

partie de GREF

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C'est juste des élèves quelconques qui font de leur mieux pour suivre en cours et vous partager leurs notes pour vous aider dans vos révisions.

Sur ce, bon travail :).

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1 Infos

You can get many infos there. <https://github.com/bashardudin/GraphsAndFlows>

2 Recap

shortest path

- single-pair (src dst) shortest path problem
- single src any destination : shortest path problem
- Any pair shortest path pb

algorithms

- Bellman-Ford [general no negative valued edges]
- Dijkstra [positive weights]
- Bellman [no cycles]
- Floyd warshall

2.1 Safest path

Aim : safest path along which to go.

To use shortest paths algorithms for it is about applying shortest paths to graphs having $-\log(\text{above weights})$.

2.2 Finding paths

To find critical paths going back from ending point you look for predecessors whose earliest starting date is earliest starting point 'E' - time task takes. And you go through recursively.

margins

It is the difference between earliest starting date of task and the latest (not delaying project).

free margin

Is the difference between earliest starting date & latest one not modifying the earliest starting date of any successors.

2.3 A bit of formalism

Let $c : R_+$ be the capacity in a given graph G (having s and t)

Then a flow on G is a function $f : A \rightarrow R_+$

Satisfying : (1) $\forall a \in A, f(a) \leq c(a)$

(2) $\forall i \in V \setminus \{s, t\} :$

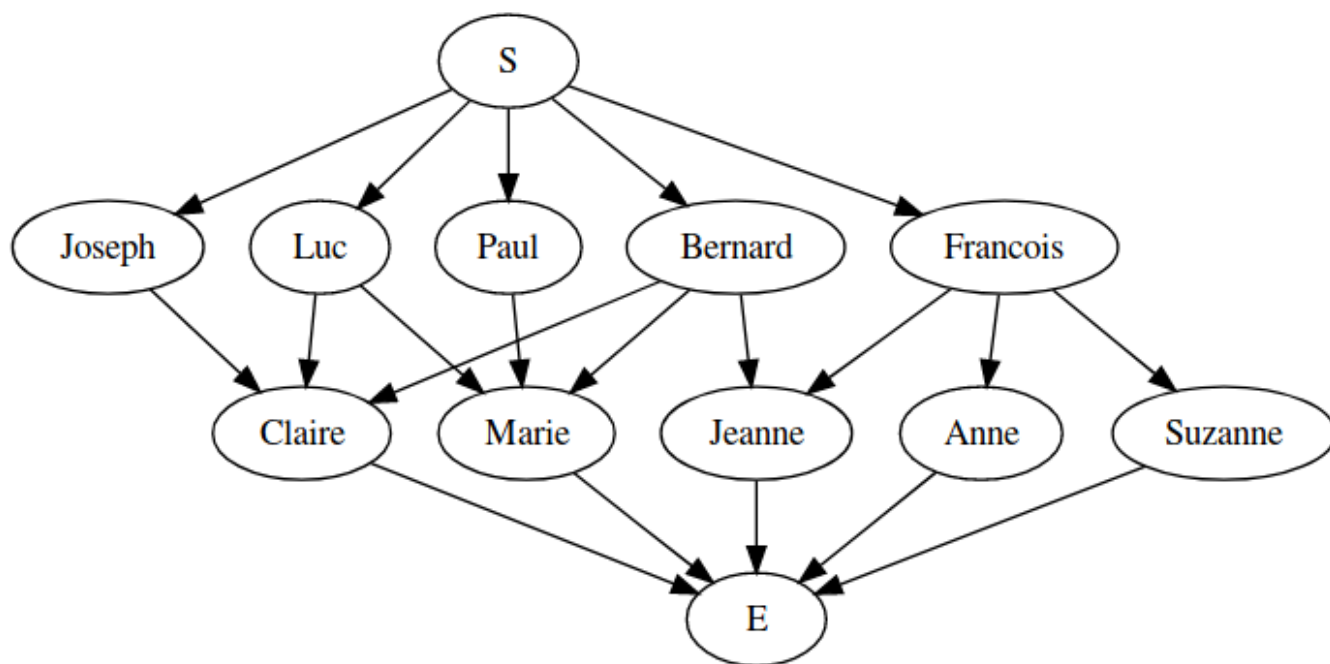
$$\sum_{a \rightarrow i} f(a) = \sum_{i \rightarrow a} f(a)$$

$$a \rightarrow i \quad i \rightarrow a$$

$$a \in A \quad i \in A$$

2.4 Exercice 6 (exercise sheet)

1)



ply apply "improving path" algo and you're done.

2) Sim-