#### Area and error calculations for the HEK

Cis Verbeeck

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# 1 Event\_C1Error, Event\_C2Error (in helioprojective cartesian coordinates)

Event\_C1Error = 
$$\frac{180^{\circ}}{\pi D_{\odot}} \cdot \left(1 + \frac{\Delta D_{\odot}}{D_{\odot}} |x - x_{\text{center}}|\right)$$
,

$$\text{Event\_C2Error} = \frac{180^{\circ}}{\pi D_{\odot}} \cdot \Big(1 + \frac{\Delta D_{\odot}}{D_{\odot}} |y - y_{\text{center}}|\Big),$$

where (x,y) are pixel coordinates,  $D_{\odot}$  is the distance observer-Sun, and  $\Delta D_{\odot}$  is its error estimate. From http://en.wikipedia.org/wiki/Astronomical\_unit, we find

$$D_{\odot} \simeq 149\,597.871\,\mathrm{Mm}.$$

Using the Earth orbit's eccentricity of  $e \simeq 0.0167$ , the yearly maximal error  $\Delta D_{\odot} \simeq 149\,597.871 \times 0.0167\,\mathrm{Mm}$ .

# 2 Area\_Raw (in Mm<sup>2</sup>)

This is the area as it is seen in the image, hence projected from a 3-D ball onto a 2-D disk.

Area\_Raw = Event\_Npixels 
$$\cdot \left(\frac{R_0}{R}\right)^2$$
,

where  $R_0$  and R are the radius of the Sun expressed in Mm respectively pixels. In [1], we find  $R_0 = 695.508$  Mm and  $\Delta R_0 = 0.026$  Mm. Note that R can be found in the FITS header of the image, and  $\Delta R = 2$  (pixels).

## 3 Area\_Uncert (in Mm<sup>2</sup>)

 $Area\_Uncert = (\frac{R_0}{R})^2 \cdot \Big( (number \ of \ pixels \ in \ contour) + 2 \cdot Event\_Npixels \cdot (\frac{\Delta R_0}{R_0} + \frac{\Delta R}{R}) \Big).$ 

## 4 Area\_AtDiskCenter (in Mm<sup>2</sup>)

This is the deprojected area, i.e., the area on the 3-D ball.

$$Area\_AtDiskCenter = \left(\frac{R_0}{R}\right)^2 \cdot \sum_{\text{pixels } (x_i, y_i)} \frac{R}{\sqrt{R^2 - (x_i - x_{\text{center}})^2 - (y_i - y_{\text{center}})^2}}.$$

Note that Area\_AtDiskCenter will go to infinity as the pixel goes toward the eastern or western limb. In order to avoid this, I propose to adopt Paul Higgins's approach to limit the correction factor (i.e., the terms of the sum) to 16, which corresponds to a LOS angle of  $\simeq 86^{\circ}$ . For AR containing a pixel with a corresponding term exceeding 16, we don't provide Area\_AtDiskCenter.

### 5 Area\_AtDiskCenterUncert (in Mm<sup>2</sup>)

$$\begin{aligned} \text{Area\_AtDiskCenterUncert} &= \left(\frac{R_0}{R}\right)^2 \cdot \sum_{\text{pixels}\,(x_i,y_i) \in \text{boundary AR}} \frac{R}{\sqrt{R^2 - (x_i - x_{\text{center}})^2 - (y_i - y_{\text{center}})^2}} \\ &+ \left(\frac{R_0^2}{R}\right) \cdot \sum_{\text{pixels}\,(x_i,y_i) \in \text{AR}} \\ &\left(\frac{|x_i - x_{\text{center}}| + |y_i - y_{\text{center}}| + 2\frac{\Delta R_0}{R_0} \cdot \left(R^2 - (x_i - x_{\text{center}})^2 - (y_i - y_{\text{center}})^2\right) + \frac{\Delta R}{R} \cdot \left(2R^2 - (x_i - x_{\text{center}})^2 - (y_i - y_{\text{center}})^2\right)}{\left(R^2 - (x_i - x_{\text{center}})^2 - (y_i - y_{\text{center}})^2\right)^{1.5}} \right). \end{aligned}$$

#### References

[1] T.M. Brown, J. Christensen-Dalsgaard, "Accurate determination of the solar photosphere radius", ApJ, 500:L195–L198, 1998.