    if(g_ptc > 0) {
        if(byteArrayCompare(g_userPin, g_cardPin) == BOOL_TRUE) {
            success:
                //__begin_secure__("stepCounter");
                g_ptc = g_ptc_INIT;
                g_authenticated = BOOL_TRUE; // Authentication();
                //__end_secure__("stepCounter");
        }
        else {
            g_ptc--;
        }
    }
}
```

Experimental Setup

What we have

- Program: SVComp or FISSC
- Vulnerability property: Reachability
- Tool: BINSEC
- Tool for robustness: BINSEC-RSE
- Inference Language:
- Implementation: PyAbd

What we do

- Check if PyAbd is able to generate a constraint

Setup

- 1 hour timeout per program
- 60 seconds timeout for BINSEC queries
- 10 seconds timeout for SMT queries
- Run in parallel on an Intel® Xeon® Gold 5220 CPU @2.20GHz machine with 36 cores, 72 threads and 96 GB of RAM

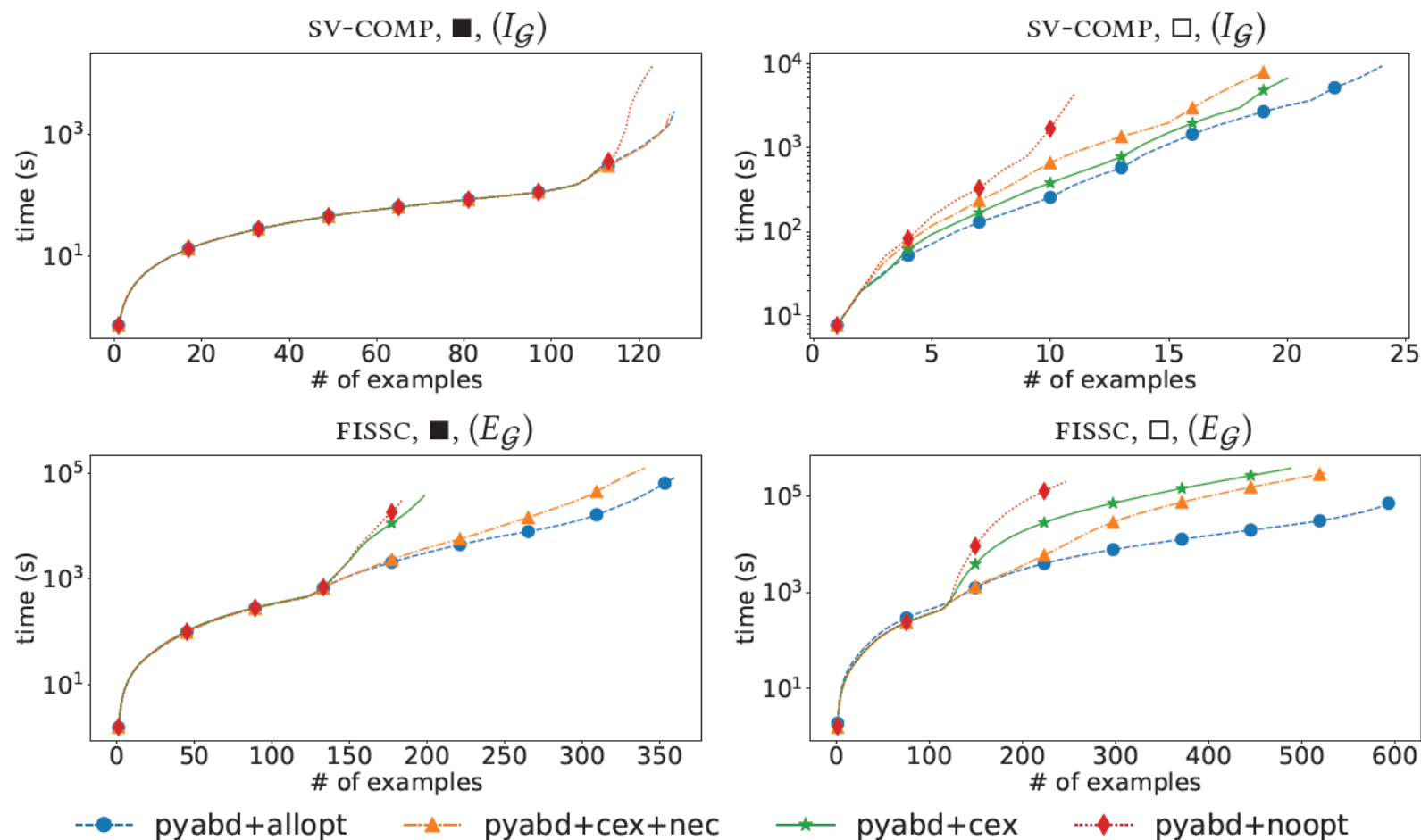
Results: Generating Constraints

Table 1. PYABD analysis results for each benchmark configuration, with (■) or without (□) controlled variables. We detail the total number of programs analyzed, the number of programs for which the target location is robustly k -reachable, and the number of programs for which PYABD finds sufficient robust k -reachability constraints (rrc), split between any sufficient rrc, and the weakest rrc constraints only.

	SV-COMP ($E_{\mathcal{G}}$)		SV-COMP ($I_{\mathcal{G}}$)		FISSC ($E_{\mathcal{G}}$)		FISSC ($I_{\mathcal{G}}$)	
	■	□	■	□	■	□	■	□
# programs	147	64	147	64	719	719	719	719
# of robust cases	111	3	111	3	129	118	129	118
# of sufficient rrc	122	5	127	24	359	598	351	589
# of weakest rrc	111	3	120	4	262	526	261	518

Conclusion: We can compute non-trivial sufficient constraints that refine the results of existing tools

Results: Influence of the ‘Efficient Strategies’



- The strategies significantly improve the capabilities of the tool
- Each strategy impacts a different part of the algorithm
- Some strategies lead to increased computation time on simple examples but permit to solve more difficult ones

Fig. 5. Cactus plot showing the influence of the strategies of Section 5 on the computation of the first sufficient k -reachability constraint with PyABD.

Results: Vulnerability Characterization

Table 3. Analysis results for the VerifyPIN fault mutants (FISSC). Top group of rows: overall results. Bottom group: number of vulnerable mutants for which at least a given percentage of tuples (userPIN / cardPIN) lead to an incorrect authentication. Analysis methods considered: PyABD^O on PIN values ; PyABD^P on PIN values plus additional constraints on other input variables; BINSEC; BINSEC/RSE; single simulation with QEMU; and exhaustive simulation QEMU+L. Each analysis method considers a total of 4810 mutant programs.

	PyABD ^O	PyABD ^P	BINSEC/RSE	BINSEC	QEMU	QEMU+L
unknown	170	170	273	170	243	284
not vulnerable (0 input)	4414	4042	4419	3921	4398	4220
vulnerable (≥ 1 input)	226	598	118	719	169	306
$\geq 0.0001\%$	226	598	118	–	–	306
$\geq 0.01\%$	209	582	118	–	–	281
$\geq 0.1\%$	173	514	118	–	–	210
$\geq 1.0\%$	167	472	118	–	–	199
$\geq 5.0\%$	166	471	118	–	–	196
$\geq 10.0\%$	118	401	118	–	–	148
$\geq 50.0\%$	118	401	118	–	–	135
100.0%	118	399	118	–	–	135

We characterize more cases than other tools and with a more precise solution

Results: Example of FISSC Constraints

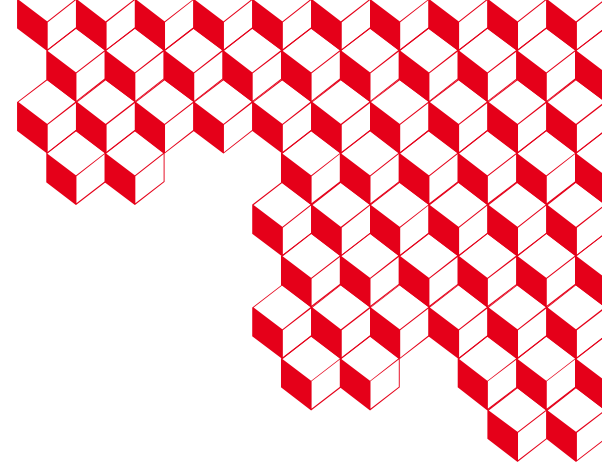
- $\text{Card}[0] == \text{User}[0] \ \&\& \ \text{User}[0] == 3$
Authentication when first digit is 3
- $\text{User}[0] == \text{User}[1] \ \&\& \ \text{User}[0] == \text{User}[2] \ \&\& \ \text{User}[0] == \text{User}[3] \ \&\& \ \text{User}[0] != 0$
Authentication when all digits are equal and non zero
- $\text{Card}[2] != \text{User}[2] \ \&\& \ \text{Card}[3] == \text{User}[3] \ \&\& \ \text{User}[1] == 5$
Authentication when we know the last digit, the 3rd is not correct and the 2nd is 5.
- $\text{R0} == \text{User}[3] \ \&\& \ \text{User}[3] == \text{User}[2] \ \&\& \ \text{User}[3] == \text{User}[1] \ \&\& \ \text{User}[3] == \text{User}[0]$
Authentication with four time the initial value of R0
- $\text{R2} = \text{0xaa} \ \&\& \ \text{R1} != \text{0x55} \ \&\& \ \text{R1} != 0$
Authentication if R2=0xaa initially and R1 distinct from both 0x55 and 0x00 initially

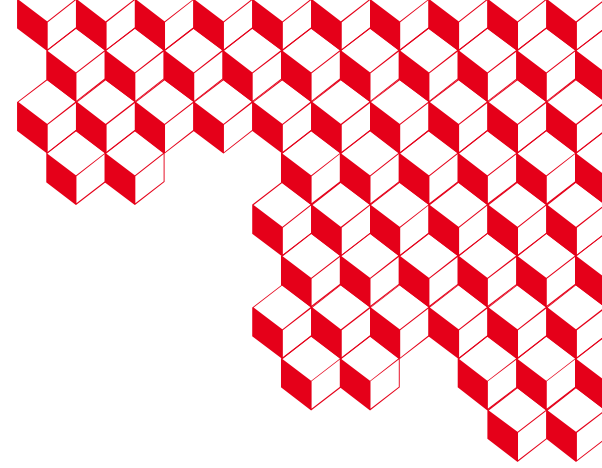
Conclusion

Conclusion

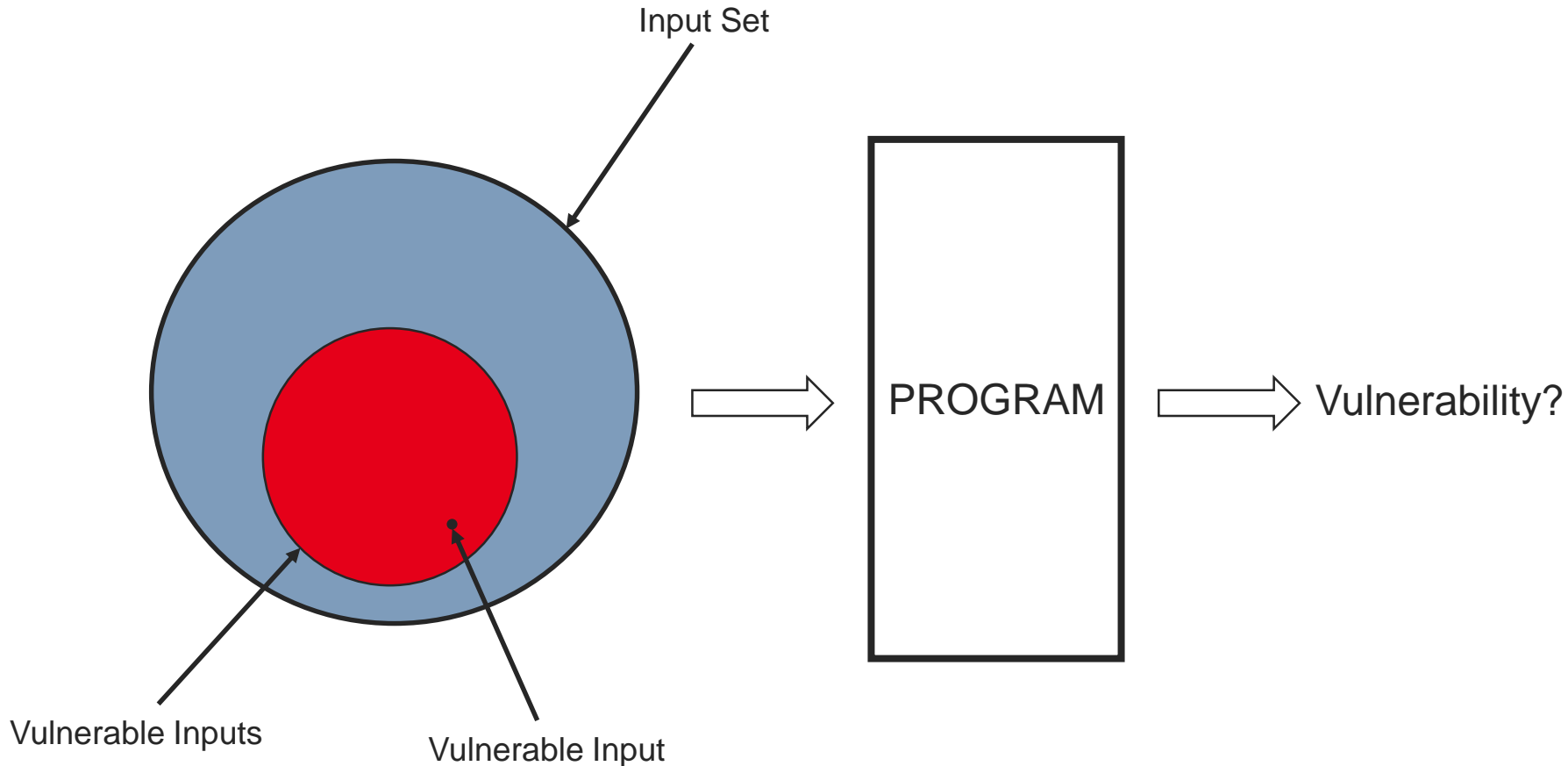
- We propose a novel abduction-based approach to automatically infer robust reachability constraints
- We implement a restriction of this approach to reachability properties on top the BINSEC robust symbolic execution engine
- We demonstrate its ability to refine the notion of robust reachability on standards benchmarks from software verification and security analysis

Questions





Recap: Formal Characterization



- **Usual Formal Evaluation (SE, BMC):** Returns 1 *Vulnerable Input* if it exists
- **Robust Formal Evaluation (RSE, RBMC):** Returns whether *Input Set* = *Vulnerable Inputs* or not
- **Formal Characterization:** Returns a logical description of *Vulnerable Inputs*

Possible Solution: Simulation



Simulation

- From a given set of possible inputs
- Execute/Simulate the program on each input
- Check if the input leads to the targeted bug

Advantages

- Very fast

Issues

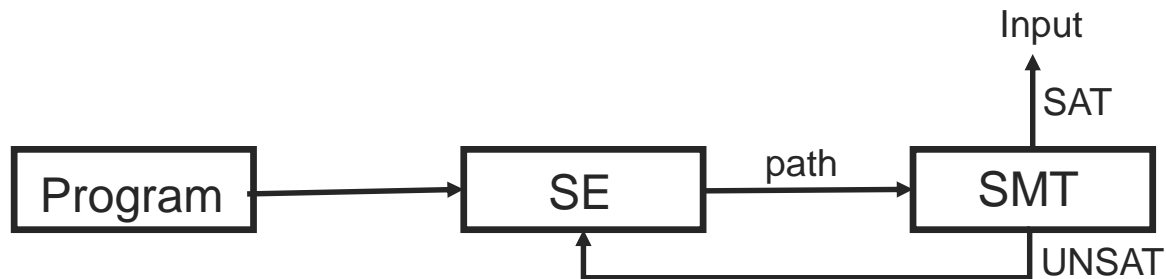
- Depends on the set of inputs
- Easily miss corner cases
- No guarantee if nothing is found

Exhaustive Simulation

- Ensures no case is missed
- Prohibitively time consuming
- Results are hard to exploit

SE Example

- Define a Target Location in a program /
- Express program execution as logic constraints
 - One formula for each possible path containing /
- Let program inputs be free variables
- Use a logic constraints solver (SMT-Solver) to look for assignments of free variables satisfying the reachability predicate



Algorithm 1: *VerifyPin(user, card)*

Input: *user*: user input, *card*: card pin

Output: *status*: authentication iff true

```
1 status ← ⊥;  
2 diff ← ⊥;  
3 for i = 0; i < 4; i ++ do  
4   if user[i] ≠ card[i] then  
5     diff ← ⊤;  
6 if i = 4 ∧ ¬diff then  
7   status ← ⊤; ← Target AND user != card  
8 return status;
```

Algorithm 2: *VerifyPinSMTConstraints*

Input: (declare-var *user*), (= *card* *card-value*)

Output: SAT(*user*)/UNSAT

```
1 (= status_0 false);  
2 (= diff_0 false);  
3 (= i_0 0);  
4 (= user[i_0] card[i_0]);  
5 (= i_1 (+ i_0 1));  
6 (= user[i_1] card[i_1]);  
7 (= i_2 (+ i_1 1));  
8 (= user[i_2] card[i_2]);  
9 (= i_3 (+ i_2 1));  
10 (distinct user[i_1] card[i_1]);  
11 (= diff_1 true);  
12 (= i_4 (+ i_3 1));  
13 (and (= i_4 4) (not diff_1));  
14 (distinct (user card));
```

Inference Languages: Variables



Symbolic Execution Recovery

- Vulnerability examples can be retrieved from the Symbolic Execution Queries
- In these examples, most variables are set to default value, because they are unconstrained: We can discard these variables
- We add to our set of variables all the others and the values they were assigned
- We build constraints following the previous grammar with these variables

Insight

- The set of variable, hence the inference language, depends on the evaluated program
- Future Sybolic Execution queries can exhibit new variables, the language can be updated accordingly

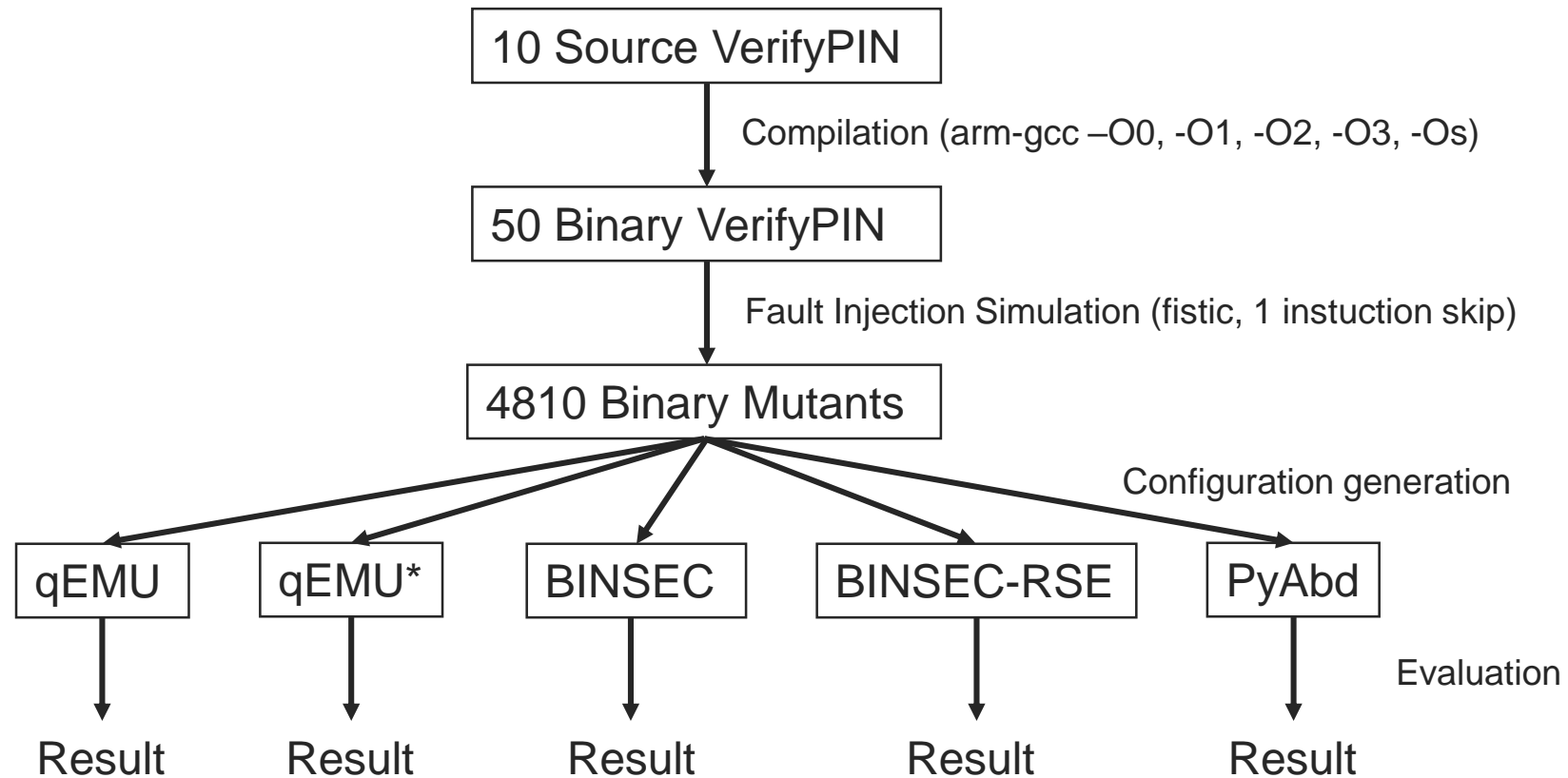
Research Questions

For our benchmarks

- Can we characterize the vulnerabilities?
- Can we generate complete characterizations?
- Do our optimization strategies improve the efficiency of the algorithm?
- How efficiently do we explore the inference language?

Instruction Skip on the FISSC VerifyPINs

Evaluation



Comparing Tools



Simulation

- We find one input that triggers the vulnerability
- Two variants:
 - Predefined test input (Qemu)
 - Loop over all possible userPIN/cardPIN values (Qemu+L)

Symbolic Execution

- The engine finds a vulnerable input
- Two variants:
 - No robustness (Binsec)
 - Robustness (Binsec/RSE)

Abduction

- Generate constraints on PIN variables and other input variables
- Two variants:
 - Constraints on non-PIN variables assumed True
 - Constraints on non-PIN variables assumed False

Comparing Tools: Severity Evaluation

- Count the number of mutant programs for which a vulnerability is found
- Count the number of couples userPIN/cardPIN for which the vulnerability is known to be triggered
- Sort the results with the assumption that more vulnerable userPIN/cardPIN couples means a more serious vulnerability
- Compare the results of the different methods

Instruction Skip Vulnerabilities of the FISSC

VerifyPIN: Analysis Time

Table 4. Analysis times (hours:minutes:seconds) for VerifyPIN (FISSC) for the analysis methods considered in Table 3. For $\text{PYABD}^{\text{O/P}}$, we report the complete analysis time ($\text{PYABD}^{\text{O/P}}$), the time for returning the first constraint ($\text{PYABD}_{\text{first}}^{\text{O/P}}$), and the time for returning the last constraint ($\text{PYABD}_{\text{last}}^{\text{O/P}}$, *i.e.* timeouts excluded).

	$\text{PYABD}^{\text{O/P}}$	$\text{PYABD}_{\text{first}}^{\text{O/P}}$	$\text{PYABD}_{\text{last}}^{\text{O/P}}$	BINSEC/RSE	BINSEC	QEMU	QEMU+L
average	0:16:57	0:01:53	0:02:45	0:00:13	0:00:04	0:00:01	1:08:43
median	0:01:25	0:00:46	0:00:46	0:00:06	0:00:03	0:00:01	1:11:38